

Solar wind predictions for the Parker Solar Probe orbit

Near-Sun extrapolations derived from an empirical solar wind model based on Helios and OMNI observations

M. S. Venzmer and V. Bothmer

University of Goettingen, Institute for Astrophysics, Friedrich-Hund-Platz 1, 37077 Göttingen, Germany

received date; accepted date

ABSTRACT

Context. The Parker Solar Probe (PSP) (formerly Solar Probe Plus) mission will be humanity's first in situ exploration of the solar corona with closest perihelia at 9.86 solar radii (R_{\odot}) distance to the Sun. It will help answer hitherto unresolved questions on the heating of the solar corona and the source and acceleration of the solar wind and solar energetic particles. The scope of this study is to model the solar wind environment for PSP's unprecedented distances during its prime mission phase during the years 2018–2025. The study is performed within the project Coronagraphic German And US Solar Probe Survey (CGAUSS) which is the German contribution to the PSP mission as part of the Wide field Imager for Solar PRobe (WISPR).

Aims. We present an empirical solar wind model for the inner heliosphere which is derived from OMNI and Helios data. The German-US space probes Helios 1 and Helios 2 flew in the 1970s and observed solar wind in the ecliptic within heliocentric distances of 0.29–0.98 au. The OMNI database consists of multi-spacecraft intercalibrated in situ data obtained near 1 au over more than five solar cycles. The international sunspot number (SSN) and its predictions are used to derive dependencies of the major solar wind parameters on solar activity and to forecast their properties for the PSP mission.

Methods. The frequency distributions for the solar wind key parameters magnetic field strength, proton velocity, density and temperature are represented by lognormal functions. In addition, we consider the velocity distribution's bi-componental shape, consisting of a slower and a faster part. Functional relations to solar activity are compiled with use of the OMNI data by correlating and fitting the frequency distributions with the SSN. Further, based on the combined data set from both Helios probes, the parameters' frequency distributions are fitted with respect to solar distance to obtain power law dependencies. Thus an empirical solar wind model for the inner heliosphere confined to the ecliptic region is derived, accounting for solar activity and for solar distance through adequate shifts of the lognormal distributions. Finally, the inclusion of SSN predictions and the extrapolation to PSP's perihelion enables us to estimate the solar wind environment for PSP's planned trajectory during its mission duration.

Results. The CGAUSS empirical solar wind model for PSP yields dependencies **on solar activity and solar distance for the solar wind parameters' frequency distributions**. The estimated solar wind median values for PSP's first perihelion in 2018 at a solar distance of 0.16 au are 87 nT, 340 km s⁻¹, 214 cm⁻³ and 503 000 K. The estimates for PSP's **first closest perihelion, occurring in 2024 at 0.046 au (9.86 R_{\odot})**, are 943 nT, 290 km s⁻¹, 2951 cm⁻³ and 1 930 000 K. **Since the modeled velocity and temperature values below about 20 R_{\odot} appear overestimated in comparison with existing observations, this suggests that PSP will directly measure solar wind acceleration and heating processes below 20 R_{\odot} as planned.**

Key words. solar wind – sun: heliosphere – sun: corona

1. Introduction

From observations of cometary tail fluctuations Biermann (1951) inferred the presence of a continuous flow of particles from the Sun. With his theoretical solar wind model Parker (1958) formulated the existence of the solar wind even before the first satellites measured it in situ in 1959 (Gringauz et al. 1960; Neugebauer & Snyder 1966). The idea of a space mission flying through the solar corona dates back to the founding year of NASA in 1958 (McComas et al. 2008). Since then several space missions have measured the solar wind in situ at a wide range of heliocentric distances, in case of Voyager 1 as far away as 138 au¹ (July 2017), having even left the heliospause into interstellar space at a distance of 121 au (Gurnett et al. 2013). Various spacecraft have provided a wealth of solar wind measurements near Earth's orbit, with WIND (Lepping et al. 1995; Ogilvie et al. 1995), SOHO (Domingo et al. 1995),

ACE (Stone et al. 1998) and DSCOVR (Burt & Smith 2012) still orbiting around the L1 point 1.5 million km ahead of Earth in the sunward direction. Additional measurements at other solar distances were provided by planetary missions to Venus and Mercury, such as PVO (Colin 1980) or MESSENGER (Belcher et al. 1991). Ulysses was the first probe that orbited the Sun out of the ecliptic plane and thus could measure solar wind even at polar latitudes (McComas et al. 1998). **The in situ solar wind measurements closest to the Sun to date were made by the Helios mission. Helios 1, launched in 1974, reached distances of 0.31 au. Helios 2, launched two years later, approached the Sun as close as 0.29 au (Rosenbauer et al. 1977).** The NASA Parker Solar Probe² (PSP), formerly Solar Probe Plus, with a planned launch date in mid 2018, will reach after six years in 2024 its closest perihelia at a distance of 9.86 solar radii (R_{\odot}), that is, 0.0459 au (Fox et al. 2015). This distance will be achieved

¹ <https://voyager.jpl.nasa.gov/>

² <http://parkersolarprobe.jhuapl.edu/>

through seven Venus gravity assists with orbital periods of 88–168 days. In its prime mission time 2018–2025 PSP provides 24 orbits with perihelia inside 0.25 au (Fox et al. 2015). Even its first perihelion, 93 days after launch in 2018, will take PSP to an unprecedented distance of 0.16 au ($35.7 R_{\odot}$). In comparison, the ESA Solar Orbiter mission with a planned launch in February 2019 will have its closest perihelia at 0.28 au (Müller et al. 2013).

The key PSP science objectives are to “trace the flow of energy that heats and accelerates the solar corona and solar wind, determine the structure and dynamics of the plasma and magnetic fields at the sources of the solar wind, and explore mechanisms that accelerate and transport energetic particles” as stated in Fox et al. (2015). To achieve these goals, PSP has four scientific instruments on board: FIELDS for the measurements of magnetic fields and AC/DC electric fields (Bale et al. 2016), SWEAP for the measurements of flux of electrons, protons and alphas (Kasper et al. 2016), ISOIS for the measurement of solar energetic particles (McComas et al. 2016) and WISPR for the measurement of coronal and inner heliospheric structures (Vourlidas et al. 2016).

The study presented in this paper is undertaken in the Coronagraphic German And US Solar Probe Survey (CGAUSS) project, which is the German contribution to the PSP mission as part of the Wide field Imager for Solar PRobe (WISPR). WISPR will contribute to the PSP science goals by deriving the 3D structure of the solar corona through which the in situ measurements are made to determine the sources of the solar wind. It will provide density power spectra over a wide range of structures (e.g., streamers, pseudostreamers and equatorial coronal holes) for determining the roles of turbulence, waves and pressure-balanced structures in the solar wind. It will also measure the physical properties, such as speed and density jumps of SEP-producing shocks and their CME drivers as they evolve in the corona and inner heliosphere (Vourlidas et al. 2016).

In order to help optimize the WISPR and PSP preplanning of the science operations knowledge of the expected solar wind environment is needed. For this purpose the solar wind environment is extrapolated down to the closest perihelion of $9.86 R_{\odot}$ distance to the Sun using in situ solar wind data from the Helios probes and near 1 au data from various satellites compiled in the OMNI solar wind database.

Generally, two types of solar wind are observed in the heliosphere, slow and fast streams (Neugebauer & Snyder 1966; Schwenn 1983). Slow solar wind has typical speeds $< 400 \text{ km s}^{-1}$ and fast solar wind has speeds $> 600 \text{ km s}^{-1}$ (Schwenn 1990, p. 144). Their different compositions and characteristics indicate different sources and generation processes (McGregor et al. 2011b). Fast streams are found to originate from coronal holes as confirmed by Ulysses’ out-of-ecliptic measurements (McComas et al. 1998). The source of slow wind and its eventually different types (Schwenn 1983), is still a subject of controversial discussions because several scenarios are possible to explain its origin from closed magnetic structures in the solar corona, such as intermittent reconnection at the top of helmet streamers and from coronal hole boundaries (Kilpua et al. 2016). The occurrence frequency of these slow and fast streams varies strongly with solar activity and their interactions lead to phenomena such as stream interaction regions and for quasi-stationary coronal source regions to co-rotating interaction regions (Balogh et al. 1999). Embedded in the slow and fast solar wind streams are transient flows of coronal mass ejections (CMEs), the faster ones driving shock waves ahead (Gosling et al. 1974). Their rate follows the solar activity cycle and varies

in near 1 au measurements between only one CME every couple of days during solar cycle minima up to multiple CMEs observed over several days at times of solar maxima, that is, the CME-associated flow share of the solar wind raises from about 5 % up to about 50 % (Richardson & Cane 2012).

It is not known which specific solar wind type or structure PSP will encounter at a given time during its mission, therefore we extrapolate the probability distributions of the major solar wind parameters from existing solar wind measurements and take solar cycle dependencies into account. As a baseline we describe the solar wind environment through the key quantities of a magnetized plasma: *magnetic field strength, density and temperature*. Furthermore, the bulk flow *velocity* is the defining parameter of the two types of solar wind. Solar wind quantities, like flux densities, mass flux and plasma beta, can directly be derived from these four parameters. In the analyses we treat the solar wind as a proton plasma—the average helium abundance is about 4.5 % and in slow wind at solar cycle minimum even less than 2 % (Feldman et al. 1978; Schwenn 1983; Kasper et al. 2012).

Our approach is to obtain analytical representations of the shapes of the solar wind parameter’s frequency distributions in Sect. 2, of their solar activity dependence in Sect. 3 and of their solar distance scaling in Sect. 4. The solar wind parameters’ frequency distributions and solar activity dependence is derived from near-Earth solar wind and sunspot number (SSN) time series with a duration of almost five solar cycles. Their distance dependency is derived from Helios solar wind measurements covering more than two third of the distance to the Sun and more than half a solar cycle. From combination of the obtained frequency distributions, SSN dependence functions and solar distance dependence functions a general solar wind model is build in Sect. 5, representing the solar activity and distance behavior. Finally, this empirical model is fed with a SSN prediction and extrapolated to PSP’s planned orbital positions in Sect. 6.

2. Frequency distributions of the solar wind parameters

The solar wind parameters are highly variable, due to short-term variations from structures like slow and fast wind streams, interaction regions and CMEs, whose rate and properties depend on the phase of the solar activity cycle. Hence, for deriving characteristic frequency distributions for the solar wind parameters, measurements over long-term time spans are needed. The abundance of the near-Earth hourly OMNI data set is ideally suited for this purpose, because it spans to date almost five solar cycles.

The OMNI 2 data set (King & Papitashvili 2005) combines solar wind magnetic field and plasma data collected by various satellites since 1963, currently by WIND and by ACE. This intercalibrated multi-spacecraft data is time-shifted to the nose of the Earth’s bow shock. The data is obtained from the OMNIWeb interface³ at NASA’s Space Physics Data Facility (SPDF), Goddard Space Flight Center (GSFC). In this study the whole hourly data until 31 December 2016 is used, starting from 27 November 1963 (for the temperature from 26 July 1965). The data coverage of the different parameters is in the range 67–74 %, corresponding to a total duration of 36–40 years. It should be noted that a test-comparison of hourly averaged with higher time resolution data for the available shorter time span 1981–2016 did not show significant differences in our results.

³ <http://omniweb.gsfc.nasa.gov/>

According to the OMNI data precision and maximal parameter ranges we specify bin sizes of 0.5 nT for the magnetic field strength, 10 km s⁻¹ for the velocity, 1 cm⁻³ for the density and 10 000 K for the temperature. The frequency distributions of the solar wind magnetic field strength, proton velocity, density and temperature are shown in Fig. 1. The solar wind magnetic field strength is in the range 0.4–62 nT, the velocity in the range 156–1189 km s⁻¹, the density in the range 0–117 cm⁻³, and the temperature in the range 3450–6.63 × 10⁶ K, the mean data values are at 6.28 nT, 436 km s⁻¹, 6.8 cm⁻³ and 1.05 × 10⁵ K. These ranges and mean values are as statistically expected from previous analyses of near 1 au solar wind data (e.g., Table 3.3 in Bothmer & Daglis (2007, p. 39)). Much higher or lower peak values at 1 au have been observed in extraordinary events, such as the 23 July 2012 ICME with a speed of over 2000 km s⁻¹ and a peak field strength of about 100 nT that was observed by STEREO A (Russell et al. 2013) or the solar wind disappearance event observed in May 1999 with density values even down to 0.2 cm⁻³ (Lazarus 2000).

The frequency distributions of the solar wind parameters magnetic field strength, proton density and temperature can well be approximated by lognormal distributions, whereas the proton velocity's frequency has a differing shape, as shown in Veselovsky et al. (2010). We investigate how well all four solar wind parameters' frequency distributions can be represented by lognormal functions, which we use in the process of a least squares regression fitting. The lognormal function

$$W(x) = \frac{1}{\sigma \sqrt{2\pi}x} \exp\left(-\frac{(\ln x - \mu)^2}{2\sigma^2}\right) \quad (1)$$

depends on the location μ and the shape parameter σ . Changes in μ affect both the horizontal and vertical scaling of the function whereas σ influences its shape. The distribution's median x_{med} and mean x_{avg} (average) positions are straightforward to interpret and are directly calculated from μ and σ :

$$x_{\text{med}} = \exp(\mu) \iff \mu = \ln(x_{\text{med}}), \quad (2)$$

$$x_{\text{avg}} = \exp\left(\mu + \frac{\sigma^2}{2}\right) \iff \sigma = \sqrt{2 \ln\left(\frac{x_{\text{avg}}}{x_{\text{med}}}\right)}. \quad (3)$$

It is apparent that the mean is always larger than the median. Replacing the variables μ and σ with these relations, the lognormal function (1) becomes

$$W(x) = \frac{1}{2 \sqrt{\pi \ln\left(\frac{x_{\text{avg}}}{x_{\text{med}}}\right)} x} \exp\left(-\frac{\ln^2\left(\frac{x}{x_{\text{med}}}\right)}{4 \ln\left(\frac{x_{\text{avg}}}{x_{\text{med}}}\right)}\right). \quad (4)$$

The values of x_{med} and x_{avg} obtained from fitting the individual solar wind frequency distributions are listed in Table 1.

From visual inspection, the resulting fit curves describe the shape of the magnetic field strength, density and temperature distributions well, as can be seen in Fig. 1. However, for the velocity the fit function appears not to be as good in describing the measured distribution's more complex shape around its peak and in the higher velocity range. This also can be inferred from the sum of absolute residuals (SAR) between data and fit, listed in Table 1 in percentage of the distribution area, being almost three times larger than those from the other parameters.

In order to find a better fit result for the velocity distribution, we assume that the velocity distribution can be made up of at

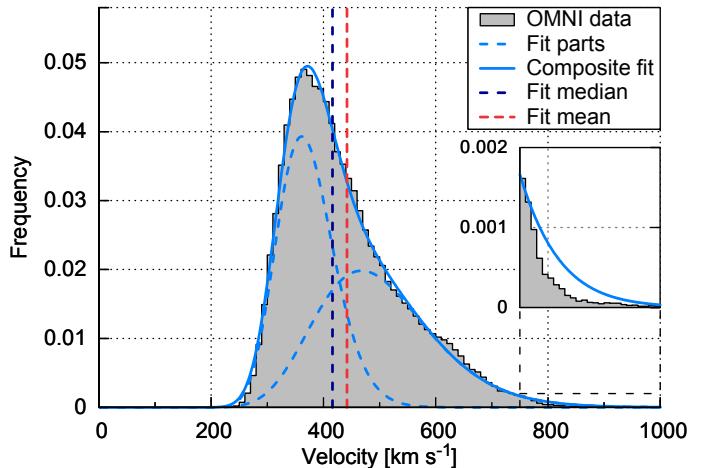


Fig. 2. The velocity's frequency distribution (same as in Fig. 1) and its compositional lognormal fit. The fit's median and mean values and its two fit parts are indicated as well. **The inset is a zoomed-in view of the high value tail of the distribution.**

least two overlapping branches (McGregor et al. 2011a). Therefore a compositional approach is chosen by combining two lognormal functions (4), involving more fit variables:

$$W_{\text{II}}(x) = c \cdot W_1(x) + (1 - c) \cdot W_2(x). \quad (5)$$

The balancing parameter c ensures that the resulting function remains normalized as it represents a probability distribution. The fitting of $W_{\text{II}}(x)$ to the velocity's frequency distribution yields the values of the now five fit parameters (c , $x_{\text{med},1}$, $x_{\text{avg},1}$, $x_{\text{med},2}$ and $x_{\text{avg},2}$) as listed in Table 1 together with the median and mean values of the composed distribution, which can be derived via solving

$$\int W_{\text{II}}(x) dx = 0 \quad \text{and} \quad \int x W_{\text{II}}(x) dx = 0. \quad (6)$$

This more complex fit function is more accurate in describing the velocity's frequency distribution as shown in Fig. 2. Thus in the following sections we keep the double lognormal ansatz for all velocity frequency fits.

For the bulk of the solar wind these static lognormal functions describe the parameters' distributions well. **The abnormally high parameter values in the distribution functions can be attributed to shock/CME events in agreement with the results of the OMNI solar wind investigations by Richardson & Cane (2012).** The simple lognormal fit functions underestimate the frequencies in their high value tails, except for the temperature's tail which is overestimated, as seen in the insets of Fig. 1, **this appears to be because CMEs do not come with abnormally high temperatures, but rather with temperatures lower than those of the average solar wind (Forsyth et al. 2006).** The velocity's compositional lognormal fit only slightly overestimates its tail as seen in the inset of Fig. 2. The slow and fast part contribute almost equally ($c \approx 0.5$) to the long-term velocity distribution function.

3. Solar activity dependence of the solar wind frequency distributions

In the next step we investigate how the long-term solar wind distribution functions presented in the previous section depend on general solar activity. Therefore we examine their correlation

Table 1. Resulting fit coefficients from the fitting of the lognormal function (4) to the shape of the solar wind parameters' frequency distributions from near 1 au OMNI hourly data. For the velocity also the fit parameters of the double lognormal function (5) are listed, as well as the median and mean values of the resulting velocity fit. **The numbers in parentheses are the estimated standard deviations of the fit parameters referred to the corresponding last digits of the quoted value. For each parameter the sum of absolute residuals between data and fit (in percentage of the distribution area) is also listed.**

Parameter	Median x_{med}	Mean x_{avg}	Balance c	SAR [%]
Magnetic field [nT]	5.661(16)	6.164(18)	–	6.83
Velocity [10^2 km s^{-1}]	4.085(19)	4.183(20)	–	18.69
Density [cm^{-3}]	5.276(24)	6.484(34)	–	6.48
Temperature [10^4 K]	7.470(17)	11.301(32)	–	5.78
Velocity	W_1 [10^2 km s^{-1}]	4.89(14)	5.00(14)	0.504(62)
	W_2	3.68(20)	3.72(20)	–
	W_{II}	4.16(14) ^a	4.42(14) ^a	–
				4.20

Notes. ^(a) Error estimates derived from the individual fit part errors.

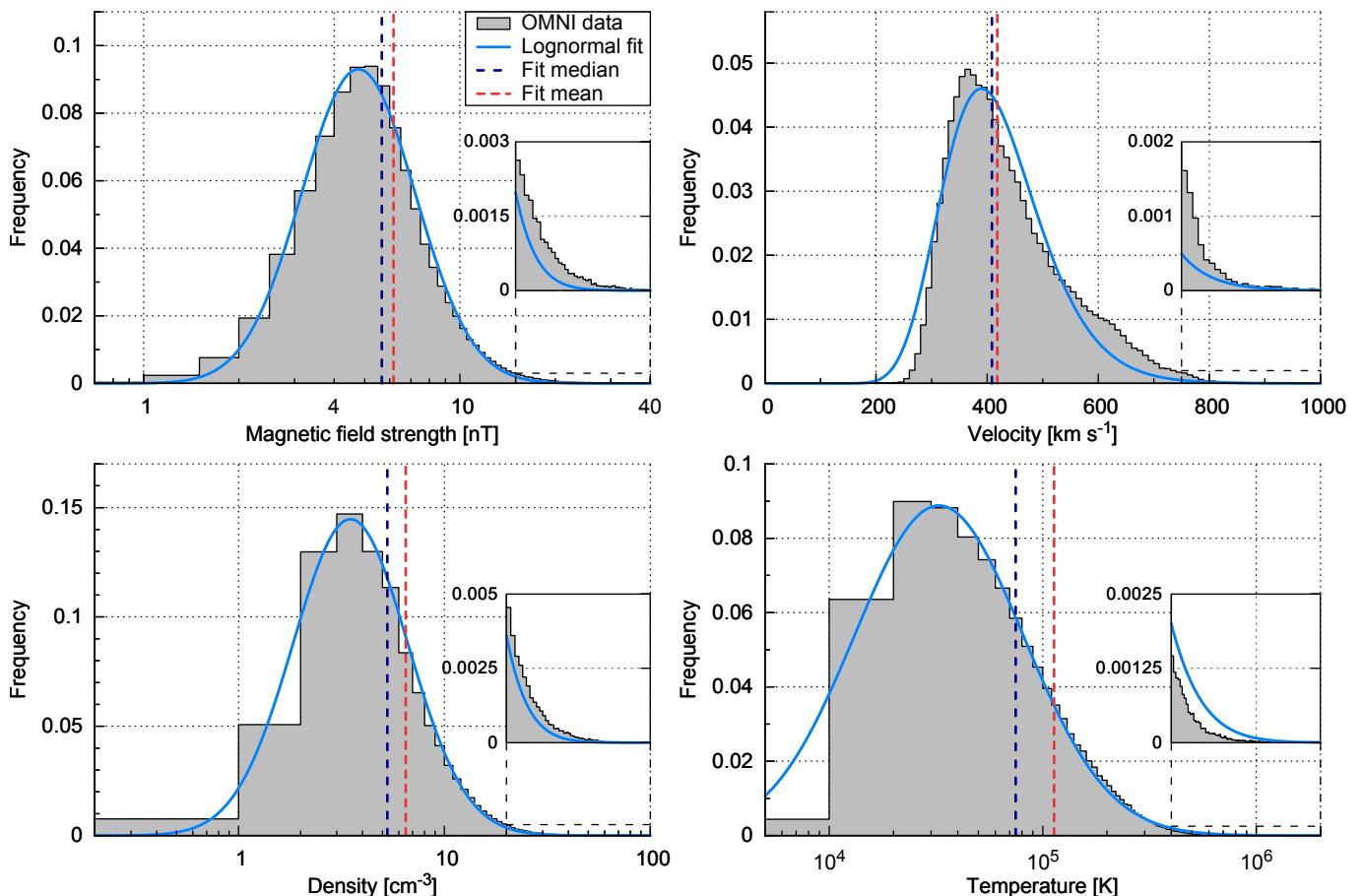


Fig. 1. Frequency distributions of the four solar wind parameters and their lognormal fits derived from the hourly OMNI data set. The histograms have bins of 0.5 nT, 10 km s⁻¹, 1 cm⁻³ and 10 000 K. The fits' median and mean values are indicated as well. The insets show zoomed-in views of the high value tails of the distributions.

with the SSN, being a commonly used long-term solar activity index, and determine the time lags with the highest correlation coefficients.

For the correlations we fit lognormal functions to the frequency distributions as in Sect. 2, but implement linear relations to the yearly SSN, allowing shifting of the distribution functions with SSN. For the velocity the approach is different insofar as its two components are kept fixed and instead their balance is modified with the changing SSN. **Thus we obtain solar activ-**

ity depending models for the frequency distributions of all four solar wind parameters.

The international sunspot number (1963–2016) is provided by the online catalogue⁴ at the World Data Center – Sunspot Index and Long-term Solar Observations (WDC-SILSO), Solar Influences Data Analysis Center (SIDC), Royal Observatory of Belgium (ROB).

⁴ <http://www.sidc.be/silso/>

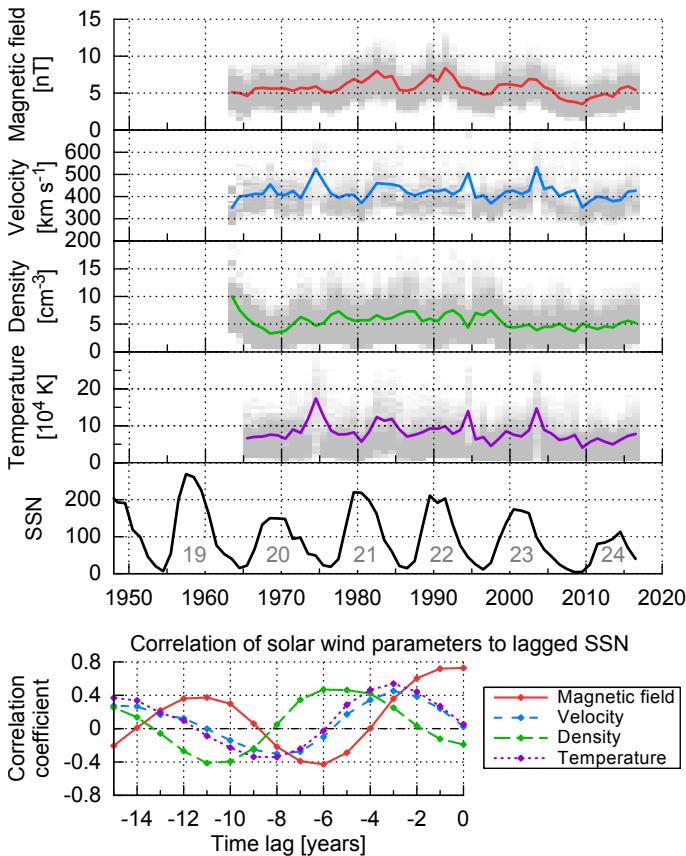


Fig. 3. The solar wind parameter yearly **frequencies** (grey shading) with **yearly medians** (lines) derived from OMNI data and the yearly SSN from the SILSO World Data Center (1963–2016) with solar cycle number (top). Their correlation coefficients with the yearly SSN are calculated for time lags back to -15 years (bottom).

Fig. 3 shows yearly medians of the solar wind parameters and the yearly SSN together with the solar cycle number. The reason for correlating the SSN to the solar wind median values is because the position of a lognormal function is defined by its median. The data are averaged to yearly values to avoid seasonal effects during the Earth's orbit around the Sun caused by its variations in solar latitude and distance. Solar wind parameter yearly data frequencies The solar wind velocity, density and temperature depend on the state of the solar cycle (Schwenn 1983). For instance the fast solar wind occurs at times when polar coronal holes extend to lower latitudes, a typical feature of the declining phase of the solar cycle as pointed out by Bothmer & Daglis (2007, p. 75, Figure 3.52). Therefore the solar wind velocity, density and temperature maxima exhibit **time lags relative** to the SSN maxima.

The correlation coefficients of the solar wind parameters with the yearly SSN shown in the bottom part of Fig. 3 are calculated for time lags back to -15 years to cover a time span longer than a solar cycle. As expected, the **amplitudes of the variations in the correlations** of all parameters decline with increasing time lag and show a **period** of about 11 years. The highest correlation coefficient of 0.728 to the SSN is found for the magnetic field strength, it has no time lag. This finding is anticipated because the SSN is found to be directly proportional to the evolution of the photospheric magnetic flux (Smith & Balogh 2003). Velocity and temperature show a **time lag** of 3 years with peak correlation coefficients of 0.453 and 0.540. The density with a correlation coefficient of 0.468 has a time lag of 6 years, which

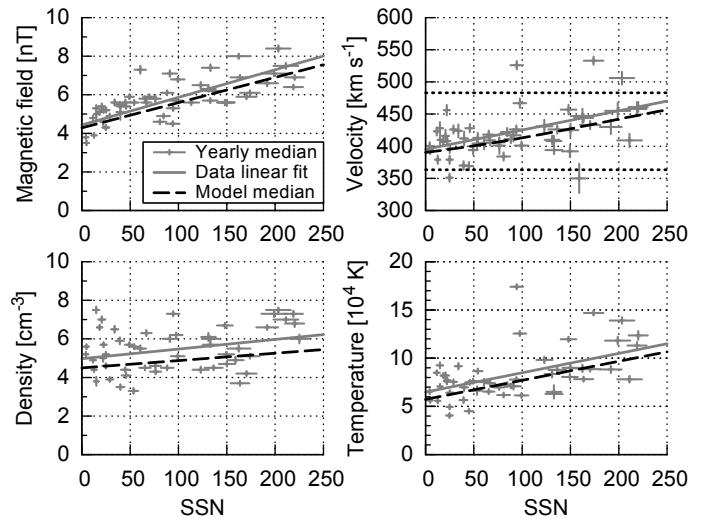


Fig. 5. Solar wind parameter median with respect to the lagged SSN. The yearly data medians (+) with their weighted linear fit (solid lines) are obtained from OMNI data. The error bars denote the SSN standard deviation and the relative weight from the yearly data coverage. The SSN dependent median (7) is derived from the lognormal model fit (dashed line). For the velocity the median is derived from the SSN weighting (9) of the slow and fast model parts, whose magnitudes are SSN independent (dotted line).

is in agreement with the by Bougeret et al. (1984) reported density anticorrelation to the SSN.

Next we create **solar activity dependent analytical representations of the solar wind frequency distributions**. This is achieved by shifting the median positions of the lognormal distributions as a linear function of SSN. To enable these shifts, we add a linear SSN dependency to the median

$$x_{\text{med}}(ssn) = a_{\text{med}} \cdot ssn + b_{\text{med}}, \quad (7)$$

using a factor to the SSN a_{med} with a baseline b_{med} . We relate the mean with a scaling factor to the median to transfer its SSN dependency:

$$x_{\text{avg}}(ssn) = (1 + a_{\text{avg}}) \cdot x_{\text{med}}(ssn). \quad (8)$$

These relations, substituted into the lognormal function (4), lead to a new SSN-dependent function $W'(x, ssn)$. This function is then fitted to the yearly data, using the yearly SSN as input parameter. The SSN is offset with the individual time lags for each parameter determined before, to benefit from the higher correlation. The three resulting fit coefficients (a_{med} , b_{med} and a_{avg}) are presented in Table 2.

As can be seen from Fig. 4, naturally, the fit models match with the general data trends, though single year variations are not replicated by the model (e.g., the high velocity and temperature values in 1974, 1994 and 2003). The comparison of this model with the yearly data median values with respect to the lagged SSN shows that the medians obtained from the modeling have a quite similar slope as shown in Fig. 5.

Again, the solar wind velocity needs a special treatment because of the application of the double lognormal distribution (5). Since it is well known that slow and fast solar wind stream occurrence rates follow the solar cycle we keep the two velocity components' positions **SSN-independent** ($x_{\text{med}} = b_{\text{med}}$) and vary instead their balance with the SSN:

$$c(ssn) = c_a \cdot ssn + c_b. \quad (9)$$

Table 2. Resulting fit coefficients from the OMNI data **based on the linear SSN dependencies (7) and (8)**. For the velocity the fit parameters from the double lognormal fit (5) and their balancing function (9) are given. **The numbers in parentheses are the estimated standard deviations of the fit parameters referred to the corresponding last digits of the quoted value.** The listed SSN time lags are used for the fits.

Parameter	Median		Mean Scaling factor a_{avg}	Balance		SSN lag [years]
	SSN factor a_{med}	Baseline b_{med}		SSN factor c_a	Baseline c_b	
Magnetic field [nT]	$1.309(19) \times 10^{-2}$	4.285(17)	$8.786(78) \times 10^{-2}$	—	—	0
Density [cm^{-3}]	$3.81(25) \times 10^{-3}$	4.495(26)	$3.050(27) \times 10^{-1}$	—	—	6
Temperature [10^4 K]	$1.974(26) \times 10^{-2}$	5.729(19)	$6.541(28) \times 10^{-1}$	—	—	3
Velocity W_1 [10^2 km s^{-1}]	—	3.633(12)	$1.008(37) \times 10^{-2}$	$-1.799(95) \times 10^{-3}$	0.638(32)	3
W_2	—	4.831(81)	$2.31(20) \times 10^{-2}$	—	—	—

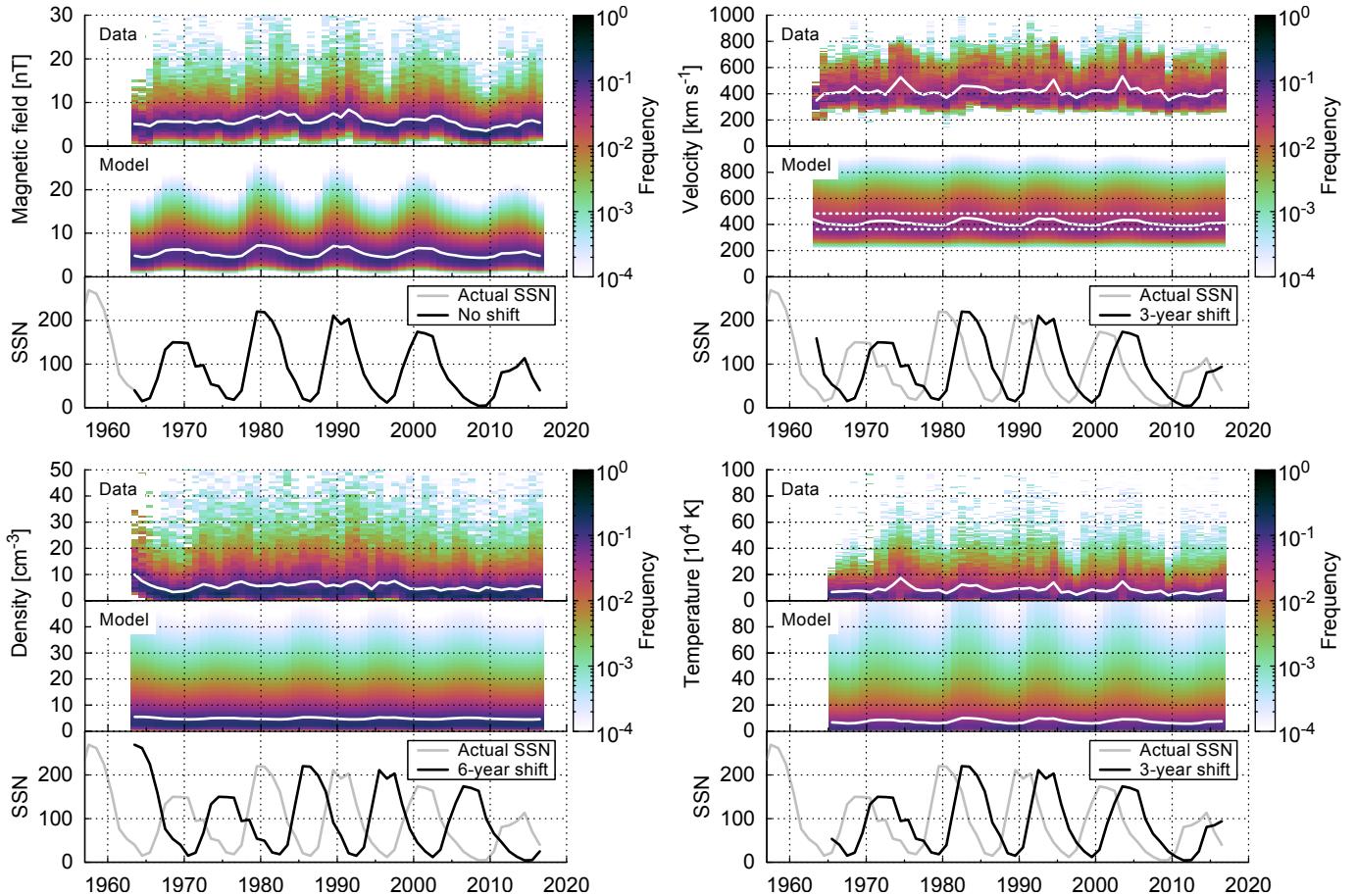


Fig. 4. Solar wind parameter yearly data frequencies and lognormal fit models, both with their median values (white lines) over the OMNI time period 1963–2016. The corresponding yearly SSN and the for the models shifted SSN are indicated by grey and black lines. The velocity median is derived from the SSN weighted constant lognormal parts (dotted lines).

The fit result (see Table 2) yields a model in which three years after solar cycle minimum (SSN of zero) the contribution of slow solar wind to the overall solar wind distribution reaches a maximum value of about 64 % and decreases with increasing SSN as shown in Fig. 6.

To investigate the amount of slow and fast wind contributions depending on solar activity, we apply the commonly used constant velocity threshold of $v_{\text{th}} = 400 \text{ km s}^{-1}$ (Schwenn 1990, p. 144). The linear fit to the yearly data ratio and the derived model ratio show a good agreement (see Fig. 6). Specific velocity thresholds between slow and fast solar wind cannot be directly compared with the to some degree steeper balance parameter of the double fit function used in this model. However, it appears being likely a more realistic approach than just taking a specific velocity threshold for the slow and fast wind, in agree-

ment with the overlapping nature of the velocity flows reported by McGregor et al. (2011a).

4. Solar distance dependency

In order to derive heliocentric distance relationships of the bulk solar wind distribution functions, we apply and fit a power law dependency to the Helios data. We evaluate the fits’ extrapolation behavior in direction to the Sun, because in a subsequent step it will be extrapolated to the PSP orbit. We use the fitting methods of Sect. 2 for the distance-binned combined data from both Helios probes. Helios’ highly elliptical orbits in the ecliptic covered a solar distance range of 0.31–0.98 au in case of Helios 1 and 0.29–0.98 au in case of Helios 2. Launched during solar cycle minimum, the data of both probes cover the rise to the maxi-

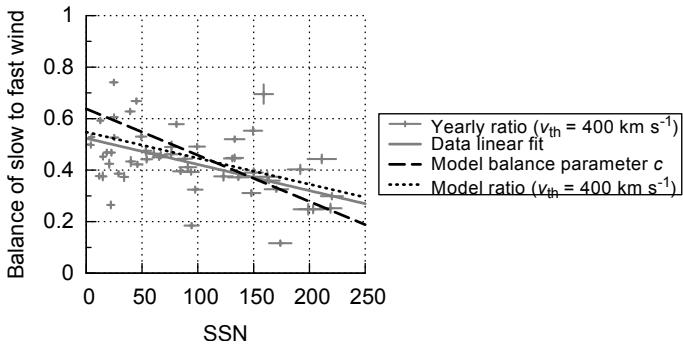


Fig. 6. Ratio of slow to fast solar wind for a by 3 years lagged SSN. The yearly ratios (+) and their weighted linear fit (solid line) are obtained from OMNI data with a threshold velocity of $v_{th} = 400 \text{ km s}^{-1}$. The error bars denote the SSN standard deviation and the relative weight from the yearly data coverage. The model's balance parameter (9) and derived ratio (same threshold) are plotted as dashed and dotted lines.

mum of cycle 21, covering ~ 6.5 years at varying distances to the Sun.

In the same way as the OMNI data we investigate hourly averages of the Helios data. The Helios 1 merged hourly data from the magnetometer and plasma instruments (Rosenbauer et al. 1977) include ~ 12.5 orbits for the time range 10 December 1974 until 14 June 1981, those for Helios 2 include ~ 8 orbits for the time span 1 January 1976 until 4 March 1980. The data are retrieved from the Coordinated Data Analysis Web (CDAWeb) interface at NASA's GSFC/SPDF⁵.

The Helios 1 magnetometer data coverage for this data set is about 43 % (i.e., 2.8 years), that of Helios 2 amounts to 54 % (i.e., 2.3 years). The plasma data coverage is 76 % (i.e., 5.0 years) in case of Helios 1 and 92 % (i.e., 3.9 years) in case of Helios 2. Thus, using this data, one has to keep in mind that its time coverage is unequally distributed over the solar cycle. Considering the data gap distributions, the amount of data during solar cycle minimum up to mid 1977, that is, the transition from minimum to maximum, covers about 68 % whereas during maximum of cycle 21 data are available only 38 % of the time. This Helios data bias towards solar minimum is the reason why in this study the Helios solar wind data are not used to derive long-term frequency distributions and solar cycle dependencies for the key solar wind parameters.

The radial dependencies of the key solar wind parameters over the distance range 0.29–0.98 au measured by both Helios probes are plotted in Fig. 7, together with their median and mean values for different solar distances, calculated for the minimal distance resolution 0.01 au of the data set. Assuming a radial solar wind outflow, it is expected that the distance dependence of the solar wind parameters over the Helios data range 0.29–0.98 au can be described through power law scaling. Therefore we use the power law function

$$x(r) = d \cdot r^e \quad (10)$$

for the regression fit of the median and mean, with r being the solar distance in astronomical units, d the magnitude at 1 au and e the exponent. The fits are weighted through the different data counts per bin. **The obtained coefficients for the median and mean power law fits (d_{med} , e_{med} , d_{avg} and e_{avg}) are listed in Table 3 and their corresponding curves are shown in Fig. 7.**

Our derived exponents agree with those found in existing studies from the Helios observations: Mariani et al. (1978) de-

rived the exponents for the magnetic field strength separately for the fast and the slow solar wind as $B_{fast} \propto r^{-1.54}$ and $B_{slow} \propto r^{-1.61}$, ours is $B_{avg} \propto r^{-1.55}$. The velocity exponent $v_{avg} \propto r^{0.049}$ matches with the values found by Schwenn (1983, 1990), who derived the distance dependencies for both Helios spacecraft separately as $v_{H1} \propto r^{0.083}$ and $v_{H2} \propto r^{0.036}$. The calculated density exponent $n_{avg} \propto r^{-2.01}$ agrees well with the Helios plasma density model derived by Bougeret et al. (1984), yielding $n \propto r^{-2.10}$. The temperature exponent $T_{avg} \propto r^{-0.79}$ is similar to those in the studies by Hellinger et al. (2011, 2013), who also derived the exponents separately for the fast and the slow solar wind: $T_{fast} \propto r^{-0.74}$ and $T_{slow} \propto r^{-0.58}$.

The mean and median velocity fit exponents acquired from the Helios data are very similar, which indicates that they just as well can be kept identical so that the basic shape of the frequency distribution does not change with distance. Contrary, the mean and median fits for the magnetic field strength cross each other at 0.339 au (see Table 3) and the mean is **getting slightly lower than the median at smaller distances**. Thus, below that distance the **frequency distribution** cannot well be described anymore by a lognormal function, **because the mean of a lognormal function has to be larger than its median** (as mentioned in Sect. 2), that is, **the location of the crossing indicates that the parameter's distribution is not anymore of a lognormal shape thereafter**. The fits for the proton temperature show a similar behavior, having an **extrapolated intersection** at 0.082 au. Therefore the extrapolation of the magnetic field and temperature distribution frequencies to the PSP orbit by applying lognormal functions is limited. **The crossing points limit the regions where the distribution's shapes can still be considered lognormal.**

In order to still fit and extrapolate lognormal functions with the data, we assume that the shapes can be considered lognormal at all distances. For the coming frequency distribution fit function we reduce the fit exponents e_{med} and e_{avg} to only one. It should be noted that this simplification leads to slightly larger modeling errors, especially in case of the magnetic field strength.

Next we retrieve the frequency distributions of the four **solar wind parameters in solar** distance bins of 0.01 au, choosing the same resolution as for the OMNI data analyzed in Sect. 2—the distributions **and their median values** are plotted in Fig. 8. For simplification, as mentioned before, we treat the exponents of the median and mean fit functions as being identical, **using one fit parameter for both**. Implementing the power law distance dependency (10) into the lognormal function (4), we get the fit parameters d'_{med} , d'_{avg} and **the common exponent e'** . Again, we use the double lognormal function (5) for the velocity distribution fit, resulting in $W''_{II}(x, r)$. The additional fit parameters are the balancing parameter c' and for the second lognormal part $d'_{med,2}$ and $d'_{avg,2}$. The resulting fit coefficients for the four solar wind parameters are presented in Table 4.

The velocity balancing parameter $c' = 0.557$ is in good agreement with the results for the SSN dependency (9), because with a mean SSN of 59 during the Helios time period, $c(59) = 0.53$, as can be seen from Fig. 6.

The power law lognormal models and the power law double lognormal model for the velocity, which result from the fitting, are plotted in Fig. 8 together with their median values. The model's magnetic field strength is broader around values of 40 nT at the lower distance boundary than the data's frequency distribution implies. This behavior is expected because of the distance independent shape approximation applied. The velocity

⁵ <http://spdf.gsfc.nasa.gov/>

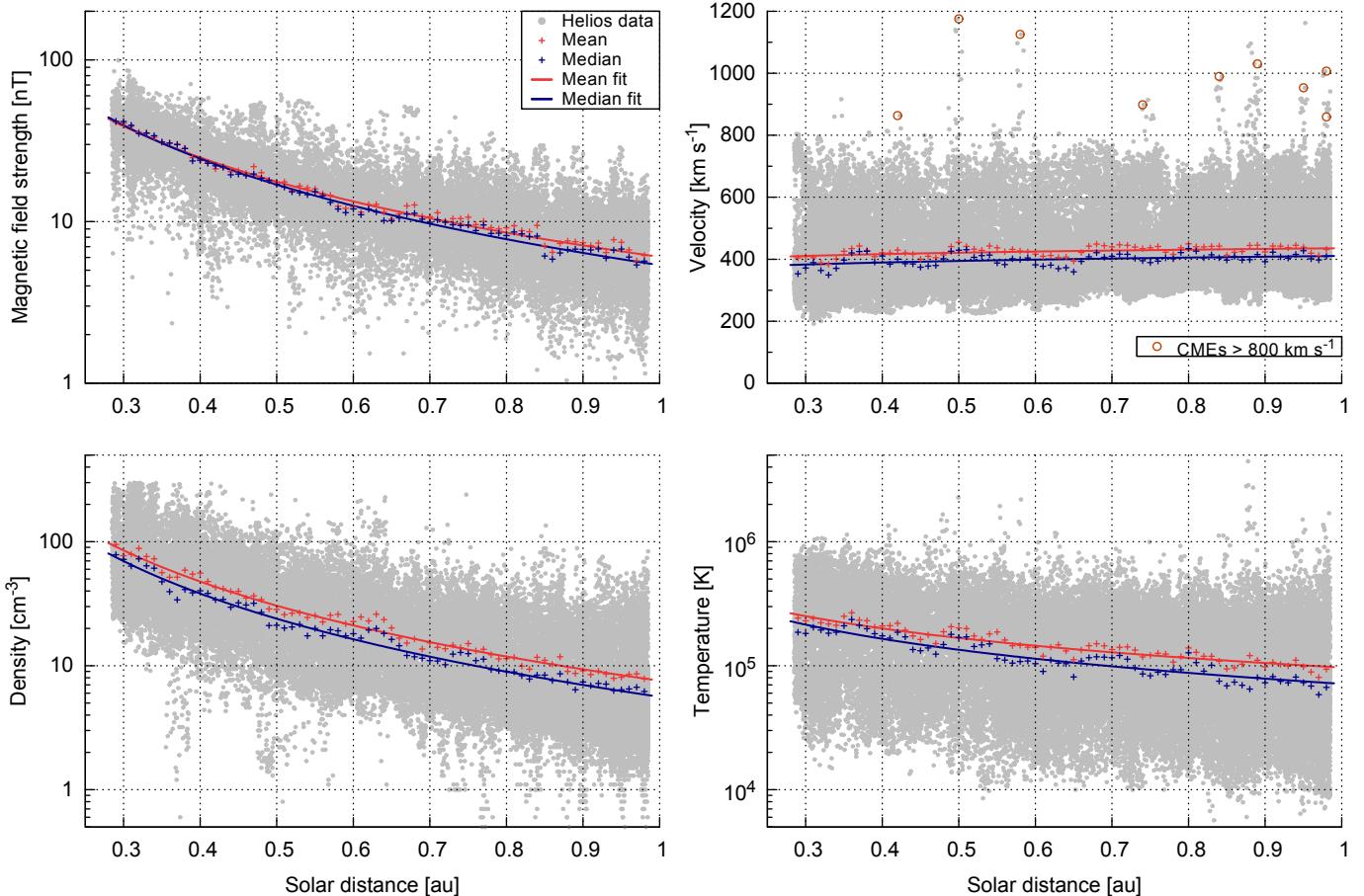


Fig. 7. Helios hourly data plots of the four solar wind parameters over solar distance. The mean and median per 0.01 au data bin and their fit curves are plotted as well. The Helios data has a native distance resolution of 0.01 au, thus, to make the abundance visible in these plots, we added a random distance value of up to ± 0.005 au. The high velocity data points above 800 km s^{-1} (circled red) are identified as CME events (e.g., Bothmer & Schwenn 1998).

Table 3. Fit coefficients for the median and mean solar distance dependencies (10) of the four solar wind parameters derived from the combined Helios 1 and 2 data. The numbers in parentheses are the estimated standard deviations of the fit parameters referred to the corresponding last digits of the quoted value. The crossing distances indicate where the median and mean fits intersect each other. The yearly variation is the weighted standard deviation derived from the yearly fit exponents seen in Fig. 9.

Parameter	Median		Mean		Crossing distance [au]	Yearly variation Δe
	d_{med}	e_{med}	d_{avg}	e_{avg}		
Magnetic field [nT]	5.377(92)	-1.655(17)	6.05(10)	-1.546(18)	0.339(11)	0.11
Velocity [10^2 km s^{-1}]	4.107(28)	0.058(13)	4.356(24)	0.049(10)	$0.7(83) \times 10^3$	0.012
Density [cm^{-3}]	5.61(27)	-2.093(46)	7.57(30)	-2.010(38)	0.027(73)	0.072
Temperature [10^4 K]	7.14(23)	-0.913(39)	9.67(21)	-0.792(28)	0.082(85)	0.050

Table 4. Fit coefficients for the distance depending single lognormal function, based on equation (4) combined with (10), respectively double lognormal function (5) for the velocity from the combined Helios data. The numbers in parentheses are the estimated standard deviations of the fit parameters referred to the corresponding last digits of the quoted value. The seasonal variations are calculated from Earth's orbital solar distance variation and the derived exponents.

Parameter	Median d'_{med}	Mean d'_{avg}	Exponent e'	Balance c'	Seasonal variation $\Delta d [\%]$	
Magnetic field [nT]	5.358(25)	5.705(28)	-1.662(11)	-	2.8	
Density [cm^{-3}]	5.424(33)	6.845(47)	-2.114(20)	-	3.6	
Temperature [10^4 K]	6.357(64)	10.72(14)	-1.100(20)	-	1.9	
Velocity [10^2 km s^{-1}]	W''_1 5.26(13)	3.707(13) 5.42(11)	3.748(16) 4.47(11) ^a	0.0990(51) -	0.557(45) -	0.17 -
	W''_2	W''_{II}				
	4.13(13) ^a	4.47(11) ^a				

Notes. ^(a) Velocity median and mean 1 au values for the resulting function. Error estimates derived from the individual fit part errors.

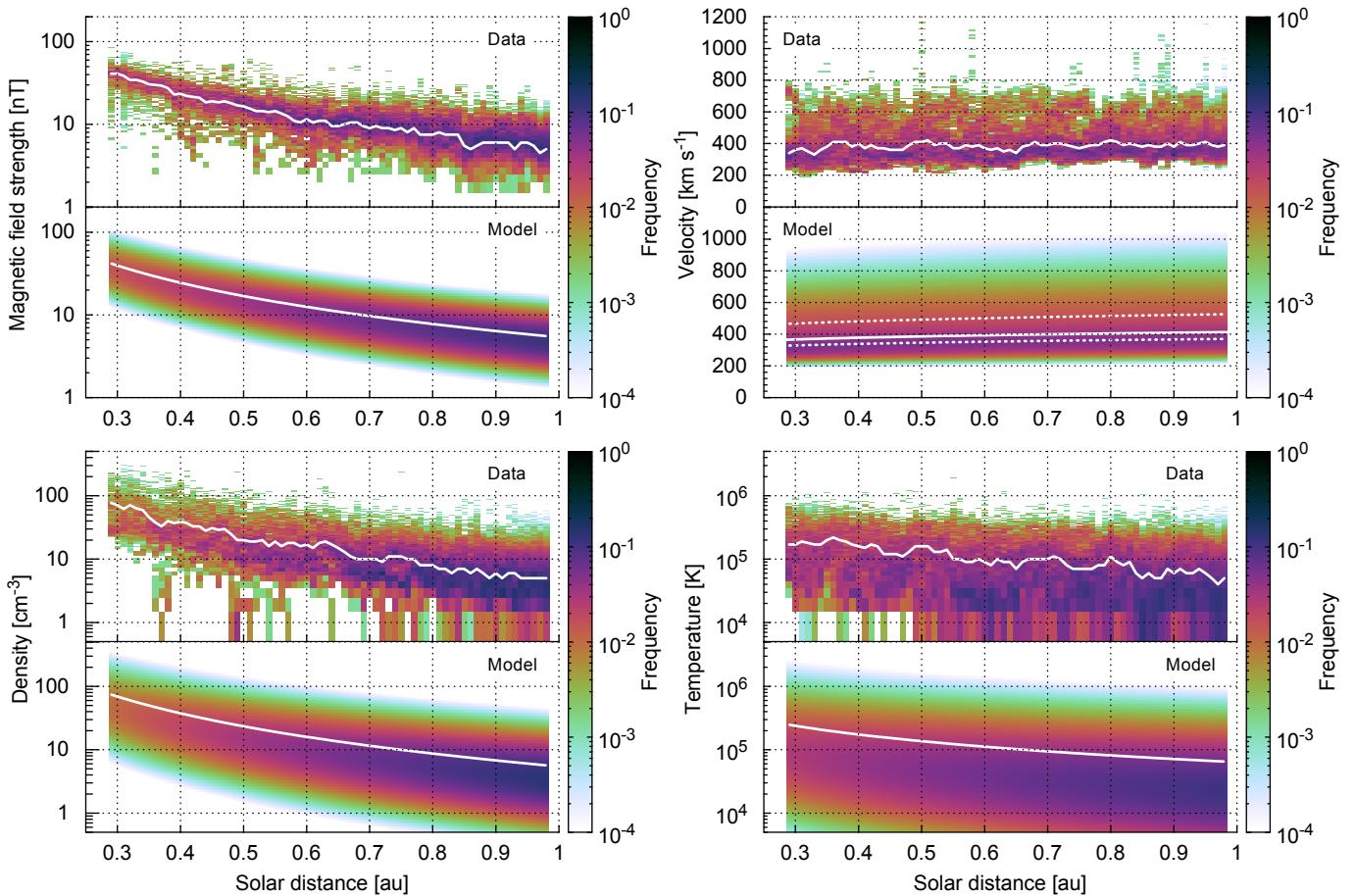


Fig. 8. Frequency distributions of the four solar wind parameters with respect to the solar distance. Plotted are the binned Helios data and the power law lognormal fit models with their median values (white lines). The double lognormal model is used for the velocity, its slow and fast parts are indicated by dotted lines.

and temperature models' upper values generally show a higher abundance than the actual data, see also zoom boxes in Figs. 1 and 2. **The increasing high velocity tail with distance arises** from using the same exponent for both slow and fast components. This effect is not seen in the data, more specifically, not only the slowest wind but also the fastest wind is expected to converge to more average speeds (Sanchez-Diaz et al. 2016).

5. Empirical solar wind model

In order to estimate the solar wind environment for the PSP orbit, we combine the results from the solar wind frequency distributions' solar activity relationships and their distance dependencies derived from the OMNI and Helios data. The result is an empirical solar wind model for the inner heliosphere which will then be extrapolated to the PSP orbit in Sect. 6.

This solar wind model for the radial distance dependence is representative for the time of the Helios observations around the rise of solar cycle 21. The variations of the yearly power law fit exponents from fitting the solar distance dependency (10) are shown in Fig. 9 together with the yearly SSN for the time period 1974–1982. It can be seen that during the Helios time period there might be some systematic variation of the exponents with solar activity—at least for the velocity and temperature exponents. However, for simplicity we assume, that the distance scaling laws can be treated as time independent and include the calculated exponents' yearly variations Δe , summarized in Table 3, as relative uncertainties.

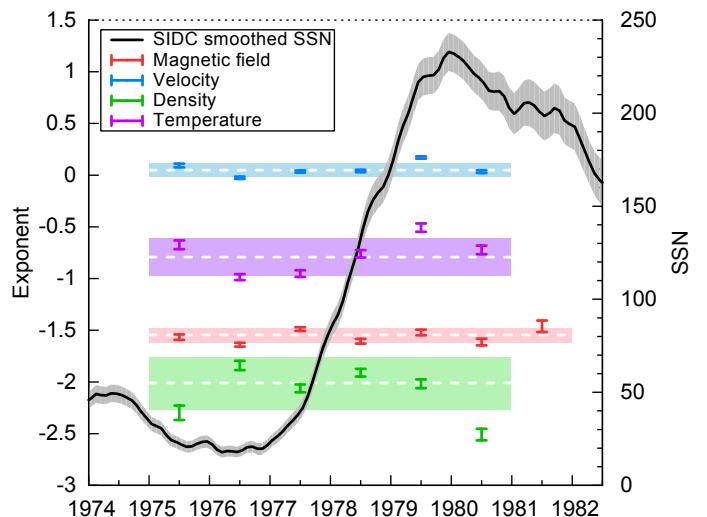


Fig. 9. Helios yearly variation of the solar wind parameter power exponents for the dependence on radial distance together with the SIDC 13-month smoothed monthly SSN. The weighted standard deviations and average values for all years are indicated by the shaded areas. In this plot the 21 days since Helios launch in the year 1974 are omitted because a distance range of merely 0.95–0.98 au was covered that year.

Since we neglect possible variations of the distance scaling laws, we combine the frequency distribution's median solar ac-

tivity dependency (7) derived for 1 au from the OMNI data with the power law exponents (10) derived from the Helios data:

$$x_{\text{med}}(ssn, r) = (a_{\text{med}} \cdot ssn + b_{\text{med}}) \cdot r^{e'} . \quad (11)$$

Thus, **implementing the median and average relations into the lognormal function (4)**, we obtain the combined model function $W'''(x, ssn, r)$ and for the velocity $W''''(x, ssn, r)$ with the double lognormal function (5). **The corresponding median and average relations for each solar wind parameter, based on values resulting from our analyses, are listed below.** Their numerical values are the fit parameters from Table 2 and the exponents from Table 4.

- The magnetic field strength relations, depending on solar activity and solar distance, are:

$$B_{\text{med}}(ssn, r) = (0.0131 \text{ nT} \cdot ssn + 4.29 \text{ nT}) \cdot r^{-1.66} , \quad (12)$$

$$B_{\text{avg}}(ssn, r) = 1.0879 \cdot B_{\text{med}}(ssn, r) . \quad (13)$$

- The proton velocity relations for the slow and fast components, depending on solar distance, are:

$$v_{\text{med}}^{\text{slow}}(r) = 363 \text{ km s}^{-1} \cdot r^{0.099} , \quad v_{\text{med}}^{\text{fast}}(r) = 483 \text{ km s}^{-1} \cdot r^{0.099} \quad (14)$$

$$v_{\text{avg}}^{\text{slow}}(r) = 1.0101 \cdot v_{\text{med}}^{\text{slow}}(r) , \quad v_{\text{avg}}^{\text{fast}}(r) = 1.023 \cdot v_{\text{med}}^{\text{fast}}(r) . \quad (15)$$

The share of both components is found to be balanced with solar activity:

$$c(ssn) = -0.00180 \cdot ssn + 0.64 . \quad (16)$$

- The derived relations of the proton density are:

$$n_{\text{med}}(ssn, r) = (0.0038 \text{ cm}^{-3} \cdot ssn + 4.50 \text{ cm}^{-3}) \cdot r^{-2.11} , \quad (17)$$

$$n_{\text{avg}}(ssn, r) = 1.305 \cdot n_{\text{med}}(ssn, r) . \quad (18)$$

- The derived proton temperature relations are:

$$T_{\text{med}}(ssn, r) = (197 \text{ K} \cdot ssn + 57\,300 \text{ K}) \cdot r^{-1.10} , \quad (19)$$

$$T_{\text{avg}}(ssn, r) = 1.654 \cdot T_{\text{med}}(ssn, r) . \quad (20)$$

These relations average over seasonal variations because they are based on yearly data. As the OMNI data are time-shifted to the nose of the Earth's bow shock, this leads to yearly solar distance variations of $\pm 1.67\%$ as it orbits the Sun. The resulting maximal solar wind parameter variation amplitudes over the year can thus be derived from the derived power law exponents. They are estimated to be smaller than 4 % as seen in Tab. 4. Bruno et al. (1986) and Balogh et al. (1999) have pointed out, that the solar wind parameters vary with latitudinal separation from the heliospheric current sheet (HCS). Its position in heliographic latitude is highly variable around the solar equator (Schwenn 1990), furthermore, the Earth's orbit varies over the course of the year by $\pm 7.2^\circ$ in latitude. **Since this latitudinal separation is highly variable, and requires significant effort to calculate for an extended time series, we have ignored this aspect in this analysis.**

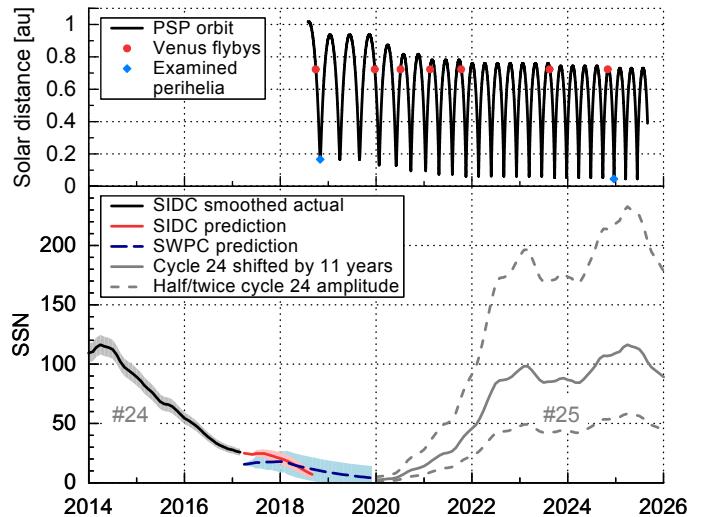


Fig. 10. PSP's solar distance during its mission time (top). Consecutive Venus flybys bring its perihelia nearer to the Sun. Actual and predicted SSN (bottom), that is, SIDC 13-month smoothed monthly actual SSN, SIDC **Standard Curves Kalman filter** prediction, SWPC prediction and by 11 years shifted SSN from previous cycle 24, together with two alternative trends of half and twice its amplitude.

6. Model extrapolation to PSP orbit

To estimate PSP's solar wind environment during its mission time for its orbital positions, **predictions of the SSN during the mission are incorporated into the empirical solar wind model derived in the previous sections** and extrapolations down to the PSP perihelion region are performed.

Parker Solar Probe is planned to launch in mid 2018. With its first Venus flyby it will swing into Venus' orbital plane, reaching already 93 days after launch in November 2018 a first perihelion with a distance of 0.16 au. Seven additional Venus flybys allow the **perihelion distance to be reduced** to a minimum of $9.86 R_\odot$. **This distance will be reached with the 22nd perihelion in December 2024** (Fox et al. 2015) as plotted in the top panel of Fig. 10.

We extrapolate the derived empirical solar wind **models** to PSP's orbital distance range and compare the results with those from the existing models shown in Fig. 11. **The model and the extrapolation are visualized for the SSN range between solar minimum and maximum ($0 \leq ssn \leq 200$), indicated by the shaded regions in the figure.** The magnetic field strength is found to increase from median values of about 43 nT at 0.25 au to 715 nT at 0.046 au for a SSN of 0. Taking a SSN of 200 increases the values to 69 nT and 1152 nT. Our extrapolation results are slightly flatter than those derived from the analytical magnetic field model by Banaszkiewicz et al. (1998), who constructed an analytic dipole plus quadrupole plus current sheet (DQCS) model for solar minimum. **It should be noted that one cannot straightforwardly compare the absolute values of our study with the values obtained by Banaszkiewicz et al. (1998) because the DQCS model assumes solar wind originating from coronal holes at higher heliographic latitudes only, neglecting the slow solar wind belt.** We suggest that the difference in slope is due to the previously mentioned (Sect. 4) changing shape of the frequency distribution with heliocentric distance, which for smaller distances deviates more from the model's lognormal distribution. The average velocity is found to decrease from 340 km s^{-1} at 0.25 au to about 290 km s^{-1} at 0.046 au **3 years after a SSN of 0 occurred, whereas** using a

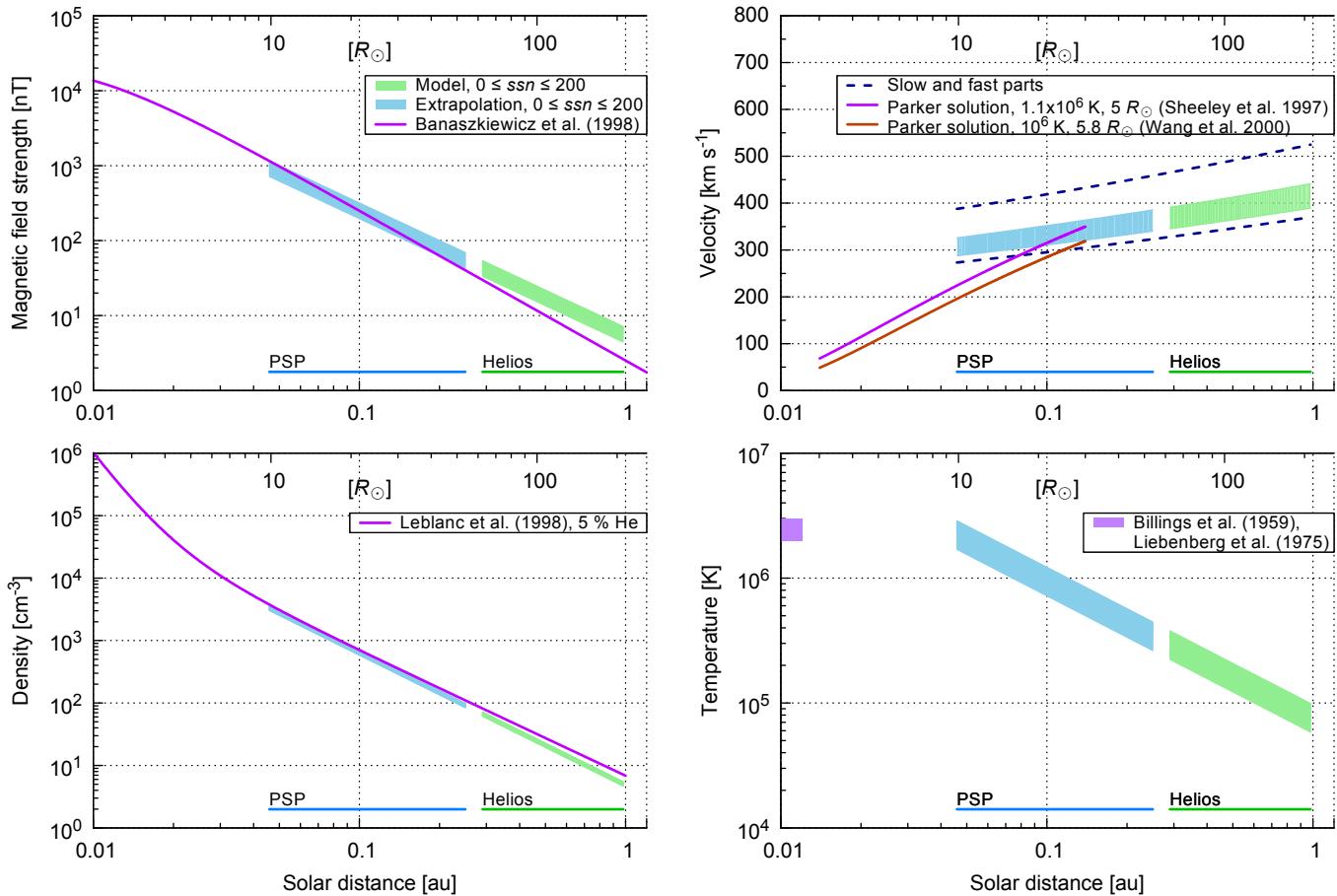


Fig. 11. Radial extrapolation of the solar wind median parameters to the PSP orbit region. The models obtained from Helios and OMNI measurements are extrapolated to the PSP region for SSN values between solar minimum and maximum, i.e., $0 \leq \text{ssn} \leq 200$. The lower edges of the shaded areas correspond to solar minimum, the upper edges to solar maximum. Also plotted are the radial dependencies of the analytic DQCS magnetic field model for solar minimum from Banaszkiewicz et al. (1998), the slow wind velocity models from Sheeley et al. (1997) and Wang et al. (2000), the density model from Leblanc et al. (1998) and the range of temperature measurements from Billings (1959) and Liebenberg et al. (1975).

SSN of 200 it decreases from 390 km s^{-1} to 330 km s^{-1} . Comparing the results with the measurements by Sheeley et al. (1997) and Wang et al. (2000) shows an overestimation in our extrapolated slow solar wind velocity values for distances below about $20 R_{\odot}$. They used LASCO coronagraph observations to track moving coronal features (blobs) in the distance range 2 – $30 R_{\odot}$ to determine speed profiles and sources of the slow solar wind and they derived temperature and sonic point values for slow solar wind with the isothermal expansion model from Parker (1958). Therefore, it generally can be expected that PSP will encounter a slower solar wind environment close to the Sun than our model estimates. Thus PSP will measure solar wind acceleration processes (McComas et al. 2008), maybe even still at $30 R_{\odot}$ as the study by Sheeley et al. (1997) suggests. The proton density increases from about 84 cm^{-3} at 0.25 au to about 3018 cm^{-3} at 0.046 au **6 years after a SSN of 0 occurred**. Being almost independent of the SSN the values for a SSN of 200 are only 17 % larger. The results are in good agreement with those of Leblanc et al. (1998), who derived an electron density model from type III radio burst observations. Their model shows that the density distance dependency scales with r^{-2} and steepens just below $10 R_{\odot}$ with r^{-6} . We assumed a solar wind helium abundance of 5 % to convert these electron densities to proton densities. The extrapolated proton temperature increases from about $260\,000 \text{ K}$ at 0.25 au to about $1\,690\,000 \text{ K}$ at 0.046 au **3 years after a SSN of 0 occurred**.

0 occurred and from $440\,000 \text{ K}$ to $2\,860\,000 \text{ K}$ for a SSN of 200. Knowing that near-Sun coronal temperatures are in the range of 2 – 3 MK (Billings 1959; Liebenberg et al. 1975), the model **overestimates** the extrapolated temperatures at the PSP perihelion distance.

Aside from the solar distance the derived solar wind parameter models depend on the SSN. Short-term predictions of the SSN can be used for the solar wind predictions of PSP's early perihelia and also for refining the solar wind predictions during PSP's mission. Several sources are available for SSN short-term predictions. The SIDC provides 12-month SSN forecasts⁶ obtained from different methods (e.g., Kalman filter **Standard Curve** method). The SSN prediction of NOAA's Space Weather Prediction Center (SWPC) follows for the time period until end of 2019 a consensus of the Solar Cycle 24 Prediction Panel⁷. The SSN for PSP's first perihelion will be small—certainly below 20, whereas **the SSN during the closest perihelia, which will commence at the end of 2024 at the likely maximum phase of cycle 25, cannot be predicted at this time. However Hathaway & Upton (2016) found indications that the next solar cycle will be similar in size to the current cycle 24. Therefore we simply assume a pattern similar to**

⁶ <http://sidc.be/silso/forecasts>

⁷ <http://www.swpc.noaa.gov/products/solar-cycle-progression>

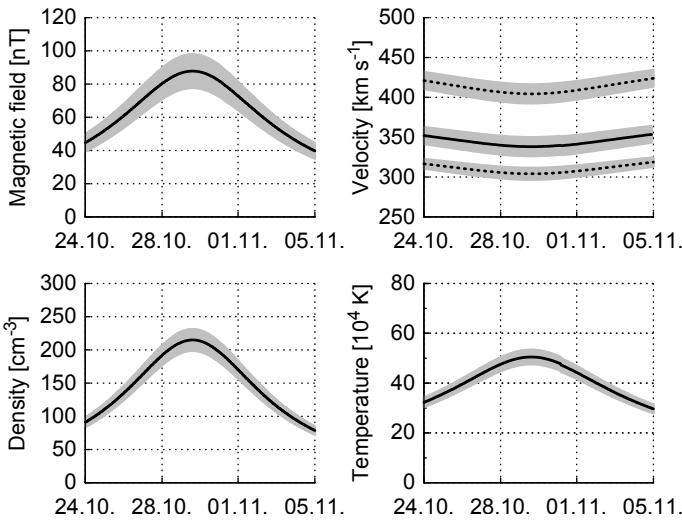


Fig. 12. Estimated solar wind parameter medians (black lines) and their error bands (grey) during 12 days in 2018 with PSP’s first perihelion at about 0.16 au. For the velocity the combined median is calculated and also the SSN-independent slow and fast parts are plotted (dotted lines).

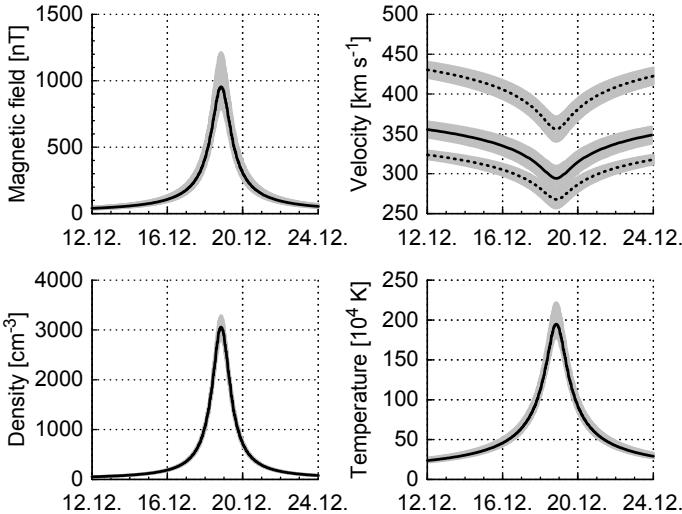


Fig. 13. Estimated solar wind parameter medians (black lines) and their error bands (grey) during 12 days in December 2024 with PSP’s 22nd (the first closest) perihelion at 0.0459 au. For the velocity the combined median is calculated and also the SSN-independent slow and fast parts are plotted (dotted lines).

the last cycle for the prediction of the next solar cycle and thus shift the last cycle by 11 years. Additionally we consider as possible alternatives SSN patterns of half and twice its amplitude as shown in **the bottom panel of Fig. 10**.

Implementing the **SSN predictions** for the PSP mission time and the orbital trajectory data, **we can infer** which solar wind parameter magnitudes can be expected. Figs. 12 and 13 show the **median values (7)** of the considered different solar wind parameters for 12-day periods, comprising the first perihelion in November 2018 and the **first closest** perihelion in December 2024. In the beginning of the mission median values of about 87 nT, 340 km s⁻¹, 214 cm⁻³ and 503 000 K are estimated to be measured at 0.16 au, increasing to about 943 nT, 290 km s⁻¹, 2951 cm⁻³ and 1 930 000 K during the **first closest** approach at 0.046 au. **Monthly SSNs—shifted by the time lags specific to the solar wind parameters—are used in the calculation of the solar wind predictions. These SSNs are either actual**

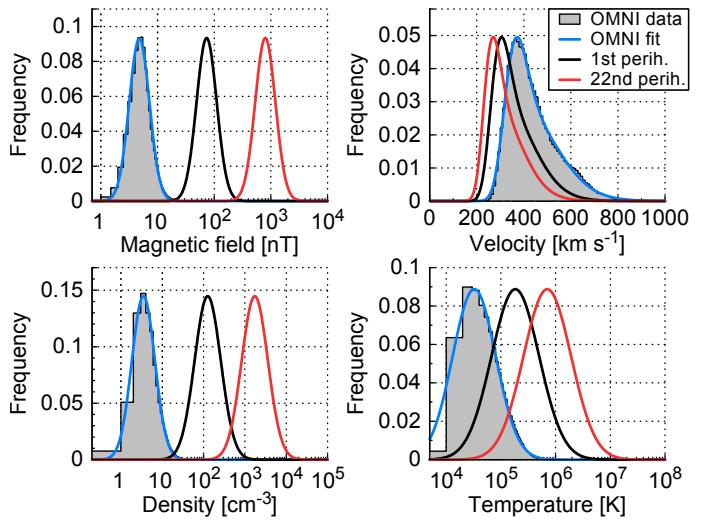


Fig. 14. Frequency distributions of the four solar wind parameters (same as in Figs. 1 and 2) and those estimated with the solar wind model for PSP’s first and 22nd (first closest) perihelion. In these figures the frequencies of both extrapolated curves are scaled for visibility to the same height as the 1 au distribution.

smoothed values from the SIDC with their reported standard deviations, short-term predictions from the SWPC with their expected ranges or actual smoothed values from the SIDC shifted by 11 years with half/twice their values as uncertainties. The error bands given in both figures, calculated from error propagation, include these SSN ranges and the derived fit parameter errors.

Finally the estimated solar wind environment can be derived from the function $W'''(x, ssn, r)$. The estimated frequency distributions of the four solar wind parameters at PSP’s first and 22nd (first closest) perihelia are plotted in Fig. 14. Note again that the velocity and temperature distributions for the 22nd perihelion are only upper limits and the actual by PSP to be encountered values are expected to be smaller.

7. Discussion and summary

The scientific objective of this study, being part of the German contribution Coronagraphic German and US Solar Probe Plus Survey (CGAUSS) to the Wide field Imager for Solar Probe (WISPR), is to model the solar wind environment for the Parker Solar Probe mission (formerly Solar probe Plus) to be launched mid 2018.

For this purpose we started the development of the empirical solar wind environment model for the near-ecliptic PSP orbit by **deriving lognormal representations of the** in situ near-Earth solar wind data collected in the OMNI database, using the frequency distributions of the key solar wind parameters magnetic field strength, **proton** velocity, density and temperature. Throughout the different analyses in our study the velocity’s frequency distribution is treated as a composition of a slow and a fast wind distribution. Each velocity part is fitted with a log-normal function, which allows for the overlap of both velocity ranges. The OMNI multi-spacecraft solar wind data is intercalibrated and covers almost five solar cycles. It thus represents solar wind gathered at different phases of solar activity in the ecliptic plane. In the next step we investigated the yearly variation of the solar wind distribution functions along with the SSN

over 53 years and derived linear dependencies of the solar wind parameters with the SSN. The radial dependencies of the solar wind distribution functions were then analyzed using Helios 1 and 2 data for the distance range 0.29–0.98 au in bins of 0.01 au, **deriving power law fit functions that** were used to scale the prior calculated SSN-dependent 1 au distribution fit functions to the PSP orbit, **taking into account** SSN predictions for the years 2018–2025, **encompassing the prime mission up to the closest approach of** $9.86 R_{\odot}$. The reason for performing the analysis this way is based on the fact that the OMNI solar wind database is much larger than the Helios database.

For determining solar activity and solar distance dependent relations for the median and average solar wind values, we could have used the simpler approach of combining the radial dependence of averaged Helios data with averaged 1 au OMNI data scaled with the SSN. It is expected that the results of a simpler analysis would have similar distance scaling results, as can be inferred from the exponents in Tables 3 and 4. However, in our study we are not only interested in averages but rather in bulk distributions, that is, the whole range of values that might occur. For the determination of the frequency distributions the use of the more complex fit model is important, because the distance between median and average values determines the width of the lognormal distributions.

It is clear that the calculated distribution functions just represent first order estimates of the real solar wind to be encountered by PSP. The solar wind environment to be encountered will depend at times of PSP on the structure of the solar corona and underlying photospheric magnetic field and on the evolution and interaction of individual solar wind streams and superimposed CMEs and shocks. However, the derived results are in good agreement with existing studies about near-Sun solar wind magnetic field strengths and densities as shown in Sect. 6. The extrapolation results of the velocity and the temperature differ from the direct measurements seen in existing studies. This suggests that below about $20 R_{\odot}$ PSP may dive into the region where the acceleration and heating of the solar wind is expected to occur (see Fig. 11). The near-Sun solar wind velocity at PSP perihelion is also expected to be slower than our model estimates, because the solar wind is assumed to be accelerated up to the height of the Alfvénic critical surface, which is predicted to lie on average around $17 R_{\odot}$ (e.g., Sittler & Guhathakurta 1999; Exarhos & Moussas 2000), scaling with solar activity within a range of between $15 R_{\odot}$ at solar minimum and $30 R_{\odot}$ at solar maximum (Katsikas et al. 2010; Goelzer et al. 2014).

We have not specifically investigated the occurrences of extreme solar wind parameters caused by CMEs or enhanced values due to stream interaction or co-rotating interaction regions. The Helios solar wind measurements plotted over radial distance in Fig. 7 show several extreme values far above the usual solar wind velocities, likely to be associated with individual CMEs. The results by Sachdeva et al. (2017) indicate that due to **solar wind drag**, the speeds of fast CMEs will commonly slow down substantially from early distances of a few solar radii. Therefore, it is expected that PSP will encounter CMEs with much higher speeds than those observed during the Helios mission. Also, the magnetic field, density and temperature values are expected to be much larger than in the average solar wind in individual fast shock associated CME events. PSP will thus also substantially improve our understanding of the near-Sun evolution of CMEs and their expansion with radial distance.

With the resulting CGAUSS empirical solar wind model for PSP the following main results for the bulk solar wind parameters and estimations for their median values at PSP's first perihelion in 2018 at a solar distance of 0.16 au and at PSP's closest perihelia beginning in 2024 at 0.046 au ($9.86 R_{\odot}$) are obtained:

- The dependency of the magnetic field strength **on solar activity and radial distance appears** valid above $20 R_{\odot}$, however near PSP's closest perihelion the actual values might be found to be slightly higher.
- The estimated magnetic field strength **median values (12)** for PSP's first and **first** closest perihelion are 87 nT and 943 nT.
- The radial dependencies of the proton velocity median values for slow and fast solar **wind (14) appear** valid above about $20 R_{\odot}$ solar distance, below they overestimate the actual solar wind velocities obtained from remote measurements. The share of their frequency distributions to the overall solar wind velocity distribution (5) is depending on solar activity **with their balance relation (16)**. Thus, at solar minimum with a SSN around 0 the slow wind **component** contributes about 64 % and **drops** to 28 % during solar maximum conditions with a SSN around 200.
- The calculated median velocity values for PSP's first and **first** closest perihelion are 340 km s^{-1} and 290 km s^{-1} .
- The **proton density relation appears** valid throughout the full PSP orbital distance range, even down to about $8 R_{\odot}$.
- The estimated density **median values (17)** for PSP's first and **first** closest perihelion are 214 cm^{-3} and 2951 cm^{-3} .
- The derived correlation function for the **proton temperature appears** to provide too high temperature values **around PSP's closest perihelion** in comparison to coronal measurements.
- The estimated temperature **median values (19)** for PSP's first and **first** closest perihelion are 503 000 K and 1 930 000 K.

The results of the modeled solar wind environment will be useful to help optimize the WISPR and in situ instrument science plannings and PSP mission operations. This also applies for the Heliospheric Imager (SoloHI) (Howard et al. 2013) and the in situ instruments on board the Solar Orbiter spacecraft.

Acknowledgements. The authors acknowledge support of the Coronagraphic German and US SolarProbePlus Survey (CGAUSS) project for WISPR by the German Aerospace Center (DLR) under grant 50 OL 1601 as national contribution to the Parker Solar Probe mission. The authors thank the Helios and OMNI PIs/teams for creating and making available the solar wind in situ data. The Helios and the OMNI data are supplied by the NASA Space Science Data Coordinated Archive (NSSDCA) and the Space Physics Data Facility (SPDF) at NASA's Goddard Space Flight Center (GSFC). Additional thanks for maintaining and providing the international sunspot number series goes to the World Data Center – Sunspot Index and Long-term Solar Observations (WDC-SILSO) at the Solar Influences Data Analysis Center (SIDC), Royal Observatory of Belgium (ROB). The PSP SPICE kernel was kindly provided by Angelos Vourlidas. **The authors thank the referee for the careful review of this manuscript and helpful comments and suggestions.**

References

- Bale, S. D., Goetz, K., Harvey, P. R., et al. 2016, *Space Sci. Rev.*, 204, 49
 Balogh, A., Bothmer, V., Crooker, N. U., et al. 1999, *Space Sci. Rev.*, 89, 141
 Banaszkiewicz, M., Axford, W. I., & McKenzie, J. F. 1998, *A&A*, 337, 940
 Belcher, J. W., Slavin, J. A., Armstrong, T. P., et al. 1991, *Mercury Orbiter: Report of the Science Working Team*
 Biermann, L. 1951, *ZAp*, 29, 274
 Billings, D. E. 1959, *ApJ*, 130, 961
 Bothmer, V. & Daglis, I. A. 2007, *Space Weather – Physics and Effects* (Praxis Publishing)

- Bothmer, V. & Schwenn, R. 1998, *Annales Geophysicae*, 16, 1
 Bougeret, J.-L., King, J. H., & Schwenn, R. 1984, *Sol. Phys.*, 90, 401
 Bruno, R., Villante, U., Bavassano, B., Schwenn, R., & Mariani, F. 1986,
Sol. Phys., 104, 431
 Burt, J. & Smith, B. 2012, in 2012 IEEE Aerospace Conference, 1–13
 Colin, L. 1980, *J. Geophys. Res.*, 85, 7575
 Domingo, V., Fleck, B., & Poland, A. I. 1995, *Sol. Phys.*, 162, 1
 Exarhos, G. & Moussas, X. 2000, *A&A*, 356, 315
 Feldman, W. C., Asbridge, J. R., Bame, S. J., & Gosling, J. T. 1978, *J. Geophys. Res.*, 83, 2177
 Forsyth, R. J., Bothmer, V., Cid, C., et al. 2006, *Space Sci. Rev.*, 123, 383
 Fox, N. J., Velli, M. C., Bale, S. D., et al. 2015, *Space Sci. Rev.*
 Goelzer, M. L., Schwadron, N. A., & Smith, C. W. 2014, *Journal of Geophysical Research (Space Physics)*, 119, 115
 Gosling, J. T., Hildner, E., MacQueen, R. M., et al. 1974, *J. Geophys. Res.*, 79,
 4581
 Gringauz, K. I., Bezrukikh, V. V., Ozerov, V. D., & Rybchinskii, R. E. 1960,
Soviet Physics Doklady, 5, 361
 Gurnett, D. A., Kurth, W. S., Burlaga, L. F., & Ness, N. F. 2013, *Science*, 341,
 1489
 Hathaway, D. H. & Upton, L. A. 2016, *Journal of Geophysical Research (Space Physics)*, 121, 10
 Hellinger, P., Matteini, L., Štverák, Š., Trávníček, P. M., & Marsch, E. 2011,
Journal of Geophysical Research (Space Physics), 116, A09105
 Hellinger, P., Trávníček, P. M., Štverák, Š., Matteini, L., & Velli, M. 2013, *Journal of Geophysical Research (Space Physics)*, 118, 1351
 Howard, R. A., Vourlidas, A., Korendyke, C. M., et al. 2013, in Proc. SPIE, Vol.
 8862, *Solar Physics and Space Weather Instrumentation V*, 88620H
 Kasper, J. C., Abiad, R., Austin, G., et al. 2016, *Space Sci. Rev.*, 204, 131
 Kasper, J. C., Stevens, M. L., Korreck, K. E., et al. 2012, *ApJ*, 745, 162
 Katsikas, V., Exarhos, G., & Moussas, X. 2010, *Advances in Space Research*,
 46, 382
 Kilpua, E. K. J., Madjarska, M. S., Karna, N., et al. 2016, *Sol. Phys.*, 291, 2441
 King, J. H. & Papitashvili, N. E. 2005, *Journal of Geophysical Research (Space Physics)*, 110, A02104
 Lazarus, A. J. 2000, *Science*, 287, 2172
 Leblanc, Y., Dulk, G. A., & Bougeret, J.-L. 1998, *Sol. Phys.*, 183, 165
 Lepping, R. P., Acuña, M. H., Burlaga, L. F., et al. 1995, *Space Sci. Rev.*, 71, 207
 Liebenberg, D. H., Bessey, R. J., & Watson, B. 1975, *Sol. Phys.*, 44, 345
 Mariani, F., Ness, N. F., Burlaga, L. F., Bavassano, B., & Villante, U. 1978,
J. Geophys. Res., 83, 5161
 McComas, D. J., Acton, L. W., Balat-Pichelin, M., et al. 2008, *Solar Probe
 Plus: Report of the Science and Technology Definition Team*, Tech. Rep.
 NASA/TM-2008-214161, National Aeronautics and Space Administration,
 Goddard Space Flight Center, Greenbelt, MD
 McComas, D. J., Alexander, N., Angold, N., et al. 2016, *Space Sci. Rev.*, 204,
 187
 McComas, D. J., Bame, S. J., Barraclough, B. L., et al. 1998, *Geophys. Res. Lett.*,
 25, 1
 McGregor, S. L., Hughes, W. J., Arge, C. N., Odstrcil, D., & Schwadron, N. A.
 2011a, *Journal of Geophysical Research (Space Physics)*, 116, A03106
 McGregor, S. L., Hughes, W. J., Arge, C. N., Owens, M. J., & Odstrcil, D. 2011b,
Journal of Geophysical Research (Space Physics), 116, A03101
 Müller, D., Marsden, R. G., St. Cyr, O. C., & Gilbert, H. R. 2013, *Sol. Phys.*,
 285, 25
 Neugebauer, M. & Snyder, C. W. 1966, *J. Geophys. Res.*, 71, 4469
 Ogilvie, K. W., Chornay, D. J., Fritzenreiter, R. J., et al. 1995, *Space Sci. Rev.*,
 71, 55
 Parker, E. N. 1958, *ApJ*, 128, 664
 Richardson, I. G. & Cane, H. V. 2012, *Journal of Space Weather and Space
 Climate*, 2, A2
 Rosenbauer, H., Schwenn, R., Marsch, E., et al. 1977, *Journal of Geophysics
 Zeitschrift Geophysik*, 42, 561
 Russell, C. T., Mewaldt, R. A., Luhmann, J. G., et al. 2013, *ApJ*, 770, 38
 Sachdeva, N., Subramanian, P., Vourlidas, A., & Bothmer, V. 2017, *Solar
 Physics*, 292, 118
 Sanchez-Diaz, E., Rouillard, A. P., Lavraud, B., et al. 2016, *Journal of Geophys-
 ical Research (Space Physics)*, 121, 2830
 Schwenn, R. 1983, in *NASA Conference Publication*, Vol. 228, NASA Confer-
 ence Publication
 Schwenn, R. 1990, *Large-Scale Structure of the Interplanetary Medium*, ed.
 R. Schwenn & E. Marsch, 99
 Sheeley, N. R., Wang, Y.-M., Hawley, S. H., et al. 1997, *ApJ*, 484, 472
 SILSO World Data Center. 1963–2016, *International Sunspot Number Monthly
 Bulletin and online catalogue*
 Sittler, Jr., E. C. & Guhathakurta, M. 1999, *ApJ*, 523, 812
 Smith, E. J. & Balogh, A. 2003, in *American Institute of Physics Conference Se-
 ries*, Vol. 679, *Solar Wind Ten*, ed. M. Velli, R. Bruno, F. Malara, & B. Bucci,
 67–70
 Stone, E. C., Frandsen, A. M., Mewaldt, R. A., et al. 1998, *Space Sci. Rev.*, 86,
 1
 Veselovsky, I. S., Dmitriev, A. V., & Suvorova, A. V. 2010, *Cosmic Research*,
 48, 113
 Vourlidas, A., Howard, R. A., Plunkett, S. P., et al. 2016, *Space Sci. Rev.*, 204,
 83
 Wang, Y.-M., Sheeley, N. R., Socker, D. G., Howard, R. A., & Rich, N. B. 2000,
J. Geophys. Res., 105, 25133