Artificial Intelligence for Robotics 1

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Sample test 1

1 Propositional Logic

Formalize the following sentences about a group of friends having a party

- 1. Alberto and Carola are going to the party
- 2. Either Beatrice or Daniele (or both) are going to the party
- 3. If Alberto goes to the party then also Enrico goes to the party
- 4. If Enrico goes to the party then Daniele does not go
- 5. If Beatrice goes to the party then either Carola or Alberto do not go

Considering the sentences above, is there going to be someone at the party? State your answer as a proof using a deduction mechanism of your choice or a semantic argument. Truth-tables are not accepted as an answer. (**Note**: the disjunction in sentence (2) is inclusive.)

2 First Order Logic

Consider the following first order theory about cocktails:

- $1. \ \forall x. (Loves(x, negroni) \rightarrow Loves(x, americano)).$
- 2. $\forall x.(Loves(x, stinger) \lor Loves(x, negroni)).$
- 3. $\exists x. \neg Loves(x, americano)$.
- 4. $\exists x.(Loves(x, stinger) \lor Loves(x, negroni))$

and tell whether each of the following sentences is either a logical consequence of the theory or not:

- 1. $\exists x.(\neg Loves(x, negroni) \land \neg Loves(x, stinger)).$
- 2. $\forall x. (\neg Loves(x, stinger) \rightarrow \neg Loves(x, americano)).$
- $3. \ \forall x. (Loves(x, negroni) \lor Loves(x, americano)).$

- 4. $\forall x.(Loves(x, americano)).$
- 5. $\forall x.((Loves(x, negroni) \land \neg Loves(x, americano)) \rightarrow \neg Loves(x, stinger)).$

Please state your answers using a deductive mechanism of your choice or a semantic argument.

3 Description Logic

Consider a knowledge base Σ in \mathcal{ALC} where the TBox is the following:

- $Person \sqsubseteq Animal \sqcap Biped$
- $Woman \equiv Person \sqcap Female$
- $Mother \equiv Woman \sqcap \exists ParentOf.Person$
- $Parent \equiv Mother \sqcup Father$
- $Man \equiv Person \sqcap \neg Woman$
- conMotherWithoutDaughter \equiv Mother $\sqcap \forall ParentOf. \neg Female$
- $GrandMother \equiv Woman \sqcap \exists ParentOf.Parent$

and the ABox is the following:

- GrandMother(Sally)
- $(Person \sqcap Man)(John)$

Using a deduction mechanism or a semantic argument, tell whether the following assertions hold:

- $\Sigma \models Woman \sqsubseteq Biped$
- $\Sigma \models Man \sqsubseteq Parent$
- $\Sigma \models \exists ParentOf.Man$
- $\Sigma \models \exists ParentOf.Person \sqsubseteq Woman$
- $\Sigma \models (\neg Woman)(John)$