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Exercises - Chapter 02

Problem 02 – Smith-McMillan

Note: Smith-McMillan is discussed in chapter 03 and it is the authors' mistake to have it by the end of chapter 02.

G1 =

$$\begin{pmatrix} \frac{s}{(s+1)^2 (s+2)^2} & \frac{s}{(s+2)^2} \\ -\frac{s}{(s+2)^2} & -\frac{s}{(s+2)^2} \end{pmatrix}$$

The Lowest Common Multiplies of the given matrix denominators is:

$$(s+1)^2 (s+2)^2$$

SmithMcMillan =

$$\begin{pmatrix} \frac{s}{(s^2 + 3s + 2)^2} & 0 \\ 0 & \frac{s^2}{s+2} \end{pmatrix}$$

G2 =

$$\begin{pmatrix} \frac{s+2}{s+1} & \frac{1}{s+2} \\ \frac{1}{s+1} & \frac{(s+1)(s+3)}{(s+2)^2} \end{pmatrix}$$

The Lowest Common Multiplies of the given matrix denominators is:

$$(s+1) (s+2)^2$$

SmithMcMillan =

$$\begin{pmatrix} \frac{1}{(s+1)(s+2)^2} & 0 \\ 0 & s^3 + 6s^2 + 10s + 4 \end{pmatrix}$$

G4 =

$$\begin{pmatrix} (s+1)(s+2) & \frac{(s+1)^2}{s+2} \\ -\frac{s+2}{(s+1)^2} & -\frac{1}{s+2} \end{pmatrix}$$

The Lowest Common Multiplies of the given matrix denominators is:

$$(s+1)^2 (s+2)$$

SmithMcMillan =

$$\begin{pmatrix} \frac{1}{(s+1)^2 (s+2)} & 0 \\ 0 & -s (s+1)^2 (s+2) \end{pmatrix}$$

G5 =

$$\begin{pmatrix} \frac{1}{s+1} & \frac{2s+4}{(s+1)(s+3)} & \frac{1}{s+4} \\ 0 & \frac{1}{s+2} & \frac{1}{s+4} \\ \frac{1}{s+1} & -\frac{(s+1)(s+3)-2(s+2)^2}{(s+1)(s+2)(s+3)} & 0 \end{pmatrix}$$

The Lowest Common Multiplies of the given matrix denominators is:

$$(s+1)(s+2)(s+3)(s+4)$$

SmithMcMillan =

$$\begin{pmatrix} \frac{1}{s^4 + 10s^3 + 35s^2 + 50s + 24} & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

G8 =

$$\begin{pmatrix} \frac{1}{s+1} & \frac{2}{s+1} & \frac{1}{s+4} \\ 0 & \frac{1}{s+2} & \frac{1}{s+4} \\ \frac{1}{s+1} & \frac{2s+6}{(s+1)(s+2)(s+3)} & 0 \end{pmatrix}$$

The Lowest Common Multiplies of the given matrix denominators is:

$$(s+1)(s+2)(s+4)$$

SmithMcMillan =

$$\begin{pmatrix} \frac{1}{s^3 + 7s^2 + 14s + 8} & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

G9 =

$$\begin{pmatrix} \frac{1}{(s+3)(s+4)} & \frac{1}{s+1} \\ \frac{1}{s+3} & 0 \end{pmatrix}$$

The Lowest Common Multiplies of the given matrix denominators is:

$$(s+1)(s+3)(s+4)$$

SmithMcMillan =

$$\begin{pmatrix} \frac{1}{s^3 + 8s^2 + 19s + 12} & 0 \\ 0 & -s - 4 \end{pmatrix}$$

G10 =

$$\begin{pmatrix} \frac{s^3 - s^2 + 1}{s^4} & \frac{1}{s^4} & -\frac{s^3 - s^2 + 2}{s^4} \\ \frac{\frac{3s}{2} + 1}{s^4} & \frac{s+1}{s^4} & -\frac{\frac{3s}{2} + 2}{s^4} \\ -\frac{-s^3 + 9s^2 + s - 1}{s^4} & -\frac{s^2 - 1}{s^4} & -\frac{-s^3 + s^2 + s}{s^4} \end{pmatrix}$$

The Lowest Common Multiplies of the given matrix denominators is:

$$2s^4$$

SmithMcMillan =

$$\begin{pmatrix} \frac{1}{2s^4} & 0 & 0 \\ 0 & \frac{1}{s^4} & 0 \\ 0 & 0 & -\frac{-4s^6 + 20s^5 + 10s^4 - 24s^3 - s^2 + 4s + 2}{s^3} \end{pmatrix}$$

G12 =

$$\begin{pmatrix} \frac{1}{(s+1)^2} & \frac{1}{(s+1)(s+2)} \\ \frac{1}{(s+1)(s+2)} & \frac{s+3}{(s+2)^2} \end{pmatrix}$$

The Lowest Common Multiplies of the given matrix denominators is:

$$(s+1)^2 (s+2)^2$$

SmithMcMillan =

$$\begin{pmatrix} \frac{1}{(s^2+3s+2)^2} & 0 \\ 0 & s+2 \end{pmatrix}$$