#### 1

# 10.5.3.15

## EE23BTECH11062 - V MANAS

#### **Question:**

A contract on construction job specifies a penalty for delay of completion beyond a certain date as follows: ₹200 for the first day, ₹250 for the second day, ₹300 for the third day, etc., the penalty for each succeeding day being ₹50 more than for the preceding day. How much money the contractor has to pay as penalty, if he has delayed the work by 30 days?

### **Solution:**

Variable	Description	Value
x(0)	First term of AP	200
d	common difference in the AP	50
x(n)	General term	$(200 + n \times 50)\mathbf{u}(\mathbf{n})$

TABLE 1 Variables Used

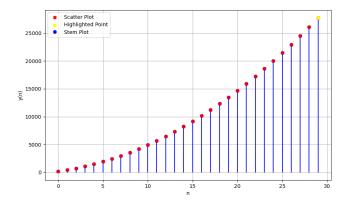


Fig. 1. Combination of scatter plot and stem plot

From equation(??)

$$\implies X(z) = \frac{200}{1 - z^{-1}} + \frac{200z^{-1}}{(1 - z^{-1})^2} \qquad |z| > |1| \quad (1)$$

$$y(n) = x(n) * u(n)$$
 (2)

$$Y(z) = X(z) U(z)$$
(3)

$$\implies Y(z) = \left(\frac{200}{1 - z^{-1}} + \frac{50z^{-1}}{(1 - z^{-1})^2}\right) \left(\frac{1}{1 - z^{-1}}\right) \tag{4}$$

$$= \frac{200}{\left(1 - z^{-1}\right)^2} + \frac{50z^{-1}}{\left(1 - z^{-1}\right)^3} \tag{5}$$

Contour integration to find z transform

$$y(29) = \frac{1}{2\pi j} \oint_c Y(Z) z^{28} dz$$
 (6)

$$= \frac{1}{2\pi j} \oint_{c} \frac{(200 - 150z^{-1})z^{28}}{(1 - z^{-1})^{3}}$$
 (7)

pole at 1 repeated 3 times

$$\therefore m = 3 \tag{8}$$

$$R = \frac{1}{(m-1)!} \lim_{z \to a} \frac{d^{m-1}}{dz^{m-1}} ((za)^m f(z))$$
(9)  
= 
$$\frac{1}{(2!)} \lim_{z \to 1} \frac{d^2}{dz^2} \left( (z-1)^3 \frac{(200-150z^{-1})z^{28}}{(1-z^{-1})^3} \right)$$

$$= \lim_{z \to 1} \frac{d^2}{dz^2} \left( 100 - 75z^{-1} \right) z^{31} \tag{11}$$

$$\implies y(n) = 27750 \tag{12}$$

(10)