

Q1

$$q = C_v f(2) \sqrt{\frac{\Delta P_v}{\rho}}$$

$$q = C_v l \sqrt{\Delta P_v}$$

a) for configuration 1,  $\Delta P = \Delta P_{v_1} + \Delta P_{v_2} = 20 \text{ psi}$

$$= \left( \frac{q}{100 l_1} \right)^2 + \left( \frac{q}{100 l_2} \right)^2 = 20$$

$q$  in terms of  $l_2$  can be given as

$$q^2 \left( \frac{10^2 l_2^2 + 100^2 l_1^2}{100^2 l_1^4 \cdot 10^2 l_2^4} \right) = 20$$

$$q = \sqrt{\frac{20 \cdot 100^4 l_1^2 \cdot 10^2 l_2^2}{10^8 l_2^4 + 100^2 l_1^2}}$$

b) for config 2,

$$\Delta P_{v_1} = \Delta P_{v_2} = 20$$

$$q = q_1 + q_2 \Rightarrow 100 l_1 \sqrt{20} + 10 l_2 \sqrt{20}$$

For series, Since the flow rate is dependent on the resistance offered by both the valves, the increase in  $l_1$ , which leads to decrease in  $R_1$ , leads to increase in overall flow rate.

for large  $l_1$ ,  $l_2$  almost acts as an independent linear valve while for lower  $l_1$ , influence can be seen on  $q$  w.r.t  $l_2$ .

In parallel configuration, ~~more flow rate will be through~~  
The more the  $l_2$  is open the valve is, the greater is the flow

$C_{v1} > C_{v2}$   $\therefore$  flow Resistance of  $V_1 < V_2$  and flow through

$V_1 > V_2$ , so the impact of  $l_2$  on  $q$  is less, while

change in  $l_1$  is huge.

Also flow in parallel is more than in series.

CL 302

HW-4

P. 2

Q2

$$Sp_{gr} = 1.11$$

$$Q = 200 \text{ gal/min} = 45.42 \text{ m}^3/\text{h}$$

$$P_T = K$$

$$\Delta P_c = C_1 Q^2 = 30 \text{ psi} = 206845 \text{ Pa}$$

$$C_1 = \frac{206}{(200)^2} \rightarrow 7.5 \times 10^{-4} \text{ gal}^2/\text{m}^2$$

$$\Delta P_v + \Delta P_c = \Delta P$$

$$P_c = C_1 Q^2 \Rightarrow C_1 = \frac{206845 \text{ N/m}^2 \cdot \text{h}^2}{45.42 \times 45.42 \cdot \text{m}^3 \cdot \text{m}^3} \Rightarrow 10.2 \times 10^{-4} \frac{\text{kg}}{\text{m}^5}$$

$$Sp_{gr} = 1.11$$

$$Q = 200 \text{ gal/min} = 0.012618 \text{ m}^3/\text{s} \Rightarrow 1.26 \times 10^{-2} \text{ m}^3/\text{s}$$

$$\Delta P_c = 30 \text{ psi} = 2.07 \times 10^5 \text{ kg} \cdot \text{m}^{-1} \cdot \text{s}^{-2}$$

$$C_1 = \frac{P_c}{Q^2} = \frac{2.07 \times 10^5}{1.26 \times 10^{-2} \times 1.26 \times 10^{-2}} = \frac{\text{kg} \cdot \text{s}^2}{\text{m}^5} = 1.3 \times 10^9$$

$$(a) = 5 \text{ psi} = 3.44 \times 10^4 \text{ Pa}$$

$$(b) = 20 \text{ psi} = 2.07 \times 10^5 \text{ kg} \cdot \text{Pa}$$

$$(c) = 90 \text{ psi} = 6.2 \times 10^5 \text{ Pa}$$



Azeotropes or constant boiling mixture.

CL 302 HW-4

$R \text{ kg m}^3$

Q2

$\rho_p g r = 1.11$

$q_f = 200 \text{ gal/min} = 45.42 \text{ m}^3/\text{h}$

$P_T = k$

$\Delta P_c = C_1 q^2 = 30 \text{ psi} = 206843 \text{ Pa}$

$C_1 = \frac{30 \text{ psi}}{(200)^2} \Rightarrow 7.5 \times 10^{-4} \text{ gal psi min}^2 / \text{gal}^2$

$\Delta P_v + \Delta P_c = \Delta P$

Flow Rate vs  $\Delta P$   
linear  
Equal V.  
 $f(l) = 0.5$

$Q = C_v f(l) \sqrt{\frac{\Delta P_v}{\rho}}$

(a)  $P_c = C_1 q^2 \Rightarrow C_1 = \frac{206843 \text{ kg/m}^3 \cdot \text{h}^2}{45.42 \times 45.42 \cdot \text{m}^3 \cdot \text{m}^3} \Rightarrow 100.26 \frac{\text{kg h}^2}{\text{m}^9}$

$\rho_p g r = 1.11$

$q = 200 \text{ gal/min} = 0.012618 \text{ m}^3/\text{s} \Rightarrow 1.26 \times 10^{-2} \text{ m}^3/\text{s}$

$\Delta P_c = 30 \text{ psi} = 2.07 \times 10^5 \text{ kg m}^{-1} \text{ s}^{-2}$

$C_1 = \frac{P_c}{q^2} = \frac{2.07 \times 10^5}{1.26 \times 10^{-2} \times 1.26 \times 10^{-2}} = \frac{\text{kg} \cdot \text{s}}{\text{m}^3 \cdot \text{m}^3 \cdot \text{m}^3} = \frac{\text{kg}}{\text{m}^5} 1.3 \times 10^9$

(a)  $= 5 \text{ psi} = 3.44 \times 10^4 \text{ Pa}$

(b)  $= 30 \text{ psi} = 2.07 \times 10^5 \text{ kg Pa}$

(c)  $= 90 \text{ psi} = 6.2 \times 10^5 \text{ Pa}$

# 9.11

let the total pressure be  $k$   
 $\Delta P_v + \Delta P_c = k$

taking  $R=10$

$$q = C_v f(l) \sqrt{\frac{\Delta P_v}{g_s}}$$

$$C_v = \frac{q}{f(l) \sqrt{\frac{\Delta P_v}{g_s}}}$$

$$C_v = \frac{200}{0.5} \left( \frac{\Delta P_v}{1.11} \right)^{-0.5} \Rightarrow$$

$$\Delta P_v = (\Delta \bar{P}_v + \Delta \bar{P}_c) - \Delta P_c = (30 + \bar{P}_v) - \frac{3}{4000} q^2$$

$$q = 400 \left( \frac{\Delta \bar{P}_v}{1.11} \right)^{-0.5}$$

$$q = \left[ 400 \sqrt{\left( \frac{1.11}{\Delta \bar{P}_v} \right)} f(l) \sqrt{\frac{1.11}{30 + \Delta \bar{P}_v - \frac{3}{4000} q^2}} \right]$$

$f(l) = l$   
for linear

$\&$

$$f(l) = R^{l-1}$$

$R$  can be assumed as nothing

a)  $\Delta \bar{P}_v = 5$

and  $f(l)$

$$q = 400 \sqrt{\frac{1.11}{5}} \cdot l \sqrt{\frac{1.11}{30 + 5 - \frac{3}{4000} q^2}}$$

$$l = \frac{q}{188.5} \left( \frac{35 - 0.00075 q^2}{1.11} \right)^{-0.5}$$

for equal  $q$ 's

$$q = 400 \sqrt{\frac{1.11}{5}} \cdot 10^{l-1} \sqrt{\frac{1.11}{35 - 0.00075 q^2}}$$

9.4

$$L = 1 + \frac{\ln \left[ \frac{q}{188.5} \left( \frac{35 - 0.00071 q^2}{1.11} \right)^{-1/2} \right]}{\ln 10}$$

b) taking inspiration from a)  $p=30$

for linear,

$$L = \frac{q}{76.94} \left( \frac{60 - 0.00075 q^2}{1.11} \right)^{-1/2}$$

for equal %

$$L = 1 + \frac{\ln \left[ \frac{q}{76.94} \left( \frac{60 - 0.00075 q^2}{1.11} \right)^{-1/2} \right]}{\ln 10}$$

c)  $p=90$

for linear

$$L = \frac{q}{44.22} \left( \frac{120 - 0.00075 q^2}{1.11} \right)^{-0.5}$$

for equal %

$$L = 1 + \frac{\ln \left[ \frac{q}{44.22} \left( \frac{120 - 0.00075 q^2}{1.11} \right)^{-0.5} \right]}{\ln 10}$$

Conclusions :

for a)

linear value is not linear,  
Eq 1% is linear for small range

for b)

linear value is linear  
initially (for low L)  
& eq 1% for is linear  
more linear than a)

for c)

linear value is more  
linear for wider values  
and also equal %  
is linear for L > 0.5

As  $\Delta \bar{P}_v \uparrow$ , it  
can handle flour rates  
above  $\bar{q}$  more easily.  
and is higher for  
equal % than linear.

$\Delta \bar{P}_v \uparrow$ ,  $L_{\text{ests}} \uparrow$

range of linearity  $\uparrow$  around nominal flow rate as  $\Delta P \uparrow$

$\Delta P \uparrow$  cost  $\uparrow$



Q3 # 9.9

$T^{\circ}\text{C}$	Measurements, mA
0	4.0
100	8.1
200	11.9
300	16.1
400	20.0

$$\frac{T_m}{T} = \frac{k}{ZS+1}$$

$$k = \frac{20-4}{400-0} = 0.04 \frac{\text{mA}}{^{\circ}\text{C}}$$

from code,  $\Delta Z$  between thermometer & transmitter =  $1.262 \text{ min} \Rightarrow 75.72 \text{ s}$

given  $Z_{\text{thermo}} = 20 \text{ s}$

$$\therefore Z_{\text{trans}} = 75.72 + 20 = 95.72 \text{ s}$$

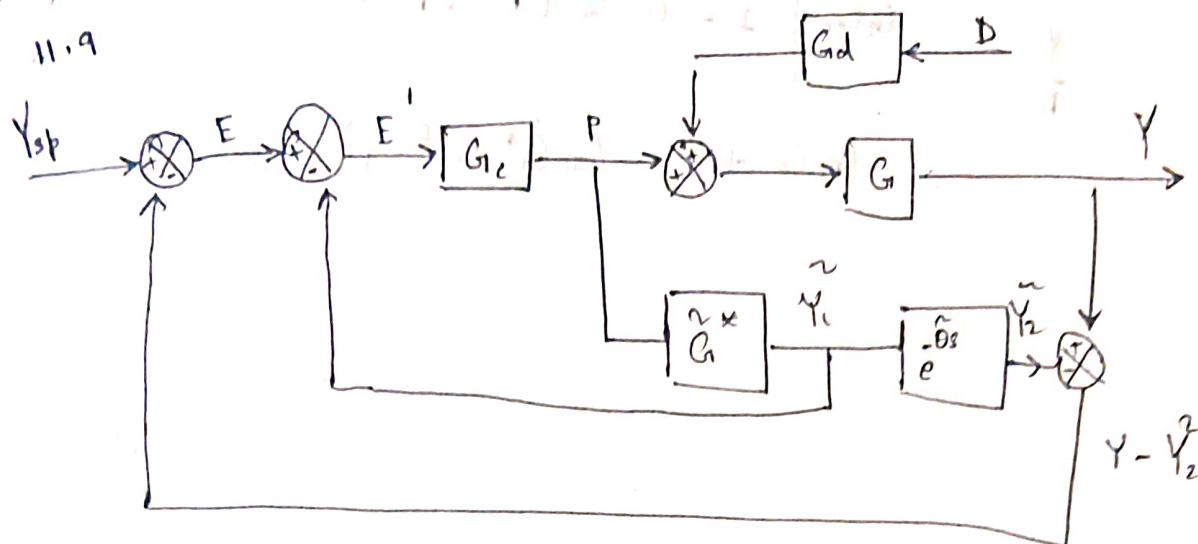
range of linearity  $\uparrow$  around nominal flow rate as  $SP \uparrow$

$SP \uparrow$ , cost  $\uparrow$



(84)

11.9



$$\tilde{Y}_2 = \tilde{Y}_1 e^{-\tilde{\theta}s} \quad \text{--- (V)}$$

$$Y_{sp} - (Y - \tilde{Y}_2) = E \quad \text{--- (IV)}$$

$$E - \tilde{Y}_1 = E' \quad \text{--- (III)}$$

$$P = G_c E' \quad \text{--- (II)}$$

$$(P + G_d D) G = Y \quad \text{--- (I)}$$

$$P \tilde{G}^* = \tilde{Y}_1 \quad \text{--- (VI)}$$

(IV) in (III)

$$\rightarrow Y_{sp} - Y + \tilde{Y}_2 - \tilde{Y}_1 = E'$$

$$\text{(V) in } \rightarrow Y_{sp} - Y + \tilde{Y}_1 \begin{bmatrix} e^{-\tilde{\theta}s} \\ -1 \end{bmatrix} = E'$$

(VI) in

$$Y_{sp} - Y + \underset{\substack{\uparrow \\ G_c E'}}{P \tilde{G}^*} \begin{bmatrix} e^{-\tilde{\theta}s} \\ -1 \end{bmatrix} = E'$$

$$Y_{sp} - Y = E' \left[ 1 - G_c \tilde{G}^* \begin{bmatrix} e^{-\tilde{\theta}s} \\ -1 \end{bmatrix} \right]$$

II in I

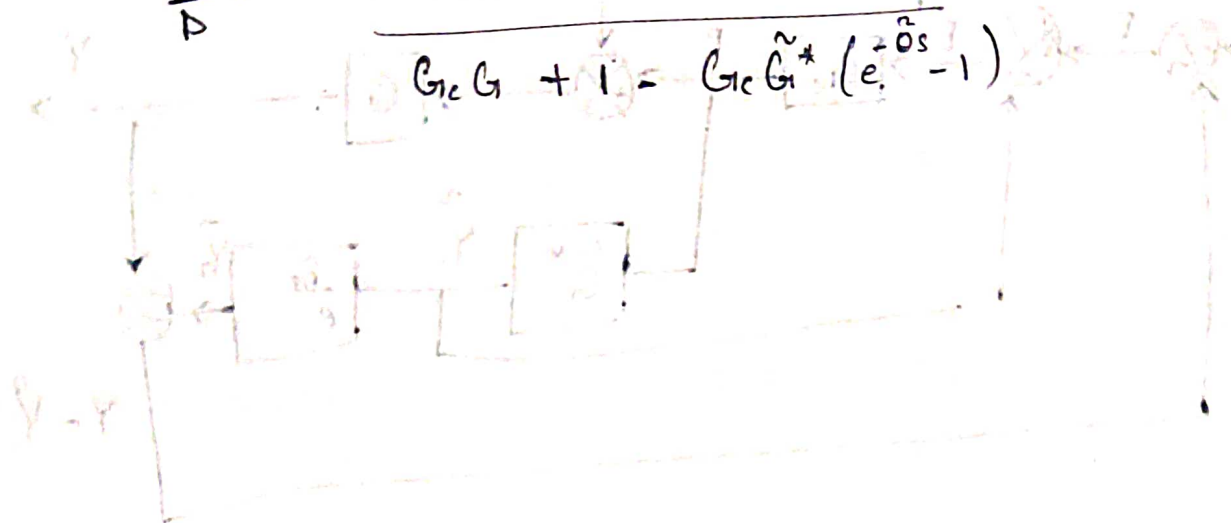
$$(G_c E' + G_d D) G = Y$$

$$(Y_{sp} - Y) - Y = -G_c G_d D \quad \text{Assuming } Y_{sp} = 0$$

 $G_c G$ 

$$\left[ \frac{G_c G + 1 - G_c \tilde{G}^* \begin{bmatrix} e^{-\tilde{\theta}s} \\ -1 \end{bmatrix}}{1 - G_c \tilde{G}^* \begin{bmatrix} e^{-\tilde{\theta}s} \\ -1 \end{bmatrix}} \right] Y = G_c G_d D$$

$$\frac{Y}{D} = \frac{G_1 G_D \left[ 1 - G_c \tilde{G}_i^* (e^{-\tilde{\theta}_s} - 1) \right]}{G_c G + 1 - G_c \tilde{G}_i^* (e^{-\tilde{\theta}_s} - 1)}$$



$$\textcircled{1} \quad \tilde{Y} = \tilde{Y}$$

$$\textcircled{2} \quad \tilde{Y} = (\tilde{Y} \cdot Y) - Y$$

$$\textcircled{3} \quad \tilde{Y} = \tilde{Y} - Y$$

$$\textcircled{4} \quad \tilde{Y} = \tilde{Y} - Y$$

$$\textcircled{5} \quad \tilde{Y} = \tilde{Y} (d \tilde{Y} + 1)$$

$$\textcircled{6} \quad \tilde{Y} = \tilde{Y} \cdot \tilde{Y}$$

$$\tilde{Y} = \tilde{Y} (d \tilde{Y} + 1)$$

$$\tilde{Y} = \tilde{Y} - \tilde{Y}$$

8s)

11.10

$$\bar{Y}_{sp} = K_m Y_{sp}$$

$$E = K_m Y_{sp} - Y K_m$$

$$E K_c = P$$

$$Y_{sp} = 0$$

Find Ans

$$K_c > 1$$

$$(D + G_1 P) G_3 = Y_3$$

$$P = -Y K_m K_c$$

$$Y_3 + P G_2 = Y$$

$$(D + G_1 (-Y K_m K_c)) G_3 + (-Y K_m K_c) G_2 = Y$$

$$D G_3 - Y K_m K_c G_1 G_3 - Y K_m K_c G_2 = Y$$

$$\frac{Y(s)}{D(s)} = \frac{1 + K_m K_c}{1 + K_m K_c G_1 G_3 + K_m K_c G_2} G_3$$

a)

$$= \frac{G_3}{1 + K_m K_c (G_1 G_3 + G_2)}$$

b)

$$G_1(s) = 5$$

$$G_2(s) = \frac{4}{2s+1}$$

$$K_m = 1$$

$$G_3(s) = \frac{1}{s-1}$$

$$\Rightarrow \frac{1/(s-1)}{1 + K_c \left[ \frac{5}{s-1} + \frac{4}{2s+1} \right]} \Rightarrow \frac{1}{(s-1) \left[ 2s^2 - s - 1 + K_c (14s + 1) \right]}$$

$$\frac{2s+1}{2s^2 + (14K_c - 1)s + (K_c - 1)}$$

1	2	$K_c - 1$
2	$14K_c - 1$	
3	$K_c - 1$	

for stable,

$$14K_c - 1 \text{ the product of roots } > 0 \text{ and sum } < 0$$

$$\therefore -\frac{(14K_c - 1)}{2} < 0 \Rightarrow K_c > 1/14 \quad \& \quad \frac{K_c - 1}{2} > 0 \Rightarrow K_c > 1$$

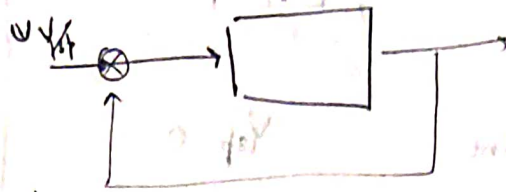
$$\therefore K_c > 1$$



Q6

11.20

$$G_{OL}(s) = 0.5 K_c e^{-3s} / (10s+1)$$



$$Y = (U - Y) G$$

$$\Rightarrow Y(1+G) = U G$$

$$G' \quad \frac{Y}{U} = \frac{G}{1+G} = \frac{0.5 K_c e^{-3s}}{(10s+1) + 0.5 K_c e^{-3s}}$$

a) Padé approx  $e^{-3s} \approx \frac{1-1.5s}{1+1.5s}$

$$\therefore G' = \frac{0.5 K_c e^{\left(\frac{1-1.5s}{1+1.5s}\right)}}{(10s+1) + 0.5 K_c \left(\frac{1-1.5s}{1+1.5s}\right)}$$

for stability, real parts of roots of  $(10s+1)(1+1.5s) + 0.5 K_c(1-1.5s) = 0$

should be  $< 0$

$$\Rightarrow 15s^2 + (11.5 - 0.75K_c)s + (1 + 0.5K_c) = 0$$

for stability,

$$11.5 - 0.75K_c > 0$$

$$\Rightarrow K_c < 15.33$$

$$1 + 0.5K_c > 0 \quad \text{or} \quad K_c > -2$$

therefore  $-2 < K_c < 15.33$

$$b) \quad s = j\omega, \quad e^{-3j\omega} = \cos(3\omega) - j\sin(3\omega)$$

focusing only on denominator part, as it only affects stability

$$(10j\omega + 1) + 0.5k_c [\cos(3\omega) - j\sin(3\omega)] = 0$$

$$\text{for roots} \quad 1 + 0.5k_c \cos(3\omega) = 0$$

$$\text{and} \quad 10\omega - 0.5k_c \sin(3\omega) = 0$$

$$\Rightarrow \omega = 0 \quad \text{or} \quad \text{gives } k_c = -2$$

$$\therefore k_c > -2$$

$$\text{or} \quad \tan(3\omega) = -10\omega$$

$$\omega = 0.58 \quad \text{or} \quad 0.88 \quad (\text{through desmos})$$

$$1 + 0.5k_c \cos(3 \times 0.58) = 0$$

$$k_c = -\frac{1}{0.5 \cos(1.74)} = 11.87$$

stable

$$k_c < 11.87$$

~~-2~~

$$\underline{\underline{0 < k_c < 11.87}}$$

$$c) \quad e^{-3s} \approx 1 - 3s$$

real parts of roots  $< 0$

roots  $< 0$

$$(10s + 1) + 0.5k_c(1 - 3s) = 0$$

$$10s + 1 - 1.5sk_c + 0.5k_c = 0$$

$$s(10 - 1.5k_c) = -0.5k_c$$

$$s = \frac{-0.5k_c}{10 - 1.5k_c}$$

$$\frac{0.5k_c}{10 - 1.5k_c} < 0$$

$$10 - 1.5k_c > 0$$

$$\boxed{10 < k_c < 6.67}$$

$$d) e^{-8s} = \frac{1}{1+3s}$$

$$(10s+1) + 0.5k_c \left( \frac{1}{1+3s} \right) = 0$$

$$(10s^2 + 13s + 1) + 0.5k_c = 0$$

$$10s^2 + 13s + 1 + 0.5k_c$$

for stability,

$$1 + 0.5k_c > 0$$

$$k_c > -2$$

e)

$$(10s+1) \left[ 1 + \frac{3}{5}s + \frac{3}{4}s^2 \right] + 0.5k_c \left[ 1 - \frac{3}{2}s + \frac{3}{4}s^2 \right] = 0$$

$$10s + 15s^2 + 7.5s^3 + 1 + 1.5s + 0.75s^2 + 0.5k_c - 0.75k_cs + 0.375k_cs^2 = 0$$

$$7.5s^3 + (15.75 + 0.375k_c)s^2 + (11.5s - 0.75k_c)s + 1 + 0.5k_c = 0$$

$$15.75 + 0.375k_c > 0$$

$$\underline{k_c > -42}$$

$$11.5 - 0.75k_c > 0$$

$$\underline{k_c < 15.33}$$

Q

$$1 + 0.5k_c > 0$$

$$\underline{k_c > -2}$$

$$\therefore -2 < k_c < 15.33$$



No, both gave the same bounds.

b and e gave the closest responses against b

Rowth Array.

$$7.5$$

$$11.5 - 0.75k_c$$

$$15.75 + 0.375k_c$$

$$1 + 0.5k_c$$

$$b_1 = 1 + 0.5$$

$$b_2 = 0$$

$$b_1 = \frac{(15.75 + 0.375k_c)(11.5 - 0.75k_c)}{15.75 + 0.375k_c} = 7.5(1 + 0.5k_c)$$

$$b_1 = \frac{181.125 - 0.28125k_c^2 - 7.5k_c - 7.5 - 3.75k_c}{15.75 + 0.375k_c}$$

$$c_1 = 1 + 0.5k_c$$

$$b_1 > 0 \Rightarrow \frac{181.125 - 0.28125k_c^2 - 11.25k_c - 7.5}{15.75 + 0.375k_c} > 0$$

$$\text{for } k_c > 0, \quad 15.75 + 0.375k_c > 0$$

$$\Rightarrow 181.125 - 0.28125k_c^2 - 11.25k_c - 7.5 > 0$$

$$\Rightarrow k_c < 11.896 \quad \text{or} \quad k_c > -51.896$$

$$\Rightarrow \underline{\underline{-42 < k_c < 11.896}}$$

if  $k_c \geq 0$

if  $k_c < -42$

$$\text{then } k_c < -51.896 \quad \text{or} \quad k_c > 11.896$$

$$\Rightarrow k_c < -51.896$$

intersection of the two, gives solution

e)

$$-2 < k_c < 11.896$$

→ 2/2 Padé gives a better approximation as the upper limit is closer to actual answer.

→ 2/2 Padé gives the best approximation (e) against b

a)  $k_c \in (-2, 15.33)$

b)  $k_c \in (0, 11.67)$

c)  $k_c \in (-2, 6.67)$

d)  $k_c \in (-2, 0)$

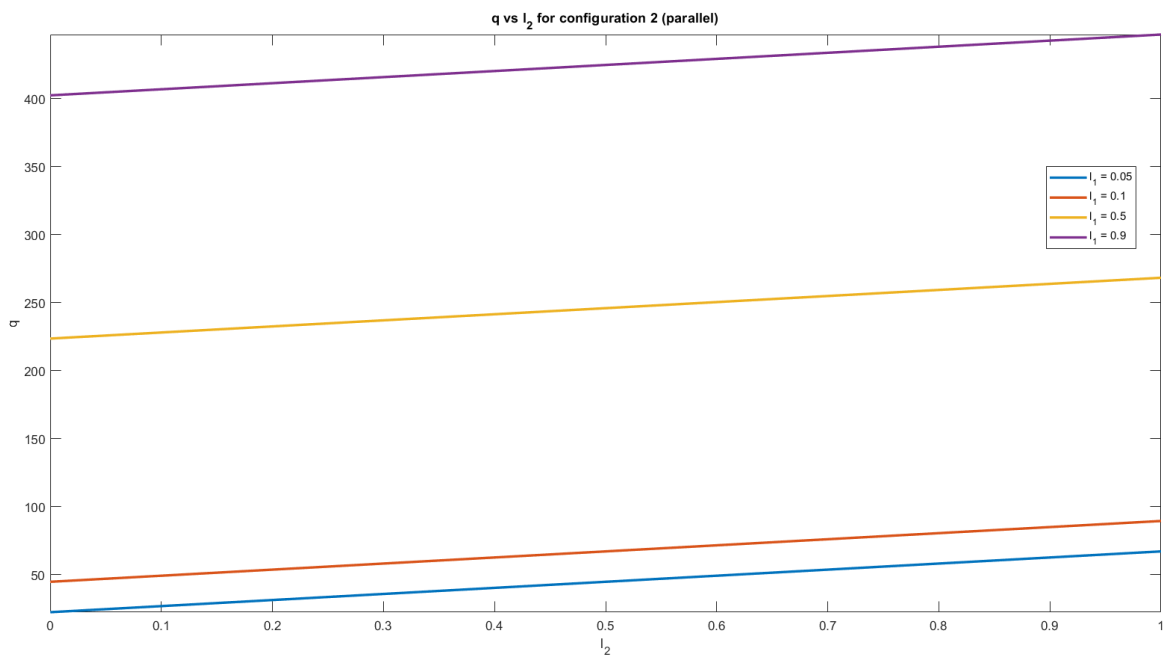
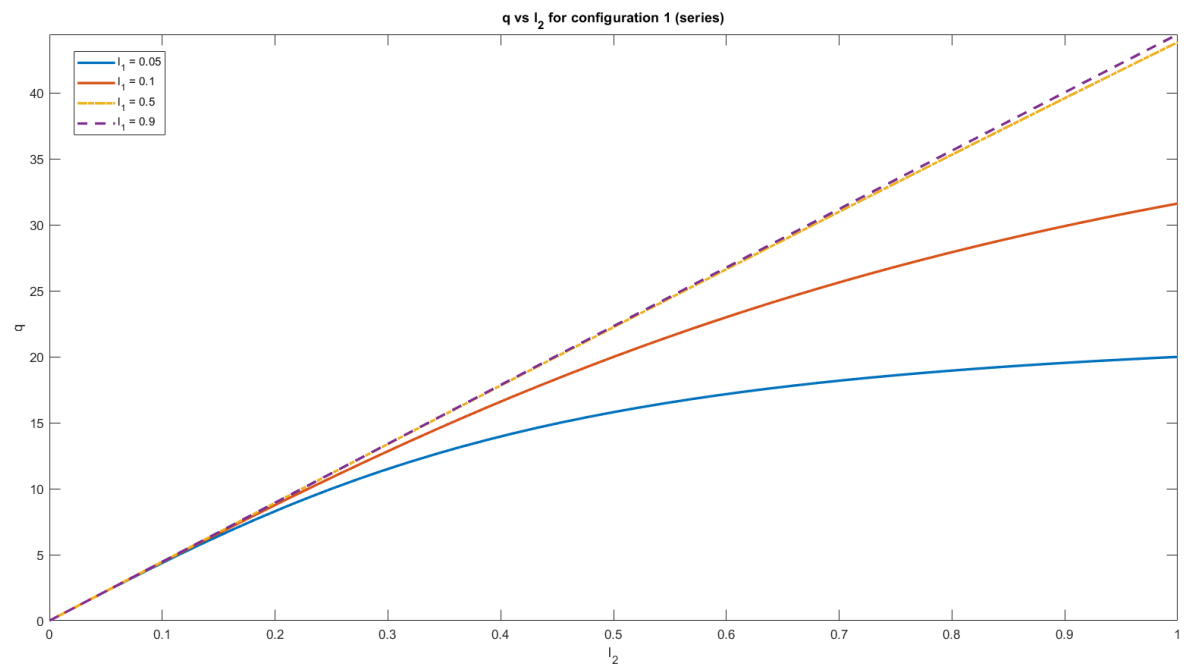
e)  $k_c \in (-2, 11.896)$

Among a) c) & d)

a) gives better

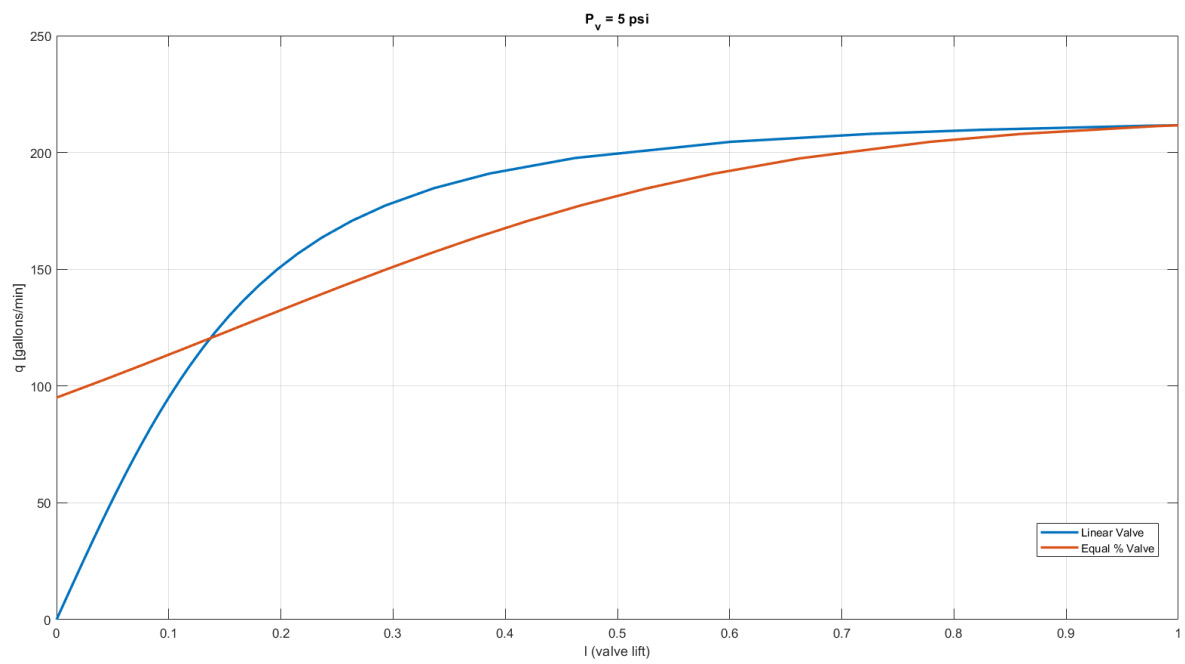
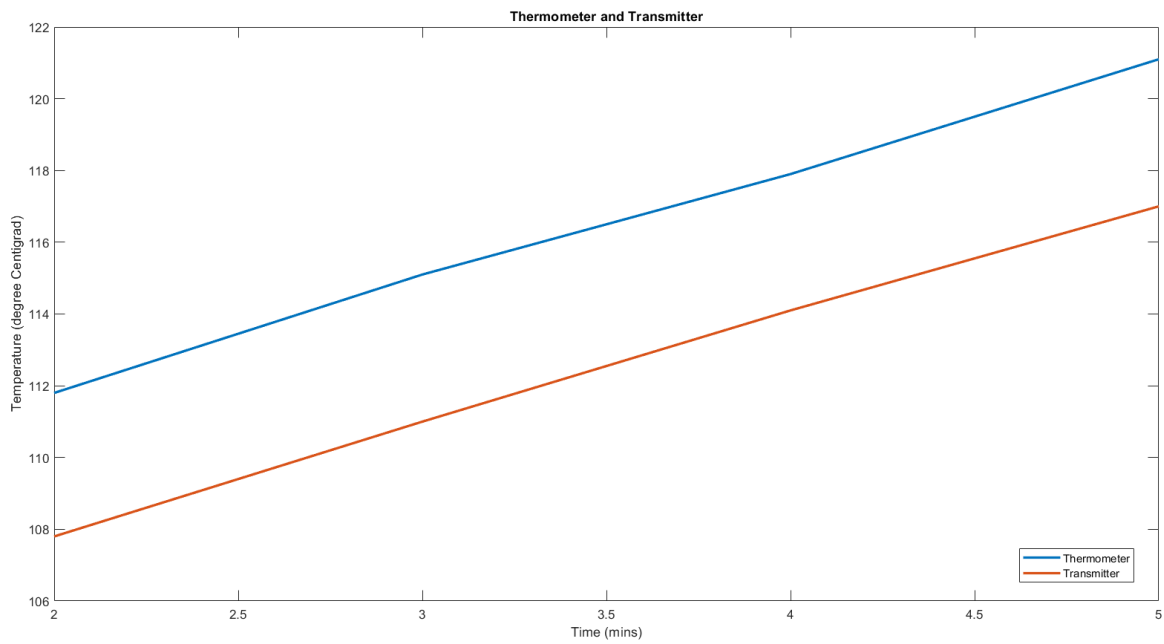
c) gives better amongst c & d (the two taylors)

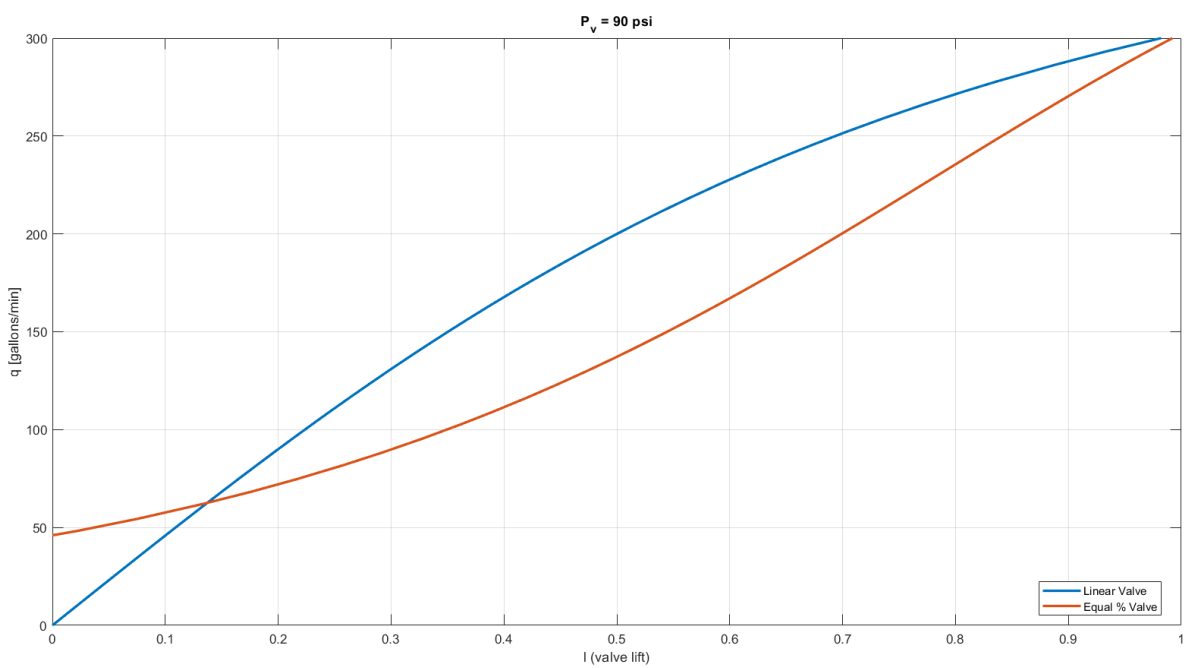
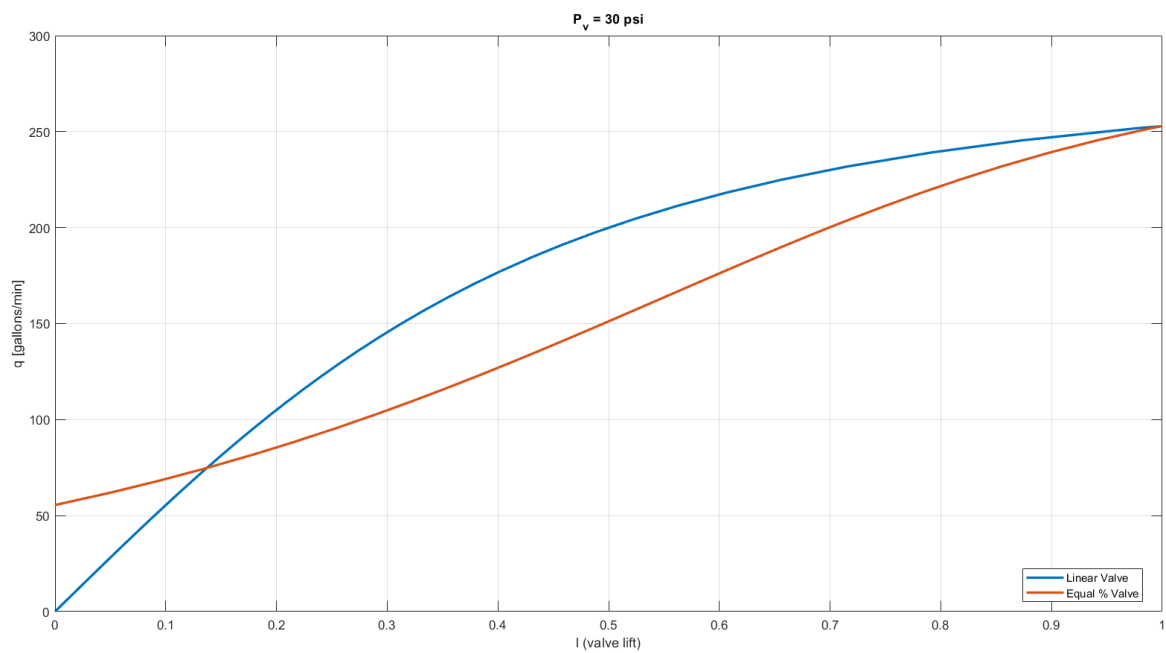
## Plots for Q1





For Question 3





```
% Q1
clc
clear
l=[0.05 0.1 0.5 0.9];
```

```
l = 1×4
    0.0500    0.1000    0.5000    0.9000
```

```
% for config 1
l1=l(1)
```

```
l1 = 0.0500
```

```
q= @(l2) (((20*100*100*10*10*l1*l1*l2*l2)/(10*10*l2*l2 + 100*100*l1*l1)).^0.5);
fplot(q,[0 1],LineWidth=2);
```

Warning: Function behaves unexpectedly on array inputs. To improve performance, properly vectorize your function to return an output with the same size and shape as the input arguments.

```
hold on
l1=l(2);
q= @(l2) (((20*100*100*10*10*l1*l1*l2*l2)/(10*10*l2*l2 + 100*100*l1*l1)).^0.5);
fplot(q,[0 1],LineWidth=2);
```

Warning: Function behaves unexpectedly on array inputs. To improve performance, properly vectorize your function to return an output with the same size and shape as the input arguments.

```
l1=l(3);
q= @(l2) (((20*100*100*10*10*l1*l1*l2*l2)/(10*10*l2*l2 + 100*100*l1*l1)).^0.5);
fplot(q,[0 1], '-.', LineWidth=2);
```

Warning: Function behaves unexpectedly on array inputs. To improve performance, properly vectorize your function to return an output with the same size and shape as the input arguments.

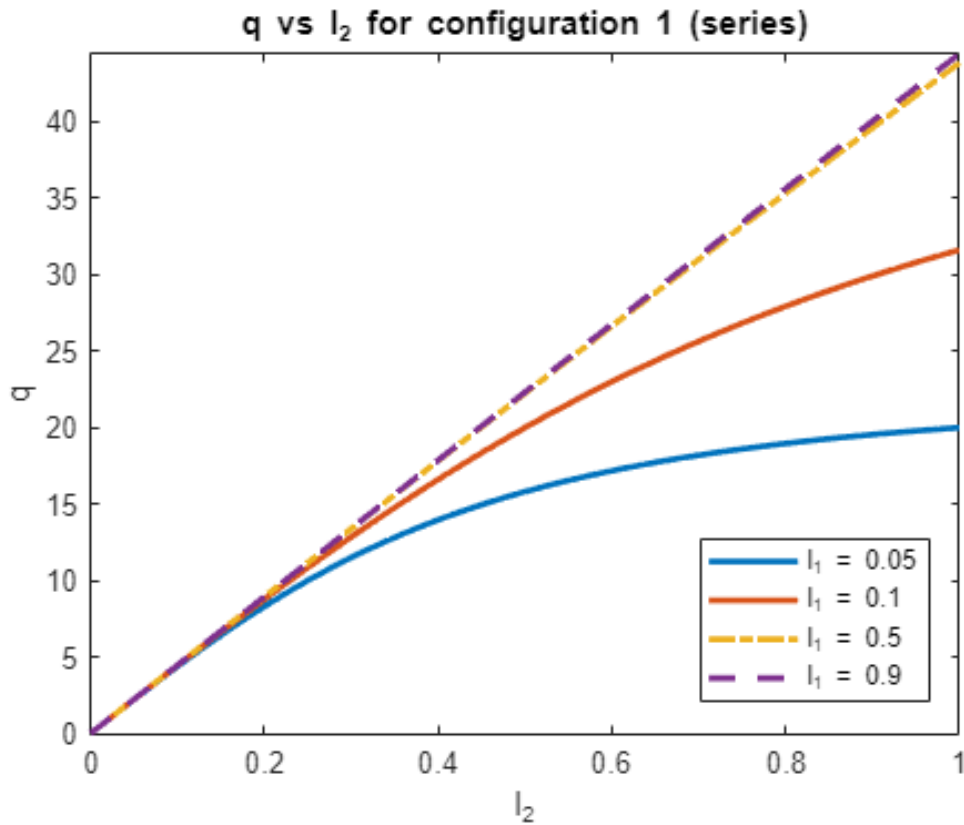
```
l1=l(4);
q= @(l2) (((20*100*100*10*10*l1*l1*l2*l2)/(10*10*l2*l2 + 100*100*l1*l1)).^0.5);
fplot(q,[0 1], '--', LineWidth=2);
```

Warning: Function behaves unexpectedly on array inputs. To improve performance, properly vectorize your function to return an output with the same size and shape as the input arguments.

```
hold off
```

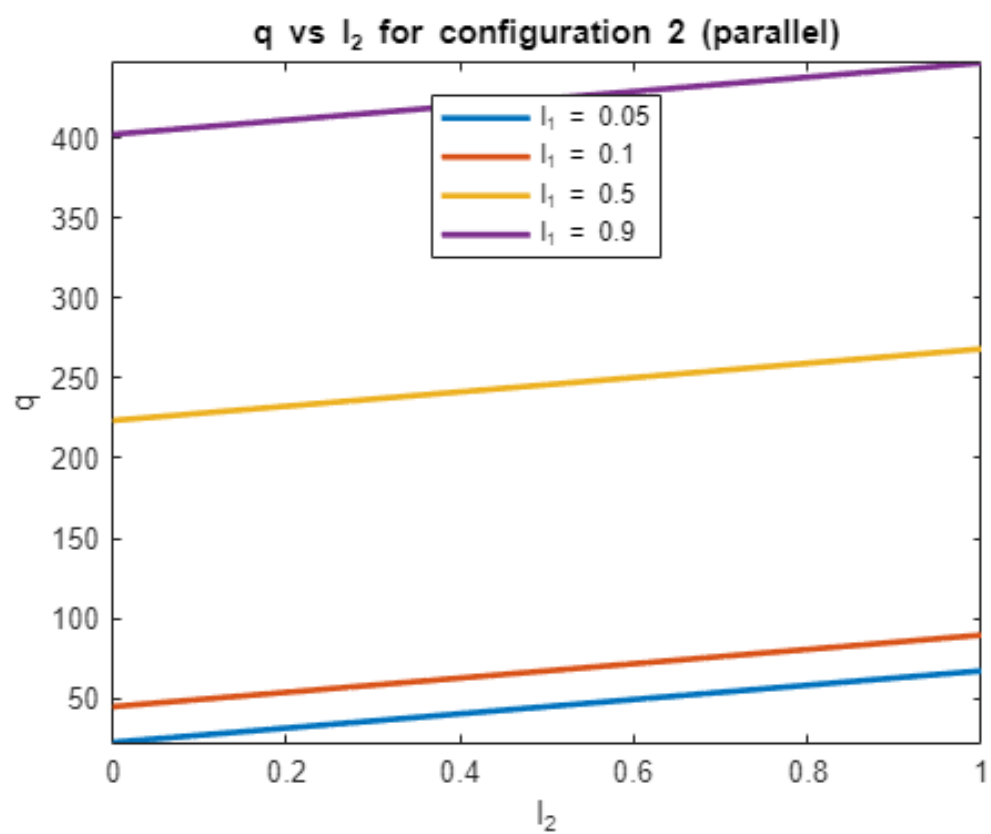
```
title('q vs l_2 for configuration 1 (series)')
xlabel('l_2')
ylabel('q')
legend('l_1 = 0.05', 'l_1 = 0.1', 'l_1 = 0.5', 'l_1 = 0.9', Location='best')
```





```
% for config 2
l1=l(1);
q=@(l2) (100*sqrt(20)*l1+10*sqrt(20)*l2);
fplot(q,[0 1],LineWidth=2);
hold on
l1=l(2);
q=@(l2) (100*sqrt(20)*l1+10*sqrt(20)*l2);
fplot(q,[0 1],LineWidth=2);
l1=l(3);
q=@(l2) (100*sqrt(20)*l1+10*sqrt(20)*l2);
fplot(q,[0 1],LineWidth=2);
l1=l(4);
q=@(l2) (100*sqrt(20)*l1+10*sqrt(20)*l2);
fplot(q,[0 1],LineWidth=2);
hold off

title('q vs l_2 for configuration 2 (parallel)')
xlabel('l_2')
ylabel('q')
legend('l_1 = 0.05','l_1 = 0.1','l_1 = 0.5','l_1 = 0.9',Location='best')
```



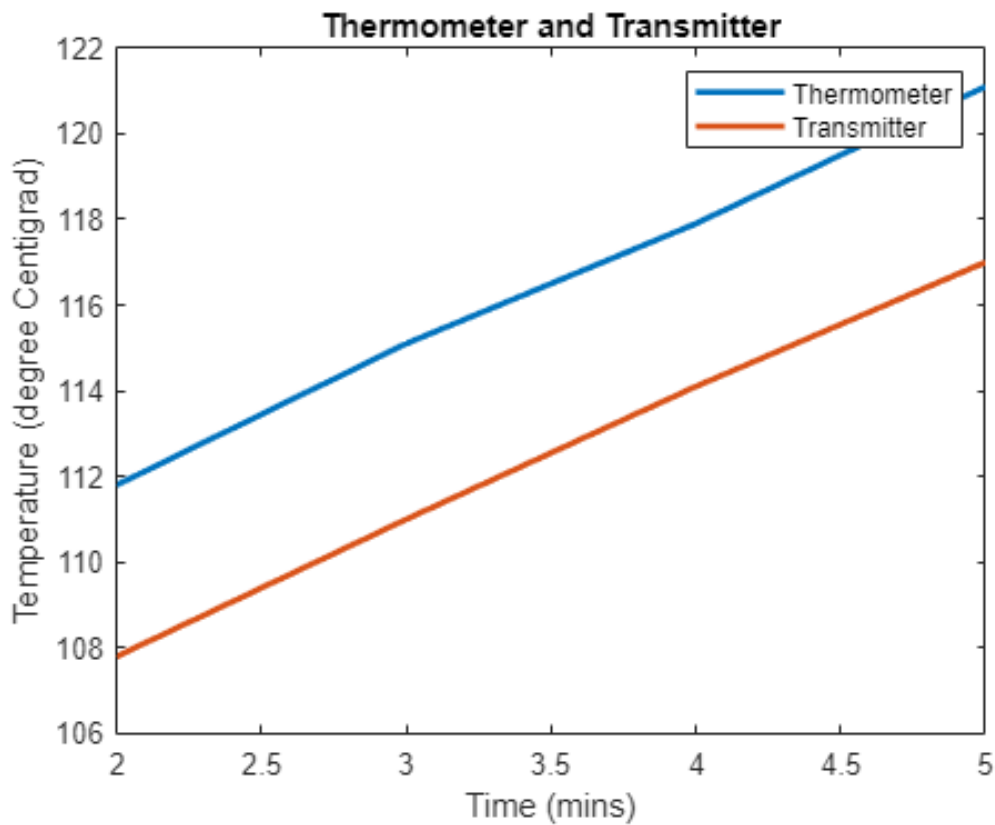
```

% Q3
clc
clear
T = [0 100 200 400];
T_m = [4 8.1 11.9 16.1 20];

t=[2 3 4 5];
Thermo = [111.8 115.1 117.9 121.1];
Trans = [107.8 111 114.1 117];

plot(t,Thermo,'LineWidth',2)
hold on
plot(t,Trans,'LineWidth',2)
hold off
title("Thermometer and Transmitter")
ylabel("Temperature (degree Centigrad)")
legend("Thermometer","Transmitter")
xlabel("Time (mins)")

```



```
x1 = interp1(Thermo,t,112)
```

```
x1 = 2.0606
```

```
x2 = interp1(Trans,t,112)
```

```
x2 = 3.3226
```

```
del_x = x2-x1
```

```
del_x = 1.2620
```

```
del_x*60
```

```
ans = 75.7185
```

```
% for linear valves
```

```
p=5
```

```
p = 5
```

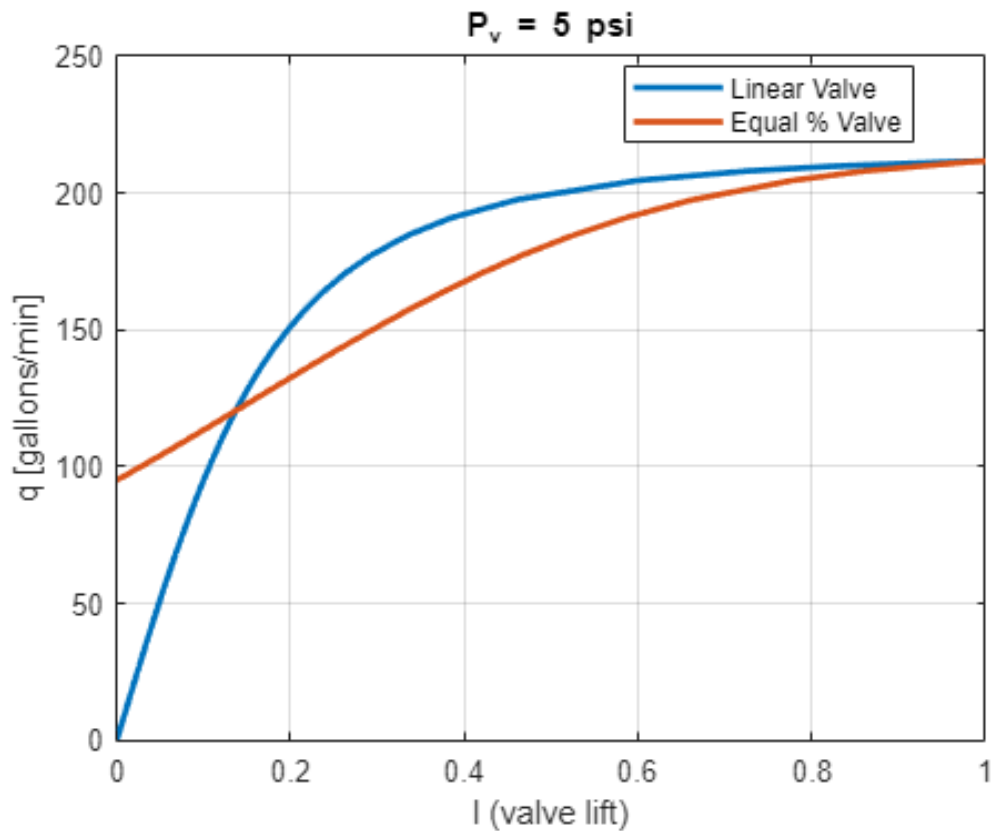
```
l = @(q) ((q/188.5).*((35-0.00075*q.*q)/1.11).^(-0.5));  
[Y,X]=fplot(l,[0 300]);
```

Warning: Having two output arguments for fplot will be removed in a future release. Use the XData and YData properties instead.

```
plot(X,Y,LineWidth=2)  
xlim([0 1]);  
grid on  
hold on  
% for equal %  
l = @(q) ( 1 + (log((q/188.5).*((35-0.00075*q.*q)/1.11).^(-0.5)))/log(10));  
[Y,X]=fplot(l,[0 300]);
```

Warning: Having two output arguments for fplot will be removed in a future release. Use the XData and YData properties instead.

```
plot(X,Y,LineWidth=2)  
xlim([0 1]);  
legend('Linear Valve', 'Equal % Valve',Location='best')  
title('P_v = 5 psi')  
hold off  
xlabel('l (valve lift)')  
ylabel('q [gallons/min]')
```



```
% for linear valves
p=30
```

```
p = 30
```

```
l = @(q) ((q/76.94).*((60-0.00075*q.*q)/1.11).^(-0.5));
[Y,X]=fplot(l,[0 300]);
```

Warning: Having two output arguments for fplot will be removed in a future release. Use the XData and YData properties instead.

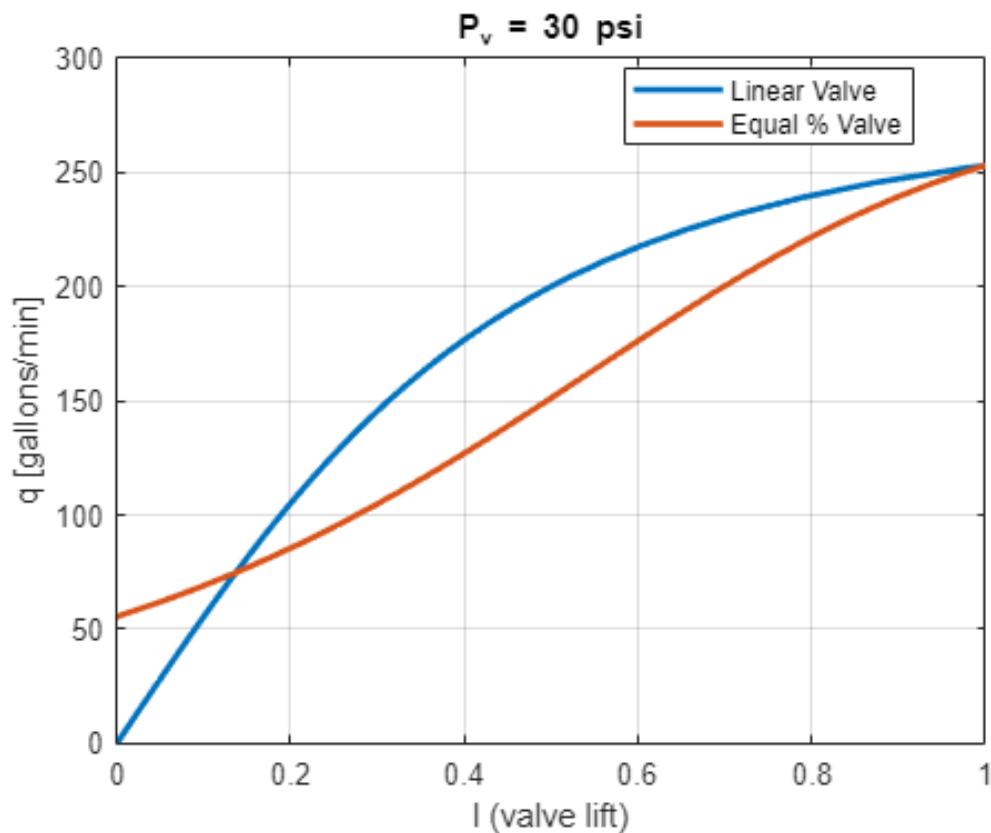
```
plot(X,Y,LineWidth=2)
xlim([0 1]);
grid on
hold on
% for equal %
l = @(q) ( 1 + (log((q/76.94).*((60-0.00075*q.*q)/1.11).^(-0.5)))/log(10));
[Y,X]=fplot(l,[0 300]);
```

Warning: Having two output arguments for fplot will be removed in a future release. Use the XData and YData properties instead.

```
plot(X,Y,LineWidth=2)
xlim([0 1]);
legend('Linear Valve', 'Equal % Valve',Location='best')
title('P_v = 30 psi')
hold off
xlabel('l (valve lift)')
```



```
ylabel('q [gallons/min]')
```



```
% for linear valves
p=90
```

```
p = 90
```

```
l = @(q) ((q/44.42).*((120-0.00075*q.*q)/1.11).^(-0.5));
[Y,X]=fplot(l,[0 300]);
```

Warning: Having two output arguments for fplot will be removed in a future release. Use the XData and YData properties instead.

```
plot(X,Y,LineWidth=2)
xlim([0 1]);
grid on
hold on
% for equal %
l = @(q) ( 1 + (log((q/44.42).*((120-0.00075*q.*q)/1.11).^(-0.5)))/log(10));
[Y,X]=fplot(l,[0 300]);
```

Warning: Having two output arguments for fplot will be removed in a future release. Use the XData and YData properties instead.

```
plot(X,Y,LineWidth=2)
xlim([0 1]);
legend('Linear Valve', 'Equal % Valve',Location='best')
title('P_v = 90 psi')
hold off
```

```
xlabel('l (valve lift)')  
ylabel('q [gallons/min]')
```

