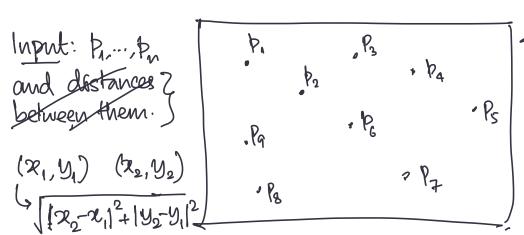
Closest pair of points



Distance metric defined. d(Pi,Pj)>0 if i#j Ps d(Pi,Pi)=0.

2 Pz Problem from Computational Geometris

Want: Find the pair that has least distance between them.

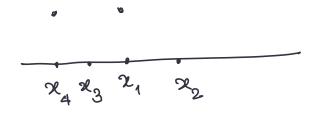
Algo 1: Look at $d(P_i, P_j)$ for all pairs $i \neq j$. $O(n^2)$ time.

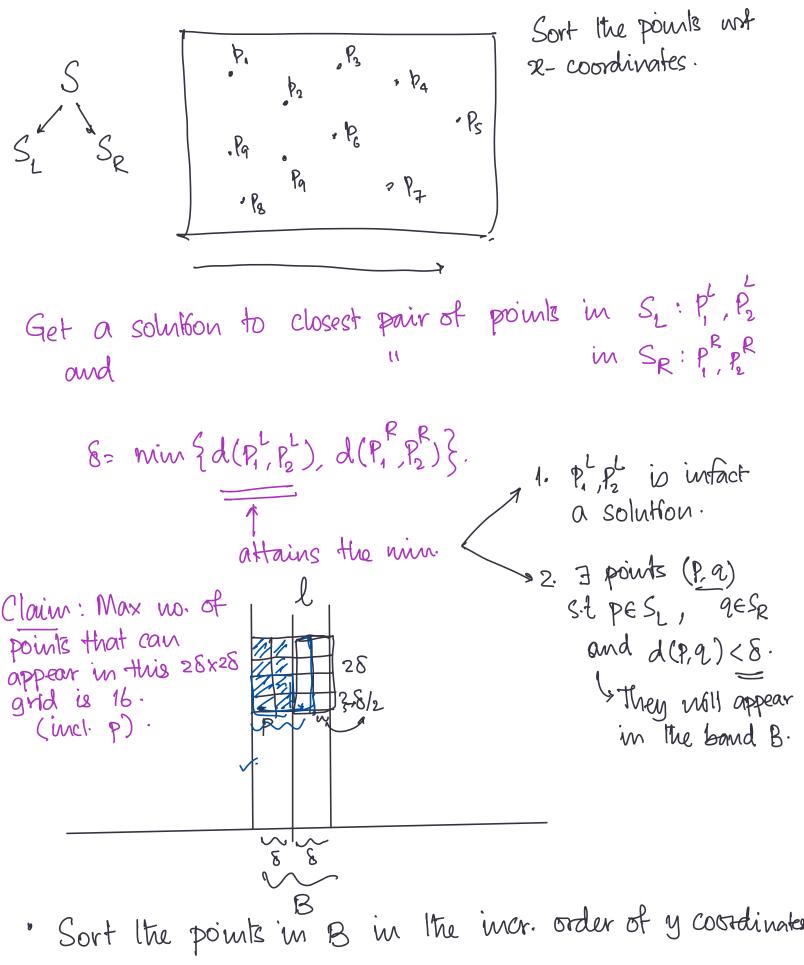
1-dimensional version: Find closest pair of points on a line.

Sort the points and then find closest successive points

O(nlogn)

-> Sort first wit 2-coordinates and then y-coordinates if there is a He wit 2-coordinates.





Sort the points in B in the mor. order of y coordinate of p and d(p,a) < 5.

- -, Max distance between any pair of points in a square of size $\frac{5}{2} \times \frac{5}{2}$ is $\frac{5}{2} \times \sqrt{2} < 8$
 - If two points exist in the same square, their dist is < 8 and this violates the fact that 8 was the min dist in L&R.
- Any point above the grid has dost strictly larger than 8.

For each p in the sorted list of points in B: compute distances of p to its 15 successive points.

Take min over all these distances.

If the min is <8 then report that corresponding pair as the closest pair of points

Else, report Pa and Pl as closest pair.

Algo:

- Sort the given points in uncr order of x-coordinates.
 - Break the problem into two parts by drawing a line L(12 axis
- Obtain solution recursively in both the "halves". Let 8 be the min of both the solutions.
- -> B = set of points that are at most & dist away from

l (x-coordinate vise)

-> Sort the points in B in incr. order of y co-ordinate.

- For each p in the sorted order: compute dist of p from 15 succ. paints

- Take min of all these distances.

If this min < 5 then report this corr. pair as the closest pair of points Else, report the min solution obtained from recursion.

Runnang Home > O(nlogn).

