Subset problem.

 $S = \{w_1, ..., w_n\}$. Find a subset of S, (say T) s.t. $Z = w_i \leq W$ Sorted in $Z = w_i$ incr. $Z = w_i \leq w_i$ $Z = w_i \leq w_i$ Z =

Want to pick a Set T= \(\frac{1}{2}i_1,...,i_k\}\) s.t \(\wint_{i_1}\)f...+\(\wint_{i_k}\)\\
and \(\frac{1}{2}\) \(\wint_{i_1}\) is maximized.

Case-1: Choose von (win < W).

We need to choose $\sum_{j=1}^{k'} w_{ij} \leq W - w_n$.

and $\sum_{j=1}^{k'} w_{ij}$ is maximised.

Opt(i,w): Optimal solution over $\{w_1,...,w_i\}$ that satisfies $\sum_{p=1}^{101} w_{ip} \leq w$.

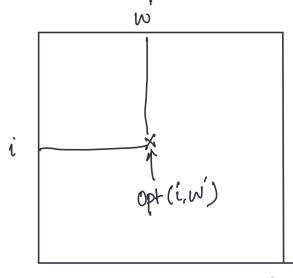
In this case, we now seek Opt (n-1, W-wn).

Case-2: Wn & optimal solution.

(, In this case, we seek Opt (n-1, W).

Opt(n,W) = max { Opt(n-1, W), Opt(n-1, W-wn) + wn }.

No. of subproblems & n.W



opt(i,w')= max { opt(i-1,w'), { opt(i-1,w'-w_c)+w_c

Base case:

Opt (1, w') for w'e [0, w].

W1 < W' - 100 - Opt (1, W') is W1.

Ele, w,>w' - Opt(1,w') -

O-1 Knapsack.

Elems

Value

14em 1

14em 2

14em 1

14em 1

14em 2

14em 1

14em 1

14em 2

14em 1

Knapsack of total webght W.

Question: Fill your knowsack s.t the value of the contents is maximized.

In other words, find a subset of items say in..., ix st Zwij wij & waximbred.

Case-1: Item n E Optimal set.

Case-2: Item $n \notin Optimal set$ VOpt(n+1, W).

NOpt(n,w)= max {Nopt(n-1,w), Nopt(n-1,w-wn)+0n}.

Matrix Chain Multiplication.

w, xw, xw3 \ \maxwa \ \maxwa \ + \ \maxwa \maxwa \ \maxwa \ \maxwa \ \maxwa \ \maxwa \maxwa \ \maxwa \maxwa \ \maxwa \maxwa \ \maxwa ABC $\longrightarrow (AB) \times C \qquad W_1 \times W_3 \times W_4$ \rightarrow A (BC) $W_2 \times W_3 \times W_4$ 6000 Awixwz Worw, Bwan Wirus Cw3xw4 w2xw3 Opt (ABC) WAXW2RW4 > min & Opt (1,2)+ Opt (3,3) + works wy , ~ W,=10 Opt (1,1)+ Opt (2,3) + w, xw, xw, xws } W2= 5 W4 = 15 Wz = 30

 $A_1 A_2 \cdots A_n$

Ai - Winxwi

A, -> Worwa

Want to find an optimal sequence of multiplications. Opt(i,i):