

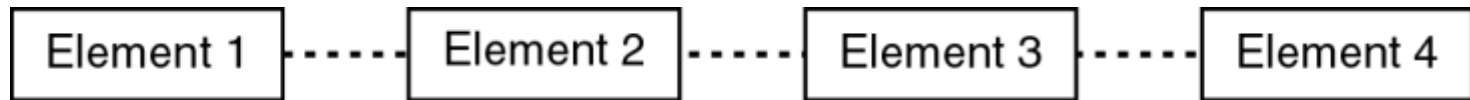
CS 242 – CS252

Data Structures

Linked lists – Part 1

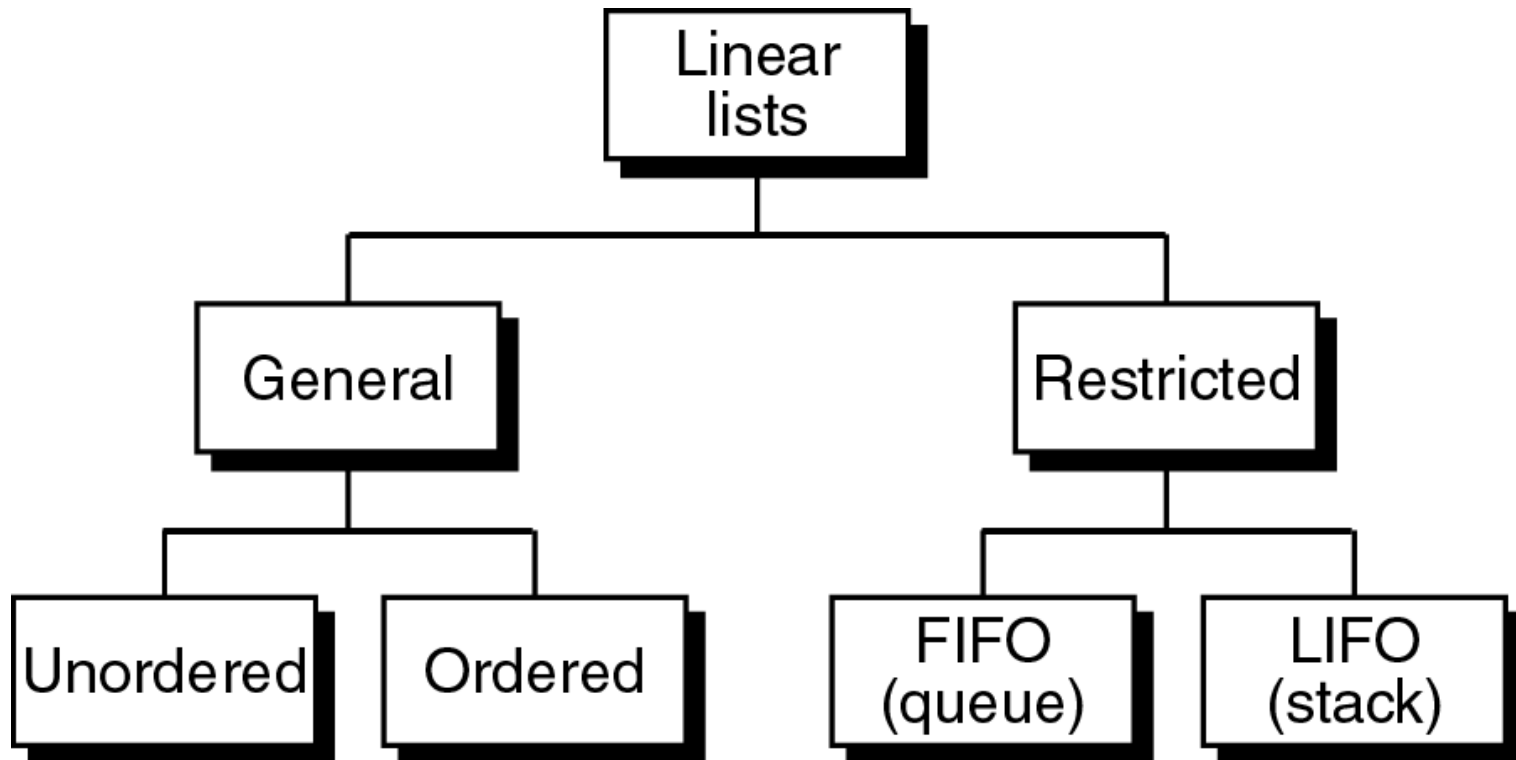
Linear List

- ▶ The sequential property of a linear list is basic to its definition and use.



- ▶ Example: Array, linked list.
- ▶ Array is the simplest linear list structure.
 - ▶ Length of arrays is fixed and unused spaces are wasted
 - ▶ Takes time and space to insert an item anywhere in the array

Linear List



Linear List

- ▶ Linear lists can be categorized into:
 - ▶ General List
 - ▶ Data can be inserted and deleted anywhere
 - ▶ There are no restrictions on the operations that can be used to process the list.
 - ▶ Restricted List
 - ▶ Data can only be inserted or deleted at the ends of structures
 - ▶ Processing is restricted to operations on the data at the ends of the list

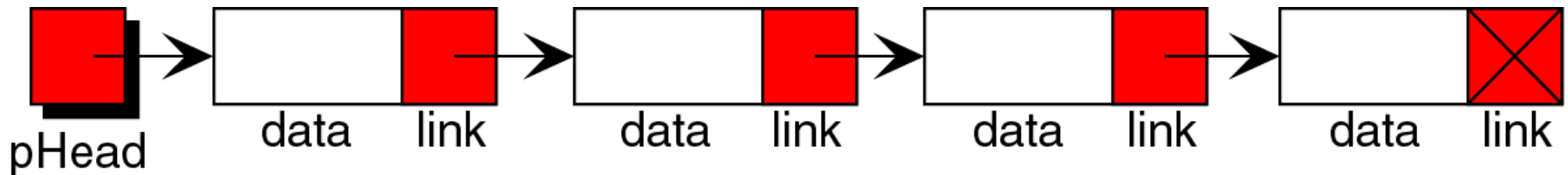
Linear List

- ▶ **General List Structures**
 - ▶ **Un-ordered (Random) list**
 - ▶ There is no ordering of the data.
 - ▶ **Ordered list**
 - ▶ The data arranged according a key.
 - ▶ A key is one or more fields within a structure that are used to identify the data or control their use.
- ▶ **Restricted List Structures**
 - ▶ **FIFO list**
 - ▶ The first in first out. Generally called a queue.
 - ▶ **LIFO list**
 - ▶ The last in first out. Generally called a stack.

Linked List

An ordered collection of data in which each element contains the location of the next element.

- ▶ The simple linked list is commonly known as a **singly linked list** because it contains only one link to a single successor.

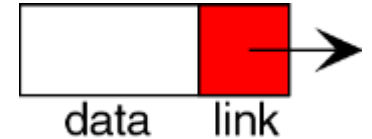


Linked List

- ▶ Each element contains:

- ▶ **Data** to be processed, useful information

- ▶ **Link**, a pointer that identifies the next element in the list, used to chain the data together



- ▶ Elements in Linked List are called **nodes**.

- ▶ Nodes are **self-referential** structures: contains a pointer member that points to a class object of the same class type.

Linked List

- ▶ **Advantages**

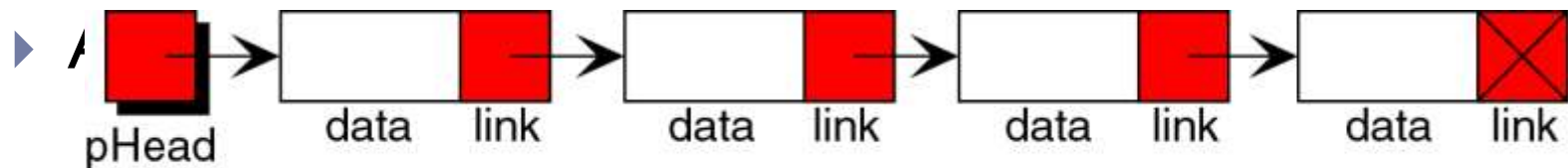
- ▶ Data easily inserted and deleted
- ▶ No need to shift elements of LL to make room for a new element or to delete an element

- ▶ **Disadvantages**

- ▶ We are limited to a sequential search

Linked List Terminology

- ▶ **Head pointer** points to the beginning of the list
- ▶ A node's **successor** is the next node in the sequence
- ▶ The **last** node has **no successor**. (link pointer = null)
- ▶ A node's **predecessor** is the previous node in the sequence
- ▶ The **first** node has **no predecessor**
- ▶ A list's **length** is the number of elements in it



(a) A linked list with a head pointer: pHead



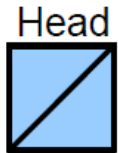
(b) An empty linked list

Linked List

- ▶ ALWAYS REMEMBER TO SET *next* TO SOME VALUE: **EITHER ANOTHER NODE OR TO NULL!!!**



Linked List examples (Single)



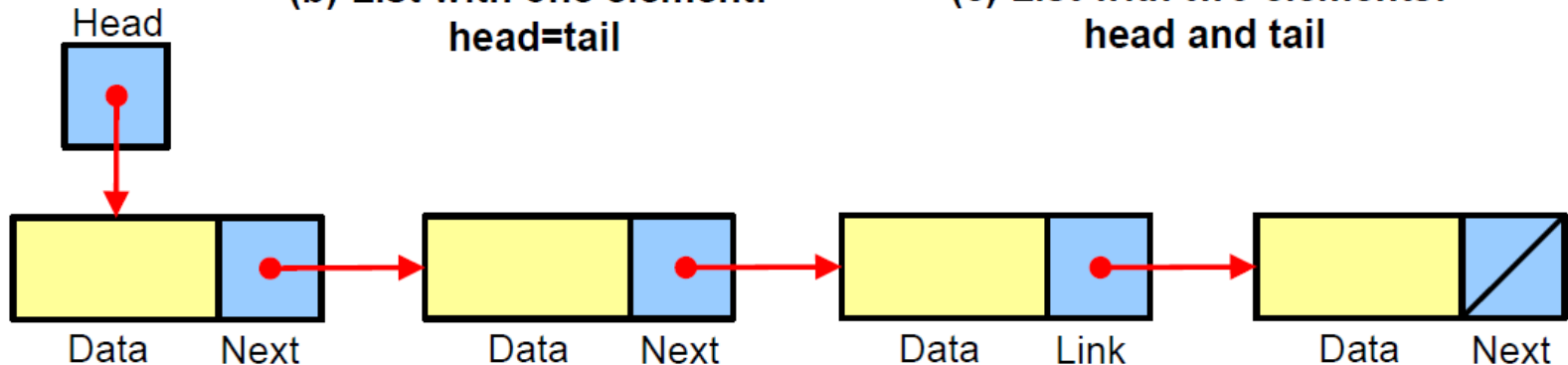
**(a) Empty List,
with no element**



**(b) List with one element:
head=tail**



**(c) List with two elements:
head and tail**

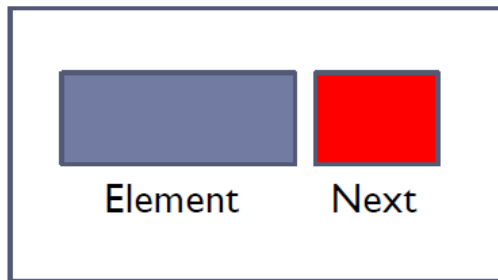


(d) List with 4 elements: head, tail, and 2 intermediate elements

Linked List: Element (Data) Node

▣ Data Node Structure

- ◆ Data type for the list elements depends entirely on the application.



```
public class Node <E>
{
    private E element;
    private Node<E> next;
    .....
}
```

Linked List: Element Node (implementation)



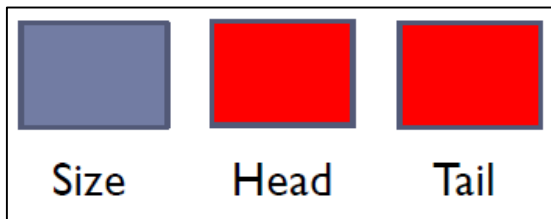
```
public class Node <E>{  
  
    private E element;  
    private Node<E> next;  
  
    public Node(E element, Node<E> next) {  
        this.element = element;  
        this.next = next;  
    }  
  
    public void setElement(E element) {  
        this.element = element;  
    }  
  
    public void setNext(Node<E> next) {  
        this.next = next;  
    }  
  
    public E getElement() {  
        return element;  
    }  
  
    public Node<E> getNext() {  
        return next;  
    }  
}
```

Linked List: Head Node

Head Node Structure

Contain:

1. Reference to head node (points to first node in a linked list or may be contain NULL if the linked list is empty)
2. Metadata which is a data about a list. Ex: count (size), reference to the last node (tail), current positions ...etc.



```
public class SinglyLinkedList<E>
{
    private Node<E> head;
    private Node<E> tail;
    private int size;
    .....
}
```

Linked List: Head Node

- ▶ References to Linked Lists:
 - ▶ A linked list must always have a head pointer.
 - ▶ Depending on how to use the list you may have several other pointers. Ex:
 - ▶ Curr or pos points to a specific location
 - ▶ Tail or rear points to the last node

Singly Linked List ADT

A complete implementation of a `SinglyLinkedList` class, supporting the following methods:

- ▶ **size()**: Returns the number of elements in the list.
- ▶ **isEmpty()**: Returns true if the list is empty, and false otherwise.
- ▶ **first()**: Returns (but does not remove) the first element in the list.
- ▶ **last()**: Returns (but does not remove) the last element in the list.
- ▶ **addFirst(e)**: Adds a new element to the front of the list.
- ▶ **addLast(e)**: Adds a new element to the end of the list.
- ▶ **removeFirst()**: Removes and returns the first element of the list.



Singly Linked List ADT

Linked list operations:

► Basic operations: which means the operation should be to complete implementation of linked list.

1. Create List
2. Insert Node
3. Delete Node
4. Empty List
5. Size

► Extra operations:

1. Search List
 2. Traverse List
 3. Retrieve Node
 4. Destroy List
-



1- Create List

- Initializes the metadata for the list.

```
head = NULL  
Tail = Null  
Size = 0
```



A- Before create list



B- After create list

1- Create List (Constructor) implementation

```
public class SinglyLinkedList<E> {  
    private Node<E> head;  
    private Node<E> tail;  
    private int size;  
  
    public SinglyLinkedList() {  
        head=null;  
        tail=null;  
        size=0;  
    }  
    // Operations on linked lists (Other methods)  
}
```

2- Insert Node

- ▶ We need only the logical predecessor to insert a node into the list.
- ▶ There are three steps for insertion:
 1. Allocate memory for the new node and insert data
 2. Point the new node to its successor.
 3. Point the new node's predecessor to the new node.

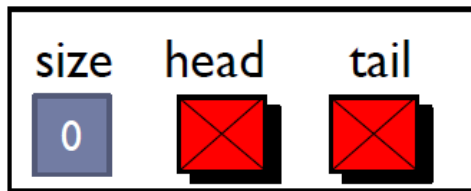
2- Insert Node

- ▶ **Insertion cases:**
 - ▶ Insert into empty list
 - ▶ Insert at beginning
 - ▶ Insert in middle
 - ▶ Insert at end

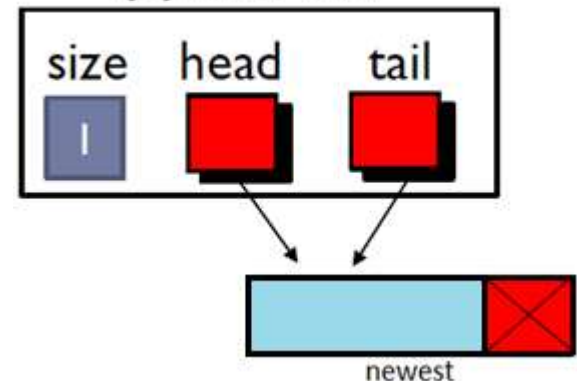
2- Insert Node

► Insert into *empty* list

(a) Before add



(b) After add



Algorithm addFirst(e):

...

newest = Node(e)

newest.next = head

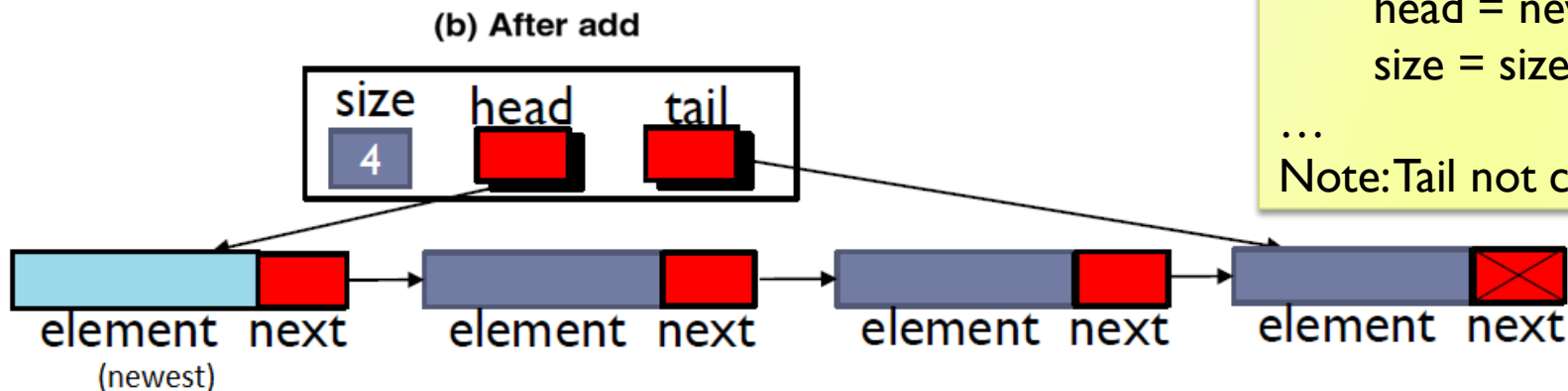
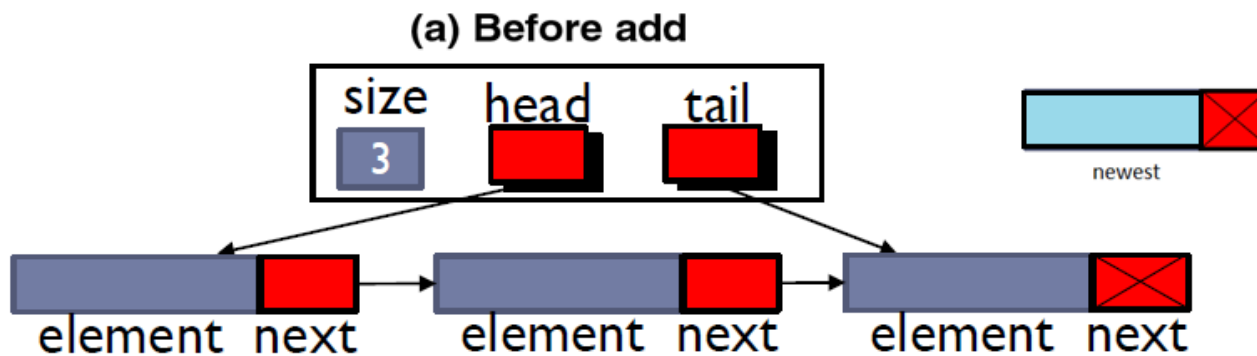
head = newest

Tail = head

size = size + 1

2- Insert Node

► Insert at **beginning (non-empty list)**



Algorithm `addFirst(e)`:

...

```
newest = Node(e)
newest.next = head
head = newest
size = size + 1
```

...

Note: Tail not changed

Insert Node

- ▶ Insert into an **empty** LL or at the **beginning** of the LL is an insertion at the **head**.

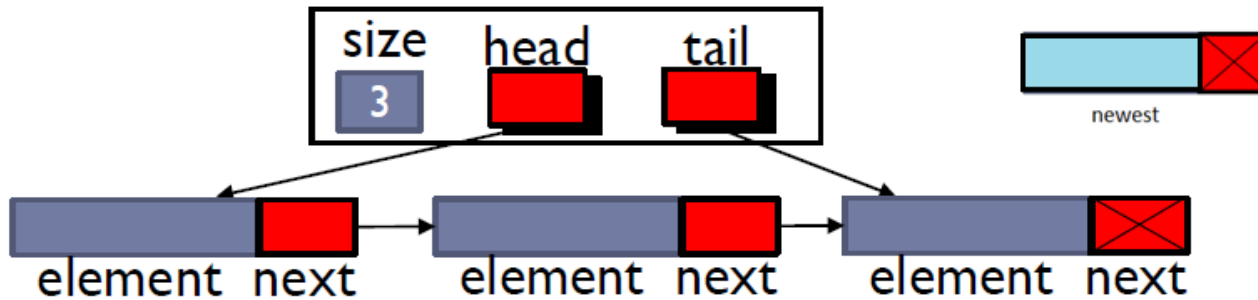
```
public void addFirst(E e) { // adds element e to the front of the list
    head = new Node<>(e, head); // create and link a new node
    if (size == 0)
        tail = head; // special case: new node becomes tail also
    size++;
}
```



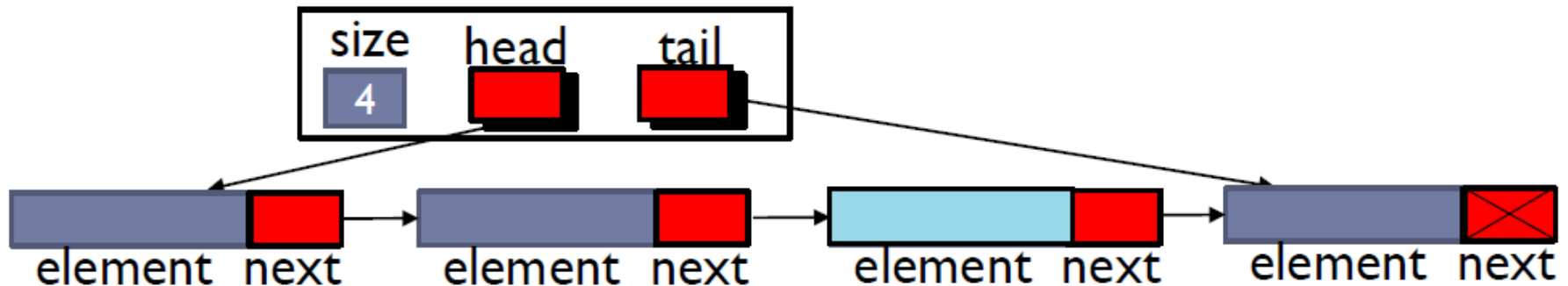
2- Insert Node

► Insert in *middle*

(a) Before add

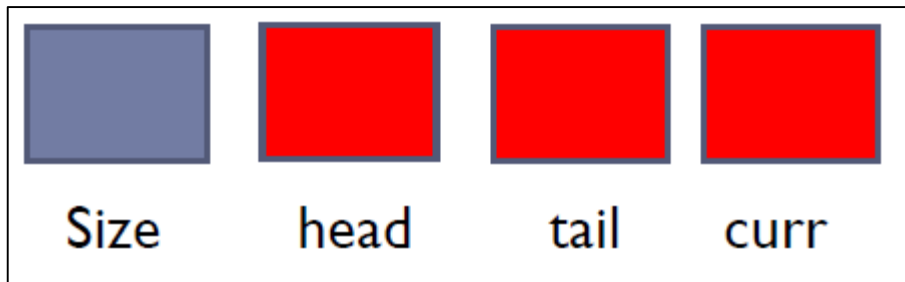


(b) After add



2- Insert Node (in middle)

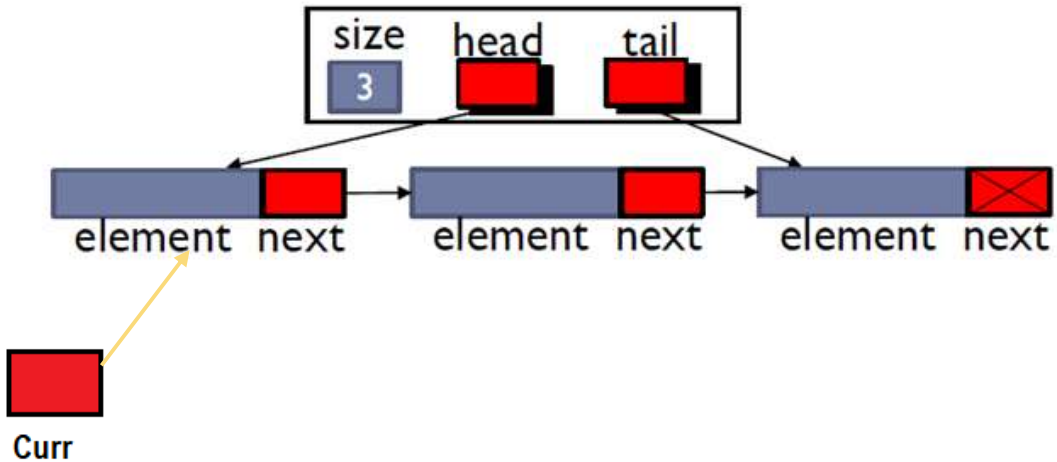
- ▶ `add(e, i)`: adding new node at **index i**
 - ▶ We have to make sure that the value of index i is within the range
- ▶ We need a reference to traverse the list
 - ▶ Contain:
 1. Reference to head node.
 2. Reference to tail node.
 3. **Curr** reference to a specific location.



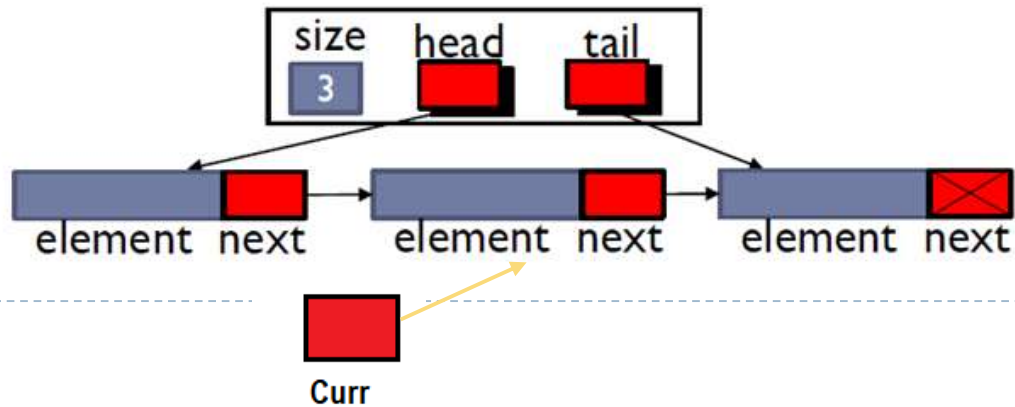
```
public class SinglyLinkedList<E> {  
    private Node<E> head;  
    private Node<E> tail;  
    private Node<E> curr;  
    private int size;  
    .....  
}
```

2- Insert Node (in middle)

1.

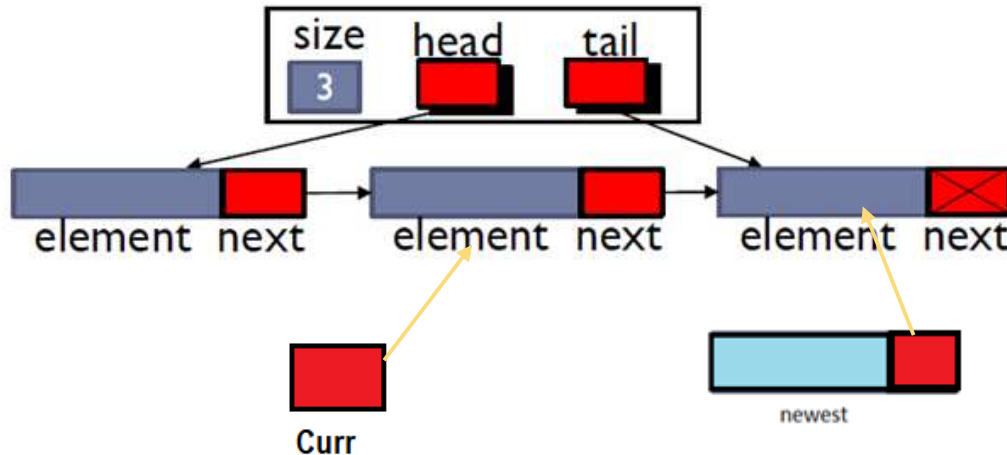


2. First, move (curr) until index-1

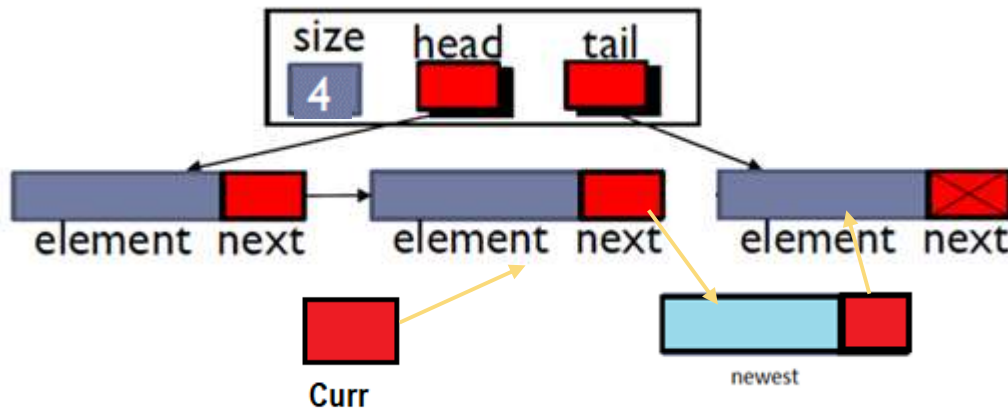


2- Insert Node (in middle)

3. Second, connect the new node to the successor of the



4. Finally, connect current node to the new node and increment the size



2- Insert Node (in middle)

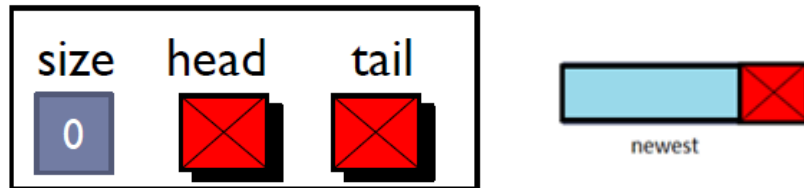
```
public void add(E element, int index)
{
    if(index<0 || index>size)
    {
        System.out.println("Out of bound!");
        return;
    }
    Node<E> newest=new Node<E>(element, null);
    if(index==0) // add at front
    {
        newest.setNext(head);
        head=newest;
        if(tail==null)
            tail=head;
    }
    else // add the middle
    {
        curr=head;
        for(int i=0;i<index-1;i++)
        {
            curr=curr.getNext();
        }
        newest.setNext(curr.getNext());
        curr.setNext(newest);
        if(tail==curr)
            tail=tail.getNext();
    }
    size++;
}
```

2- Insert Node

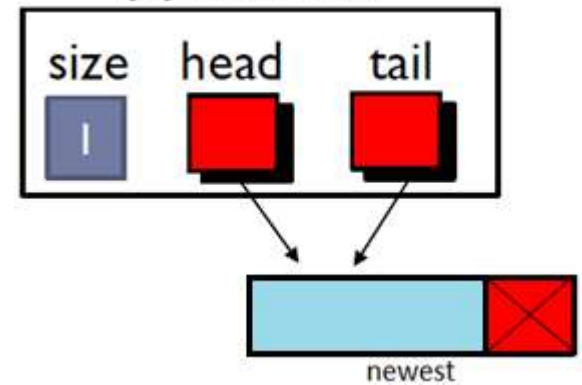
► Insert at **end**

► empty list

(a) Before add

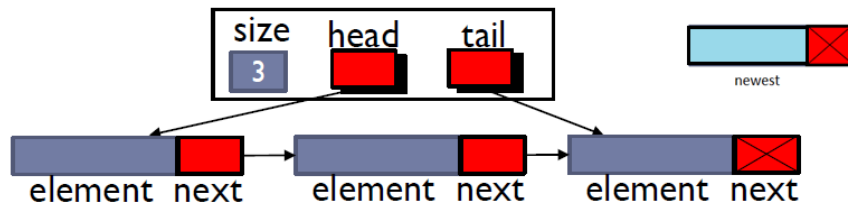


(b) After add

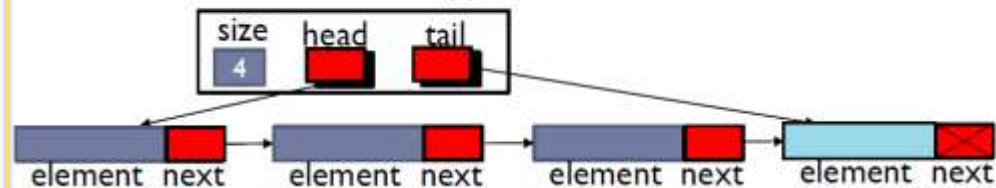


► Non – empty list

(a) Before add



(b) After add



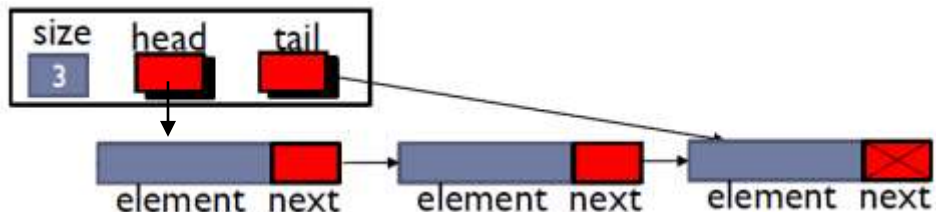
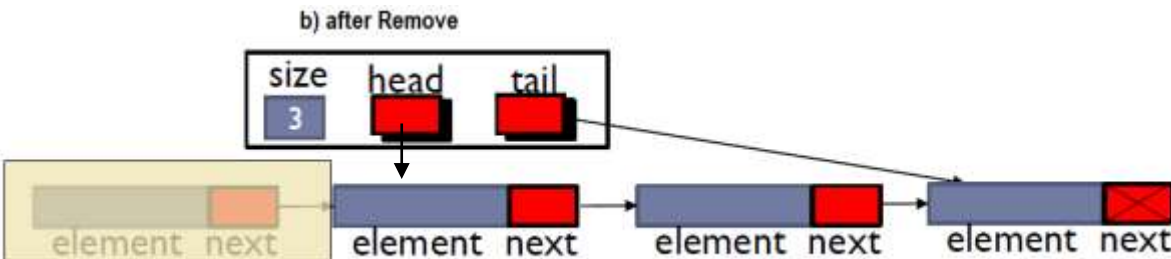
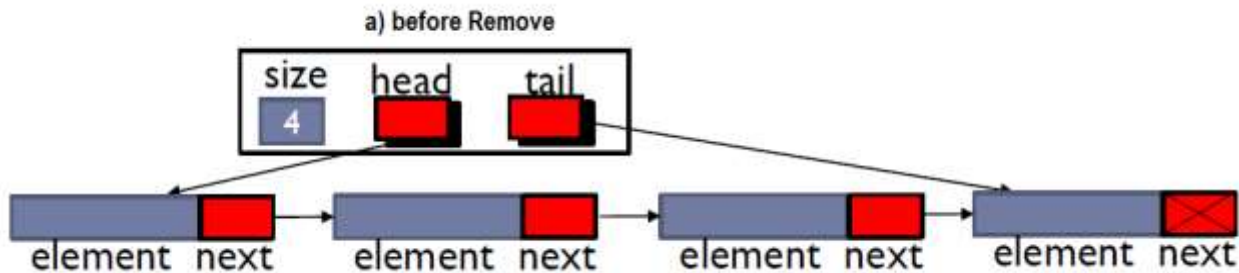
2- Insert Node at end

Algorithm addLast(e):
 newest = Node(e)
 newest.next = null
 If isEmpty
 head = newest
 else
 tail.next = newest
 tail = newest
 size = size + 1

```
public void addLast(E e) { // adds element e to the end of the list
    Node<E> newest = new Node<>(e, null); // node will eventually be the tail
    if (isEmpty())
        head = newest; // special case: previously empty list
    else
        tail.setNext(newest); // new node after existing tail
        tail = newest; // new node becomes the tail
        size++;
}
```

3- Delete (Remove) Node

A. Remove *beginning* (at head)



Algorithm removeFirst():

```
if head == null then
    Print "the list is empty"
else
    head = head.next
    size = size - 1
```


3- Delete (Remove) Node.

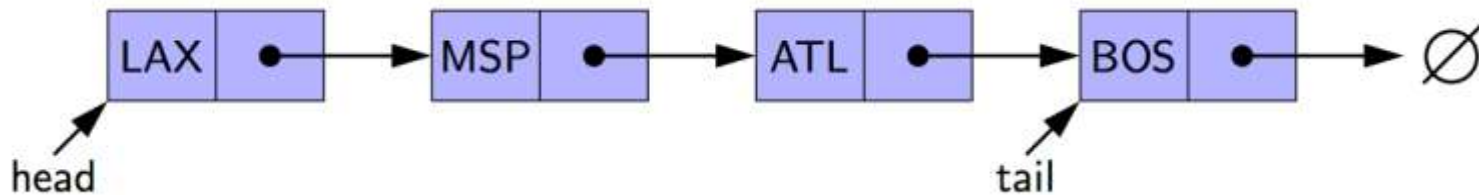
```
,  
public E removeFirst( ) { // removes and returns the first element  
if (isEmpty( )) return null; // nothing to remove  
E answer = head.getElement( );  
head = head.getNext( ); // will become null if list had only one node  
size--;  
if (size == 0)  
tail = null; // special case as list is now empty  
return answer;  
}
```



3- Delete (Remove) Node

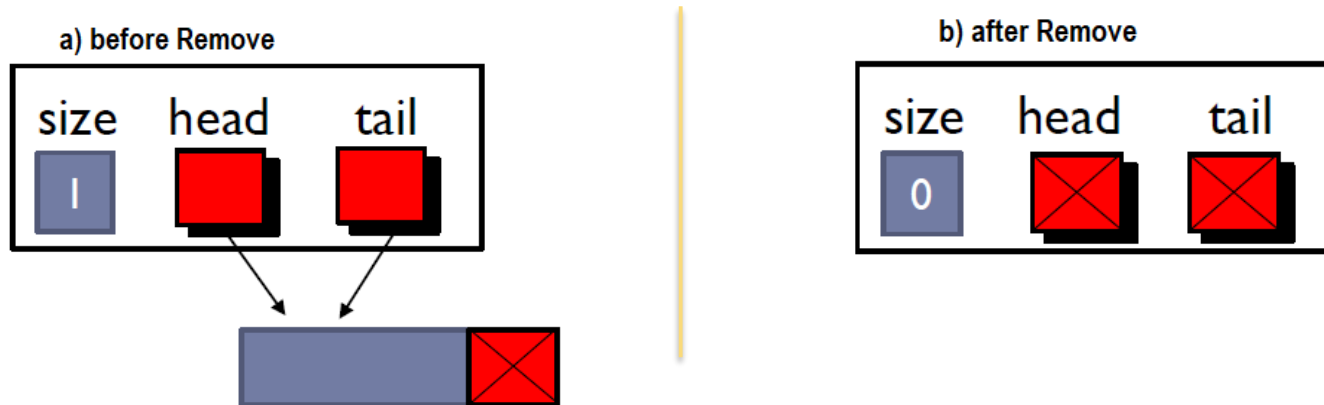
B. Remove **End or last** (at tail)

- ▶ Removing at the tail of a singly linked list is not efficient!
 - ▶ we must be able to access the node before the last node.
 - ▶ The only way to access this node is to start from the head of the list and search all the way through the list which is time consuming.



3- Delete (Remove) Node

c. Deleting from a list of only one element

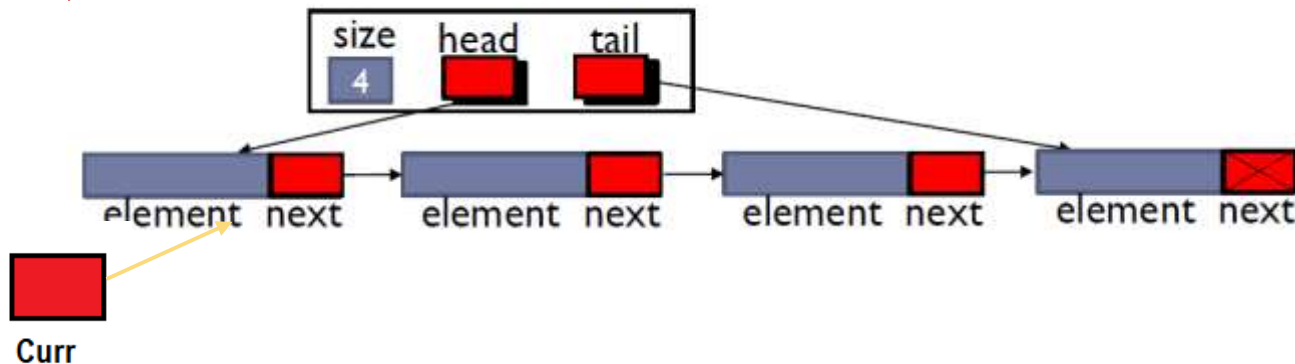


Head = tail = null
size = 0

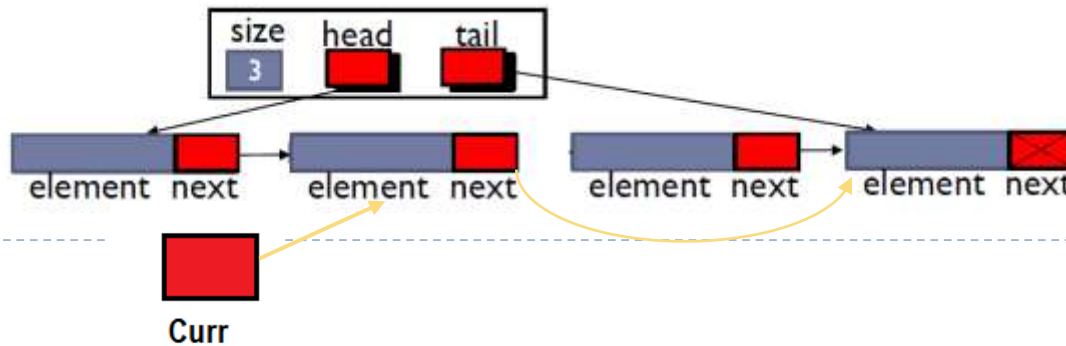
3- Delete (Remove) Node

D. Remove from *middle* (at index i)

- ▶ **remove(e,i)**: removing node at index i and return its element.
- ▶ Similar to add(e,i) in [slide 26](#).
- 1. First, move curr until index -1



- 2. Second, connect the node at i-1 with the node at i+1



3- Delete (Remove) Node

► Remove from ***middle*** (at index i)

```
public E remove(int index)
{
    if(index<0 || index>=size)
    {
        System.out.println("Out of bound!");
        return null;
    }
    E element;
    if(index==0) // remove from front
    {
        element=head.getElement();
        head=head.getNext();
        if(head==null)
            tail=null;
    }
    else
    {
        curr=head;
        for(int i=0;i<index-1;i++)
        {
            curr=curr.getNext();
        }
        element=curr.getNext().getElement();
        if(tail==curr.getNext())
        {
            tail=curr;
        }
        curr.setNext(curr.getNext().getNext());
    }

    size--;
    return element;
}
```

4- Empty list & 5- Size

Algorithm size():
return size

Algorithm isEmpty():
return head==null

Singly Linked List ADT

Node class

```
public class Node <E>{

    private E element;
    private Node<E> next;

    public Node(E element, Node<E> next) {
        this.element = element;
        this.next = next;
    }

    public void setElement(E element) {
        this.element = element;
    }

    public void setNext(Node<E> next) {
        this.next = next;
    }

    public E getElement() {
        return element;
    }

    public Node<E> getNext() {
        return next;
    }
}
```

Singly Linked List ADT

SLL class

```
// instance variables of the SinglyLinkedList
public class SinglyLinkedList<E> {

    private Node<E> head;
    private Node<E> tail;
    private int size;

    public SinglyLinkedList() {

        head = null;
        tail = null;
        size = 0;
    }
}
```



Singly Linked List ADT

SLL class

```
// access methods
public int size() {
    return size;
}

public boolean isEmpty() {
    return size == 0;
}

public E first() { // returns (but does not remove) the first element
    if (isEmpty()) {
        return null;
    }
    return head.getElement();
}

public E last() { // returns (but does not remove) the last element
    if (isEmpty()) {
        return null;
    }
    return tail.getElement();
}
```

Singly Linked List ADT

SLL class

```
// update methods

public void addFirst(E e) { // adds element e to the front of the list
    head = new Node<>(e, head); // create and link a new node
    if (size == 0) {
        tail = head; // special case: new node becomes tail also
    }
    size++;
}

public void addLast(E e) { // adds element e to the end of the list
    Node<E> newest = new Node<>(e, null); // node will eventually be the tail
    if (isEmpty()) {
        head = newest; // special case: previously empty list
    } else {
        tail.setNext(newest); // new node after existing tail
    }
    tail = newest; // new node becomes the tail
    size++;
}
```



Linked Lists: Performance Analysis

Method	Big-O
<u>size()</u>	$O(1)$
<u>isEmpty()</u>	$O(1)$
<u>first()</u>	$O(1)$
<u>last()</u>	$O(1)$
<u>addFirst(e)</u>	$O(1)$
<u>addLast(e)</u>	$O(1)$
<u>removeFirst()</u>	$O(1)$



Using SinglyLinkedList

```
public static void main(String[] args) {  
    // TODO code application logic here  
    SinglyLinkedList<String> MyFirstList=new SinglyLinkedList<String>();  
  
    System.out.println("List size="+MyFirstList.size());  
  
    MyFirstList.addLast("Fahad");  
    MyFirstList.addLast("Kholid");  
    MyFirstList.addLast("Norah");  
    MyFirstList.addLast("Sara");  
  
    System.out.println("List size="+MyFirstList.size());  
    System.out.println("First element="+MyFirstList.first());  
    System.out.println("Last element="+MyFirstList.last());  
  
    MyFirstList.removeFirst();  
    MyFirstList.removeFirst();  
  
    System.out.println("List size="+MyFirstList.size());  
    System.out.println("First element="+MyFirstList.first());  
    System.out.println("Last element="+MyFirstList.last());  
}
```

Example: Output

```
run:  
List size=0  
List size=4  
First element=Fahad  
Last element=Sara  
List size=2  
First element=Norah  
Last element=Sara  
BUILD SUCCESSFUL (total time: 0 seconds)
```

