

$$\mathbf{A} = \{\{\mathbf{a}, 1 - \mathbf{a}\}, \{1 - \mathbf{b}, \mathbf{b}\}\}$$

$$\{\{\mathbf{a}, 1 - \mathbf{a}\}, \{1 - \mathbf{b}, \mathbf{b}\}\}$$

$$\mathbf{MatrixForm}[\mathbf{HH} = \mathbf{Eigenvectors}[\mathbf{A}]^T]$$

$$\mathbf{Eigenvalues}[\mathbf{A}]$$

$$\begin{pmatrix} 1 & -\frac{-1+\mathbf{a}}{-1+\mathbf{b}} \\ 1 & 1 \end{pmatrix}$$

$$\{1, -1 + \mathbf{a} + \mathbf{b}\}$$

$$\mathbf{MatrixForm}[\mathbf{hh} = \mathbf{Inverse}[\mathbf{HH}]]$$

$$\begin{pmatrix} \frac{1}{1-\frac{1}{-1+\mathbf{b}}+\frac{\mathbf{a}}{-1+\mathbf{b}}} & \frac{-1+\mathbf{a}}{\left(1-\frac{1}{-1+\mathbf{b}}+\frac{\mathbf{a}}{-1+\mathbf{b}}\right)(-1+\mathbf{b})} \\ -\frac{1}{1-\frac{1}{-1+\mathbf{b}}+\frac{\mathbf{a}}{-1+\mathbf{b}}} & \frac{1}{1-\frac{1}{-1+\mathbf{b}}+\frac{\mathbf{a}}{-1+\mathbf{b}}} \end{pmatrix}$$

$$\mathbf{d} = \mathbf{DiagonalMatrix}[\{1, 0\}]$$

$$\{\{1, 0\}, \{0, 0\}\}$$

$$\mathbf{MatrixForm}[\mathbf{HH.d.hh}]$$

$$\begin{pmatrix} \frac{1}{1-\frac{1}{-1+\mathbf{b}}+\frac{\mathbf{a}}{-1+\mathbf{b}}} & \frac{-1+\mathbf{a}}{\left(1-\frac{1}{-1+\mathbf{b}}+\frac{\mathbf{a}}{-1+\mathbf{b}}\right)(-1+\mathbf{b})} \\ \frac{1}{1-\frac{1}{-1+\mathbf{b}}+\frac{\mathbf{a}}{-1+\mathbf{b}}} & \frac{-1+\mathbf{a}}{\left(1-\frac{1}{-1+\mathbf{b}}+\frac{\mathbf{a}}{-1+\mathbf{b}}\right)(-1+\mathbf{b})} \end{pmatrix}$$

$$\mathbf{MatrixForm}[\mathbf{HH} = \mathbf{Eigenvectors}[\mathbf{A}^T]]$$

$$\mathbf{Eigenvalues}[\mathbf{A}]$$

$$\begin{pmatrix} -\frac{1-\mathbf{b}}{-1+\mathbf{a}} & 1 \\ -1 & 1 \end{pmatrix}$$

$$\{1, -1 + \mathbf{a} + \mathbf{b}\}$$