

## Homework 1

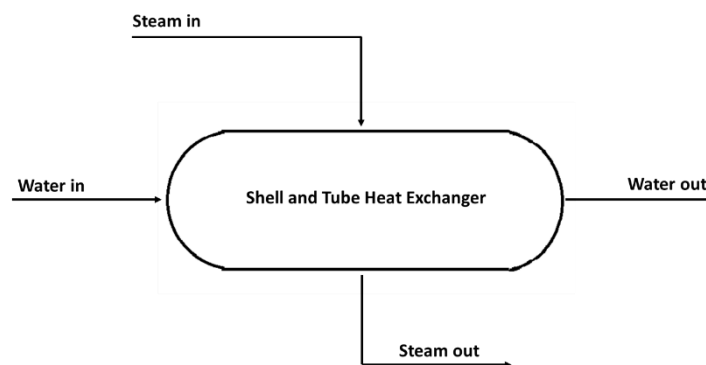
### Instructions:

- Total of 8 questions:
- HW1 will count for 5% of the overall marks.
- Grading here will be out of 70 marks
- The HW should be submitted on MS Team. The deadline is Friday 21<sup>st</sup> Jan 2022 Midnight.
- TA help session can be arranged based on your requests.

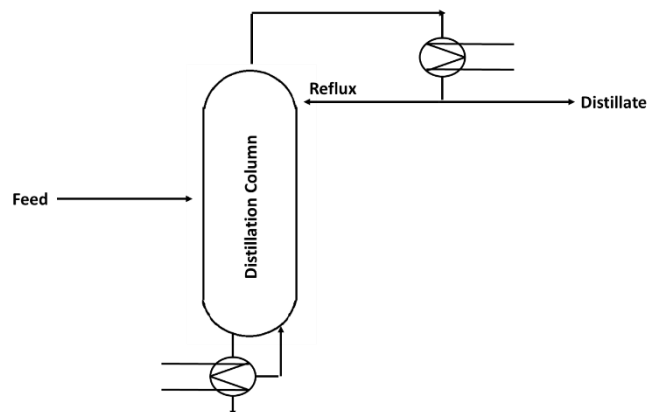
### 1. Marks: [5]

Propose a feedback control method and feedforward control method with schematics diagrams for the following: Choose appropriate MV. You can just choose 1 MV for each question.

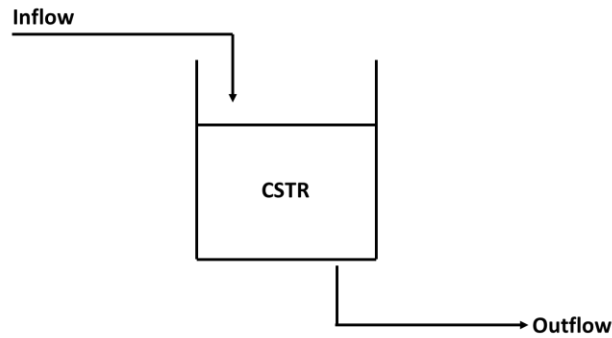
- a) To maintain the exit temperature of water (**water out**) in the shell and tube heat exchanger.



- b) To maintain the production of distillate (**composition**) with the required percentage of the product.



- c) To maintain the height of liquid column in the CSTR. Choose appropriate MV.



## 2. Marks: [10]

Tutorial 2 covered the derivation of 2.4.6 “The Continuous Stirred-Tank Reactor (CSTR)” equations. The following equations were derived:

$$V \frac{dc_A}{dt} = q(c_{Ai} - c_A) - Vkc_A \quad 1$$

$$V\rho C \frac{dT}{dt} = wC(T_i - T) + (-\Delta H_R)Vkc_A + UA(T_c - T) \quad 2$$

Where the reaction constant is Arrhenius function of temperature, i.e.

$$k = k_0 e^{-E/RT} \quad 3$$

- Explain each term present in equations 1 and 2 along with their units. [2]
- Is this linear or non-linear model? [1]
- Solve example 2.5 (Page no. – 27,4<sup>th</sup> edition) by simulating the system using ode15s using the values given in Table 2.3. [7]

**3. Laplace Transform: [10 (3+3+4)]**

- a. Let  $f(s) = \frac{(s-1)(s+1)}{s(s+3)(s-4)}$ . Find  $f(t = 0)$ .  
 b. Find the solution of the following set of equations:

$$\frac{dx_1}{dt} = 2x_1 + x_2 + 1; \quad x_1(0) = 0$$

$$\frac{dx_2}{dt} = 2x_1 + 3x_2 + e^t; \quad x_2(0) = 0$$

- c. Solve the following equation for  $x(t)$

$$\frac{dx}{dt} = \int_0^t x(t) dt - t$$

$$x(0) = 3$$

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**4. Marks: 35**

For the given system (Figure 1) of the tank, answer the following questions. Where  $F_{in}$  and  $F_{out}$  are volumetric flow rate.

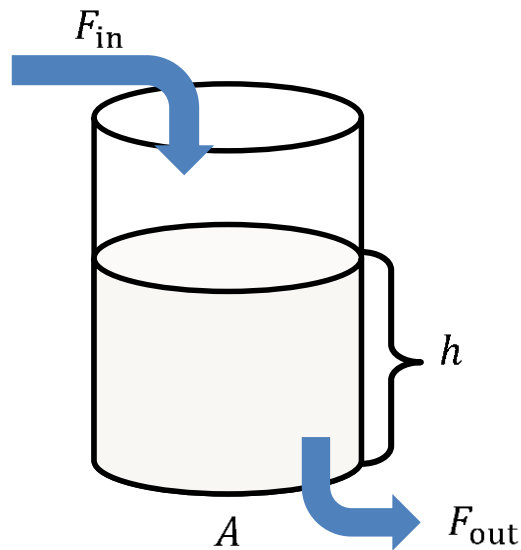


Figure 1

**System#1  $F_{out}$  is constant:**

- a. What will be the steady state model for the tank system? [1]

- b. What will be the dynamic model for the tank system if the density of the fluid is assumed to be constant? [2]
- c. For  $A = 1\text{m}^2$ ,  $F_{\text{in}} = 1\text{m}^3/\text{h}$  and  $F_{\text{out}} = 1.1\text{m}^3/\text{h}$ , when will be the tank become empty if it is initially filled up to 1m. Find the solution analytically. [2]

**System#2  $F_{\text{out}}$  is linear function of height ( $F_{\text{out}} = \alpha_1 h$ )**

- d. If  $F_{\text{out}} = \alpha_1 h$  where  $\alpha_1 = 0.001$ , [10 marks, provided the plot is good]
- Find the analytical solution of the model equation. What is the time constant.
  - Using ode15s, find the numerical solution and plot both the profiles on the same plot (time axis for the plot should be at least 8 times the time constant).
  - What will be the steady state value of height of the tank? Does analytical solution agree with the numerical solution? If not, check your calculations.

**Instructions for plotting:** Plots should be neat with proper axis labels and titles along with legends. Unfinished/unreadable plots will lead to **0 marks** for the entire questions d.

**System#3  $F_{\text{out}}$  is nonlinear function of height ( $F_{\text{out}} = \alpha_1 h$ )**

- e. If  $F_{\text{out}} = \alpha_2 \sqrt{h}$  where  $\alpha_2 = 0.0005$ , [9 marks, provided the plot is good and correct]
- Is it possible to get analytical solution of the model equation? [-]
  - Using ode15s, find the numerical solution and plot both the profiles on the same plot (time axis for the plot should be at least 8 times the time constant).
  - What will be the steady state value of height of the tank? Does analytical solution agree with the numerical solution? If not, check your calculations.

**Instructions for plotting:** Plots should be neat with proper axis labels and titles along with legends. Unfinished/unreadable plots will lead to **0 marks** for the entire questions d.

- f. Which of the system is self-regulating? [1]  
(System#1 (constant  $F_{\text{out}}$ ), System#2, System#3)
- g. For system#3, how does the height profile will change if we change the  $F_{\text{in}} = \frac{1.1\text{m}^3}{\text{h}}$  (from its previous value of  $1\text{m}^3/\text{h}$ ) after it has reached the steady state? What will be the new steady state height? How much time (let's call it  $\tau_{\text{app}}$ ) does it take to reach the 63% of the difference in the steady state height? How much percentage difference in the heights will be covered after time  $3\tau_{\text{app}}$ ? [5]
- h. For system#3, how does the height profile will change if,  $F_{\text{in}} = 0.9\text{m}^3/\text{h}$  (from its previous value of  $F_{\text{in}} = 1\text{m}^3/\text{h}$ )? What will be the new steady state height? How much time (let's call it  $\tau_{\text{app}}$ ) does it take to reach the 63% of the difference in the steady state height? How much percentage difference in the heights will be covered after time  $3\tau_{\text{app}}$ ? [5]

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5. Marks: [4]

Take the following question from the Seborg Book Chapter #2

2.3 Two tanks are connected together in the following unusual way in Fig. E2.3.

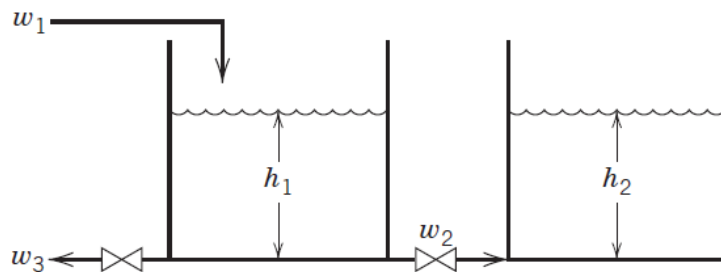


Figure E2.3

- (a) Develop a model for this system that can be used to find  $h_1$ ,  $h_2$ ,  $w_2$ , and  $w_3$  as functions of time for any given variations in inputs.
- (b) Perform a degrees of freedom analysis. Identify all input and output variables.

Notes:

The density of the incoming liquid,  $\rho$ , is constant.

The cross-sectional areas of the two tanks are  $A_1$  and  $A_2$ .

$w_2$  is positive for flow from Tank 1 to Tank 2.

The two valves are linear with resistances  $R_2$  and  $R_3$ .

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Take the following questions from the Seborg Book Chapter #1

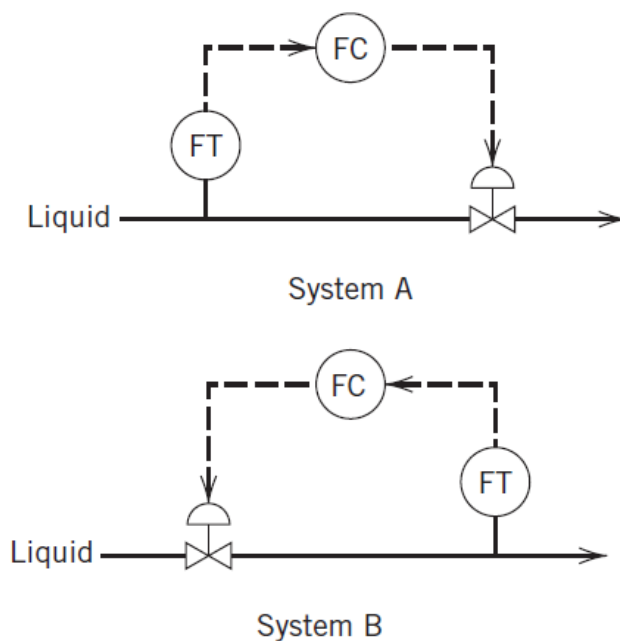
6. Marks: [2]

1.3 In addition to a thermostatically operated home heating system, identify two other feedback control systems that can be found in most residences. Describe briefly how each of them works; include sensor, actuator, and controller information.

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7. Marks: [2]

**1.9** Two flow control loops are shown in Fig. E1.9. Indicate whether each system is either a feedback or a feedforward control system. Justify your answer. It can be assumed that the distance between the flow transmitter (FT) and the control valve is quite small in each system.



**Figure E1.9**

**8. Marks: [2]**

**1.10** In a thermostat control system for a home heating system,

- (a) Identify the manipulated variable
- (b) Identify the controlled variable
- (c) How is the manipulated variable adjusted?
- (d) Name one important disturbance (it must change with respect to time).