

# MEEN-673 Nonlinear Finite Element Analysis

## Assignment-5

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*Please follow the order and format used here. Just fill out the values of in the corresponding tables for each problem. If you have any plots that you want to include, include them at the end of each problem and name them appropriately.*

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### Problem 1 :Simply Supported plate (SS-3)

Input files for Problem 1 goes here. Example:

Problem 1a: Simply supported(SS3) plate 8X8 L4

```
1                                MODEL (Not used)
4 2 1 1 NA NA NA 1 2          NPE,NGPF,NGPR,NGPS,NSTR,MESH,NPRNT,IGRAD,NONLIN
3                                SS

8 8                                NX,NY
0 0.625 0.625 0.625 0.625 0.625 0.625 0.625 0.625 0.625  XO,DX(I)
0 0.625 0.625 0.625 0.625 0.625 0.625 0.625 0.625 0.625  YO,DY(I)

84                                NSPV
zeros(NSPV,1)                    VSPV
Table                            ISPV
```

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Problem 1b: Simply supported(SS3) plate 4X4 Q9

```
2                                MODEL (Not Used)

9 3 2 2 NA NA NA 1 2          NPE,NGPF,NGPR,NGPS,NSTR,MESH,NPRNT,IGRAD,NONLIN
                                3      SS

4 4                                NX,NY
0 1.25  1.25 1.25  1.25      XO,DX(I)
0 1.25  1.25 1.25  1.25      YO,DY(I)

84                                NSPV
zeros(NSPV,1)                    VSPV
Table                            ISPV
```

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## Problem 2 : Clamped square plate

Input files for problem 2 goes here. Example

Problem 2a: Clamped plate 8X8 L4

```
1                                MODEL (Not Used)
4 2 1 1 NA NA NA 0 1 2        NPE,NGPF,NGPR,NGPS,NSTR,MESH,NPRNT,IGRAD,NONLIN
4                                SS
117                             NX,NY
0 0.625 0.625 0.625 0.625 0.625 0.625 0.625 0.625 0.625 XO,DX(I)
0 0.625 0.625 0.625 0.625 0.625 0.625 0.625 0.625 YO,DY(I)

117                             NSPV
zeros(NSPV,1)                  VSPV
Table                          ISPV
```

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Problem 2b: Clamped plate 4X4 Q9

```
2                                MODEL
9 3 2 2 NA NA 0 1 2          NPE,NGPF,NGPR,NGPS,NSTR,MESH,NPRNT,IGRAD,NONLIN
4                                SS
4 4                             NX,NY
0 1.25 1.25 1.25 1.25 XO,DX(I)
0 1.25 1.25 1.25 1.25 YO,DY(I)

117                             NSPV
zeros(NSPV,1)                  VSPV
Table                          ISPV
```

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| Load<br>Parameter (P) | SS - 3<br>8*8 L4<br>(w/h) | SS - 3<br>4*4 Q9<br>(w/h) | Clamped<br>8*8 L4<br>(w/h) | Clamped<br>4*4 Q9<br>(w/h) |
|-----------------------|---------------------------|---------------------------|----------------------------|----------------------------|
| 0.15625               | 0.172027                  | 0.16667                   | 0.051358                   | 0.051456                   |
| 0.3125                | 0.308954                  | 0.30017                   | 0.102226                   | 0.102401                   |
| 0.46875               | 0.413766                  | 0.40286                   | 0.152155                   | 0.152371                   |
| 0.625                 | 0.497089                  | 0.4847                    | 0.200778                   | 0.200986                   |
| 0.78125               | 0.566082                  | 0.55258                   | 0.247819                   | 0.247969                   |
| 0.9375                | 0.625051                  | 0.61066                   | 0.293101                   | 0.293141                   |
| 1.09375               | 0.676668                  | 0.66154                   | 0.336531                   | 0.336417                   |
| 1.25                  | 0.722678                  | 0.70692                   | 0.378086                   | 0.377777                   |
| 1.40625               | 0.764272                  | 0.74797                   | 0.41779                    | 0.417257                   |
| 1.5625                | 0.802297                  | 0.78552                   | 0.455705                   | 0.454923                   |
| 1.71875               | 0.837379                  | 0.82017                   | 0.491915                   | 0.490866                   |
| 1.875                 | 0.869988                  | 0.8524                    | 0.526512                   | 0.525185                   |
| 2.03125               | 0.90049                   | 0.88255                   | 0.559595                   | 0.557983                   |
| 2.1875                | 0.929175                  | 0.91092                   | 0.591264                   | 0.589363                   |
| 2.34375               | 0.956274                  | 0.93772                   | 0.621614                   | 0.619422                   |
| 2.5                   | 0.981977                  | 0.96315                   | 0.650735                   | 0.648255                   |
| 2.65625               | 1.00644                   | 0.98737                   | 0.678714                   | 0.675947                   |
| 2.8125                | 1.029797                  | 1.01049                   | 0.70563                    | 0.702581                   |
| 2.96875               | 1.052156                  | 1.03263                   | 0.731556                   | 0.728229                   |
| 3.125                 | 1.073614                  | 1.05388                   | 0.75656                    | 0.752961                   |
| 3.28125               | 1.094251                  | 1.07433                   | 0.780703                   | 0.776838                   |
| 3.4375                | 1.114139                  | 1.09403                   | 0.804043                   | 0.799917                   |
| 3.59375               | 1.133338                  | 1.11306                   | 0.82663                    | 0.822251                   |
| 3.75                  | 1.151903                  | 1.13146                   | 0.848514                   | 0.843887                   |
| 3.90625               | 1.169881                  | 1.14928                   | 0.869736                   | 0.864869                   |
| 4.0625                | 1.187316                  | 1.16657                   | 0.890339                   | 0.885237                   |
| 4.21875               | 1.204244                  | 1.18336                   | 0.910357                   | 0.905026                   |
| 4.375                 | 1.220701                  | 1.19968                   | 0.929825                   | 0.924272                   |
| 4.53125               | 1.236715                  | 1.21557                   | 0.948774                   | 0.943004                   |
| 4.6875                | 1.252316                  | 1.23104                   | 0.967233                   | 0.961252                   |
| 4.84375               | 1.267527                  | 1.24614                   | 0.985228                   | 0.979041                   |
| 5                     | 1.282371                  | 1.26087                   | 1.002783                   | 0.996397                   |

Table 1: Load parameter versus  $\frac{w}{h}$  for both SS-3 and clamped plates (Deflection at centre, ie  $x=0$  ,  $y=0$ )

| Load Parameter<br>(P) | SS-3 8*8 L4   |               |               |               |               |
|-----------------------|---------------|---------------|---------------|---------------|---------------|
|                       | $\sigma_{xx}$ | $\sigma_{yy}$ | $\sigma_{xy}$ | $\sigma_{yz}$ | $\sigma_{xz}$ |
| 0.15625               | 73118.11231   | 25839.48      | 4.614969      | -2476.99      | -1800.75      |
| 0.3125                | 138055.2533   | 48907.21      | 61.36717      | -4262.78      | -3137.71      |
| 0.46875               | 191616.6951   | 67889.95      | 140.0896      | -5439.38      | -4061.35      |
| 0.625                 | 236552.2295   | 83753.64      | 222.76        | -6230.4       | -4718.86      |
| 0.78125               | 275346.4956   | 97399.86      | 302.6116      | -6780.42      | -5206.52      |
| 0.9375                | 309658.9068   | 109434.7      | 377.4598      | -7173.16      | -5580.74      |
| 1.09375               | 340581.3114   | 120257.2      | 446.8365      | -7458.56      | -5875.58      |
| 1.25                  | 368854.6433   | 130137.9      | 510.9118      | -7667.89      | -6112.62      |
| 1.40625               | 395000.4386   | 139266.7      | 570.0783      | -7821.62      | -6306.22      |
| 1.5625                | 419398.3798   | 147781.3      | 624.7853      | -7933.68      | -6466.3       |
| 1.71875               | 442333.0889   | 155784.4      | 675.4729      | -8013.89      | -6599.95      |
| 1.875                 | 464023.3422   | 163355        | 722.5466      | -8069.32      | -6712.38      |
| 2.03125               | 484640.9519   | 170554.4      | 766.3703      | -8105.23      | -6807.51      |
| 2.1875                | 504323.7283   | 177431.9      | 807.2702      | -8125.56      | -6888.35      |
| 2.34375               | 523182.5762   | 184026.9      | 845.5221      | -8133.36      | -6957.27      |
| 2.5                   | 541310.0716   | 190372        | 881.3811      | -8130.98      | -7016.12      |
| 2.65625               | 558783.0597   | 196494.5      | 915.0672      | -8120.28      | -7066.41      |
| 2.8125                | 575666.3691   | 202416.9      | 946.7746      | -8102.76      | -7109.37      |
| 2.96875               | 592015.2226   | 208158.6      | 976.6747      | -8079.6       | -7145.99      |
| 3.125                 | 607877.0696   | 213736.1      | 1004.92       | -8051.78      | -7177.11      |
| 3.28125               | 623292.9994   | 219163.7      | 1031.645      | -8020.09      | -7203.44      |
| 3.4375                | 638298.8462   | 224453.7      | 1056.97       | -7985.19      | -7225.55      |
| 3.59375               | 652926.0618   | 229616.9      | 1081.004      | -7947.62      | -7243.96      |
| 3.75                  | 667202.4143   | 234662.9      | 1103.843      | -7907.84      | -7259.09      |
| 3.90625               | 681152.5512   | 239600.2      | 1125.573      | -7866.22      | -7271.3       |
| 4.0625                | 694798.4586   | 244436.1      | 1146.274      | -7823.08      | -7280.92      |
| 4.21875               | 708159.8376   | 249177.4      | 1166.016      | -7778.7       | -7288.22      |
| 4.375                 | 721254.4169   | 253830.1      | 1184.863      | -7733.3       | -7293.45      |
| 4.53125               | 734098.2123   | 258399.6      | 1202.874      | -7687.08      | -7296.81      |
| 4.6875                | 746705.7454   | 262890.9      | 1220.101      | -7640.21      | -7298.49      |
| 4.84375               | 759090.2271   | 267308.3      | 1236.595      | -7592.83      | -7298.66      |
| 5                     | 771263.7149   | 271655.9      | 1252.397      | -7545.06      | -7297.45      |

Table 2: Load parameter versus stresses for SS-3 8X8 L4  
(at center)

| Load     | SS-3 4*4 Q9   |               |               |               |               |
|----------|---------------|---------------|---------------|---------------|---------------|
| Paramete | $\sigma_{xx}$ | $\sigma_{yy}$ | $\sigma_{xy}$ | $\sigma_{yz}$ | $\sigma_{xz}$ |
| 0.15625  | 31831.94      | 17826.34      | -4964.8       | -1976.2       | -393.791      |
| 0.3125   | 60237.77      | 35967.39      | -9004.54      | -3539.5       | -672.704      |
| 0.46875  | 84195.96      | 52814.36      | -12167        | -4717.02      | -845.02       |
| 0.625    | 104783.1      | 68288.35      | -14735.8      | -5632.1       | -945.729      |
| 0.78125  | 122946.9      | 82605.26      | -16907.5      | -6370.26      | -999.05       |
| 0.9375   | 139319.3      | 95973.58      | -18801.1      | -6983.82      | -1019.79      |
| 1.09375  | 154317.5      | 108556.6      | -20490.6      | -7505.66      | -1017.22      |
| 1.25     | 168226.5      | 120478.5      | -22024.3      | -7957.4       | -997.454      |
| 1.40625  | 181248.1      | 131834.8      | -23435.3      | -8353.96      | -964.662      |
| 1.5625   | 193530.5      | 142700.3      | -24746.8      | -8706.02      | -921.823      |
| 1.71875  | 205186        | 153134.5      | -25976.2      | -9021.46      | -871.117      |
| 1.875    | 216301.4      | 163185.7      | -27136.4      | -9306.29      | -814.188      |
| 2.03125  | 226945.7      | 172893.8      | -28237.5      | -9565.17      | -752.297      |
| 2.1875   | 237174.8      | 182292.3      | -29287.4      | -9801.78      | -686.433      |
| 2.34375  | 247033.8      | 191408.8      | -30292.4      | -10019.1      | -617.371      |
| 2.5      | 256561.1      | 200267.9      | -31257.9      | -10219.6      | -545.744      |
| 2.65625  | 265788.5      | 208890.2      | -32188.1      | -10405.2      | -472.062      |
| 2.8125   | 274743.4      | 217294        | -33086.6      | -10577.7      | -396.745      |
| 2.96875  | 283449.1      | 225495        | -33956.4      | -10738.4      | -320.137      |
| 3.125    | 291925.9      | 233507.5      | -34800.2      | -10888.6      | -242.526      |
| 3.28125  | 300191.4      | 241343.8      | -35620.2      | -11029.3      | -164.153      |
| 3.4375   | 308261.3      | 249015.1      | -36418.4      | -11161.5      | -85.2194      |
| 3.59375  | 316149.3      | 256531.5      | -37196.4      | -11285.8      | -5.89618      |
| 3.75     | 323867.6      | 263902        | -37955.8      | -11403        | 73.67192      |
| 3.90625  | 331427.1      | 271134.7      | -38697.8      | -11513.7      | 153.362       |
| 4.0625   | 338837.7      | 278237.3      | -39423.6      | -11618.5      | 233.0692      |
| 4.21875  | 346108.2      | 285216.3      | -40134.4      | -11717.7      | 312.7041      |
| 4.375    | 353246.7      | 292078.2      | -40830.9      | -11811.9      | 392.1903      |
| 4.53125  | 360260.5      | 298828.7      | -41514.2      | -11901.4      | 471.4622      |
| 4.6875   | 367156.1      | 305472.9      | -42184.9      | -11986.5      | 550.464       |
| 4.84375  | 373939.8      | 312015.9      | -42843.7      | -12067.6      | 629.1477      |
| 5        | 380617        | 318462        | -43491.3      | -12144.9      | 707.4725      |

Table 3: Load parameter versus stresses for SS-3 4X4 Q9  
(at center)

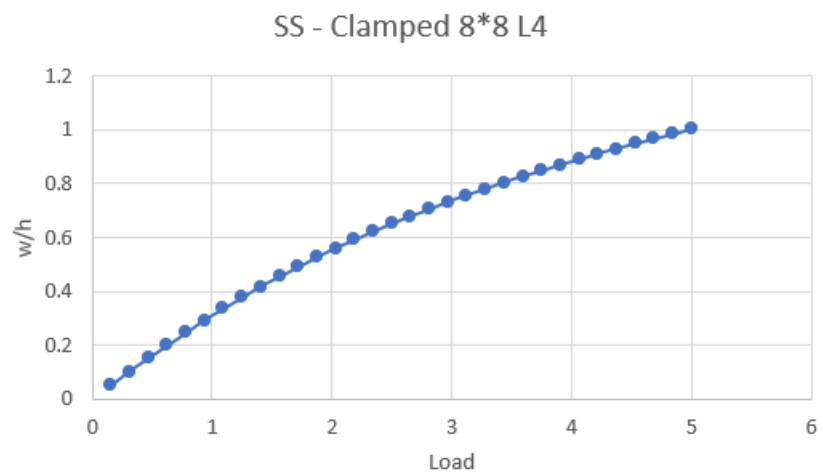
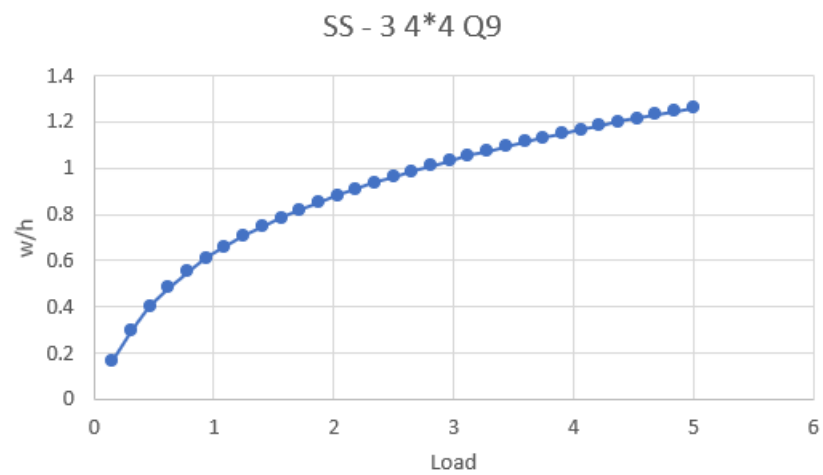
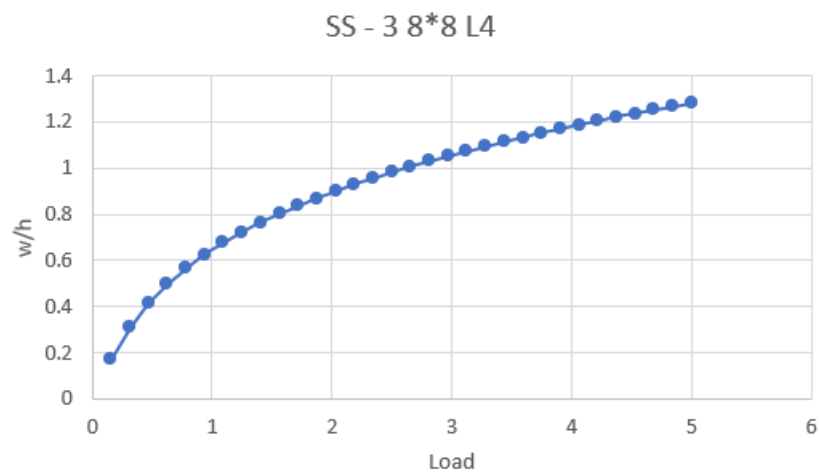
| Load     | Clamped 8*8 L4 |               |               |               |               |
|----------|----------------|---------------|---------------|---------------|---------------|
| Paramete | $\sigma_{xx}$  | $\sigma_{yy}$ | $\sigma_{xy}$ | $\sigma_{yz}$ | $\sigma_{xz}$ |
| 0.15625  | 24107.77       | 9392.815      | -289.808      | -349.206      | -355.108      |
| 0.3125   | 48871.92       | 19068.33      | -570.635      | -687.846      | -704.139      |
| 0.46875  | 74001.61       | 28904.4       | -839.082      | -1006.48      | -1041.62      |
| 0.625    | 99223.71       | 38785.78      | -1092.74      | -1297.62      | -1363.15      |
| 0.78125  | 124302.1       | 48612.41      | -1330.22      | -1556.18      | -1665.6       |
| 0.9375   | 149047.3       | 58303.76      | -1551.09      | -1779.36      | -1947.12      |
| 1.09375  | 173318.7       | 67799.75      | -1755.6       | -1966.41      | -2207         |
| 1.25     | 197019.3       | 77058.98      | -1944.55      | -2118.08      | -2445.37      |
| 1.40625  | 220089.6       | 86055.78      | -2119.01      | -2236.21      | -2662.98      |
| 1.5625   | 242498.7       | 94776.87      | -2280.23      | -2323.25      | -2860.99      |
| 1.71875  | 264237.3       | 103218.1      | -2429.49      | -2381.98      | -3040.75      |
| 1.875    | 285311.5       | 111382.1      | -2568.03      | -2415.27      | -3203.73      |
| 2.03125  | 305737.5       | 119275.7      | -2697         | -2425.91      | -3351.37      |
| 2.1875   | 325538.3       | 126908.6      | -2817.48      | -2416.55      | -3485.08      |
| 2.34375  | 344740.8       | 134292.3      | -2930.43      | -2389.65      | -3606.18      |
| 2.5      | 363373.4       | 141439.2      | -3036.7       | -2347.41      | -3715.88      |
| 2.65625  | 381465.7       | 148361.6      | -3137.04      | -2291.84      | -3815.3       |
| 2.8125   | 399046.8       | 155072.3      | -3232.13      | -2224.71      | -3905.45      |
| 2.96875  | 416145         | 161583.2      | -3322.53      | -2147.6       | -3987.24      |
| 3.125    | 432787.5       | 167906        | -3408.76      | -2061.89      | -4061.47      |
| 3.28125  | 449000         | 174051.6      | -3491.27      | -1968.82      | -4128.89      |
| 3.4375   | 464806.7       | 180030.5      | -3570.44      | -1869.46      | -4190.15      |
| 3.59375  | 480230.3       | 185852.4      | -3646.62      | -1764.74      | -4245.83      |
| 3.75     | 495292.3       | 191526.3      | -3720.11      | -1655.5       | -4296.47      |
| 3.90625  | 510012.4       | 197060.7      | -3791.16      | -1542.47      | -4342.52      |
| 4.0625   | 524409.1       | 202463.4      | -3860.01      | -1426.27      | -4384.41      |
| 4.21875  | 538499.7       | 207741.9      | -3926.87      | -1307.47      | -4422.52      |
| 4.375    | 552300.2       | 212903        | -3991.9       | -1186.56      | -4457.18      |
| 4.53125  | 565825.5       | 217952.8      | -4055.28      | -1063.95      | -4488.71      |
| 4.6875   | 579089.6       | 222897.4      | -4117.14      | -940.035      | -4517.36      |
| 4.84375  | 592105.4       | 227742.3      | -4177.61      | -815.134      | -4543.4       |
| 5        | 604884.9       | 232492.4      | -4236.8       | -689.538      | -4567.04      |

Table 4: Load parameter versus stresses for Clamped 8X8 L4  
(at center)

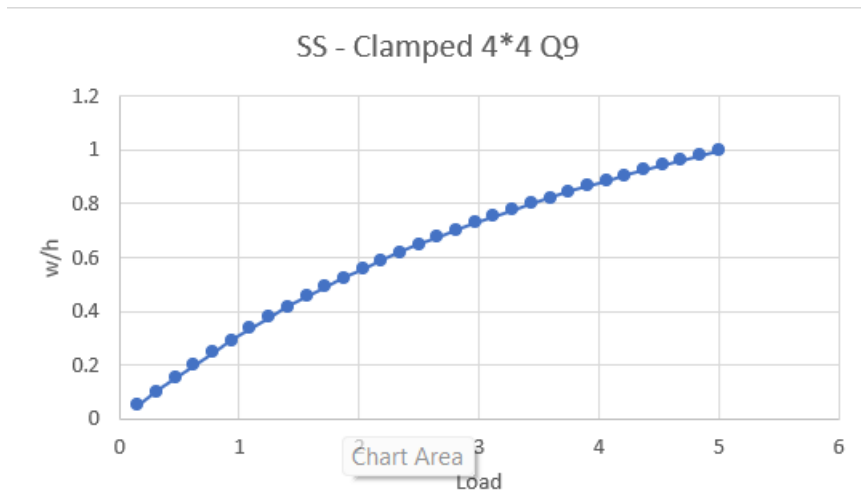
| Load      | Clamped 4*4 Q9 |               |               |               |               |
|-----------|----------------|---------------|---------------|---------------|---------------|
| Parameter | $\sigma_{xx}$  | $\sigma_{yy}$ | $\sigma_{xy}$ | $\sigma_{yz}$ | $\sigma_{xz}$ |
| 0.15625   | 7126.219       | -985.152      | -2133.09      | -2255.09      | -241.127      |
| 0.3125    | 14351.16       | -1614.95      | -4217.27      | -4492.75      | -478.984      |
| 0.46875   | 21622.82       | -1861.37      | -6233.45      | -6697.05      | -710.59       |
| 0.625     | 28894.52       | -1712.82      | -8167.31      | -8854.62      | -933.471      |
| 0.78125   | 36127.46       | -1172.86      | -10009.7      | -10955.3      | -1145.78      |
| 0.9375    | 43291.7        | -257.147      | -11756.2      | -12992.1      | -1346.28      |
| 1.09375   | 50365.73       | 1010.269      | -13406.3      | -14960.9      | -1534.32      |
| 1.25      | 57335.35       | 2600.519      | -14962.4      | -16860.1      | -1709.69      |
| 1.40625   | 64192.2        | 4482.759      | -16428.7      | -18689.7      | -1872.5       |
| 1.5625    | 70932.29       | 6626.225      | -17810.6      | -20451        | -2023.12      |
| 1.71875   | 77554.84       | 9001.549      | -19114.1      | -22146.2      | -2162.06      |
| 1.875     | 84061.23       | 11581.5       | -20345.1      | -23777.8      | -2289.91      |
| 2.03125   | 90454.26       | 14341.3       | -21509.6      | -25348.9      | -2407.31      |
| 2.1875    | 96737.61       | 17258.74      | -22613.1      | -26862.4      | -2514.92      |
| 2.34375   | 102915.5       | 20314.06      | -23660.8      | -28321.3      | -2613.36      |
| 2.5       | 108992.3       | 23489.76      | -24657.4      | -29728.7      | -2703.25      |
| 2.65625   | 114972.4       | 26770.43      | -25607.4      | -31087.2      | -2785.17      |
| 2.8125    | 120860.4       | 30142.52      | -26514.7      | -32399.5      | -2859.67      |
| 2.96875   | 126660.3       | 33594.12      | -27382.8      | -33668.3      | -2927.26      |
| 3.125     | 132376.3       | 37114.75      | -28215        | -34895.8      | -2988.42      |
| 3.28125   | 138012.3       | 40695.2       | -29014.1      | -36084.3      | -3043.59      |
| 3.4375    | 143571.8       | 44327.37      | -29782.9      | -37235.8      | -3093.17      |
| 3.59375   | 149058.4       | 48004.1       | -30523.6      | -38352.2      | -3137.55      |
| 3.75      | 154475.3       | 51719.09      | -31238.4      | -39435.4      | -3177.07      |
| 3.90625   | 159825.4       | 55466.76      | -31929.3      | -40487        | -3212.06      |
| 4.0625    | 165111.7       | 59242.17      | -32597.9      | -41508.6      | -3242.82      |
| 4.21875   | 170336.7       | 63040.95      | -33245.9      | -42501.6      | -3269.62      |
| 4.375     | 175503         | 66859.2       | -33874.8      | -43467.4      | -3292.71      |
| 4.53125   | 180612.8       | 70693.48      | -34485.7      | -44407.2      | -3312.34      |
| 4.6875    | 185668.5       | 74540.7       | -35080        | -45322.3      | -3328.73      |
| 4.84375   | 190671.9       | 78398.12      | -35658.7      | -46213.7      | -3342.07      |
| 5         | 195625.1       | 82263.29      | -36222.8      | -47082.5      | -3352.56      |

Table 5: Load parameter versus stresses for Clamped 4X4 Q9  
(at center)

## Deflection Graphs







## Stress Graphs

