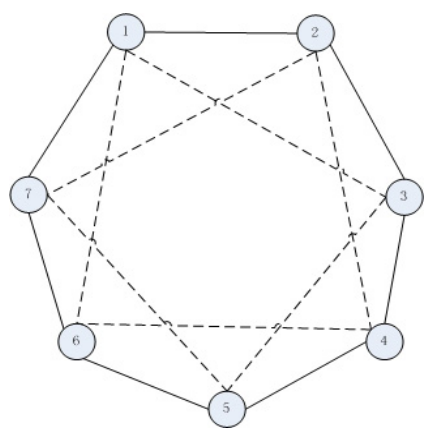
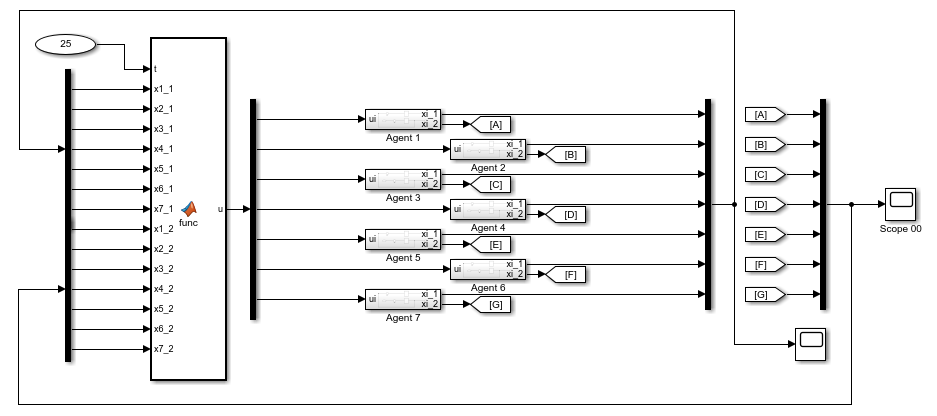
# Q\_04 Simulation Report

Given the following topology,

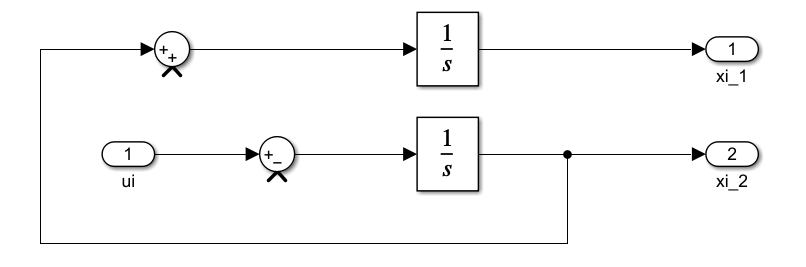
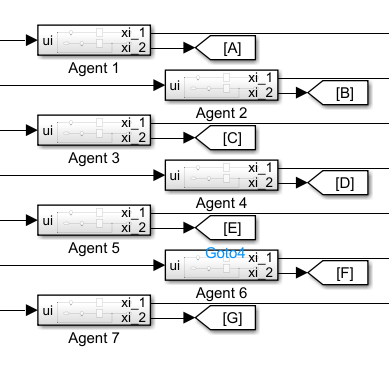


the multi-agent system would be simulated in MATLAB Simulink as in the following figure.



## Agent Dynamics Simulation

Each agent is designed within a subsystem block in which two integrator states are considered as given in the problem. The control signal is the only input to the agents and the outputs are agents' states.



Also the following values have been set as the initial conditions of each agent states.











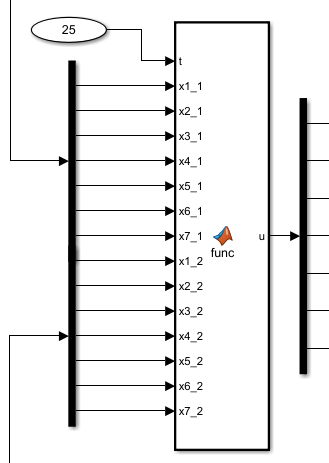




## Agents Input

Each agent input is of Control Signal type. The control signal is derived from the presented control protocol of the MAS.

The available MATLAB Function block in which the control protocol is implemented provides the agents with the control signal term.



There you could find how the control protocol is implemented. Also you could find the script in the following:

function u = func(t, x1\_1, ...

x2\_1, ...

x3\_1, ...

x4\_1, ...

x5\_1, ...

x6\_1, ...

x7\_1, ...

x1\_2, ...

x2\_2, ...

x3\_2, ...

x4\_2, ...

x5\_2, ...

x6\_2, ...

x7\_2)

states\_1 = [x1\_1, x2\_1, x3\_1, x4\_1, x5\_1, x6\_1, x7\_1, ]';

states\_2 = [x1\_2, x2\_2, x3\_2, x4\_2, x5\_2, x6\_2, x7\_2, ]';

numSates = 7;

L\_1st\_neighbour = [ 2,-1,0,0,0,0,-1;

-1,2,-1,0,0,0,0;

0,-1,2,-1,0,0,0;

0,0,-1,2,-1,0,0;

0,0,0,-1,2,-1,0;

0,0,0,0,-1,2,-1;

-1,0,0,0,0,-1,2;];

L\_tilda = [ 4 -1 -1 0 0 -1 -1;

-1 4 -1 -1 0 0 -1;

-1 -1 4 -1 -1 0 0;

0 -1 -1 4 -1 -1 0;

0 0 -1 -1 4 -1 -1;

-1 0 0 -1 -1 4 -1;

-1 -1 0 0 -1 -1 4;

];

L\_2nd\_neighbour = L\_tilda - L\_1st\_neighbour;

eigLtilda = eig(L\_tilda);

eigLtilda = sort(round(eigLtilda\*1000)/1000);

eigL1st = eig(L\_1st\_neighbour);

eigL1st = sort(round(eigL1st\*1000)/1000);

gamma\_1 = 1;

gamma\_2 = sqrt(4\*gamma\_1/eigLtilda(2));

u = real(-gamma\_1\*L\_1st\_neighbour\*states\_1 - gamma\_2\*L\_1st\_neighbour\*states\_2 - gamma\_1\*L\_2nd\_neighbour\*states\_1 - gamma\_2\*L\_2nd\_neighbour\*states\_2);

end

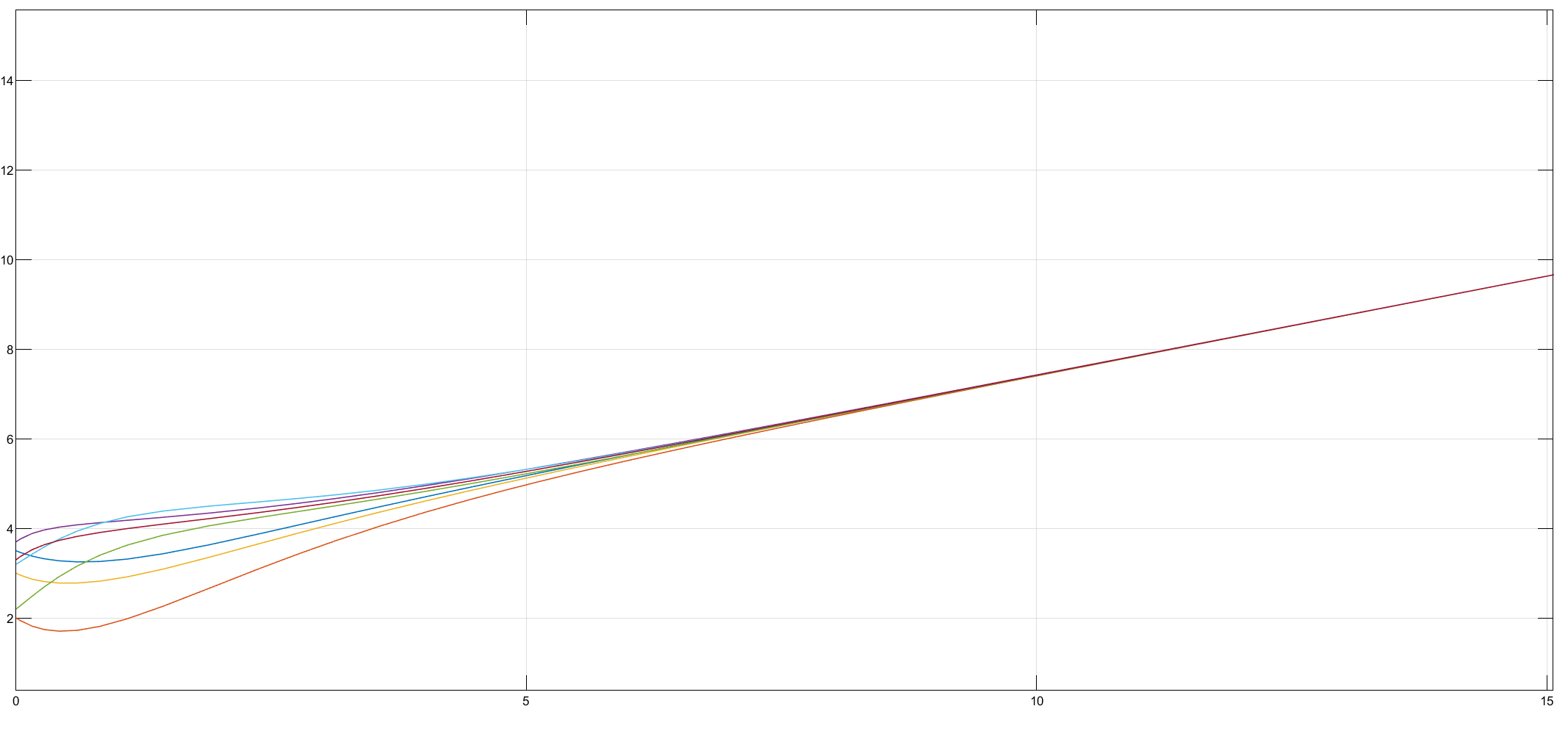
First, the Laplacian matrix of the given topology considering the first-order neighbors is formed in L\_1st\_neighbour, considering first-order and second-order neighbors in L\_tilda and the states vectors are set up. Hence, the corresponding Laplacian matrix according to the second-order neighbors obtains in L\_2nd\_neighbour = L\_tilda - L\_1st\_neighbour. Finally, the algorithm protocol is presented and the control signal is defined as the output of the function.

## Run and Simulate

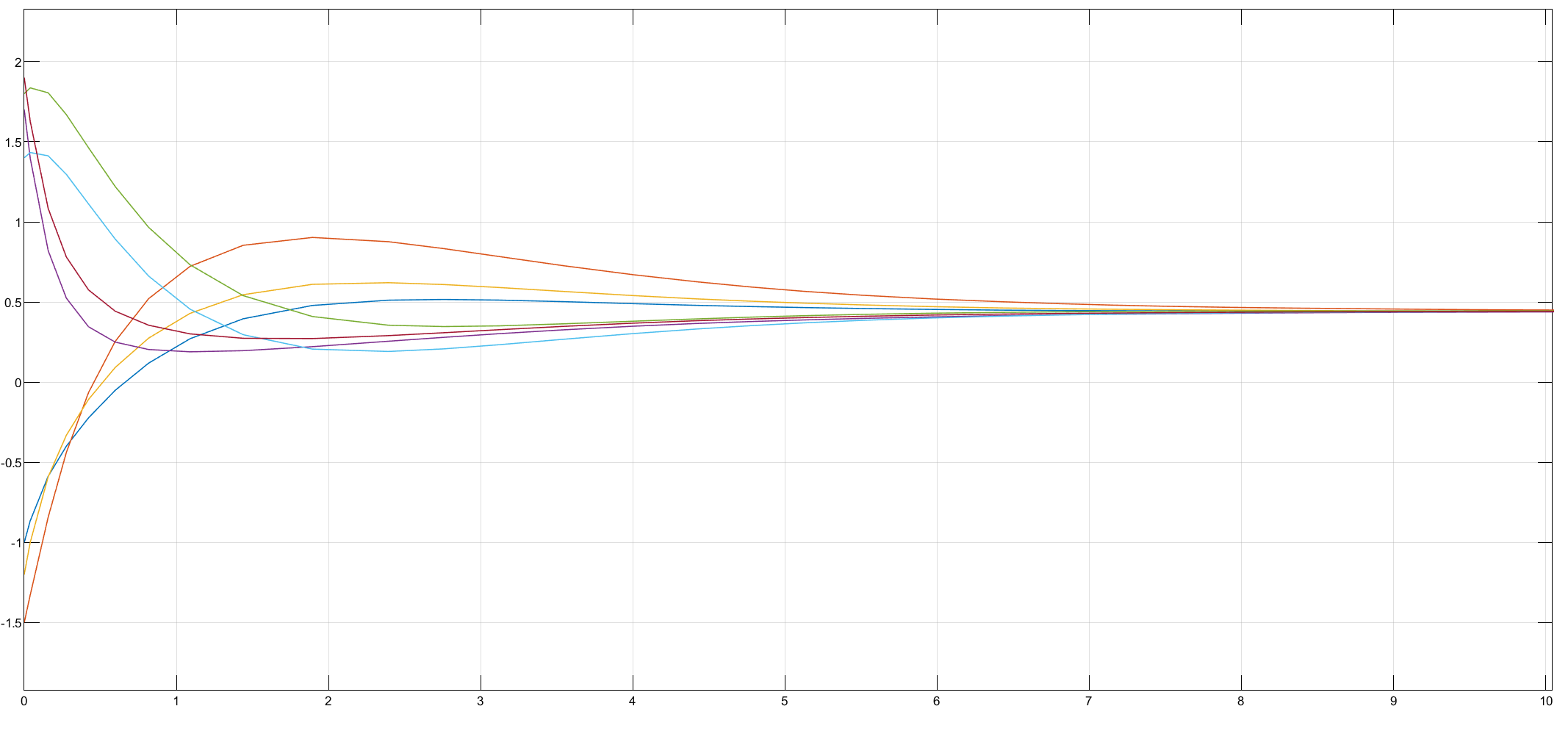
Running the simulation for 25 seconds leads into the following results:

* **1st-order neighbours only (case 0)**



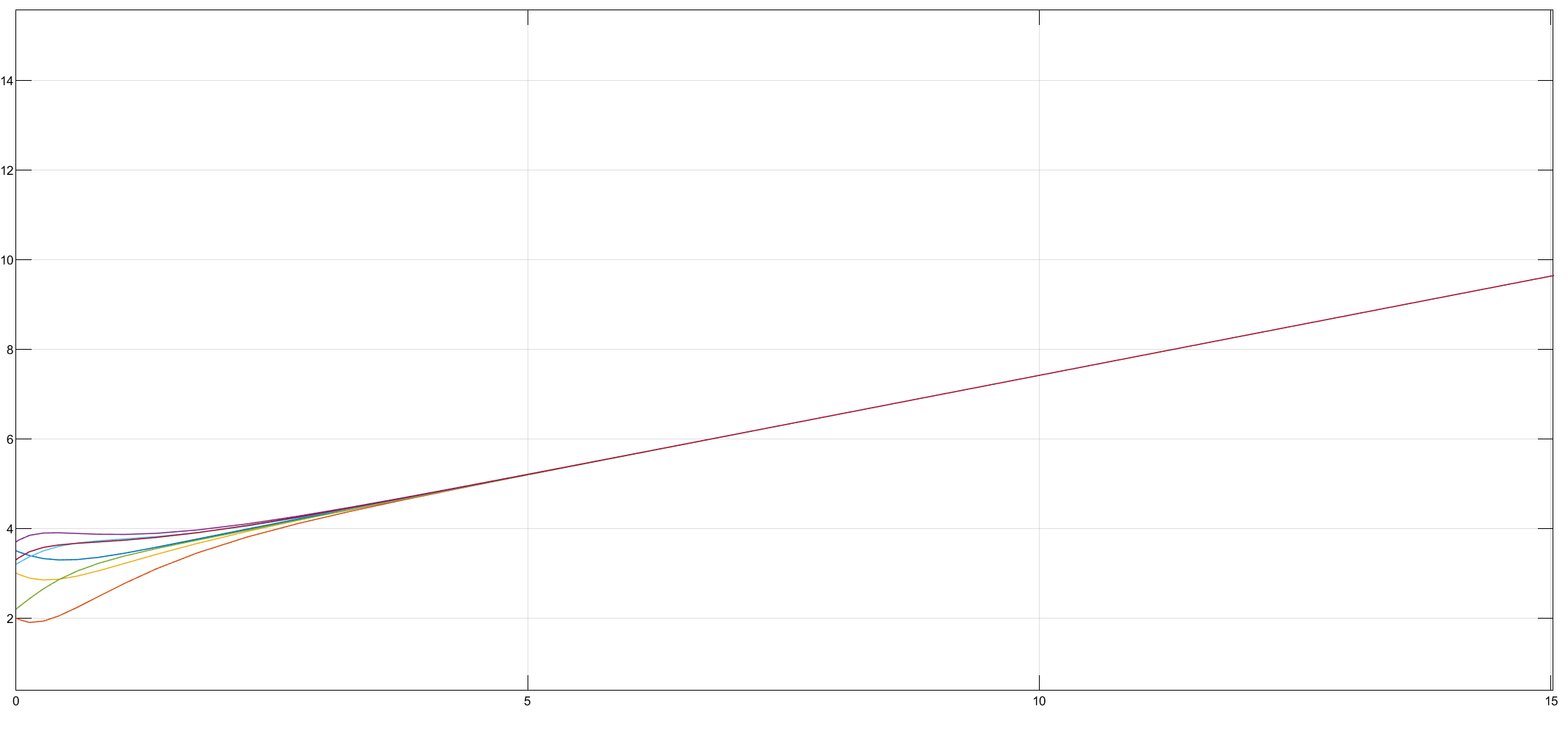




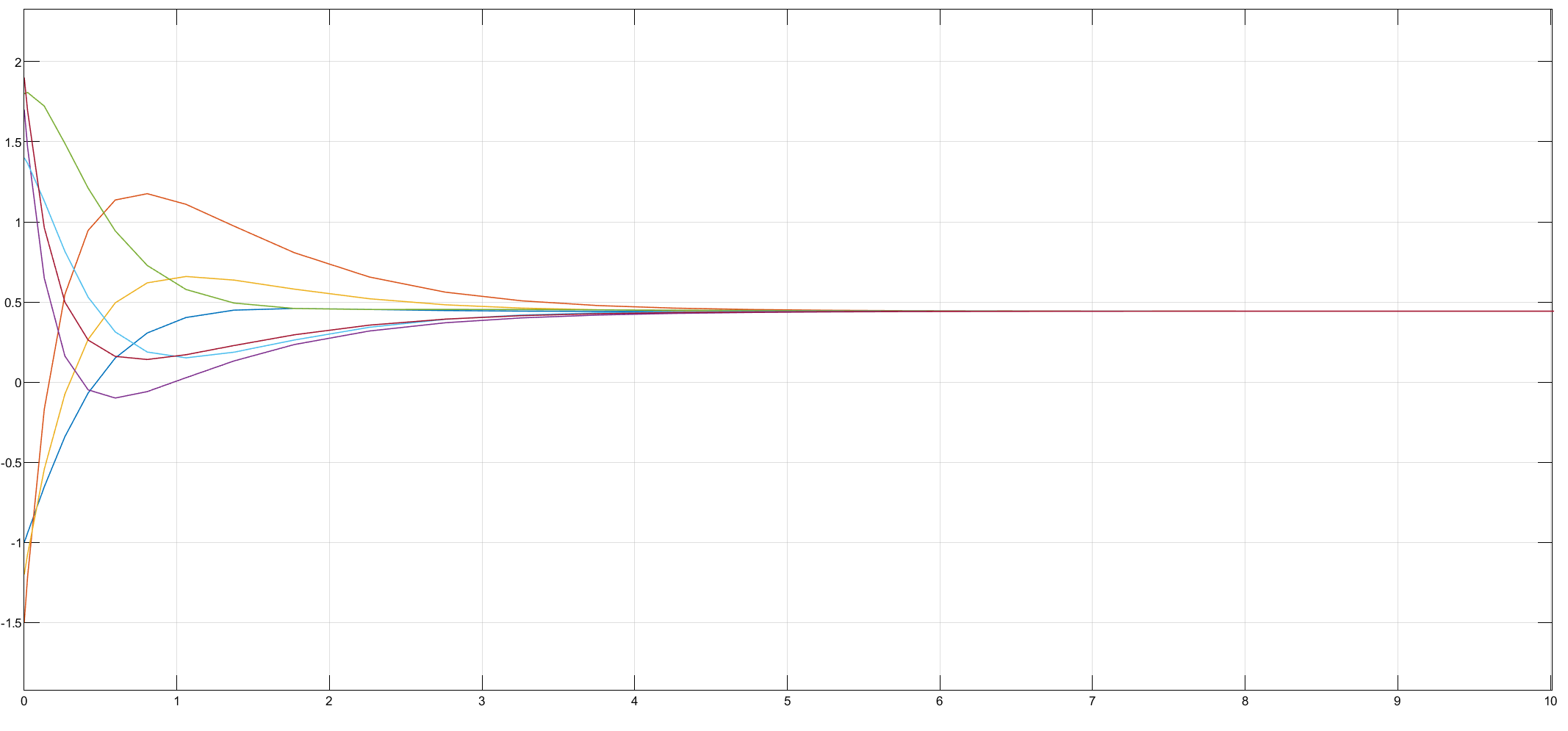


* **1st&2nd-order neighbors (case I)**



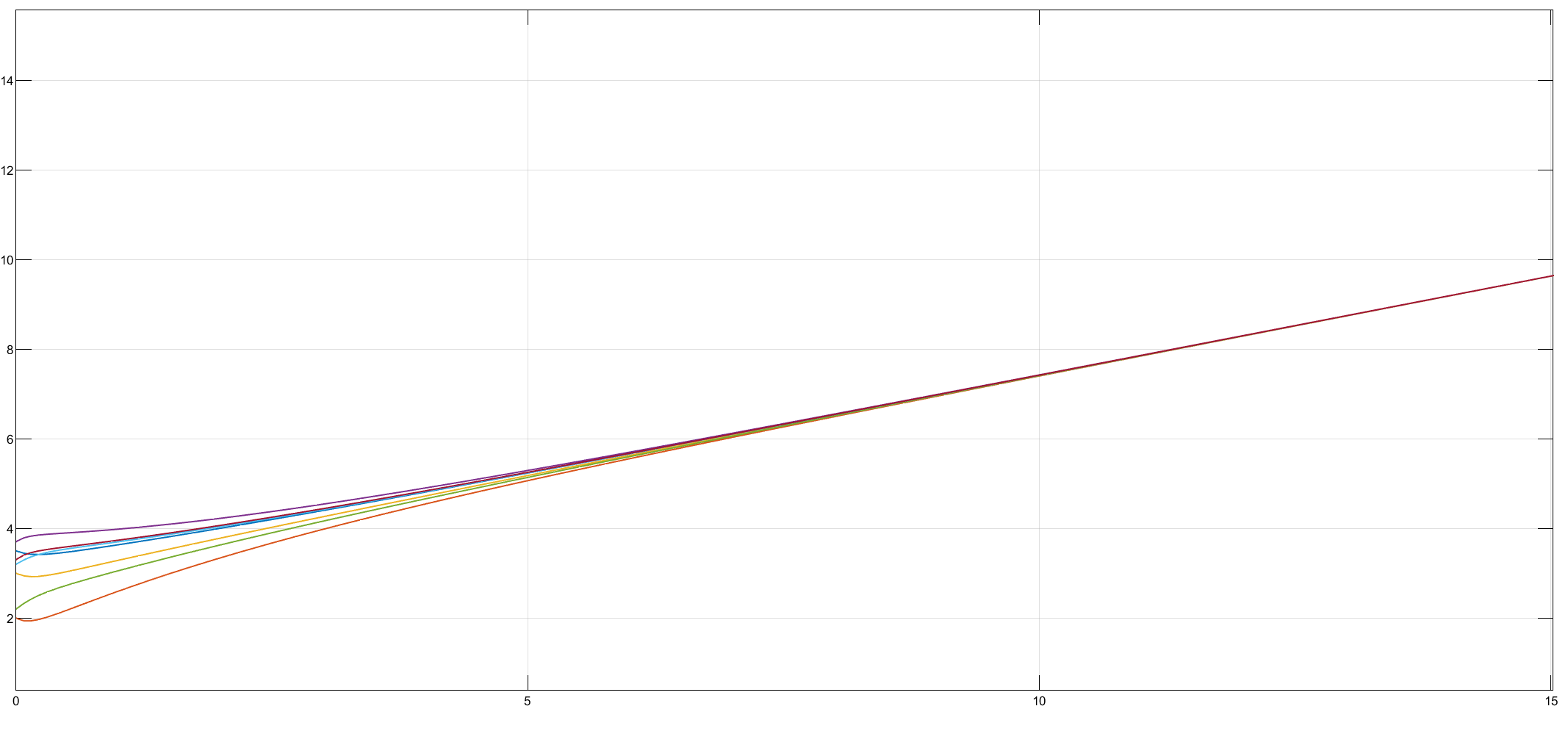




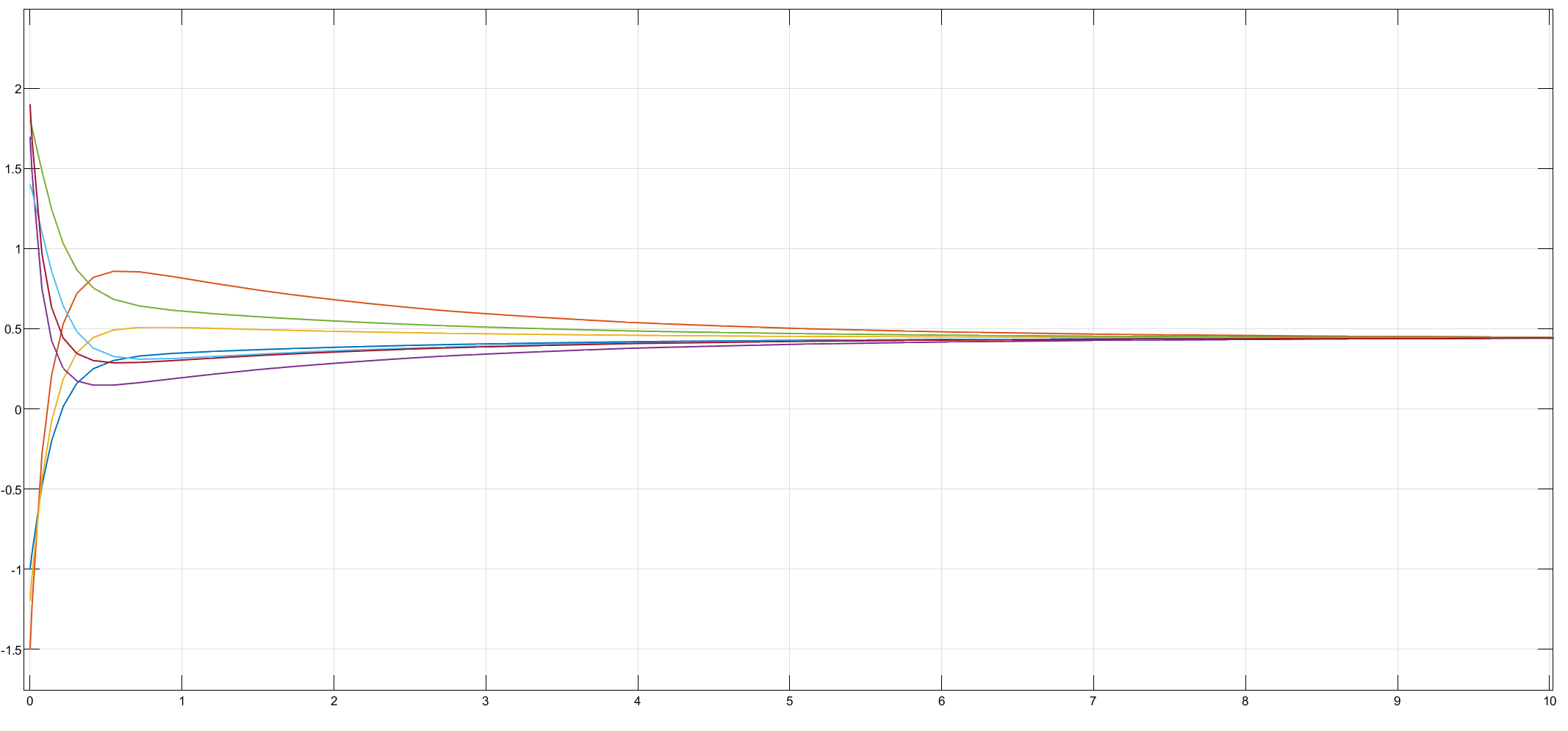


* **1st&2nd-order neighbors (case II)**



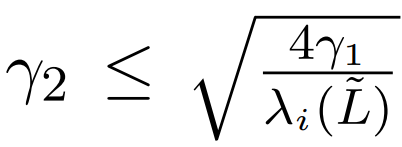




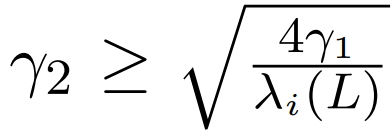


It is observed that in all cases, states are all reached consensus. Comparing  state of the three cases shows that the slowest consensus rate is for case 0 where the agents are using their first-order neighbors information. Case I and II have the higher consensus rate. Also Case I reaches the consensus faster than case II since:

* case I



* case II



You could find the consensus rates in the following figure and compare the results.

