Regression Week 4: Ridge Regression Assignment 1

In this assignment, we will run ridge regression multiple times with different L2 penalties to see which one produces the best fit. We will revisit the example of polynomial regression as a means to see the effect of L2 regularization. In particular, we will:

- Use a pre-built implementation of regression (GraphLab Create) to run polynomial regression
- Use matplotlib to visualize polynomial regressions
- Use a pre-built implementation of regression (GraphLab Create) to run polynomial regression, this time with L2 penalty
- Use matplotlib to visualize polynomial regressions under L2 regularization
- Choose best L2 penalty using cross-validation.
- Assess the final fit using test data.

We will continue to use the House data from previous assignments. (In the next programming assignment for this module, you will implement your own ridge regression learning algorithm using gradient descent.)

If you are doing the assignment with IPython Notebook

An IPython Notebook has been provided to you below for this quiz. This notebook contains the instructions, quiz questions and partially-completed code for you to use as well as some cells to test your code.

What you need to download

If you are using GraphLab Create:

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- Download the King County House Sales data In SFrame format: kc_house_data.gl.zip (https://eventing.coursera.org/api/redirectStrict
 - /pFKKj27cPp5TIWmf7rh177kFAkTWxP5KOMxzKa8NWK_KQXB4D9b4FWBxWolYBZjYlMVP7CInpIqhOk8qGg3fiw.yb Tm-pTvfl-
 - $W9WrZeqbBnA.dwHSgU_0zCtCbuxD_nA128jfBMepz2kRsdvarhBqb1OLegnVGS6gOx5F9_CCr1bFvuqO3tu-filled for the control of the control of$ ZRV-yiVjk6ymvWU3SjNpryT02XUyse6h7uSJWCOsOBc4jgUzKMvA1VH8Vu-
 - 8KGoE621nO4zGkiAP5G_YviFgdxFTyCbBA_g63nJ_P80mkcDzhuVPybvuFl1loTvof81ZBTtEQ_KP82DWq39T144xBLX ekvgCV37u1c5mgjMet5dHlWw 4GiWeKcTwNnz7Fbcqn4tb9TLHC37arpo7lALwX71WvEXoYvQ0sW8HyU0GgLZ9wH 18buphHCk3uLTqED99j_loOqoll5jMEzkbiVbByTELT6qysDGMuG_sToC8CVNXBIYRIJGQlWn6nY-ntsoTSwrqEo7zZcm57i0dymPPgcGzB0UXAOuq9V3-aVH5iJNCEeo3GoJI2m)
- Download the companion IPython Notebook: week-4-ridge-regression-assignment-1-blank.ipynb (https://eventing.coursera.org/api/redirectStrict/LaNdRtF5uyw7ntUL99ayz5jBFwM94GgY-OnrnHvsMyfdbm9xUtLNftL_uLlj_4igFrf_gW9mBmO26okua2_eqA.fylAy0elEMTTYhzZcZR00Q.DhTJ7Z633Dlzoymau52tHLGz2yWUTDBD7d_pRge5wllvuOWwoHrWe5998nX4cnKMy4bDj0UpavxurzH7yDN1DaAKH9ZC2jmTlSLdBRliDamLgToILt2BQQ3xSSok7UWVDK 7rL5tHFUNfQ9bXDVok3nhEXPDIIHaliEyKAhuhl0ZL_FWpG1DmRuPf09O_D6ArDljSvei3LI_yqL4rfyYnmQqxA4jCZ-

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3PGIL3L_scTQkRH3fQFsDGD5xKDlZjXCixvcRsed7xEUIQNrm2GQUgc_JXLifSJbaSmmyogPGT9r8j4h8vLxCaGsfqXOmd87-wlu0v55fbf0tV4rN-eH8rZ1-RmBZYRczGdmmr5rSeGHBxkNJu6YB-2kd8Oy0dcJU4gOEyLGkQ14vAXnvmNyZjmrHOJJsCrtMQbopu1Z1EzMjLhBsWuj7LlJMeknNyhDWI5mNXX57lwuQs9N0rlupUMCGH3E0)

• Save both of these files in the same directory (where you are calling IPython notebook from) and unzip the data file

If you are not using GraphLab Create:

- Download the King County House Sales data csv file: kc_house_data.csv (https://eventing.coursera.org /api/redirectStrict/4Zhvl9WKRMaRDdVGnEMCLwJ7XepwG3HAm-slx5vexmp4r67v_ysUf-cjdfyGDPEqnlpRDgiBYzLviUPS9gliFg.t5fatXT1wBvF4d7R3gtiKA.MoCUtG1fnt5l_D89Hdn3G88tqMZd0n0iyl4KVurcg ydSX5vTd7F9N8eyF8MZplVsDh8BrAEPOrrWa0697OMENykqMHWfl2N7alyPPjw3kbcwkiaQl4D5TZL4EsEYbVHVRM jiQgZal3DlfRzvY2Gpev0utxXgDH63PPPSuzSNcwiki137sNtTs05JhvOyYiLzP4Gt5OhdQfQGjP9U9Gaqbg6hDJ_GMJAd SaFtVeeRBZMR7WcASiCB08g0dTyYn0DAoDnN5QwqtQnGl7BKigx9pHXGS6abTj0Zeghif-YlZHQGD6jaPibdEevphXhR9-dhPygZdiSar-NR5-kxBnw5xz_9EGDKGvL5ZuqZxTVs6KETR-r6xeW8Z9-6Hu1BYzNt693b30xQ9SF3lB9RDr_URAoNzxE6mleqENiLFX3uHXtUduttIPu-w434zp2zB9yF)
- NOTE: The following files are from Module 3 (Polynomial Regression)
- Download the King County House Sales training data csv file: wk3_kc_house_train_data.csv (https://eventing.coursera.org/api/redirectStrict/MNdwvia9evMBMLIJix1MRai4hOCj8TINcXrKzstT5t60UUHJbDE--zMoZbBcXQfFYVZvIbNjXmBQUCRIX7zIZw.9DiZzXsEEVnd3LSm3tkRnw.A-w4HkcliwzJajunz0-FbbWHsOZJpD0AR4RqJHb0aynOe15gn1ygA2fGP86VQ54uHtvN5Zf-VE4WFRbxtCpB_N8t8mXpoQ8YeRG_F1wuNJXWHTPRzCsrn5oyCFXacCqRir3k3dFH36D5uKP7nvBJWordo1Mllmm_A6M7rb_Jnys5Us9is3yLSGcbCcqGwe6wK4CbHlnd6CONj1cIfo_5KhFp5NlawwL_I_T7QpElhk1DgYrFs9GgTEt2S7A1h_c1zInZ_M1raGfW77GoRyARBd2mrho8ZLZuF8fACm1R7l1YRCRT8mZ6DWtV1oiJgnilOralflGhmD8r1W5XG8iZJUc-2J_mOULHRbqW7f0poZ0IRryR9KHrUOnVifVO0bYd_RAJTDIAglWY7jUNp_4mUegfliH5N4xdgzSJEw5HAudJlB49mCxUu-zVZaAP6r4Dfy_T1tBNtkkUYNRA5c-hbA)
- Download the King County House Sales validation data csv file: wk3_kc_house_valid_data.csv (https://eventing.coursera.org/api/redirectStrict/3XbeiLbOQst4E9CWJGqbs0rGntOh3-tZGWDIZP_jJtyQQ85Dx5JDUVh4a1KceokNUXZizQCYwRYODpl8YM12NA.44p6Ld1xoO5TEVlfVPNu7g.DkRPyWCv3m tldk0EEUFNO0rlOaGW1c8qbxvWc9ZSEEU09D_lPCjrTHp5B24_Awxhju0HF4l7UO8VoZB2YFcnSpjKlFJT3kKL3hhBAIL VUK81lnrf96uNZvpP_w-7qcTRNv2CMbhanRALqS48DtEfyPACRVgkdSCEFRYj9FZMdK-eMnQkXy-ezcllX--HBY1Dq0gYl4jTjM2HB_w8Fp7EjjV2rYp0veeiPaqyRmH30iizvGYsgORUFDaeZySWUBZCxUy13flRQOdTnmC-b7dRV2B6pX2BYV7QatcnOr2dnX9553fonLlNvWx2zvGwbldn6YMJyQDu-9FcBfZxPoLLPKWt0Je_iPNQUwQ9Eiz6TUk4577QgB-BPtMz8o3rlTlWy-KHKmNTbUrEE-pdd5tYlxGD_XihxdMQU9y4zWNiysAH2xOD1PSOSw-NnJqQiZDei1u_aaKiLVoyX7NR2SK10w)
- Download the King County House Sales testing data csv file: wk3_kc_house_test_data.csv (https://eventing.coursera.org/api/redirectStrict /r0Zwa104KLASXOZvzq_glg1l2IPXqLNXawtRahtYDp1FI0BdkaWpwyOl8rxmDs3xsD889xy2WOyFqGE0CL071g.hwq GW8tuzAMger0N1yexuw.lzaElXWSZDvgpIEeX4Cwhs0y1M-Te5JLg-ZSodhzUyHIrpSKdpR65dwnFor-5siKqnn4dNtD-ZdRci7JxciqLRfMoFQcFv75_y7jyNivW2-seDqbLnMoN9wzB34JV8ZdGXPZG69JEKJ-hsefyJ-WCAvakMK-xSpguBbn7JqA9PuaxtJj4PHWVlsjk6ClajJhnV6r5u8PzuwX0s4JHZMUetieCLzIxCinnwXI-93KaQmlEiDhtosKDeY_EDUkiPUXfgkb8ZwYCcCmK5LT7qoOz8aJW_GT6mvWKfpMuxvqZTOZ8DnyKdiysTpYvuRdEe Edcwmtb9RD4sSKm9OTa3vj_yuL97KnPOy6UgH8FC08x354fjYeyztKKOsG0M81jEOoQdhc9dU24IEbWhk69r1of0D A4O5BSmccMCpk-urL46p9Y-fnIBi62xRsdexcoBVsKo9vz1KNUf4LUhP7hRSzRQ)
- Download csv file containing randomly shuffled rows of training and validation data combined: wk3_kc_house_train_valid_shuffled.csv (https://eventing.coursera.org/api/redirectStrict /45VsPtASbiGD3713VCQUh68y_zB7LKRMsuXmjeIMI8wghBQP_Q1RDC0db8cnX9XbgWgFEUX6iwHAMKdY76Qj5A. FY4HPr0_ZPoqfyNEaXaMQw.6Vc- 0uDVSCQwDECcthYzz8s33ETnZi8_NMebsqTKLXgRkdgQbmlif5bJSVgToMivcURX6xCvoywtywe1sQHZ0Ztq2wpKWg tl2h9H5- CfUlq8MMSPmw8VvcKmKyPkC09y8EN4Tooh2wTd587uo4DLGXafmUnSXNkmRbRfMpp8wDUs9sj6M6mZr9pdB-

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- Download the King County House Sales subset 1 data csv file: wk3_kc_house_set_1_data.csv (https://eventing.coursera.org/api/redirectStrict/oylGTI_x9TtgY6PSoTeoxLzCg42BOzJb4U_msbzpMj GJ1d72XpmbdVVkkIJK C6eNJVqVrOKx5lkb50vXGrQ.RIAu6Q7OVtUrwAPlkx KKg.idlxTqvsl9miKu CNqBnuovH 2tKc2CP8Mt0F2xb6bkaahJZdnJPKYnG6e3uCHzUT37u5mbrr3Vwwbub4_QOsiDj-oZn7WSswGZN5RHSyMj4pqgwqROlz8szFbyenloyhzxLhBPWY-HnPqyLnOjTxq7L0W4OhBo6DpuRmXnrphz8bnmeS6frExnkjkj9JPTdklu6Zm7QoWdyfPbqPj34_zRMiMYwa4ybwZQx8cNxtMhR3N_z3vlC8YkKgc1SABRcRi9M7Ij_MSbTdQFJdLloOhDi3dlGqk4dVfc9 mUa0YjZlhSMgaQ7rem0bxWrdqXDfp6bL0YmdNEEC9_W_qr__IUbfKPk069yABJTzU4aOwRO4wRVJIy8MtKzl9woH9MLhtoMq2OXnGE59n9q_4kUau6_37ExikAdZxdXonkLfUyHYjPm3rppdZezZiC5JCWowfxBYO1cSaUR-Yof8QBg)
- Download the King County House Sales subset 2 data csv file: wk3_kc_house_set_2_data.csv (https://eventing.coursera.org/api/redirectStrict /2AvyX_VCmOD92w41fVP7n92G7D3v2RnzsBgnJYVy5gWr5ZWF45Q9a-3gWs0iZCivRbh9SoNCWtQ2hGS3gJLdpQ.7ocxuP4qypkWrAB4TEPMRQ.bBagRnsLUn0slowNoTr8YeN9aE_G642Gn rIUEGNoYt1U86kjhcjlArlyLNK-dsCPRiSy-_F6YIR0_AZwVrOJ6uX-czKAvgmcaiAauXKqpwFRK7CjJ9tYOO6rvHiw53PCxr-4DR-SQhIRKXgPvZ0V40fJ17PiRAedJBZdXZ3ktbnwAcC8xnDIYWetzlI6DwHmeyJN-B3N2CRYg e-F0XNd440r8HaAzbFa rOAH1KG wnW OcCf vLwqHZqY60SEolwhleQFlWtdbmvOpUhe NDiUWkGcj2CGBMTITa8K nQs7BiZhyVc6UD_KvCJOcjfi60ILm9cmvpDlt3WHH8lsy95AbTlHhS0Rc_foa3UlQcjlcJytzlcCeqJz47vtJik1lyWplimM5nJ _rJS6UUCZrg0QbDjeansXfS_1UcrYwjBOvf3cOzVoUKEuSEjSxpOCa4rhqDtBgBRiJd8Q0bgvA)
- Download the King County House Sales subset 3 data csv file: wk3_kc_house_set_3_data.csv (https://eventing.coursera.org/api/redirectStrict/QZSAuAuMXcOpELFwev3uSwYqAsLTfSf3OuxydrUPfJnWHh3j0TPIOCMQCD6xeRPYMv-plMy1k-0yz8rM0PZ9g.7llgdbx9-0y9lkuT5ZIVA.G5esznPUmm2SKsUB7EdTo9CrfVva0vTEKgD7WS2hDU6Ow1tw1c94lkW-InDc8gjUX3k1V7AtAARx7J0ugRtrVS3I -MvWbBEh20X8QiRpsGY2LV9iyPabDKopmV-8K6NO_mnPFMfmM4LP47d8m7ufeLbY0uP-KlLczR9By-tY84wmJlLU3sp5-CVMCPHyrwxuuHwAL5rWAlxPz4hM92eCxDit_H0NHuqzJwm5wQJMJEPeY-3H0U-fB7DzfdhW48KKvn86u5i39d6ClvPE7qOmjlEfMWEKYi479Kc4tHfb9k8_puHq7ZZDTINeMZSOlhlFxiuzeOf_JT1HUhfa2kFQMnwvjyQtZ azTsiwvfoyklq7OOXwhsaq-mJI05VXICx2IeV1etKq_-XaeXoBmKBZN1HbfuEeLmz7CfLM2i-_xotaiaLRgZhwv5UlsAn7eMvRaH8pP7OH_-Odl0OJQ8V1A)
- Download the King County House Sales subset 4 data csv file: wk3_kc_house_set_4_data.csv (https://eventing.coursera.org/api/redirectStrict/UAEPszs3F0OrEVpf8s6HCVjo Odik9pNPBmVVeS9DXGEmB22-Cji2AzszloYcrpi06ecT8HyyxZpI62 s7Hs8A.n9QReoSz7LHzCkTkqfF1GA.uILyl1GIJsf53rtL68PYtYmWdLcKeXTtq-0X6m l7roNjbkrl60f8Y-C-ypEX2MpSEIK1sdHKVlxO166Nrzb7FN9DD7L4aAdh5cJH61wcL8QfBSlymdGk0kZA15KnhpIAg9stgMJGPhcD3darE 6vpeF9wFpgzM8k8ED2Z1Tv166zXXX3mU00klms20Gx-IiDHzEE5U_BQRjD82lzkQHh8hGe7KYsW0lyF1EMNWvApAGj9pdylba9G6JipUgdj3FlRYEOprubnM0uHRwW7V_dpQtYbiPScFLyRxtic0WRvC7T9y5IG71m8qf_BZyziSlhcla447BD-60DURqVD2pVkdVw08-wUfHSYfA6eUG uXqTWJgxJ36ibnB88Ky2-XipmmiWGfrD54qimjz-DICRoTNZCgH bFe-Gp1J0c2nTYg4b9YdQptvZb-ILBakhZcmo6kN4JtDnjuDfBBJenwbw)

Useful resources

You may need to install the software tools or use the free Amazon EC2 machine. Instructions for both options are provided in the reading for Module 1 (Simple Regression).

If you are following the IPython Notebook and/or are new to numpy, then you might find the following tutorial helpful: numpy-tutorial.ipynb (https://eventing.coursera.org/api/redirectStrict /bApDY5Ciz8nYxZISgcYPvgonxTJEKfjRTtP08mUh9HGDql_Tfsxab0lhT-

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lRw.ZkyyLqZtoGiCu18HOITs0may78PSdFpflDmH50qDv8jJ24OhRWAGUtbJwfu72vdCEACeKUjZEwJ-BdQuTLe7yYw_3FywO-

krpScbNwK6rD8htjjxNLVZmWYWkWLD77jSsnLGJXxKPxosZufaX_HtYv_ZT4yaGlnATKissaB4zelbmWERcW2VWHpP52nZ5JFV4R6LQvBEUYFmU_xsfQxvgVloF197xAMIc2XFdDmk7E9mq8sH-

F6m9ev0kSOBXLv0uFEpcj0tNKZVCjrsz9q9wZYGjkAhn LABnEHydbyVvX-6leOFUQBw9t-

6I Htfv0cQVN1 49PsTQMaJeD9jJS5CnK8jwJIEU5E6FYRbteSFW9EhLEeZfRWTUcK8OKZHtgvh9kXUR7mgkY1yQL2Rhy v0IwYeNy72Is3WohEcPTHQ8fe9amGx74YImEvZGu7)

If you are using GraphLab Create and the companion IPython Notebook

Open the companion IPython notebook and follow the instructions in the notebook.

If instead you are using other tools to do your homework

You are welcome to write your own code and use any other libraries, like Pandas or R, to help you in the process. If you would like to take this path, follow the instructions below.

- 1. Copy and paste the 'polynomial_sframe' function (or equivalent) from Module 3 (Polynomial Regression). This function accepts an array 'feature' and a maximal 'degree' and returns an data frame (e.g. SFrame) with the first column equal to 'feature' and the remaining columns equal to 'feature' to increasing integer powers up to 'degree'.
- 2. For the remainder of the assignment we will be working with the house Sales data as in Module 3 (Polynomial Regression). Load in the data and also sort the sales data frame by 'sqft_living'. When we plot the fitted values we want to join them up in a line and this works best if the variable on the X-axis (which will be 'sqft_living') is sorted.
- e.g. if you're using SFrame

```
sales = graphlab.SFrame('kc_house_data.gl/')
sales = sales.sort('sqft_living')
```

- 3. Generate polynomial features up to degree 15 using the polynomial_sframe function (or equivalent) and fit a linear model with these features. After fitting the model, print out the learned weights.
- 4. Quiz Question: What's the learned value for the coefficient of feature power_1?

Observe Overfitting

- 5. Recall from Module 3 (Polynomial Regression) that the polynomial fit of degree 15 changed wildly whenever the data changed. In particular, when we split the sales data into four subsets and fit the model of degree 15, the result came out to be very different for each subset. The model had a high variance. We will see in a moment that ridge regression reduces such variance. But first, we must reproduce the experiment we did in Module 3.
- 6. If you're using SFrame then create four subsets as follows:
- first split sales into 2 subsets with .random_split(.5) use seed = 0.
- next split these into 2 more subsets (4 total) using random_split(0.5) again set seed = 0.
- you should have 4 subsets of (approximately) equal size, call them set_1, set_2, set_3, and set_4

If you're not using SFrame then please download the provided csv files for each subset.

- 7. Just as we did in Module 3 (Polynomial Regression), fit a 15th degree polynomial on each of the 4 sets, plot the results and view the weights for the four models. The four curves should differ from one another a lot, as should the coefficients you learned.
- 8. Quiz Question: For the models learned in each of these training sets, what are the smallest and largest

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Ridge regression comes to rescue

- 9. Generally, whenever we see weights change so much in response to change in data, we believe the variance of our estimate to be large. Ridge regression aims to address this issue by penalizing "large" weights. (Weights of model15 looked quite small, but they are not that small because 'sqft_living' input is in the order of thousands.)
- 10. Using your tool of choice, fit a 15th-order polynomial model on set_1, set_2, set_3, and set_4, this time with L2 penalty of 1e5. These curves should vary a lot less, now that you introduced regularization.
- 11. QUIZ QUESTION: For the models learned with regularization in each of these training sets, what are the smallest and largest values you learned for the coefficient of feature power_1? (For the purpose of answering this question, negative numbers are considered "smaller" than positive numbers. So -5 is smaller than -3, and -3 is smaller than 5 and so forth.)

Selecting an L2 penalty via cross-validation

12. Just like the polynomial degree, the L2 penalty is a "magic" parameter we need to select. We could use the validation set approach as we did in the last module, but that approach has a major disadvantage: it leaves fewer observations available for training. Cross-validation seeks to overcome this issue by using all of the training set in a smart way.

We will implement a kind of cross-validation called k-fold cross-validation. The method gets its name because it involves dividing the training set into k segments of roughtly equal size. Similar to the validation set method, we measure the validation error with one of the segments designated as the validation set. The major difference is that we repeat the process k times as follows:

- Set aside segment 0 as the validation set, and fit a model on rest of data, and evalutate it on this validation set
- Set aside segment 1 as the validation set, and fit a model on rest of data, and evalutate it on this validation set
- ...
- Set aside segment k-1 as the validation set, and fit a model on rest of data, and evalutate it on this validation set

After this process, we compute the average of the k validation errors, and use it as an estimate of the generalization error. Notice that all observations are used for both training and validation, as we iterate over segments of data.

- 13. To estimate the generalization error well, it is crucial to shuffle the training data before dividing them into segments. We reserve 10% of the data as the test set and randomly shuffle the remainder. Le'ts call the shuffled data 'train_valid_shuffled'.
- If you are using GraphLab Create, run the following:

```
(train_valid, test) = sales.random_split(.9, seed=1)
train_valid_shuffled = graphlab.toolkits.cross_validation.shuffle(train_valid, random_seed=0)
```

- If you are not using GraphLab Create, please download the csv file containing pre-shuffled rows of training and validation sets combined: wk3_kc_house_train_valid_shuffled.csv (https://eventing.coursera.org /api/redirectStrict
 - /45VsPtASbiGD3713VCQUh68y_zB7LKRMsuXmjeIMI8wghBQP_Q1RDC0db8cnX9XbgWgFEUX6iwHAMKdY76Qj5A. FY4HPr0 ZPoqfyNEaXaMQw.6Vc-
 - $0 uDVSCQwDECcthYzz8s33ETnZi8_NMebsqTKLXgRkdgQbmlif5bJSVgToMivcURX6xCvoywtywe1sQHZ0Ztq2wpKWgtl2h9H5-\\$
 - CfUlq8MMSPmw8VvcKmKyPkC09y8EN4Tooh2wTd587uo4DLGXafmUnSXNkmRbRfMpp8wDUs9sj6M6mZr9pdB-

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D1uGnMQRKrtM4LflwxN_YpschbJHejg8YDFdljRbxSVH2e9ZoWXl5H34jeZmj8MK790jlkeyQZFimfV-Jb4fOSpEFwwBKBwC6_o9-g_YZh4-gfb3NPpv-652jvJqjC37Vz_T1Hn8XTk6GTrVg04Vr2fryl_yTedWDydqqz4YsFLWicROUvz4k46SNY07H-2Yemg7EYOKVf4JmHbQMxlpsYZAD6h8g5NFw0LcCDHZzgnQZZ-ZQtuJaQhPWobrTeEAGbxCE-GpjLG6Oy2OpOcBPNk85hPcwe61PCn7YpaatpSH1jU6Q). In practice, you would shuffle the rows with a dynamically determined random seed.

14. Once the data is shuffled, we divide it into equal segments. Each segment should receive n/k elements, where n is the number of observations in the training set and k is the number of segments. Since the segment 0 starts at index 0 and contains n/k elements, it ends at index (n/k)-1. The segment 1 starts where the segment 0 left off, at index (n/k). With n/k elements, the segment 1 ends at index (n*2/k)-1. Continuing in this fashion, we deduce that the segment i starts at index (n*i/k) and ends at (n*(i+1)/k)-1.

With this pattern in mind, we write a short loop that prints the starting and ending indices of each segment, just to make sure you are getting the splits right.

```
n = len(train valid shuffled)
k = 10 # 10-fold cross-validation
for i in xrange(k):
    start = (n*i)/k
    end = (n*(i+1))/k-1
    print i, (start, end)
```

Notation for array slicing depends on the tool you are using, bu many tools adopt range notation, where the starting and ending indices are separated by a colon. In this notation, the first index (0) is included in the slice but the last index (10) is excluded.

```
train_valid_shuffled[0:10] # select rows 0 to 9
```

If the observations are grouped into 10 segments, the segment i is given by

```
start = (n*i)/10
end = (n*(i+1))/10
train_valid_shuffled[start:end+1]
```

Meanwhile, to choose the remainder of the data that's not part of the segment i, we select two slices (0:start) and (end+1:n) and paste them together. Consult the manual for your tool of choice for a way to combine the two slices.

e.g. in SFrame

```
\label{train_valid_shuffled[0:start].append(train_valid_shuffled[end+1:n])} train_valid_shuffled[0:start].append(train_valid_shuffled[end+1:n])
```

e.g. in Pandas

```
train_valid_shuffled[0:start].append(train_valid_shuffled[end+1:n])
```

15. Now we are ready to implement k-fold cross-validation. Write a function that computes k validation errors by designating each of the k segments as the validation set. It accepts as parameters (i) k, (ii) l2_penalty, (iii) dataframe, (iv) name of output column (e.g. price) and (v) list of feature names. The function returns the average validation error using k segments as validation sets.

For each i in [0, 1, ... k-1]:

- Compute starting and ending indices of segment i and call 'start' and 'end'
- Form validation set by taking a slice (start:end+1) from the data.
- Form training set by appending slice (end+1:n) to the end of slice (0:start).

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- Train a linear model using training set just formed, with a given I2_penalty
- Compute validation error using validation set just formed

e.g. in Python:

```
def k_fold_cross_validation(k, 12_penalty, data, output_name, features_list):
    ...
    return [average validation error]
```

16. Once we have a function to compute the average validation error for a model, we can write a loop to find the model that minimizes the average validation error. Write a loop that does the following:

- We will again be aiming to fit a 15th-order polynomial model using the sqft_living input
- For each I2_penalty in [10^1, 10^1.5, 10^2, 10^2.5, ..., 10^7] (to get this in Python, you can use this Numpy function: np.logspace(1, 7, num=13).), run 10-fold cross-validation with I2_penalty
- Report which L2 penalty produced the lowest average validation error.

Note: since the degree of the polynomial is now fixed to 15, to make things faster, you should generate polynomial features in advance and re-use them throughout the loop. Make sure to use train_valid_shuffled when generating polynomial features!

- 17. Quiz Question: What is the best value for the L2 penalty according to 10-fold validation?
- 18. Once you found the best value for the L2 penalty using cross-validation, it is important to retrain a final model on all of the training data using this value of I2_penalty. This way, your final model will be trained on the entire dataset.
- 19. Quiz Question: Using the best L2 penalty found above, train a model using all training data. What is the RSS on the TEST data of the model you learn with this L2 penalty?

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