

generic (or parametric) polymorphism

the ability for an entity to behave in the same way regardless of “input” or “contained” type

But what about (+)?

$(+) :: \text{Int} \rightarrow \text{Int} \rightarrow \text{Int}$

$(+) :: a \rightarrow a \rightarrow a$

ad hoc polymorphism


the ability for an entity to behave differently on different “input” or “contained” types

typeclass


a set of types^{*} defined by an interface (set of functions) that the type must implement

or type constructors

+ type var




```
class Eq a where  
  (==) :: a -> a -> Bool
```




```
class Show a where  
  show :: a -> String
```


+ typeclass
constraint



```
> :type (==)  
(==) :: Eq a => a -> a -> Bool
```



```
> :type show  
show :: Show a => a -> String
```



Polymorphic values revisited

`[] :: [a]`

`undefined :: a`

`1 :: Num a => a`

`[a]`



`[] a`

`Set a`

Higher-order typeclasses

But what about `map`?

`list-map ::` $[]\ a \rightarrow []\ b$
 $(a \rightarrow b) \rightarrow \underline{[a]} \rightarrow \underline{[b]}$

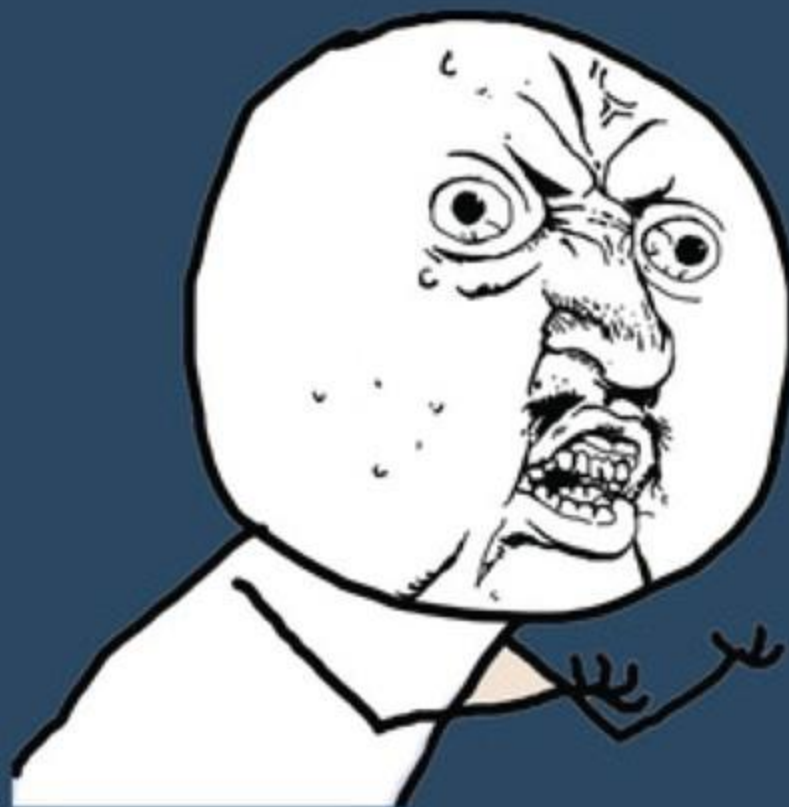
`stream-map ::`
 $(a \rightarrow b) \rightarrow \underline{\text{Stream}}\ a \rightarrow \underline{\text{Stream}}\ b$

`vector-map ::`
 $(a \rightarrow b) \rightarrow \underline{\text{Vector}}\ a \rightarrow \underline{\text{Vector}}\ b$


```
class Functor f where  
  fmap :: (a -> b) -> f a -> f b
```

Representing failing computations

C COMPILER



**Y U NO TELL ME WHERE THE
SEGMENTATION FAULT IS**

In Haskell, types are “non-null.”

If function `f` returns an `Int`, it can’t return “`null`” or “`None`”.

But sometimes we want to encode the possibility of failure.

```
data Maybe a = Nothing | Just a
```

Encoding failure: parsing integers

```
read :: Read a => String -> a
```

```
readMaybe :: Read a => String -> Maybe a
```

Chaining failing computations

```
s = null;
if (x != null) {
    y = x.f();
    if (y != null) {
        z = y.g();
        if (z != null) {
            for (a in z) {
                if (a != null) {
                    s = update(s, a);
                }
            }
        }
    }
}
```

```
if (s != null) {
    return s.h();
}
```



```
case x of
  Nothing -> Nothing
  Just x' ->
    case f x' of
      Nothing -> Nothing
      Just y ->
        case g y of
          Nothing -> Nothing
          Just z ->
            foldl _____ Nothing z
```

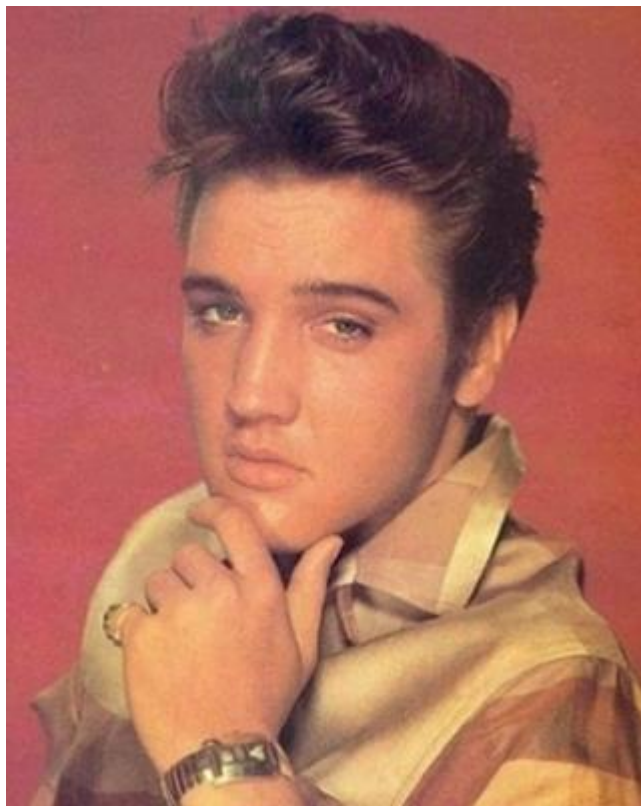
Some shortcuts from other languages

Elvis operator `?:`

`x?:y`

Safe navigation operator `?.`

`x?.y`



Back to Haskell

`couldFail :: _ -> Maybe _`

Given `x = couldFail y`, what now?

“If null then null, else do something”

```
add10Maybe :: Maybe Int -> Maybe Int  
add10Maybe Nothing = Nothing  
add10Maybe (Just x) = Just (add10 x)
```

```
lengthMaybe :: Maybe [a] -> Maybe Int  
lengthMaybe Nothing = Nothing  
lengthMaybe (Just xs) = Just (length xs)
```

“If null then null, else do something”

```
add10Maybe :: Maybe Int -> Maybe Int  
add10Maybe Nothing = Nothing  
add10Maybe (Just x) = Just (add10 x)
```

```
lengthMaybe :: Maybe [a] -> Maybe Int  
lengthMaybe Nothing = Nothing  
lengthMaybe (Just xs) = Just (length xs)
```

```
try :: (a -> b) -> Maybe a -> Maybe b
try _ Nothing = Nothing
try f (Just x) = Just (f x)
```

```
try :: (a -> b) -> Maybe a -> Maybe b
try _ Nothing = Nothing
try f (Just x) = Just (f x)
```


Maybe is a functor!

```
try :: (a -> b) -> Maybe a -> Maybe b
fmap :: (a -> b) ->          f a ->          f b
```

“If null then null, else do something **that might fail**”

```
recipMaybe :: Maybe Float -> Maybe Float
recipMaybe Nothing = Nothing
recipMaybe (Just x) = if x == 0
                        then Nothing
                        else Just (1 / x)
```

```
headMaybe :: Maybe [a] -> Maybe a
headMaybe Nothing = Nothing
headMaybe (Just xs) = if null xs
                        then Nothing
                        else Just (head xs)
```

“If null then null, else do something that might fail”

```
recipMaybe :: Maybe Float -> Maybe Float
recipMaybe Nothing = Nothing
recipMaybe (Just x) = if x == 0
                        then Nothing
                        else Just (1 / x)
```

```
headMaybe :: Maybe [a] -> Maybe a
headMaybe Nothing = Nothing
headMaybe (Just xs) = if null xs
                       then Nothing
                       else Just (head xs)
```

```
tryFail :: (a -> Maybe b) -> Maybe a -> Maybe b
tryFail _ Nothing = Nothing
tryFail f (Just x) = f x
```

```
andThen :: Maybe a -> (a -> Maybe b) -> Maybe b
Nothing `andThen` _ = Nothing
(Just x) `andThen` f = f x
```

(the backticks allow a binary function to be used infix)

x `andThen` f
`andThen` g
`andThen` h

Encoding error information with `Either`

```
data Either a b = Left a | Right b
```

We often use `Either String b` to represent a successful `(Right b)` value, or an error with message `(Left msg)`.