Hashing

TO PASS 60% or higher

TOTAL POINTS 3

1. What is the minimum size of an array that can be used in the direct addressing scheme to store a map from 7-digit phone numbers to names?

- 0 10000000
- 20000000
- 0 1000000



Correct! 7-digit phone numbers correspond to integers from 0 to 9999999.

2. If it is guaranteed that the total length of all occurrences of a Pattern in a Text is at most L, which of the below estimates of the average running time of Rabin-Karp's algorithm to find all occurrences of the Pattern in the Text is the most tight out of the correct ones?

1 / 1 point

1/1 point

- \bigcirc O(|Text| + |Pattern| + L)
- $\bigcirc O(|Text||Pattern| + L)$
- $\bigcirc O(|Text||Pattern|L)$
- $\bigcirc O(|Text| + |Pattern|)$



✓ Correct

Correct! Estimate from the lecture is O(|Text| + (q+1)|Pattern|), where q is the number of occurrences of the Pattern in the Text, and L=q|Pattern| in this case.

3. Let us slightly change the polynomial hash function for strings and set

 $h(S) = \big(\sum_{j=0}^{|S|-1} x^{|S|-1-j} S[j]\big) \bmod p. \text{ Let us fix some } Text \text{ and some } Pattern. \text{ Denote by } H[i] \text{ the } I[i] \text{ the }$

hash function of the substring Text[i..i+|Pattern|-1] of the Text starting from position i and having the same length as Pattern (for all appropriate positions i where the Pattern can occur in the Text). Which of the below formulas is the correct recurrence to compute H[i+1] given H[i]?

- $\bigcirc \hspace{0.1cm} H[i+1] = (xH[i] + Text[i+|Pattern|] x^{|Pattern|}Text[i]) \bmod p$
- $\bigcirc \ \ H[i+1] = (xH[i] + x^{|Pattern|}Text[i+|Pattern|] Text[i]) \bmod p$
- $\bigcirc \ \ H[i+1] = (xH[i] + Text[i+|Pattern|-1] x^{|Pattern|}Text[i]) \ \mathrm{mod} \ p$
- $\bigcirc H[i] = (xH[i+1] + Text[i] x^{|Pattern|}Text[i+|Pattern|]) \bmod p$

✓ Correct

Correct! When we move one position to the right from position i, each term must increase the power of x in it by one, the first term $x^{[Pattern]}Text[i]$ must be subtracted after that, and a new $\operatorname{term} Text[i+|Pattern|] \text{ must be added}.$