```
#include<stdio.h>
#include<math.h>

#define f(x) 1/(x)

int main(){
   float x0 ,xn, T[10][10],h,sm,sl,a;
   int i,k,c,r,m,p,q;

   printf("Enter Lower and Upper Limit\n");
   scanf("%f %f",&x0,&xn);
   printf("Enter p and q of required T(p,q) \n");
   scanf("%d %d",&p,&q);

   h = xn-x0;
   T[0][0] = h/2*((f(x0))+(f(xn)));

   for(i=1;i<=p;i++){
      sl = pow(2,i-1);
      sm = 0;
      for(k=1;k<=sl;k++){
         a = x0+(2*k-1)*h/pow(2,i);
         sm = sm+(f(a));
      }
      T[i][0] = T[i-1][0]/2+sm*h/pow(2,i);
   }
   for(c=1;c<=p;c++){
      for(k=1;k<=c&&k<=q;k++){
```

```
        m=c-k;
        T[m+k][k] = (pow(4,k)*T[m+k][k-1]-T[m+k-1][k-1])/(pow(4,k)-1);
      }
   }

   printf("\n Romberg Estimate of Integration = %f\n",T[p][q]);
   getchar();
  getchar();
   return 0;
}
```

Taylor series method

```
#include<stdio.h>

#include<math.h>

int fact(int n){
   if(n == 1)
      return 1;
   else
      return (n * fact(n - 1));
}

int main(){
   float x,x0,yx0,yx,fdy,sdy,tdy;

   printf("Enter initial values of x and y \n");
   scanf("%f %f",&x0,&yx0);
```

```
   printf("Enter x at which function to be evaluated\n");
   scanf("%f",&x);

   fdy = (x0)*(x0)+(yx0)*(yx0);
   sdy = 2*(x0) + 2*(yx0)*fdy;
   tdy = 2+2*yx0*sdy+2*fdy*fdy;

   yx = yx0+(x-x0)*fdy+(x-x0)*sdy/fact(2)+(x-x0)*(x-x0)*(x-x0)*tdy/fact(3);
   printf("Function Value at x = %f is %f\n",x,yx);
   getchar();
  getchar();
   return 0;
}
```

Picard method

```
#include<stdio.h>

#include<math.h>

#define y1(x) exp(x) + pow(x,2) - 3*x
#define y2(x) 1 + x + pow(x,2)/2 + pow(x,3)/6 + pow(x,2) - 3*x
#define y3(x) 1 + x + pow(x,2)/2 + pow(x,3)/6 + pow(x,4)/24 + pow(x,2) - 3*x

int main(){
   float x, x0, y0, y;

   printf("Enter initial values of x and y: \n");
```

```
   scanf("%f %f", &x0, &y0);

   printf("Enter x at which function is to be evaluated: \n");
   scanf("%f", &x);

   y = y0;
   y = y0 + y1(x);
   y = y0 + y2(x);
   y = y0 + y3(x);

   printf("Function Value at x = %f is %f\n", x, y);
   getchar();
  getchar();
   return 0;
}
```

Heun's method

```
#include<stdio.h>
#include<math.h>
#define f(x,y) 2*y/x
int main(){
   float x,xp,x0,y0,y,h,m1,m2;

   printf("Enter initial value of x and y:\n");
   scanf("%f %f",&x0,&y0);

   printf("Enter x at which function to be evaluated: \n");
   scanf("%f",&xp);
```

```
   printf("Enter the step size: \n");
   scanf("%f",&h);

   y=y0;
   x=x0;

   for(x=x0;x<xp;x=x+h){
      m1 = f(x,y);
      m2=f(x+h,y+h*m1);
      y=y+h/2*(m1+m2);
   }
   printf("Function Value at x = %f is %f \n",xp,y);
   return 0;
}
```

RK method

```
#include <stdio.h>
#include <math.h>

#define f(x, y) (2 * (x) + (y))

int main() {
   float x, xp, x0, y, y0, h, m1, m2, m3, m4;

   printf("Enter initial values (x0, y0): ");
   scanf("%f %f", &x0, &y0);
```

```
    printf("Enter x at which function is to be evaluated (xp): ");
    scanf("%f", &xp);

    printf("Enter step size (h): ");
    scanf("%f", &h);

    y = y0;
    x = x0;

    for (x=x0 ; x < xp; x = x+h) {
        m1 = f(x, y);
        m2 = f(x + h / 2, y + (h / 2) * m1);
        m3 = f(x + h / 2, y + (h / 2) * m2);
        m4 = f(x + h, y + h * m3);

        y = y + (h / 6) * (m1 + 2 * m2 + 2 * m3 + m4);
    }

    printf("Function value at x = %.2f is y = %.4f\n", xp, y);
    return 0;
}
```

Shooting method

```
#include <stdio.h>
#include <math.h>

// Define functions f1 and f2
```

```
#define f1(x, y, z) (z)
#define f2(x, y, z) (6 * (x))

int main() {
   float xa, xb, ya, yb, z0, x, h, xp, sol, error, E;
   float V[3], g[3], ny, nz;
   int i;

   // Input boundary conditions
   printf("Enter Boundary Conditions (xa, ya, xb, yb): ");
   scanf("%f %f %f %f", &xa, &ya, &xb, &yb);

   // Input the x value where function is required
   printf("Enter x at which value is required (xp): ");
   scanf("%f", &xp);

   // Input step size
   printf("Enter the step size (h): ");
   scanf("%f", &h);

   // Input accuracy limit
   printf("Enter accuracy limit (E): ");
   scanf("%f", &E);

   x = xa;
   V[1] = ya;
   g[1] = (yb - ya) / (xb - xa);  // Initial guess
```

```
printf("g1 = %f\n", g[1]);

while (x < xb) {
   ny = V[1] + (f1(x, V[1], g[1])) * h;
   nz = g[1] + (f2(x, V[1], g[1])) * h;
   x = x + h;
   V[1] = ny;
   g[1] = nz;

   if (x == xp)
      sol = V[1];
}

V[1] = V[1];

if (V[1] < yb)
   g[2] = g[1] = 2 * g[1];
else
   g[2] = g[1] = (1.0 / 2.0) * g[1];

// Iterative shooting method loop
while (1) {
   x = xa;
   V[2] = ya;
   g[2] = g[1] - ((V[2] - yb) / (V[2] - V[1])) * (g[2] - g[1]);

   while (x < xb) {
      ny = V[2] + (f1(x, V[2], g[2])) * h;
```

```
        nz = g[2] + (f2(x, V[2], g[2])) * h;
        x = x + h;
        V[2] = ny;
        g[2] = nz;

        if (x == xp)
           sol = V[2];
      }

      error = fabs(V[2] - yb) / yb;
      V[1] = V[2];
      g[1] = g[2];

      if (error < E) {
        printf("y(%.2f) = %.4f\n", xp, sol);
        break;
      }
   }
   return 0;
}
```

Laplace equation

```
#include <stdio.h>
#include <math.h>

int main() {
   int n,i, j, k;
   float sum, error, E[10], a[10][10], b[10], new_x[10], old_x[10];
```

```
printf("Enter the dimension of plate (n,n): ");
scanf("%d", &n);

printf("Enter temperatures at left, right, top, and bottom: ");
float tL, tR, tT, tB;
scanf("%f %f %f %f", &tL, &tR, &tT, &tB);

// Initialize matrix
for ( i = 0; i <= n; i++){
   a[i][i] = -4;
}
for(i = 0; i <= n ; i++){
   a[i][n-i] = 0;
}

for (i = 0; i < n; i++) {
   for(j=0;j<=n;j++){
      if(i != j && j != (n-i)){
         a[i][j] = 1;
      }

   }
}
for(i=0;i<=n;i++){
   b[i] = 0;
   k=0;
}
```

```
for(i = 1;i<n;i++){
   for(j=1;j<n;j++){
      if((i-1) == 0){
         b[k] = b[k] - tL;
      }
      if((i+1) == 0){
         b[k] = b[k] - tR;
      }
      if((j-1) == 0){
         b[k] = b[k] - tB;
      }
      if((j+1) == n){
         b[k] = b[k] - tT;
      }
      k++;
   }
}

// Accuracy limit
printf("Enter accuracy limit: ");
scanf("%f", &error);

// Iterative calculation
while (1) {
   for (i = 0; i < n; i++) {
      sum = b[i];
      for (j = 0; j < n; j++)
         sum -= a[i][j] * old_x[j];
```

```
            new_x[i] = sum / a[i][i];
            E[i] = fabs(new_x[i] - old_x[i]) / fabs(new_x[i]);
        }

        // Check if error is within the limit
        for (i = 0; i < n; i++) {
            if (E[i] > error)
                break;
        }

        if (i == n)
            break;

        for (i = 0; i < n; i++)
            old_x[i] = new_x[i];
    }

    // Output solution
    printf("Solution:\n");
    for (i = 0; i < n; i++)
        printf("x[%d] = %.6f\n", i, new_x[i]);

        return 0;
}
```

POission equation

```
#include <stdio.h>
#include <math.h>

#define MAX 10  // Maximum grid size

int main() {
   int n, i, j, k;
   float sum, error, E[MAX], a[MAX][MAX], b[MAX], new_x[MAX], old_x[MAX];

   printf("Enter the dimension of plate (n,n): ");
   scanf("%d", &n);

   printf("Enter temperatures at left, right, top, and bottom: ");
   float tL, tR, tT, tB;
   scanf("%f %f %f %f", &tL, &tR, &tT, &tB);

   // Initialize coefficient matrix
   for (i = 0; i < n; i++) {
      for (j = 0; j < n; j++) {
         a[i][j] = (i == j) ? -4 : 0;
         if (j == i - 1 || j == i + 1)
            a[i][j] = 1;
      }
   }

   // Initialize right-hand side vector
   for (i = 0; i < n; i++) {
      b[i] = 0;
```

```
}

// Apply boundary conditions
k = 0;
for (i = 1; i < n - 1; i++) {
   for (j = 1; j < n - 1; j++) {
      if (i - 1 == 0)
         b[k] -= tL;
      if (i + 1 == n - 1)
         b[k] -= tR;
      if (j - 1 == 0)
         b[k] -= tB;
      if (j + 1 == n - 1)
         b[k] -= tT;
      k++;
   }
}

// Accuracy limit
printf("Enter accuracy limit: ");
scanf("%f", &error);

// Initialize guess values
for (i = 0; i < n; i++) {
   old_x[i] = 0;
}

// Iterative calculation using Gauss-Seidel Method
```

```
while (1) {
   for (i = 0; i < n; i++) {
      sum = b[i];
      for (j = 0; j < n; j++) {
         if (i != j)
            sum -= a[i][j] * old_x[j];
      }
      new_x[i] = sum / a[i][i];
      E[i] = fabs(new_x[i] - old_x[i]) / fabs(new_x[i]);
   }

   // Check if error is within the limit
   int converged = 1;
   for (i = 0; i < n; i++) {
      if (E[i] > error) {
         converged = 0;
         break;
      }
   }

   if (converged)
      break;

   for (i = 0; i < n; i++)
      old_x[i] = new_x[i];
}

// Output solution
```

```
    printf("Solution:\n");
    for (i = 0; i < n; i++)
        printf("x[%d] = %.6f\n", i, new_x[i]);

    return 0;
}
```