CS 480 Syllabus and Portfolio Winter 2019

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Portfolio

Course Tracker

You are required to track your progress in the course using this table.

Note: Currently, you see full credit for week one's work. (\checkmark means yes. Blank means no.) Update the table for week 2 and all subsequent weeks each class day and week during the semester.

Week	CRU	PFP	CDL	SAQ	PAQ	CDL	PPL
1	✓	✓	✓	✓	✓	✓	100%
2	✓	√	✓	✓	✓	✓	100%
3	√	✓	✓	✓	✓	✓	85%
4	✓	✓	✓	✓	✓	✓	100%
5	✓	✓	✓	✓	✓	✓	100%
6	✓	✓	✓	✓	✓	✓	100%
7	✓	✓	✓	✓	✓	✓	100%
8	✓	✓	✓	✓	✓	✓	100%
9							
10							
11							
12							
13							

This is an honest and true record of my work for this course.

Signature:		
Signature:		

Grade Claims

On the week indicated, bring this updated document to my office and make your claim.

Claim Week	Grade Claim	Instructor Grade	Adjusted Grade
5	A-		
9	A		
13 - 14			

Evidences

Fill in your evidences here each week to build your portfolio. The number of pieces of evidence are determined by you. However, the more you have the better off you will be.

Week 5

Chapter 7 Exercises [100%]

DONE Exercise 7.5: NFA to DFA

• 1.

```
NFA
I : 0|1 -> I
I : 0|'' -> S0
S0 : 1 -> S01
S01 : 0 -> S010
S010 : 1 -> F
F : 0|1 -> F
```

```
strings = ["{0:b}".format(i).zfill(4) for i in range(0, 20)]
accepts = ["accepts" if accepts_nfa(nfa7_5, s) else "rejects" for s in strings]
list(zip(strings, accepts))
```

• 2. A. Define language described in 5.2.1 in formal terms: $L = \{w : \in \Sigma^* : \forall x \in \{p \in parts(w): len(p) = 3\} : count(x, 1) = 2\}$

Any word w in $\{0,1\}^*$ where for all partitions of w with length 3 have exactly two 1's.

```
Negated: L = {w: \in \Sigma^*: \exists x \in \{p \in parts(w): len(p) = 3\} : count(x, 1) != 2 }
```

Any word w wherin exists a partition x of length three which does not have exactly two 1's

So yes, this is a correct negation. B.

complement_of_blocks_of_3 = md2mc('''
NFA
I : 0 -> I
I : 1 -> I
I : 0 -> S0
I : 1 -> S1
S0 : 0 -> S00
S0 : 1 -> S01
S1 : 0 -> S10

```
S01 : 0 -> F
S10 : 0 -> F
S00 : 0 -> F
S00 : 1 -> F
F : 0 \rightarrow F
F : 1 -> F
,,,)
dotObj_nfa(complement_of_blocks_of_3)
dotObj_dfa(min_dfa(comp_dfa(min_dfa(nfa2dfa(complement_of_blocks_of_3)))))
C.
nums = []
it = 1
while len(nums) < 20:
  for i in itertools.product([0,1],repeat=it):
    nums.append(i)
  it += 1
values = []
for each in nums:
  word = ""
  for i in each:
    word += str(i)
  values.append(word)
for each in values:
    print("String: ", each, " Accepted NFA: ", accepts_nfa(complement_of_blocks_of
```

• 3

Worked on it with Daniel, Matt, Seth. Couldn't figure it out.

DONE Exercise 7.6.1: Brzozoski's DFA minimization

• 1. Beginning DFA

```
bloated_dfa = md2dc('''
DFA
IS1 : a -> FS2
IS1 : b -> FS3
```

```
FS2 : a -> S4
FS2 : b -> S5
FS3 : a -> S5
FS3 : b -> S4
S4 : a | b -> FS6
S5 : a | b -> FS6
FS6 : a | b -> FS6
'''')
```

Reverse turning it into an NFA

```
rev_bloated_nfa = md2mc('''
NFA
IS6 : a | b -> IS6
IS6 : a | b -> S4
IS6 : a | b -> S5
S4 : a -> IS2
S4 : b -> IS3
S5 : a -> IS2
IS2 : a -> FS1
IS3 : b -> FS1
'''')
```

Turn NFA into DFA

```
rev_bloated_dfa = md2mc('''
DFA
ISO : a | b -> FS1
FS1 : a | b -> S2
S2 : a | b -> FS3
FS3 : a | b -> FS3
'''')
```

Reverse reversed DFA

```
min_nfa = md2mc('''
NFA
IS1 : a | b -> IS1
```

```
IS1 : a | b -> S2
S2 : a | b -> IS3
IS3 : a | b -> FS4
```

Convert back to dfa

```
min_dfa = md2mc('''
DFA
IS0 : a | b -> FS1
FS1 : a | b -> S2
S2 : a | b -> FS3
FS3 : a | b -> FS3
''')
```

3.

```
blimp = md2mc(''')
DFA
I1 : a -> F2
I1 : b -> F3
F2 : a -> S8
F2 : b -> S5
F3 : a -> S7
F3 : b -> S4
S4 : a \mid b \rightarrow F6
S5 : a \mid b \rightarrow F6
F6 : a \mid b \rightarrow F6
S7 : a \mid b \rightarrow F6
S8 : a -> F6
S8 : b -> F9
F9 : a -> F9
F9 : b -> F6
,,,)
min1 = min_dfa(blimp)
min2 = min_dfa_brz(blimp)
iso_dfa(min1, min2)
```

True

Chapter 8 Exercises [100%]

DONE Exercise 8.2: NFA Operations

• 1. 001100100 001000101

re_8_5_nfa = md2mc('''

• 2.

NFA

```
I1 : '' -> St1
 I1 : '' -> St2
 St1 : '' -> I1
 St2 : a \rightarrow St3
 St3 : '' -> I1
 IF2 : '' -> St4
 IF2 : '' -> St5
 St4 : c \rightarrow St6
 St6 : ',' -> St7
 St7 : d -> St8
 St8 : '' -> IF2
 St5 : b -> St9
 St9 : '' -> IF2
 I1 : '' -> IF2
 ,,,)
 dotObj_nfa(re_8_5_nfa)
3.
 re_8_5_nfa = re2nfa("(','+a)*(b+cd)*")
 dotObj_nfa(re_8_5_nfa)
 re_8_5_nfa_hand = md2mc(''')
 NFA
 I1 : '' -> St1
 I1 : '' -> St2
 St1 : '' -> I1
 St2 : a -> St3
 St3 : '' -> I1
 IF2 : '' -> St4
 IF2 : '' -> St5
```

```
St4 : c -> St6
St6 : '' -> St7
St7 : d -> St8
St8 : '' -> IF2
St5 : b -> St9
St9 : '' -> IF2
I1 : '' -> IF2
''')
dotObj_nfa(re_8_5_nfa_hand)
iso_dfa(nfa2dfa(re_8_5_nfa_hand))
True!
```

DONE Exercise 8.8: Sylvester's Formula

• 1. No. Any linear combination of 3 and 6 will always have to be a multiple of three. This means there are infinitely many natural numbers which cannot be expressed by 3 and 6.

2.

The requirement that the greatest common divisor (GCD) equal 1 is necessary in order for the Frobenius number to exist. If the GCD were not 1, every integer that is not a multiple of the GCD would be inexpressible as a linear, let alone conical, combination of the set, and therefore there would not be a largest such number. For example, if you had two types of coins valued at 4 cents and 6 cents, the GCD would equal 2, and there would be no way to combine any number of such coins to produce a sum which was an odd number. On the other hand, whenever the GCD equals 1, the set of integers that cannot be expressed as a conical combination of $\{a1, a2, \ldots, an\}$ is bounded according to Schur's theorem, and therefore the Frobenius number exists.

Wiki

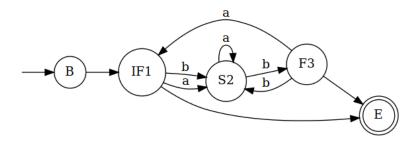
Exercise 8.8.5: Postage Stamp

- 1. a. p,q = 5, 11 F(p,q) = (5*11) 5 11 = 55 5 11 = 39 b. p,q = 5, 1 F(p,q) = 39 p,q,r = 5, 7,11 F(p,q,r) = 13
- 2.

Week 6

Monday, Feb 11

CDL



Chapter 9 [100%]

DONE Exercise 9.2: NFA to RE

- 1. Deleting the "X" state last produced the smaller regular expression. This is due to the nature of how states are removed from the NFA. If we remove the "busy" state last, then most of the states leading to it have already been collapsed, leading to less states needing to be collapsed in the final iteration.
 - a. Delete Order:

Produced Regex:

$$(((c + ((b + a) + a)) + ((b + a) + a)) (((p + q))* ((n + m) + m)))$$

Delete Order

- b Delete order:

Produced Regex:

- 2. Heuristically, it seems better to eliminate the busy state last. This is due to the reason I explained above. This could perhaps change based on the nfa and the number of "busy" states.
- 3. We could always convert them back to an nfa and check for language equivelance.

DONE Exercise 9.5: nfa2re: RE Size

• 1.

```
md2mc('''
NFA

I : '' -> A

I : '' -> C

A : '' -> B

B : 1 -> D

C : 0 -> E

D : '' -> G

E : '' -> G

G : 1 -> F

''')
```

Delete Order: I, A, B, C, D, E, G, F.

- Step 1. Add real I (S) and real F (Q)

```
md2mc('''

NFA

S: '' -> I

I: '' -> A

I: '' -> G

A: '' -> B

B: 1 -> D

C: 0 -> E

D: '' -> G

E: '' -> A

E: '' -> G

G: 1 -> F

F: '' -> Q

''')
```

```
IΑ
                                                 IG
                                                            =
                                                 AB
                                                            =
                                                                  \epsilon
                                                 AC
                                                            =
                                                                  \epsilon
                                                 BD
                                                           =
                                                                  1
                                                 CE
                                                           =
                                                                  0
                                                 DG
                                                           =
                                                 EA
                                                 EG
                                                           =
                                                 \operatorname{GF}
                                                 FQ
                                                           =
 – Remove I i = S, j = a R1a = \epsilon, R2a = , R3a = \epsilon, R4a = i = S, j
    = g R1<sub>g</sub> = \epsilon, R2<sub>g</sub> = , R3<sub>g</sub> = \epsilon, R4<sub>g</sub> =
                                                  \frac{(\epsilon)()^*(\epsilon) \cup ()}{(\epsilon)()^*(\epsilon) \cup ()} 
                                SA
                                SG
                                          =
                                AΒ
                                AC
                                BD
                                          =
                                                 1
                                                                                   1
                                CE
                                          =
                                                 0
                                \overline{DG}
                                          =
                                EA
                                          =
                                EG
                                          =
                                \operatorname{GF}
                                          =
                                FQ
                                          =
– Remove A i = S, j = b R1_B = \epsilon, R2_B = \epsilon, R3_B = \epsilon, R4_B = i = \epsilon
    S, j = c R1_C = \epsilon, R2_C = R3_C = \epsilon, R4_C = i = E, j = E R1_E = \epsilon
    \epsilon,\,\mathrm{R2_E}= , \mathrm{R3_E}= , \mathrm{R4_C}=
                                                 (\epsilon)()^*(\epsilon) \cup ()
                                                (\epsilon)()^*(\epsilon) \cup ()
(\epsilon)()^*(\epsilon) \cup ()
                                SG
                                BD
                                          =
                                                 1
                                CE
                                                 0
                                          =
                                \overline{\mathrm{DG}}
                                                 (\epsilon)()^*(\epsilon) \cup ()
                                ES
                                EG
                                          =
                                                 \epsilon
                                                                                 \epsilon
                                GF
                                          =
                                                 1
                                                                                 1
```

SI

 ϵ

FQ

```
- Remove B i = S, j = D R1 = \epsilon, R2 = , R3 = 1, R4 =
                                     (\epsilon)()^*(\epsilon) \cup ()
                        SC
                        SD
                                     (\epsilon)()^*(1) \cup ()
                                                              1
                        SG
                                     (\epsilon)()^*(\epsilon) \cup ()
                        CE
                                     0
                        DG
                               = (\epsilon)()^*(\epsilon) \cup ()
                        ES
                        EG
                        GF
                               =
                                     1
                                                              1
                        FQ
                               =
                                     \epsilon
 – Remove C i = S, j = E R1 = \epsilon, R2 = , R3 = 0, R4 =
                                     (\epsilon)()^*(1) \cup ()
                        SD
                                     (\epsilon)()^*(0) \cup ()
                        SE
                        SG
                                     (\epsilon)()^*(\epsilon) \cup ()
                        DG
                                     (\epsilon)()^*(\epsilon) \cup ()
                        ES
                        EG
                        GF
                               =
                                   1
                                                              1
                        FQ
                               =
                                     \epsilon
– Remove D i = S, j = G R1 = 1, R2 = , R3 = \epsilon, R4 = \epsilon
                       SE
                               = (\epsilon)()^*(0) \cup ()
                                   (1)()^*(\epsilon) \cup (\epsilon)
                       SG
                              = (\epsilon)()^*(\epsilon) \cup ()
                       ES
                       EG
                              = \epsilon
                       GF
                               =
                                    1
                                                         = 1
                       FQ
                               =
- Remove E i = S, j = S R1 = 0, R2 = , R3 = \epsilon, R4 = i = S, j =
   G R1 = 0, R2 = R3 = \epsilon, R4 = 1
                             = (0)()^*(\epsilon) \cup ()
                     SS
                                                                 0
                            = (0)()^*(\epsilon) \cup (1)
                     SG
                                                             0 + 1
                     \operatorname{GF}
                                                                 1
                     FQ = \epsilon
- Remove G i = S, j = F R1 = 0+1, R2 = , R3 = 1, R4 =
                         = (0)()^*(\epsilon) \cup ()
                  SS
                                                       = 0
                  SF
                         = (0+1)()^*(1) \cup ()
                                                       = (0+1)1
                  FQ =
```

$$\begin{array}{lll} - \ \text{Remove F i} = S, \ j = Q \ R1 = (0+1)1, \ R2 = , \ R3 = \epsilon, \ R4 = \\ & SS &= \ (0)()^*(\epsilon) \cup () &= \ 0 \\ & SQ &= \ (0+1)1()^*(\epsilon) \cup () &= \ (0+1)1 \\ \\ - \ \text{Final REGEX} \ ((((0\ ((0)^*\ ((1+\ ``) +\ ``))) + ((1+\ ``) +\ ``))) + ((1+\ ``) +\ ``)) \end{array}$$

((1 + "") + "")) 1)

SIIΑ IG ACABBDCE $\overline{\mathrm{DG}}$ EAEGGF= 1FQ = ϵ

Week 7

DONE Wednesday, FEB 20, 2019 [100%]

DONE Warmup CDL the boy sees a flower

Noun Phrase Verb Phrase Complex Noun Complex Verb

Arcticle Noun Verb Noun Phrase

the boy Article Noun sees the boy flower sees a

SENTANCE => NOUN-PHRASE VERB-PHRASE

- => COMPLEX-NOUN COMPLEX-VERB
- => ARTICLE NOUN VERB NOUN-PHRASE
- => the boy sees COMPLEX-NOUN
- => the boy sees ARTICLE NOUN
- => the boy sees a flower

DONE 2nd Warmup CDL a girl with a flower likes the boy SENTANCE

- => NP VP
 - => CN PP VP
 - => A N P CN CV
 - => a girl with A N V NP
 - => a girl with a flower likes CN
 - => a girl with a flower likes A N
 - => a girl with a flower likes the boy

DONE 3rd Warmpup CDL the girl touches the boy with the flower S

- => NP VP
 - => NP CV PP
 - => CN V NP P CN
 - => CN V CN P CN
 - => A N V A N P A N
 - => the girl touches the boy with the flower

DONE 4th Warmup CDL

 $S \rightarrow aB$

B -> "

bbB

B -> bb

bbB

DONE 5th Warmup CDL

S -> "

 $S \rightarrow aSbb$

DONE 6th Warmup CDL

S -> λ

S -> B

B -> bB

B -> λ

DONE REAL CDL $L = \{s : s \in \{a, b\}^* \text{ and } \#_b (s) = 2\#_a (s) \}$

 $S \mathrel{->} a \mathrel{S} b \mathrel{S} b$

 $S \rightarrow b S a S b$

 $S \rightarrow b S b S a$

S -> ϵ

REAL CDL pt 2 $L = \{s : s \in \{a, b\}^* \text{ and } \#_b (s) = 2\#_a (s) + 3\}$

 $S \rightarrow A$

S -> ϵ

A -> B b b b

 $B \rightarrow a B b B b$

B -> b B a B b

B -> b B b B a

 $B -> \epsilon$

DONE Friday, FEB 22, 2019 [100%]

DONE CDL Build two PDA

One to recognize the language of EvenPalindromes over $\Sigma=\{0,\ 1\}, \{ww^R: w\in\Sigma\ \}$ (4 states)

The other to recognize the language of MarkedPalindromes over $\Sigma = \{0, 1\}$ with # as the the **marked** character.

 $\{w\#w^R:w\in\Sigma\ \}$ (4 states)

I: 0, # : 0# -> A

I: 1, # : 1# -> A

A : O, O : OO -> A

 $A : 1, 0 : 01 \rightarrow A$

 $A : 0, 1 : 01 \rightarrow A$

 $A : 1, 1 : 11 \rightarrow A$

A : #, 0 : 0 -> B A : #, 1 : 1 -> B

B : 1, 1 : ', -> B

B : 0, 0 : ', -> B

B : '', #: # -> F

DONE Chapter 11 Exercises [100%]

DONE 11.5.1 [100%]

• **DONE** 11.5.1.1 Sentance 1 + 2 * 3

- CFG1

• DONE 11.5.1.2 Sentence: 1 + $^{\sim}$ 2 * 3

```
#+NAME CFG 1

E -> 1 | 2 | 3 | ~E | E+E | E*E | (E)

Parse Tree 1

E /|\
E + E | /|\
1 E * E | | |
~E 3 |
2

Parse Tree 2
```

• DONE 11.5.1.3 I would argue that they denote the same context free language because they contain the same set of terminals and transitions. While the transition functions are not the same, (CFG1 is ambigious), they can produce language equivalent parse trees, meaning any sentance that can be turned into a parse tree with CFG1 can also be turned into a parse tree with CFG2 (and vice versa)

DONE 11.10.1 [100%]

• **DONE** 11.10.1.5

– Case 1 (OP is AND)
$$L_{abcd}=\{a^ib^jc^kd^l:\,i,j,k,l\geq 0 \text{ and } ((i=j) \text{ AND } (k=l))\}$$

- - Case 1 OP=AND Assume $L_{acbd}=\{a^i\ c^k\ b^j\ d^l:\ i,j,k,l,\geq 0\ and\ ((i=j)\ AND\ (k=l))\ is\ context\ free.$

Pumping Lemma applies & garuntees an N>0

Pick N of the pumping lemma. Pick $z=a^n$ c^n b^n d^n . Break z into uvwxy, with $|vwx| \le n$ and $vx \ne \epsilon$. Then vwx contains one or two different symbols. In both cases, the string uwy connot be in L.

Context Free Languages cannot match two substrings of arbitrary length over an alphabet of at least two symbols.

- Case 2 OP=OR

$$L_{acbd} = \{a^i \ c^k \ b^j \ d^l: \ i,j,k,l, \geq 0 \ and \ ((i=j) \ OR \ (k=l))$$

This isn't complete, but I feel like it is close

Week 8

DONE Chapter 13 Exercises [100%]

DONE Exercise 13.8: DTM and NDTM Design [100%]

• **DONE** 1

Current	Symbol	Next	Symbol	Move
State	Read	State	Written	Direction
i0		fhalt	0	S
i0	0	fhalt	1	S
i0	1	q1	0	R
q1	0	fhalt	1	S
q1	1	q1	0	R
q1		fhalt	1	\mathbf{S}

• **DONE** 2 Assuming there is a '#' at the start of the string and a '\$' at the end. If they do not exist, I would just add the states to add them before starting the "count".

Basic idea, bounce back and forth "matching up" pairs of 1's and 0's until you run out. Depending on which number you've started on, you will need to accept or reject upon reaching a specific side of the tape. q2 handles switching between matching an initial 0 to a 1, or an initial 1 to a 0. Note, that a string such as 10011 would start with an initial 1, match it to the first zero, and then "restart" on the second zero. The q2 state handles that restart.

I am making no claim that this is the "best" program for this particular problem, but it has worked on every string I've thrown at it.

Current	Symbol	Symbol	Move	Next
State	Read	Written	Direction	State
i0	#	#	R	q2
q1	*	*	R	q1
q1	1	1	\mathbf{S}	q2
q1	\$	\$	\mathbf{S}	A
q1	0	0	\mathbf{S}	q2
q2	1	X	R	q3
q2	0	Y	R	q5
q2	*	#	R	q2
q2	#	#	\mathbf{S}	R
q3	0	*	${ m L}$	q4
q3	1	1	R	q3
q3	*	*	R	q3
q3	\$	\$	\mathbf{S}	A
q4	X	#	R	q1
q4	1	1	${f L}$	q4
q4	*	*	${ m L}$	q4
q5	0	0	R	q5
q5	1	*	${ m L}$	q6
q5	#	#	\mathbf{S}	R
q5	*	*	R	q5
q5	\$	\$	\mathbf{S}	R
q6	0	0	${ m L}$	q6
q6	1	1	L	q6
q6	Y	#	R	q2
q6	*	*	L	q6

```
(princ "TM\n")  
(loop for (cs sr sw md ns) in (cddr table)  
do (princ (format "%s : %s ; %s , %s -> %s\n" cs sr sw md ns)))
```

TM Graph

