

1. A perceptron is linear, but XOR is not linearly separable.

MLPs add hidden layers and nonlinearity, enabling multiple decision boundaries.

2. Bcoz the composition of linear function is still linear.

Gradients shrink bcoz multiple repeated multiplication of derivatives  $< 1$  like sigmoid or tanh.

ReLU doesn't saturate for positive inputs & has derivative 1.

3. Necessary bcoz self attention likes sequence order. Sinusoidal PE is fixed & extrapolates to longer sequences.

Absolute PE is flexible but limited to trained sequence. ROPE encodes relative position in attention space.

4. Query - what a token is searching for  
Key - what token represents.  
Value - info returned after attention.

Scaling by  $\sqrt{d_k}$  prevents large dot products that cause softmax saturation.

- Bcoz tokens strongly attend to themselves.

5. Multiple heads allow the model to attend to different features & relationships simultaneously.

$d_{model}$  - total embedding dimension  
 $h$  - no. of attention heads



$$d\_head = d\_model / h$$

6- Greedy decoding selects highest probability token at each step  
Beam keeps multiple candidate sequences

Eg - Greedy  $\rightarrow$  I am fine  
Beam  $\rightarrow$  I am finally feeling much better

$$1. d\_head = \frac{d\_model}{h} = \frac{768}{12} = 64$$

Q, K, V has a weight matrix of size  $768 \times 768$   
parameters per matrix =  $768^2 = 589824$   
Total for Q, K, V =  $3 \times 589824 =$

$$2. \text{Softmax} = \frac{e^{x_i}}{\sum e^{x_i}}$$

$\rightarrow e^2 + e^1 + e^0 = 11.11$

$$\frac{e^2}{11.11} = 0.665 \quad \frac{e^1}{11.11} = 0.245 \quad \frac{e^0}{11.11} = 0.090$$

$$[0.665, 0.245, 0.090]$$

3. Numpy —

```
import numpy as np
def attention(Q, K, V):
```

```
    dk = Q.shape[-1]
```

```
    scores = Q @ K.T / np.sqrt(dk)
```

```
    weights = np.exp(scores) / np.sum(np.exp(scores), axis=-1, keepdims=True)
```

```
    output = weights @ V
```

```
    return output, weights
```



#### 4. Numpy Version - Masked Attention.

```

import numpy as np
def masked_attention(Q, K, V):
    dk = Q.shape[-1]
    scores = Q @ K.T / np.sqrt(dk)

    seq_len = scores.shape[0]
    mask = np.triu(np.ones((seq_len, seq_len)), k=1)

    scores = np.where(mask == 1, -np.inf, scores)

    weights = np.exp(scores) / np.sum(np.exp(scores), axis=1,
    and output = weights @ V
    keepdims = True)
    return output, weights
    
```