

Assignment 7

Lempel-Ziv Compression

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1 Introduction

Compressing data means reducing the number of bits needed to represent it. Compressed data, due to its reduced size, is a lot faster to transfer and less expensive to store, freeing up storage and increasing network capacity. Algorithms that perform data compression are known as data compression algorithms. Data compression algorithms are divided into two categories: lossy and lossless. Lossy compression algorithms compress more than lossless compression algorithms, but at the cost of losing some information, which can't be recovered. Lossy compression algorithms are typically used for audio and video files, where a loss in quality is tolerable and often not noticeable. Lossless compression algorithms on the other hand don't compress as much, but do not lose any data, meaning compressed information can be exactly reconstructed back into its uncompressed form. Lossless compression algorithms are used for data that must maintain integrity, such as binaries, text documents, and source code.

2 Lempel-Ziv Compression

Abraham Lempel and Jacob Ziv published papers for two lossless compression algorithms, LZ77 and LZ78, published in 1977 and 1978, respectively. The core idea behind both of these compression algorithms is to represent repeated patterns in data with using pairs which are each comprised of a code and a symbol. A code is an unsigned 16-bit integer and a symbol is a 8-bit ASCII character.

Assume, for example, we have some string “*abab*”. Assume we also have a dictionary where the key is a prefix, also known as a word, and the value is a code that we can utilize for fast look-ups. Since codes are 16-bit unsigned integers, we will give the dictionary a limit of $2^{16} - 1$ possible codes. Why don't we have 2^{16} codes? Because we will be reserving a code to be used as a stop code which indicates the end of our encoded data. We will define the maximal usable code as `MAX_CODE`, which has the value $2^{16} - 1$. The dictionary is initialized with the empty word, or a string of zero length, at the index `EMPTY_CODE`, which is a macro for 1. We will specify the first index in which a new word can be added to as the macro `START_CODE`, which has the value 2.

We now consider the first character: ‘*a*’. Since this is the first character, we know that the string of all previously seen characters up to this point must be the empty word; we haven't considered any characters prior to this point. We then append the current character ‘*a*’ to the empty word, which yields the word “*a*”. We check the dictionary in vain to see if we've encountered this word before. Since we haven't yet seen this word, we will add this first word to the dictionary and assign it the first available code of 2, or `START_CODE`. We set our previously seen word to be the empty word and output the pair (`EMPTY_CODE`, ‘*a*’).

We continue on, now considering the second character: ‘*b*’. We append this character to our previously seen word, which yields “*b*” as our current word. We again check the dictionary in vain to see if we've encountered this word before. Since we haven't, we add this word to the dictionary and assign it the next available code of 3. We set the previously seen word to the empty word and output the pair (`EMPTY_CODE`, ‘*b*’).

The next character we see is ‘*a*’. We append this character to our previously seen word, which yields “*a*” as our

Compression Example

Initialized dictionary		Adding “a”		Adding “b”		Adding “ab”	
Word	Code	Word	Code	Word	Code	Word	Code
“”	EMPTY_CODE	“”	EMPTY_CODE	“”	EMPTY_CODE	“”	EMPTY_CODE
	START_CODE	“a”	START_CODE	“a”	START_CODE	“a”	START_CODE
	3		3	“b”	3	“b”	3
	4		4		4	“ab”	4

	MAX_CODE		MAX_CODE		MAX_CODE		MAX_CODE

current word. We check the dictionary to see if we’ve encountered this word before. Indeed we have. We set the previously seen word to “a” and proceed to the next character without any further output.

We read in the last character, ‘b’. We append this character to our previously seen word, which yields “ab”. Clearly, this word isn’t in the dictionary, so pair comprised of the current symbol, ‘b’, and the code of the previously we add it and assign it the next available code of 4. What should we output? The seen word. Since our previously seen word at this stage was “a”, this code will be 2. Thus, we output (2, ‘b’). To finish off compression, we output the final pair (STOP_CODE, 0). As you can imagine, this pair signals the end of compressed data. The symbol in this final pair isn’t used and the value is of no significance. The macro STOP_CODE has the value of 0.

Of course, a compression algorithm is useless without a corresponding decompression algorithm. Assume we’re reading in the output from the preceding compression example. The output was comprised of the following pairs, in order: (EMPTY_CODE, ‘a’), (EMPTY_CODE, ‘b’), (2, ‘b’), (STOP_CODE, 0). Similar to the compression algorithm, the decompression algorithm initializes a dictionary containing only the empty word. The catch is that the key and value for the decompressing dictionary is swapped; each key is instead a code and each value a word. As you might imagine, the decompression algorithm is the inverse of the compression algorithm, and thus from the output pairs, the decompression algorithm will recreate the same dictionary used during compression to output the decompressed data.

We consider the first pair: (EMPTY_CODE, ‘a’). We append the symbol ‘a’ to the word denoted by EMPTY_CODE, which is the empty word. Thus, the current word is “a”. We add this word to the dictionary and assign it the next available code of 2, then output the current word “a”.

We consider the next pair: (EMPTY_CODE, ‘b’). We append the symbol ‘b’ to the word denoted by EMPTY_CODE, which is the empty word. Thus, the current word is “b”. We add this word to the dictionary and assign it the next available code of 3, then output the current word “b”.

We now consider the next pair: (2, ‘b’). We append the symbol ‘b’ to the word denoted by the code 2, which we previously added to our dictionary. The word denoted by this code is “a”, whence we obtain our current word of “ab”. We add this word to the dictionary and assign it the next available code of 4, then output the current word “ab”. Finally, we read in the last pair: (STOP_CODE, 0). Since the code is STOP_CODE, we know that we have finished decompression.

If the basic idea behind the compression and decompression algorithms do not immediately make sense to you, or if you desire a more visual representation of how the algorithms work, make sure to attend section and get help early! Things will not get easier as time goes on.

3 Your Task

Your task is to implement two programs called encode and decode which perform LZ78 compression and decompression, respectively. The requirements for your programs are as follows:

Decompression Example

Initialized dictionary		Adding “a”		Adding “b”		Adding “ab”	
Code	Word	Code	Word	Code	Word	Code	Word
EMPTY_CODE	“”	EMPTY_CODE	“”	EMPTY_CODE	“”	EMPTY_CODE	“”
START_CODE		START_CODE	“a”	START_CODE	“a”	START_CODE	“a”
3		3		3	“b”	3	“b”
4		4		4		4	“ab”
...		
MAX_CODE		MAX_CODE		MAX_CODE		MAX_CODE	

1. encode can compress any file, text or binary.
2. decode can decompress any file, text or binary, that was compressed with encode.
3. Both use variable bit-length codes.
4. Both perform read and writes in efficient blocks of 4KB.

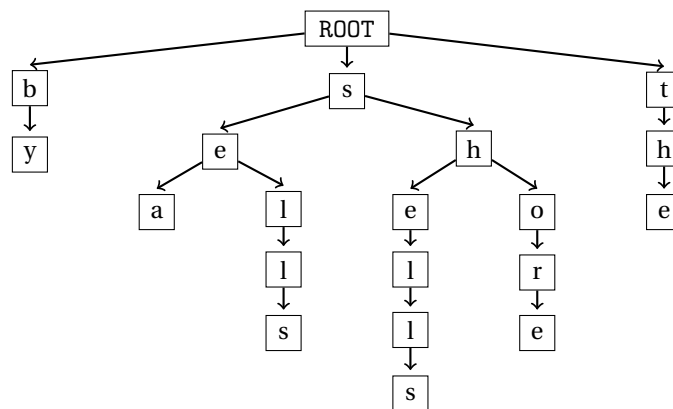
4 Specifics

You will need to implement some new ADTs for this assignment: an ADT for tries and an ADT for words. In addition to these new ADTs, you will need to be concerned about variable-length codes and I/O.

4.1 Tries

The most costly part of compression is checking for existing prefixes, or words. You could utilize a hash table, or just an array to store words, but that wouldn't be optimal, as many of the words you need to store are prefixes of other words. Instead you choose to utilize a *trie*.

A trie¹ is an efficient information re-*trie*-val data structure, commonly known as a prefix tree. Each node in a trie represents a symbol, or a character, and contains n child nodes, where n is the size of the alphabet you are using. In most cases, the alphabet used is the set of ASCII characters, so $n = 256$. You will use a trie during compression to store words.



Above is an example of a trie containing the following words: “*She*”, “*sells*”, “*sea*”, “*shells*”, “*by*”, “*the*”, “*sea*”, “*shore*”. Searching for a word in the trie means stepping down for each symbol in the word, starting from the root.

¹ Edward Fredkin, “Trie memory.” *Communications of the ACM* 3, no. 9 (1960): 490–499.

Stepping down the trie is simply checking if the current node we have traversed to has a child node representing the symbol we are looking for, and setting the current node to be the child node if it does exist. Thus, to find “*sea*”, we would start from the trie’s root and step down to ‘*s*’, then ‘*e*’, then ‘*a*’. If any symbol is missing, or the end of the trie is reached without fully matching a word, while stepping through the trie, then the word is not in the trie. You *must* follow the specification shown below when implementing your trie ADT.

```

1 #ifndef __TRIE_H__
2 #define __TRIE_H__
3
4 #include <inttypes.h>
5
6 #define ALPHABET 256
7
8 typedef struct TrieNode TrieNode;
9
10 //
11 // Struct definition of a TrieNode.
12 //
13 // children: Each TrieNode has ALPHABET number of children.
14 // code:      Unique code for a TrieNode.
15 //
16 struct TrieNode {
17     TrieNode *children[ALPHABET];
18     uint16_t code;
19 };
20
21 //
22 // Constructor for a TrieNode.
23 //
24 // code:      Code of the constructed TrieNode.
25 // returns: Pointer to a TrieNode that has been allocated memory.
26 //
27 TrieNode *trie_node_create(uint16_t code);
28
29 //
30 // Destructor for a TrieNode.
31 //
32 // n:         TrieNode to free allocated memory for.
33 // returns: Void.
34 //
35 void trie_node_delete(TrieNode *n);
36
37 //
38 // Initializes a Trie: a root TrieNode with the code EMPTY_CODE.
39 //
40 // returns: Pointer to the root of a Trie.
41 //
42 TrieNode *trie_create(void);
43
44 //
45 // Resets a Trie to just the root TrieNode.
46 //

```

```

47 // root:      Root of the Trie to reset.
48 // returns: Void.
49 //
50 void trie_reset(TrieNode *root);
51
52 //
53 // Deletes a sub-Trie starting from the sub-Trie's root.
54 //
55 // n:          Root of the sub-Trie to delete.
56 // returns: Void.
57 //
58 void trie_delete(TrieNode *n);
59
60 //
61 // Returns a pointer to the child TrieNode representing the symbol sym.
62 // If the symbol doesn't exist, NULL is returned.
63 //
64 // n:          TrieNode to step from.
65 // sym:        Symbol to check for.
66 // returns: Pointer to the TrieNode representing the symbol.
67 //
68 TrieNode *trie_step(TrieNode *n, uint8_t sym);
69
70 #endif

```

trie.h

The `TrieNode` struct will have the three fields shown above. Each trie node has an array of 256 pointers to trie nodes as children, one for each ASCII character. It should be easy to see how this simplifies searching for the next character in a word in the trie. The code field stores the 16-bit code for the word that ends with the trie node containing the code. This means that the code for some word “*abc*” would be contained in the trie node for ‘*c*’. Note that there isn’t a field that indicates what character a trie node represents. This is because the trie node’s index in its parent’s array of child nodes indicates what character it represents. The `trie_step()` function will be repeatedly called to check if a word exists in the trie. A word only exists if the trie node returned by the last step corresponding to the last character in the word isn’t NULL.

4.2 Word Tables

Although compression can be performed using a trie, decompression still needs to use a look-up table for quick code to word translation. This look-up table will be defined as a new struct called a `WordTable`. Since we can only have $2^{16} - 1$ codes, one of which is reserved as a stop code, we can use a fixed word table size of `UINT16_MAX`, where `UINT16_MAX` is a macro defined in `inttypes.h` as the maximum value of a unsigned 16-bit integer. Hint: this has the exact same value as `MAX_CODE`, which we defined earlier. Why aren’t we using hash tables to store words? Because there is a *finite* number of codes. Each index of this word table will be a new struct called a `Word`. You will store words in byte arrays, or arrays of `uint8_t`. This is because strings in C are null-terminated, and problems with compression occur if a binary file is being compressed and contains null characters that are placed into strings. Since we need to know how long a word is, a `Word` will also have a field for storing the length of the byte array, since we can’t use `string.h` functions like `strlen()` on byte arrays. You *must* use the following specification for the new `Word` ADT.

```

1 #ifndef __WORD_H__
2 #define __WORD_H__
3

```

```

4 #include <inttypes.h>
5
6 //
7 // Struct definition of a Word.
8 //
9 // syms:  A Word holds an array of symbols, stored as bytes in an array.
10 // len:   Length of the array storing the symbols a Word represents.
11 //
12 typedef struct Word {
13     uint8_t *syms;
14     uint32_t len;
15 } Word;
16
17 //
18 // Define an array of Words as a WordTable.
19 //
20 typedef Word * WordTable;
21
22 //
23 // Constructor for a word.
24 //
25 // syms:      Array of symbols a Word represents.
26 // len:       Length of the array of symbols.
27 // returns:   Pointer to a Word that has been allocated memory.
28 //
29 Word *word_create(uint8_t *syms, uint64_t len);
30
31 //
32 // Constructs a new Word from the specified Word appended with a symbol.
33 // The Word specified to append to may be empty.
34 // If the above is the case, the new Word should contain only the symbol.
35 //
36 // w:         Word to append to.
37 // sym:       Symbol to append.
38 // returns:   New Word which represents the result of appending.
39 //
40 Word *word_append_sym(Word *w, uint8_t sym);
41
42 //
43 // Destructor for a Word.
44 //
45 // w:         Word to free memory for.
46 // returns:   Void.
47 //
48 void word_delete(Word *w);
49
50 //
51 // Creates a new WordTable, which is an array of Words.
52 // A WordTable has a pre-defined size of MAX_CODE (UINT16_MAX - 1).
53 // This is because codes are 16-bit integers.
54 // A WordTable is initialized with a single Word at index EMPTY_CODE.

```

```

55 // This Word represents the empty word, a string of length of zero.
56 //
57 // returns: Initialized WordTable.
58 //
59 WordTable *wt_create(void);
60
61 //
62 // Resets a WordTable to having just the empty Word.
63 //
64 // wt:      WordTable to reset.
65 // returns: Void.
66 //
67 void wt_reset(WordTable *wt);
68
69 //
70 // Deletes an entire WordTable.
71 // All Words in the WordTable must be deleted as well.
72 //
73 // wt:      WordTable to free memory for.
74 // returns: Void.
75 //
76 void wt_delete(WordTable *wt);
77
78 #endif

```

4.3 Codes

It is a requirement that your programs, encode and decode, be able to read and write pairs containing variable bit-length codes. As an example, assume we are going to write the pair (13, 'a'). What is the minimum number of bits needed to represent 13? We can easily calculate the minimum number of bits needed to represent any integer $x \geq 1$ using the formula $\lfloor \log_2(x) \rfloor + 1$. The only edge case is with 0, whose bit-length is 1. Thus, we calculate that the minimum number of bits needed to represent 13, or the bit-length of 13, to be 4. That being said, in practice, the bit-length of the code in the pair you're going output wouldn't be the bit-length of the code itself, but rather the bit-length of the *next available code* assignable, as described in the earlier compression example. The reason for this is because decompression *must* know at all times the bit-length of the code it is going to read. Because the dictionary constructed by decompression contains exactly the words and codes contained by the trie constructed by compression, it is evident that, by using the bit-length of the next available code, that compression and decompression will agree on the variable bit-lengths of codes. Note that only codes have variable bit-lengths: symbols in a pair are always 8 bits.

As an example, assume we are going to output the pair (13, 'a'), and the next available code assignable in our dictionary is 64. We will need to convert this pair to binary, starting with the code. As stated earlier, the bit-length of the code is the bit-length of the next available code. We calculate that the bit-length of 64 is 7. We start from the least significant bit of our code, 13, and construct the code portion of the pair's binary representation: 1011000. Notice the padded zeroes and that the binary is reversed. Zeroes are padded because the bit-length of 64 is 7, while the bit-length of 13 is 4, which is why there are three padded zeroes. In the same fashion, we start from the least significant bit of our symbol, 'a', and add the symbol portion of the pair's binary representation to the previous code portion, which yields 101100010000110, since the ASCII value of 'a' is 97.

Now assume that we are reading in the binary 101100010000110 and converting that back into a pair. We know that the next available code assignable by compression and decompression are the same at every step. Thus, we know that compression must have output the pair's code with the bit-length of 64, which is 7. We go through the

first 7 bits of the binary: 1, 0, 1, 1, 0, 0, and 0, summing up the bits as we go, simulating how positional numbering systems work. This means we perform $1 \cdot 2^0 + 0 \cdot 2^1 + 1 \cdot 2^2 + 1 \cdot 2^3 + 0 \cdot 2^4 + 0 \cdot 2^5 + 0 \cdot 2^6 = 13$, exactly the code output by compression. We do the same for the remaining 8 bits to reconstruct the symbol.

```

1 #ifndef __CODE_H__
2 #define __CODE_H__
3
4 #include <inttypes.h>
5
6 #define STOP_CODE    0           // Signals end of decoding/decoding.
7 #define EMPTY_CODE   1           // Code denoting the empty Word.
8 #define START_CODE   2           // Starting code of new Words.
9 #define MAX_CODE     UINT16_MAX  // Maximum code.
10
11 #endif

```

code.h

4.4 I/O

It is also a requirement that your programs, encode and decode, perform efficient I/O. Reads and writes will be done 4KB, or a block, at a time, which implicitly requires that you buffer I/O. Buffering is the act of storing data into a buffer, which you can think of as an array of bytes. Below is an I/O module that you are required to implement for the assignment.

```

1 #ifndef __IO_H__
2 #define __IO_H__
3
4 #include "word.h"
5 #include <inttypes.h>
6 #include <stdbool.h>
7
8 #define MAGIC 0x8badbeef    // Program's magic number.
9
10 //
11 // Struct definition of a FileHeader.
12 //
13 // magic:      Magic number indicating a file compressed by this program.
14 // protection: Protection/permissions of the original, uncompressed file.
15 //
16 typedef struct FileHeader {
17     uint32_t magic;
18     uint16_t protection;
19 } FileHeader;
20
21 //
22 // Reads in sizeof(FileHeader) bytes from the input file.
23 // These bytes are read into the supplied FileHeader, header.
24 //
25 // infile:    File descriptor of input file to read header from.
26 // header:    Pointer to memory where the bytes of the read header should go
27 //            .
28 // returns:   Void.

```



```

28 //
29 void read_header(int infile, FileHeader *header);
30
31 //
32 // Writes sizeof(FileHeader) bytes to the output file.
33 // These bytes are from the supplied FileHeader, header.
34 //
35 // outfile: File descriptor of output file to write header to.
36 // header: Pointer to the header to write out.
37 // returns: Void.
38 //
39 void write_header(int outfile, FileHeader *header);
40
41 //
42 // "Reads" a symbol from the input file.
43 // The "read" symbol is placed into the pointer to sym. (e.g. *sym = val)
44 // In reality, a block of symbols is read into a buffer.
45 // An index keeps track of the currently read symbol in the buffer.
46 // Once all symbols are processed, another block is read.
47 // If less than a block is read, the end of the buffer is updated.
48 // Returns true if there are symbols to be read, false otherwise.
49 //
50 // infile: File descriptor of input file to read symbols from.
51 // sym: Pointer to memory which stores the read symbol.
52 // returns: True if there are symbols to be read, false otherwise.
53 //
54 bool read_sym(int infile, uint8_t *sym);
55
56 //
57 // Buffers a pair. A pair is comprised of a code and a symbol.
58 // The bits of the code are buffered first, starting from the LSB.
59 // The bits of the symbol are buffered next, also starting from the LSB.
60 // The code buffered has a bit-length of bitlen.
61 // The buffer is written out whenever it is filled.
62 //
63 // outfile: File descriptor of the output file to write to.
64 // code Code of the pair to buffer.
65 // sym: Symbol of the pair to buffer.
66 // bitlen: Number of bits of the code to buffer.
67 // returns: Void.
68 //
69 void buffer_pair(int outfile, uint16_t code, uint8_t sym, uint8_t bitlen);
70
71 //
72 // Writes out any remaining pairs of symbols and codes to the output file.
73 //
74 // outfile: File descriptor of the output file to write to.
75 // returns: Void.
76 //
77 void flush_pairs(int outfile);
78

```

```

79 //
80 // "Reads" a pair (code and symbol) from the input file.
81 // The "read" code is placed in the pointer to code (e.g. *code = val)
82 // The "read" symbol is placed in the pointer to sym (e.g. *sym = val).
83 // In reality, a block of pairs is read into a buffer.
84 // An index keeps track of the current bit in the buffer.
85 // Once all bits have been processed, another block is read.
86 // The first bitlen bits are the code, starting from the LSB.
87 // The last 8 bits of the pair are the symbol, starting from the LSB.
88 // Returns true if there are pairs left to read in the buffer, else false.
89 // There are pairs left to read if the read code is not STOP_CODE.
90 //
91 // infile:  File descriptor of the input file to read from.
92 // code:    Pointer to memory which stores the read code.
93 // sym:     Pointer to memory which stores the read symbol.
94 // bitlen:  Length in bits of the code to read.
95 // returns: True if there are pairs left to read, false otherwise.
96 //
97 bool read_pair(int infile, uint16_t *code, uint8_t *sym, uint8_t bitlen);
98
99 //
100 // Buffers a Word, or more specifically, the symbols of a Word.
101 // Each symbol of the Word is placed into a buffer.
102 // The buffer is written out when it is filled.
103 //
104 // outfile: File descriptor of the output file to write to.
105 // w:       Word to buffer.
106 // returns: Void.
107 //
108 void buffer_word(int outfile, Word *w);
109
110 //
111 // Writes out any remaining symbols in the buffer.
112 //
113 // outfile: File descriptor of the output file to write to.
114 // returns: Void.
115 //
116 void flush_words(int outfile);
117
118 #endif

```

io.h

Notice that there is a struct definition in the module interface. That is the struct definition for the file header, which contains the magic number for your program and the protection bit mask for the original file. The file header is the first thing that appears in a compressed file. The magic number field, magic, serves as a unique identifier for files compressed by encode. decode should only be able to decompress files which have the correct magic number. This magic number is 0x8badbeef. The function read_header() reads in the header and verifies the magic number. The protection bit mask comes from the original file. The output file in which you write to must have the same protection bits as the original file.

All reads and writes in this program must be done using the system calls read() and write(), which means that you must use the system calls open() and close() to get your file descriptors. As stated earlier, all reads and

writes must be performed in efficient blocks of 4KB. You will want to use two static 4KB `uint8_t` arrays to serve as buffers: one to store binary pairs and the other to store characters. Each of these buffers should have an index, or a variable, to keep track of the current byte or bit that has been processed.

5 Program Options

Your encode program must support the following `getopt()` options:

- `-v` : Display compression statistics
- `-i <input>` : Specify input to compress (`stdin` by default)
- `-o <output>` : Specify output of compressed input (`stdout` by default)

Your decode program must support the following `getopt()` options:

- `-v` : Display decompression statistics
- `-i <input>` : Specify input to decompress (`stdin` by default)
- `-o <output>` : Specify output of decompressed input (`stdout` by default)

The verbose option enables a flag to print out informative statistics about the compression or decompression that is performed. These statistics include the compressed file size, the uncompressed file size, and the compression ratio. The formula for the compression ratio is $100 \times (1 - (\text{compressed size} / \text{uncompressed size}))$. The verbose output of both encode and decode must match the following:

```
1 Compressed file size: X bytes
2 Uncompressed file size: X bytes
3 Compression ratio: XX.XX%
```

6 Compression

The following steps for compression will refer to the input file descriptor to compress as `infile` and the compressed output file descriptor as `outfile`.

1. Open `infile` with `open()`. If an error occurs, print a helpful message and exit with a status code indicating that an error occurred. `infile` should be `stdin` if an input file wasn't specified.
2. The first thing in `outfile` must be the file header, as defined in the file `io.h`. The magic number in the header must be `0x8badbeef`. The file size and the protection bit mask you will obtain using `fstat()`. See the man page on it for details.
3. Open `outfile` using `open()`. The permissions for `outfile` should match the protection bits as set in your file header. Any errors with opening `outfile` should be handled like with `infile`. `outfile` should be `stdout` if an output file wasn't specified.
4. Write the filled out file header to `outfile` using `write_header()`. This means writing out the struct itself to the file, as described in the comment block of the function.
5. Create a trie. The trie initially has no children and consists solely of the root. The code stored by this root trie node should be `EMPTY_CODE` to denote the empty word. You will need to make a copy of the root node and use the copy to step through the trie to check for existing prefixes. This root node copy will be referred to as `curr_node`. The reason a copy is needed is that you will eventually need to reset whatever trie node you've stepped to back to the top of the trie, so using a copy lets you use the root node as a base to return to.

6. You will need a monotonic counter to keep track of the next available code. This counter should start at `START_CODE`, as defined in the supplied `code.h` file. The counter should be a `uint16_t` since the codes used are unsigned 16-bit integers. This will be referred to as `next_code`.
7. You will also need two variables to keep track of the previous trie node and previously read symbol. We will refer to these as `prev_node` and `prev_sym`, respectively.
8. Use `read_sym()` in a loop to read in all the symbols from `infile`. Your loop should break when `read_sym()` returns false. For each symbol read in, call it `curr_sym`, perform the following:
 - (a) Set `next_node` to be `trie_step(curr_node, curr_sym)`, stepping down from the current node to the currently read symbol.
 - (b) If `next_node` is not `NULL`, that means we have seen the current prefix. Set `prev_node` to be `curr_node` and then `curr_node` to be `next_node`.
 - (c) Else, since `next_node` is `NULL`, we know we have not encountered the current prefix. We buffer the pair (`curr_node->code`, `curr_sym`), where the bit-length of the buffered code is the bit-length of `next_code`. We now add the current prefix to the trie. Let `curr_node->children[curr_sym]` be a new trie node whose code is `next_code`. Reset `curr_node` to point at the root of the trie and increment the value of `next_code`.
 - (d) Check if `next_code` is equal to `MAX_CODE`. If it is, use `trie_reset()` to reset the trie to just having the root node. This reset is necessary since we have a finite number of codes.
 - (e) Update `prev_sym` to be `curr_sym`.
9. After processing all the characters in `infile`, check if `curr_node` points to the root trie node. If it does not, it means we were still matching a prefix. Buffer the pair (`prev_node->code`, `prev_sym`). The bit-length of the code buffered should be the bit-length of `next_code`. Make sure to increment `next_code` and that it stays within the limit of `MAX_CODE`. Hint: use the modulo operator.
10. Buffer the pair (`STOP_CODE`, 0) to signal the end of compressed output. Again, the bit-length of code buffered should be the bit-length of `next_code`.
11. Make sure to use `flush_pairs()` to flush any unwritten, buffered pairs.
12. Use `close()` to close `infile` and `outfile`.

7 Decompression

The following steps for decompression will refer to the input file to decompress as `infile` and the uncompressed output file as `outfile`.

1. Open `infile` with `open()`. If an error occurs, print a helpful message and exit with a status code indicating that an error occurred. `infile` should be `stdin` if an input file wasn't specified.
2. Read in the file header with `read_header()`, which also verifies the magic number. If the magic number is verified then decompression is good to go and you now have a header which contains the original protection bit mask.
3. Open `outfile` using `open()`. The permissions for `outfile` should match the protection bits as set in your file header that you just read. Any errors with opening `outfile` should be handled like with `infile`. `outfile` should be `stdout` if an output file wasn't specified.
4. Create a new word table with `wt_create()` and make sure each of its entries are set to `NULL`. Initialize the table to have just the empty word, a word of length 0, at the index `EMPTY_CODE`. We will refer to this table as `table`.

5. You will need two `uint16_t` to keep track of the current code and next code. These will be referred to as `curr_code` and `next_code`, respectively. `next_code` should be initialized as `START_CODE` and functions exactly the same as the monotonic counter used during compression, which was also called `next_code`.
6. Use `read_pair()` in a loop to read all the pairs from `infile`. We will refer to the code and symbol from each read pair as `curr_code` and `curr_sym`, respectively. The bit-length of the code to read is the bit-length of `next_code`. The loop breaks when the code read is `STOP_CODE`. For each read pair, perform the following:
 - (a) As seen in the decompression example, we will need to append the read symbol with the word denoted by the read code and add the result to `table` at the index `next_code`. The word denoted by the read code is stored in `table[curr_code]`. We will append `table[curr_code]` and `curr_sym` using `word_append_sym()`.
 - (b) Buffer the word that we just constructed and added to the table with `buffer_word()`. This word should have been stored in `table[next_code]`.
 - (c) Increment `next_code` and check if it equals `MAX_CODE`. If it has, reset the table using `wt_reset()` and set `next_code` to be `START_CODE`. This mimics the resetting of the trie during compression.
7. Flush any buffered words using `flush_words()`.
8. Close `infile` and `outfile` with `close()`.

8 LZ78 Algorithm Pseudocode

8.1 Compression

COMPRESS(*infile, outfile*)

```

1  root = TRIE_CREATE()
2  curr_node = root
3  prev_node = NULL
4  curr_sym = 0
5  prev_sym = 0
6  next_code = START_CODE
7  while READ_SYM(infile, &curr_sym) is TRUE
8      next_node = TRIE_STEP(curr_node, curr_sym)
9      if next_node is not NULL
10         prev_node = curr_node
11         curr_node = next_node
12     else
13         BUFFER_PAIR(outfile, curr_node.code, curr_sym, BIT-LENGTH(next_code))
14         curr_node.children[curr_sym] = TRIE_NODE_CREATE(next_code)
15         curr_node = root
16         next_code = next_code + 1
17     if next_code is MAX_CODE
18         TRIE_RESET(root)
19         curr_node = root
20         next_code = START_CODE
21     prev_sym = curr_sym
22 if curr_node is not root
23     BUFFER_PAIR(outfile, prev_node.code, prev_sym, BIT-LENGTH(next_code))
24     next_code = (next_code + 1) % MAX_CODE
25 BUFFER_PAIR(outfile, STOP_CODE, 0, BIT-LENGTH(next_code))
26 FLUSH_PAIRS(outfile)

```

8.2 Decompression

DECOMPRESS(*infile*, *outfile*)

```
1  table = WT_CREATE()
2  curr_sym = 0
3  curr_code = 0
4  next_code = START_CODE
5  while READ_PAIR(infile, &curr_code, &curr_sym, BIT-LENGTH(next_code)) is TRUE
6      table[next_code] = WORD_APPEND_SYM(table[curr_code], curr_sym)
7      buffer_word(outfile, table[next_code])
8      next_code = next_code + 1
9      if next_code is MAX_CODE
10         WT_RESET(table)
11         next_code = START_CODE
12  FLUSH_WORDS(outfile)
```

9 Deliverables

You will need to turn in:

1. Makefile:

- `CFLAGS=-Wall -Wextra -Werror -Wpedantic` must be included.
- `CC=clang` must be specified.
- `make clean` must remove all files that are compiler generated.
- `make infer` must run `infer` on your program. Complaints generated by `infer` must be either fixed or explained in your README.
- `make encode` should build your encode program.
- `make decode` should build your decode program.
- `make` should build both encode and decode, as should `make all`.
- Your programs should have no memory leaks.

2. Your programs *must* have the following source and header files:

- `encode.c`: contains the `main()` function for the encode program.
- `decode.c`: contains the `main()` function for the decode program.
- `trie.c` and `trie.h`: the source and header file for the Trie ADT.
- `word.c` and `word.h`: the source and header file for the Word ADT.
- `io.c` and `io.h`: the source and header for the I/O module.
- `code.h`: the header file containing macros for special codes.

3. You may have other source and header files, but *do not try to be overly clever*.

4. `README.md`: This must be in markdown. This should describe how to use your program and Makefile. This also contains any explanations for complaints generated by `infer`.

5. `DESIGN.pdf`: This must be a PDF. The design document should describe your design for your program with enough detail that a sufficiently knowledgeable programmer would be able to replicate your implementation. This does not mean copying your entire program in verbatim. You should instead describe how your program works with supporting pseudo-code.

6. Working encode and decode programs, along with test files, will be available on CANVAS.

10 Submission

To submit your assignment, refer back to `assignment0` for the steps on how to submit your assignment through `git`. Remember: *add*, *commit*, and *push*!

Your assignment is turned in *only* after you have pushed. If you forget to push, you have not turned in your assignment and you will get a *zero*. “I forgot to push” is not a valid excuse. It is *highly* recommended to commit and push your changes *often*.