

```
%% This is a Pseudo Code on how the entire FEM 2D 1DOF code✓  
works !!!
```

```
%% Main Script - FEM2D.m
```

```
Define all inputs constants
```

```
Define all Essential and Natural Boundary Conditions
```

```
Define element length along x and y direction
```

```
Define Guess Vector and initialize previous iteration solution✓  
vector (GPU)
```

```
% Calculate NOD (connectivity Matrix) and GLXY (global coord of✓  
all nodes)
```

```
Call "MeshR" function to define NOD and GLXY
```

```
Initiate iteration
```

```
while (iter is less than ITMAX) && (convergence not achieved)
```

```
    Initialize Global stiffness and force matrix
```

```
    for (iterate for all elements)
```

```
        if (applying for Direct ,Newtons's iteration)
```

```
            Define ELU for particular element from last and✓  
last-to-last iteration
```

```
            Define ELXY (global coords of all element node)✓  
from GLXY
```

```
        end
```

```
    % Calculate Elemental Stiffness (ELK) and force matrix✓  
(ELF)
```

```
    Call "ELEMATRC2D" function to calculate ELK & ELF
```

```
    Assemble ELK and ELF into GLK and GLF using NOD matrix  
end
```

```
% Apply Essential and Natural Boundary Condition on GLK and✓
```

GLF

Call "BNDRYUNSYM" function to calculate updated GLK and GLF

if NONLIN == 1 % that is for Direct iteration

Update previous iteration solution (GPU)

Calculate current iteration solution (GCU)

elseif NONLIN == 2 % that is for Newton's iteration

Update previous iteration solution

Calculate current iteration solution by adding GLK\GLF
with previous solution
end

% Note for Newton's iteration,

% One should apply the essential BCs for the very first
iteration.

% Afterwards VSPV = 0

if iter == 1 % after applying EBCs for 1st iteration,
change value of VSPV.

if NONLIN > 1 % For Newton's Iteration only

all elements in VSPV = 0

end

end

Calculate Error using the formula for this iteration

if error < epsilon

that means it converged.

get out of while loop

end

end % end of while loop

if convergence ~= 1

that means, iter > ITMAX.

```
Hence print "Error: Did Not Converge".
end

if convergence == 1 % that is it converged
    print final solution
end

%%✓
-----✓
--%

%           MeshR
% Pseudo code for MeshR Function

Define important constants - NXX, NYY, NXX1, NYY1, NEM (total✓
number of elements), NNM (total number of nodes)

% Special Case
if NPE == 8 % Quadratic element with 8 nodes / element
    NNM = NNM - NEM;
end

% Special Case of 9 noded element
if NPE == 9
    K0 = 1;
else
    K0 = 0;
end

Defining 1st element node 1, 2 and 3. % NOD(1,1) ; NOD(1,2) &✓
NOD(1,3)

if NPE == 9 % Special case of 9 noded element
    Defining 3rd node of 9 noded element.
end
```

Define 4th node

```
if NPE > 4 % For 8 noded and 9 noded element
```

```
    Defining node 5,6,7,8
```

```
    if NPE == 9 % Special 9 noded element case
```

```
        Defining 9th node
```

```
    end
```

```
end
```

```
if NY > 1 % Case when we have multiple elements along y✓  
direction
```

```
    Defining NOD matrix for all elements above the 1st element✓  
    (in y direction) using the NOD defined matrix for 1st element✓  
end.
```

```
if NX > 1 % case when we have multiple elements along x✓  
direction
```

```
    for NI = 2:NX
```

```
        for I = 1:NPE
```

```
            Defining NOD matrix for all elements right to the✓  
first element (ie, in x direction) using the NOD defined matrix✓  
for 1st element end.
```

```
        end
```

```
    for NJ = 2:NY
```

```
        Defining NOD matrix for all elements using✓  
previously defined elements
```

```
    end
```

```
end
```

```
end
```

```
% Generating Global Coords for all the nodes
```

```
Increase size of DX and DY by 1 and add 0 as their last✓
```

element.

```

if NPE == 8 % Case of Quadratic 8 noded element case
    % Note - 1st element 1st node == Global Node 1
    for NI = 1:NEY1
        Defining coords of nodes of Nith element
        for NJ = 1:NX
            Defining coords all nodes to the right of 1st nodal✓
element on x axis (only the first row of nodes)
        end
        if NI<=NY
            Defining coords of all nodes above 1st node on y✓
axis (only the first column of the nodes)
            for II = 1:NX
                Defining coords of all nodes in horizontal✓
fashion
            end
        end
    end
else % Case of 9 noded or 4 noded element
    for NI = 1:NEY1
        for NJ = 1:NEX1
            Defining coord of nodes of Nith element
            if NJ<NEX1
                if IEL == 2 % Special case of 9 noded element
                    Changing XC to include the middle 9th node
                end
            end
        end
    end
end

%%✓
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--%
```

```

%                               ELEMATRC2D
% Pseudo code for ELEMATRC2D Function

Call "Gaus_int" function to get Gauss Points and Weights

Define Differential Equation Coefficients

Initialize ELK and ELF

if NONLIN > 1 % That is for Newton's Iteration
    Initialize Tangent Matrix
end

% Since 2D, there is 2 integral for the 2 perpendicular✓
directions
% Hence, we will implement Gaussian Quadrature twice

for NI = 1:NGPF % For 1st Gaussian Quadrature
    for NJ = 1:NGPF % For 2nd Gaussian Quadrature
        Call "INTERPLN2D" function to get interpolation✓
        functions (SFL), their global derivative (GDSFL) and✓
        determinant of Jacobian

        Define Gaussian Quadrature constant (CONST)

        Initialize X, Y, U, dU/dX, dU/dY

        for I = 1:NPE
            if NONLIN>0 % that is for Newton's and direct✓
iteration method
                Calculate U, dU/dX, dU/dY
                % U = sum(ELU*SFL) ; dU/dX = sum(ELU*d(SFL)✓
/dX) ; du/dY = sum(ELU,d(SFL)/dY)
            end
            Define local node coordinates.

```

```

end
Define A11, A22 and FXY

for I = 1:NPE
    Define ELF
        %ELF = sum(SFL*FXY). % Multiply with CONST to
eliminate the need to integrate
        for J = 1:NPE
            Define ELK
        end
    end
    if NONLIN > 1 %If using Newton's Iteration
        Define Tangent Matrix (TANG)
    end
end
end

% Compute Residual vector and finalize tangent matrix

if NONLIN > 1 % If using Newton's iteration
    for I = 1:NPE
        for J = 1:NPE
            Calculating Residual.
            Equating residual to ELF, since we will export ELF
from this function

            Adding calculated ELK with TANG to completely
calculate the tangent matrix
            Equating TANG to ELK since we will export ELK from
this function.
        end
    end
end

%%

```

```
-----✓  
--%  
%                INTERPLN2D  
  
Define local coordinates of master element  
  
if NPE == 4 % Considering the case of 4 noded element  
    for I = 1:NPE  
        Defining interpolation function  
        Defining d(SFL)/dx in local coordinate  
        Defining d(SFL)/dy in local coordinates  
    end  
elseif NPE == 8 % Case of 8 noded element  
    for I = 1:NPE  
        if I <= 4 % Subcase of the 4 nodes placed at the 4✓  
vertices of the master element  
            Defining SFL, DSFL wrt x and DSFL wrt y (local✓  
coord)  
        else  
            if I <= 6 % For nodes 5 and 6  
                Defining SFL, DSFL wrt x and DSFL wrt y (local✓  
coord)  
            else % For nodes 7 & 8  
                Defining SFL, DSFL wrt x and DSFL wrt y (local✓  
coord)  
            end  
        end  
    end  
elseif NPE == 9 % Case of 9 noded element  
    for I = 1:NPE  
        if I <= 4  
            Defining SFL, DSFL wrt x and DSFL wrt y (local✓  
coord)  
        else  
            if I <= 6 % For nodes 5 and 6
```



```

        Defining SFL, DSFL wrt x and DSFL wrt y (local✓
coord)
    else
        if I <= 8 % For nodes 7 & 8
            Defining SFL, DSFL wrt x and DSFL wrt y✓
(local coord)
        else % For node 9
            Defining SFL, DSFL wrt x and DSFL wrt y✓
(local coord)
        end
    end
end
end
end
end
end

```

% Compute Jacobian

Initializing Jacobian Matrix (GJ)

```

for I = 1:2
    for J = 1:2
        for K = 1:NPE
            Calculating Jacobian Matrix
        end
    end
end
end

```

Calculating GJ inverse

Calculating Determinant of Jacobian matrix

Initializing GDSFL Matrix

```

for I = 1:2
    for J = 1:NPE
        for K = 1:2
            Calculating GDSFL
        end
    end
end

```

```

    end
end

%%✓
-----✓
--%
%          BNDRYUNSYM

if NSPV ~= 0 % Check if there is any defined Essential BCs
    for NP = 1:NSPV % Looping for all the given EBCs
        Equating the row in GLK of the particular DOF = 0
        Equating the diagonal element of the row = 1
        Equating the element of GLF of corresponding DOF with✓
given EBC value

        % Note - This process is independent of the type of✓
solver used.
        % Newton' iteration will be satisfied in the main✓
script

    end
end

if NSSV ~= 0 % Check if there is any defined Natural BCs
    for NS = 1:NSSV
        Adding NBCs value to GLF
    end
end

%%✓
-----✓
--%
%          Gaus_int

```

Takes Number of Gaus Point as input

output is 1D array of all the Gauss Points and Gauss Weight for✓
the given number of gaus points