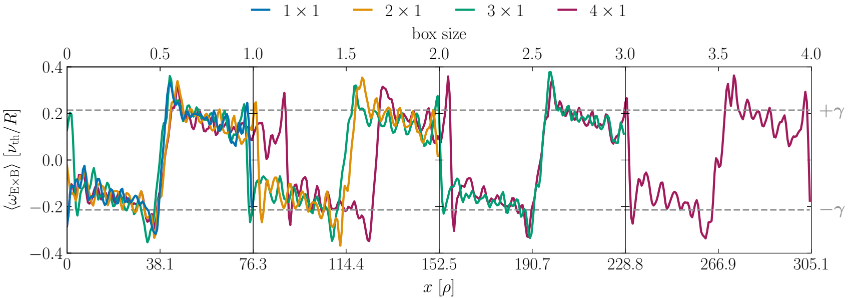
UNIVERSITÄT BAYREUTH

SIZE CONVERGENCE OF THE E×B STAIRCASE PATTERN IN FLUX TUBE SIMULATIONS OF ION TEMPERATURE GRADIENT-DRIVEN TURBULENCE

June 24, 2023



Manuel Lippert

Theoretical Physics V

MOTIVATION

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Does the basic pattern size always converges to the box size, or is there a typical mesoscale size inherent to staircase structures also in a local flux-tube description?

CHARGED PARTICLE MOTION

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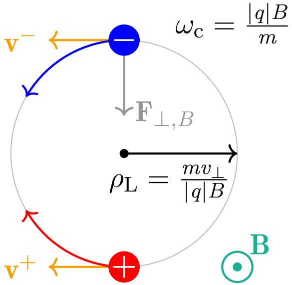
Lorentz force

$$F_{\perp,B} = |q|v_\perp B$$



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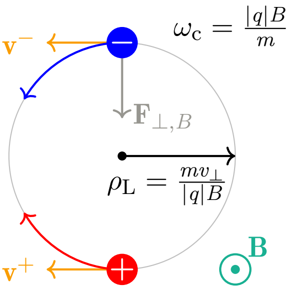

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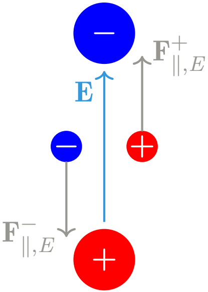

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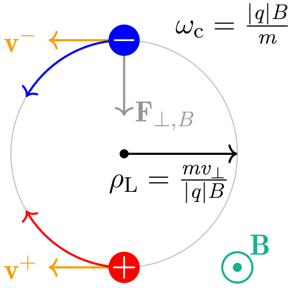

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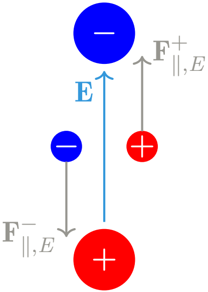
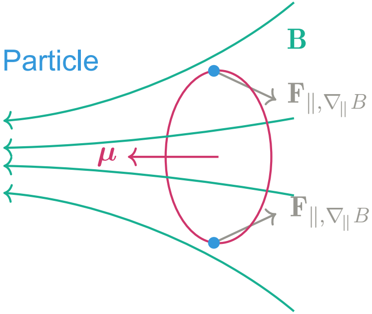


Inhomogeneous magnetic field

$$F_{\parallel,\nabla_\parallel B} = -\underbrace{\frac{mv_\perp^2}{2B}}_{\mu} \nabla_\parallel B$$



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$\mathbf{E} \times \mathbf{B}$ Drift

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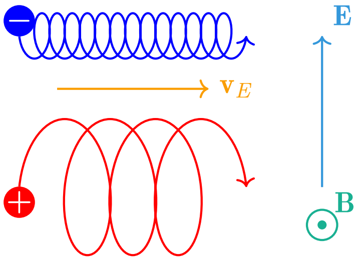

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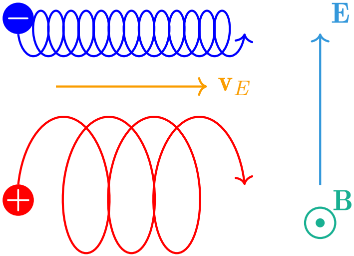
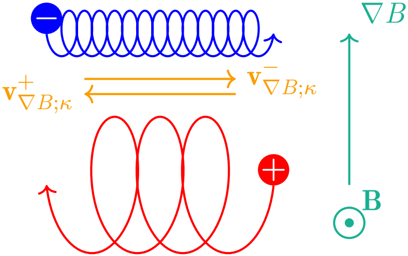
∇B Drift

$$\mathbf{v}_{\nabla B} = \frac{mv_\perp^2}{2q}\frac{\mathbf{B}\times\nabla B}{B^3}$$

Curvature Drift

$$\mathbf{v}_\kappa = \frac{mv_\parallel^2}{qB^2}\mathbf{B} \times \underbrace{\boldsymbol{\kappa}}_{\frac{\nabla B}{B}} = \frac{mv_\parallel^2}{q}\frac{\mathbf{B}\times\nabla B}{B^3}$$





MAGNETIC CONFINEMENT IN TOKAMAK

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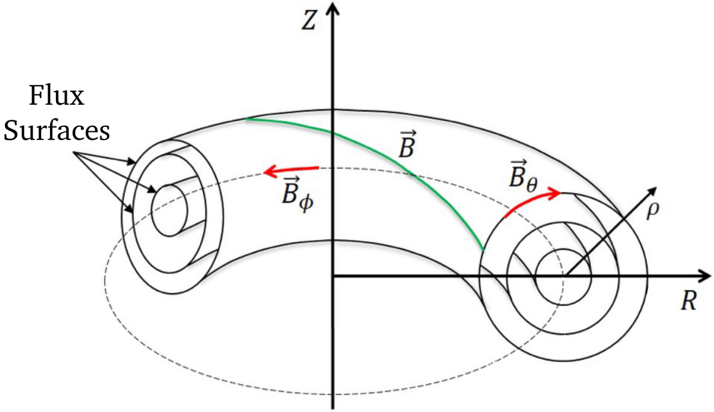

$$\beta = \frac{nT}{\mu_0 B^2/2}$$

ION TEMPERATURE GRADIENT (ITG)-DRIVEN INSTABILITY

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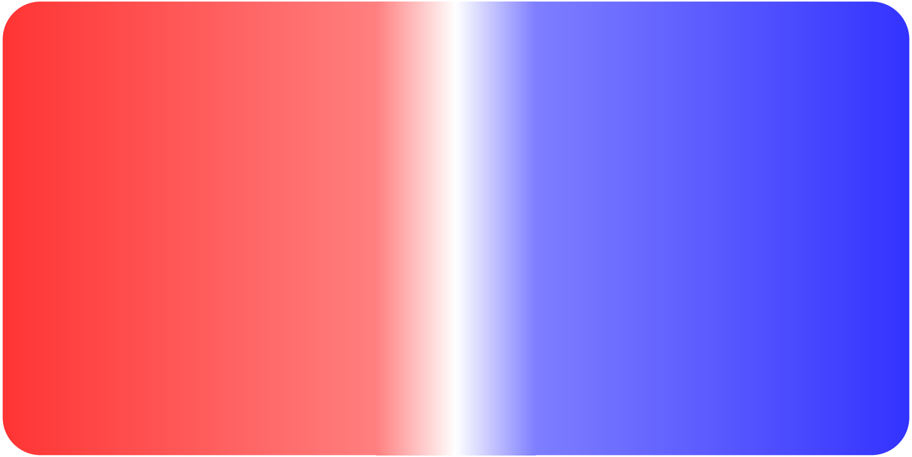

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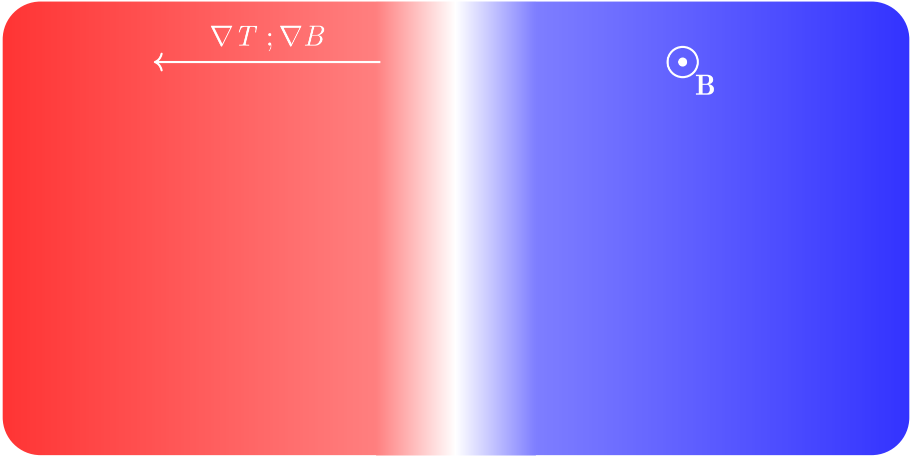

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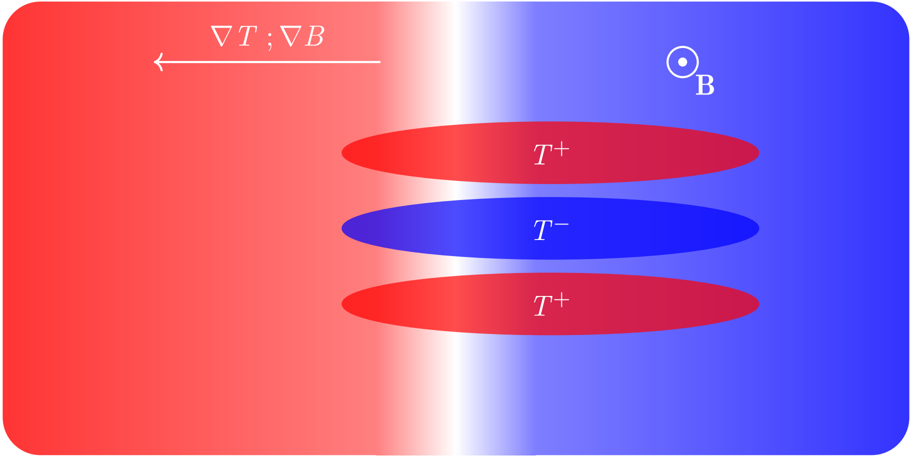

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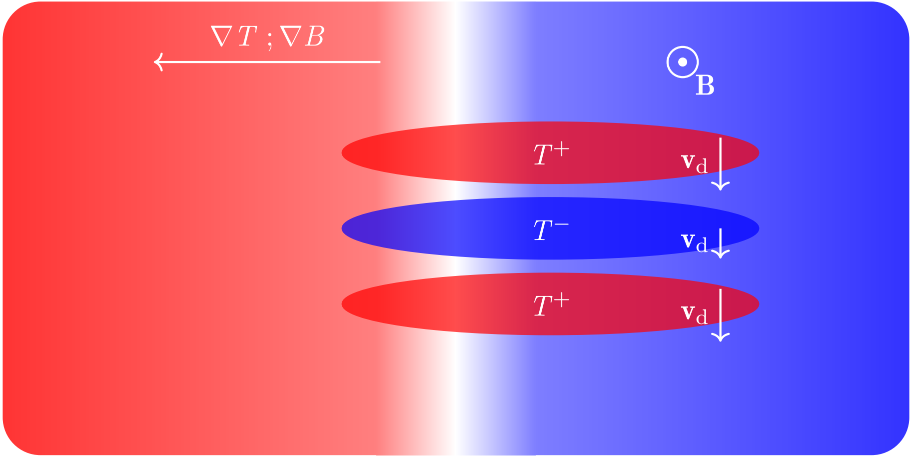

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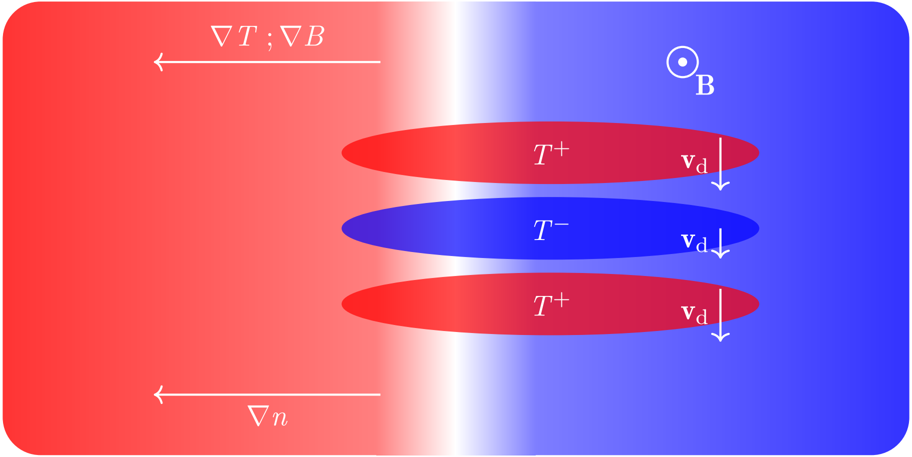

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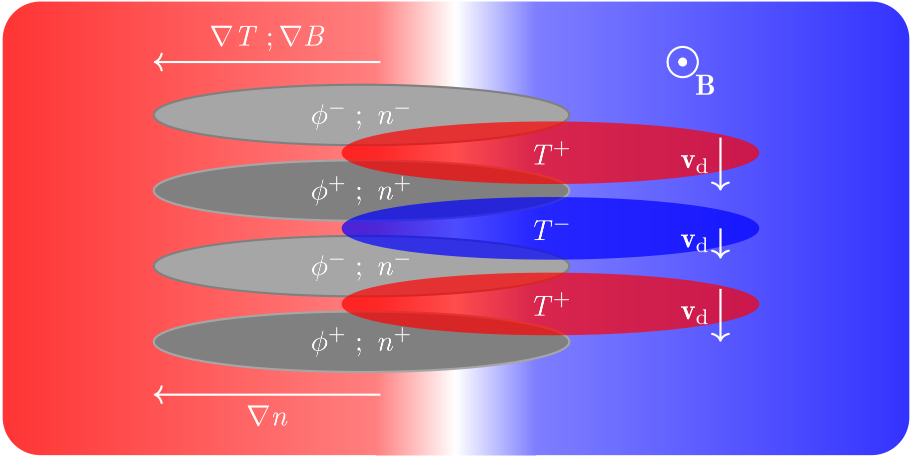

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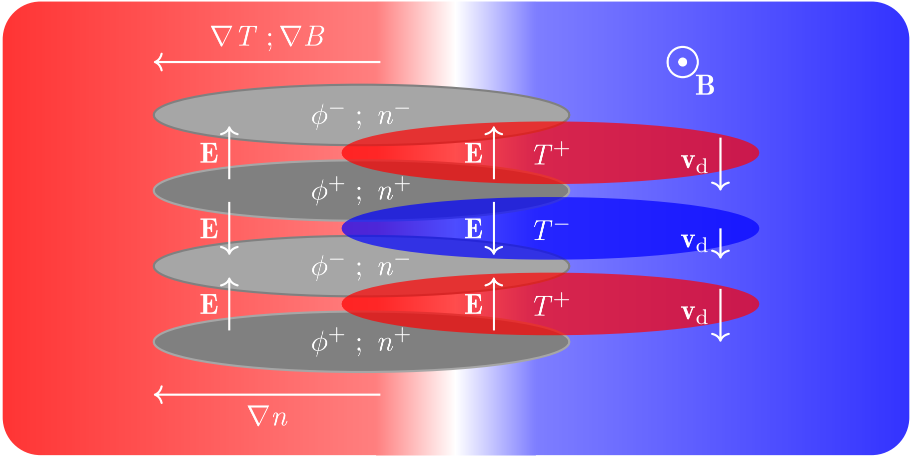

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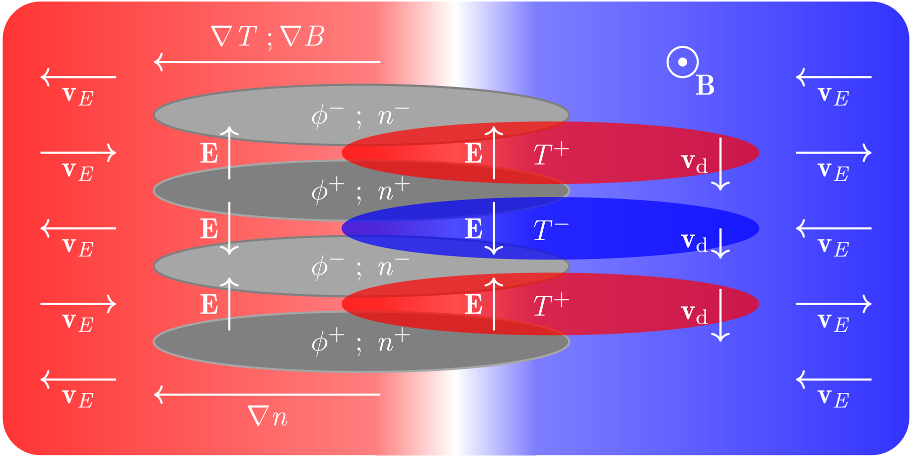

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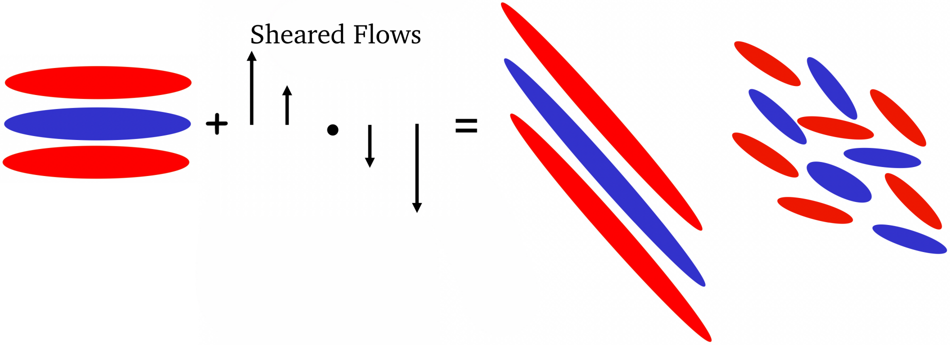

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$$\omega_{\mathrm{E\times B}} = \frac{1}{2}\frac{\partial^2 \langle\phi\rangle}{\partial x^2} \qquad \langle\phi\rangle = \frac{1}{L_y}\int_0^{L_y} \mathrm{d}y\; \phi(x, y, s = 0)$$

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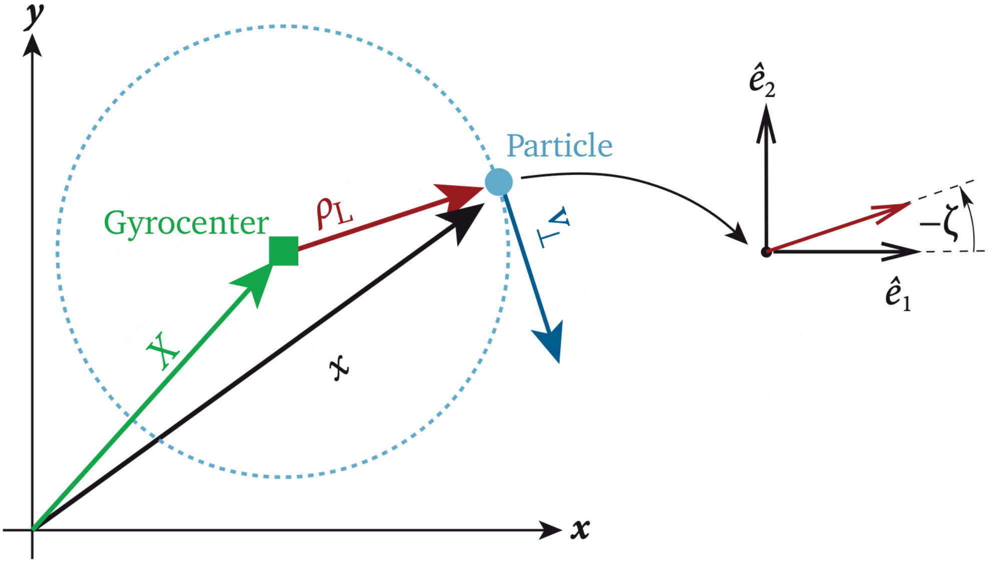

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$$\frac{\partial g}{\partial t} + \mathbf{v}_{\chi} \cdot \nabla g + (v_{\parallel}\mathbf{b} + \mathbf{v}_{\mathrm{D}}) \cdot \nabla(\delta f) - \frac{\mu B}{m} \frac{\mathbf{B}\cdot\nabla B}{B^2} \frac{\partial(\delta f)}{\partial v_{\parallel}} = S$$

Gyrokinetic Equation

$$g \sim (f_0 + \delta f) \qquad S \sim (f + f_0) \qquad \mathbf{v}_{\mathrm{D}} \sim \nabla B \qquad \mathbf{v}_{\chi} \sim \mathrm{E} \times \mathrm{B} \qquad f(x, y, s, v_{\parallel}, \mu)$$

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S6	21	83	16	64	9	1	$\lvert\nu_\parallel\rvert$	0.2	0.1	0.1	6	1.4	2.1

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- Standard box size $(L_x,\ L_y) = (76.3,\ 89.8)\,\rho$

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- Waltz criterion $|\omega_{\mathrm{E\times B}}| \approx \gamma$

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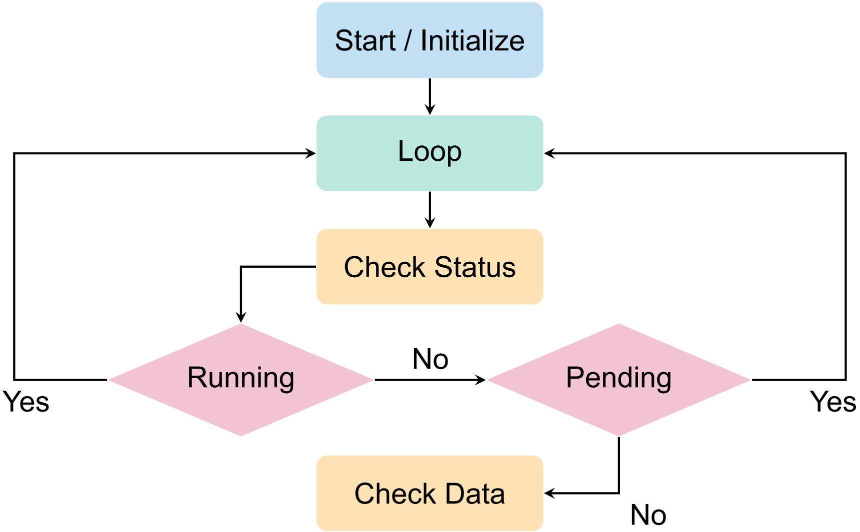

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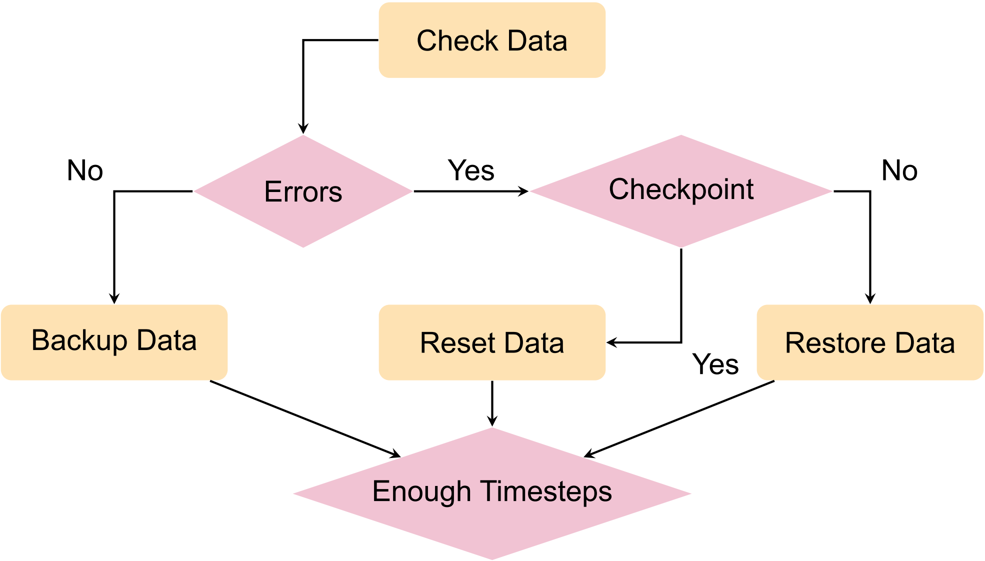

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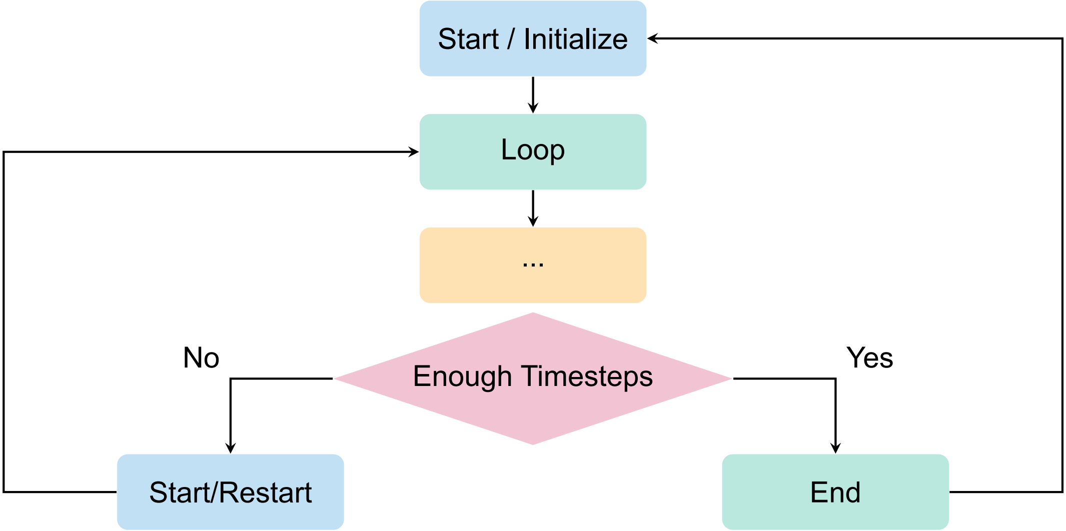

VARIATION OF COMPUTATIONAL RESOLUTION

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Goals:

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Verification:

1. Reduce only one number of grid points and look if criterias **(1), (2)** are satisfied
2. Reduce to known the minimum number of grid points to verify result in general.

BENCHMARK

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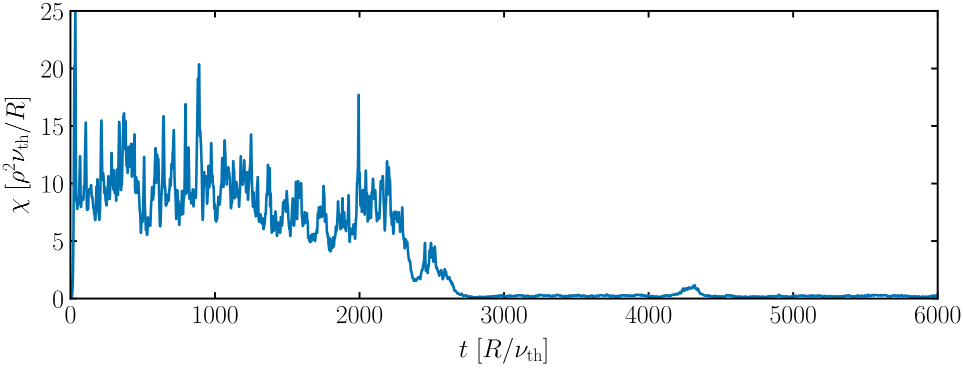

25
20
15
10
5
0
0
1000
2000
3000
4000
5000
6000
$\chi\ [\rho^2 \nu_{\mathrm{th}}/R]$
$t\ [R/\nu_{\mathrm{th}}]$

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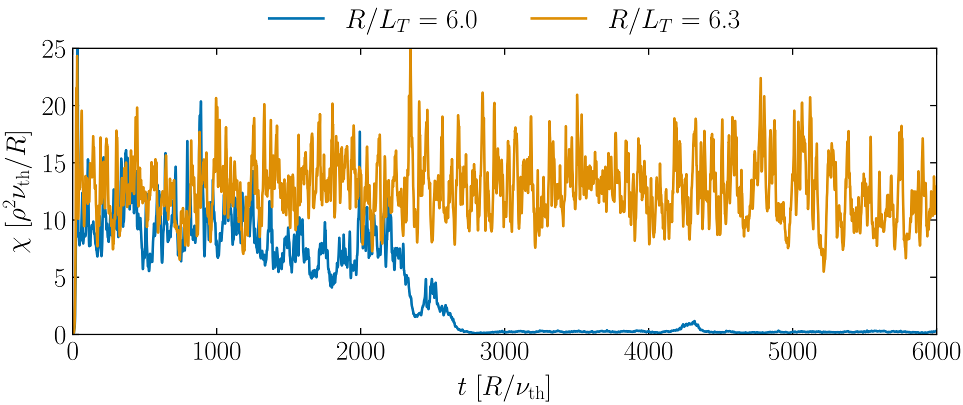

$R/L_T = 6.0$
$R/L_T = 6.3$
25
20
15
10
5
0
$\chi\ [\rho^2 \nu_{\mathrm{th}}/R]$
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REDUCTION OF GRID POINTS

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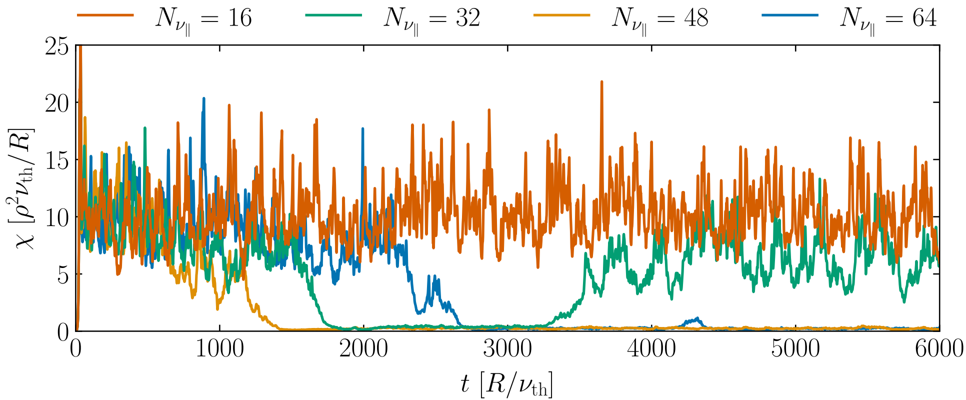

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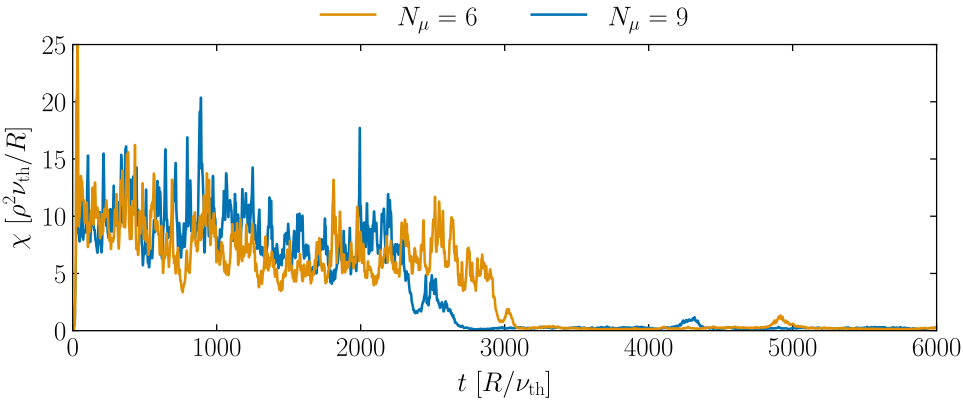

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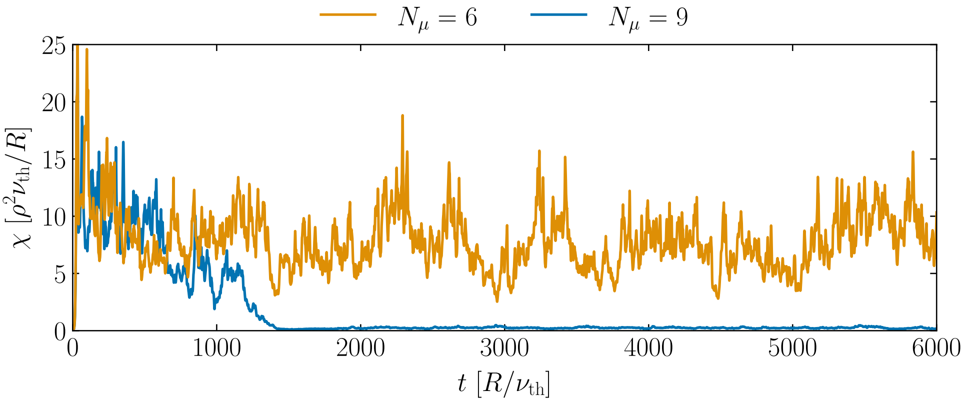

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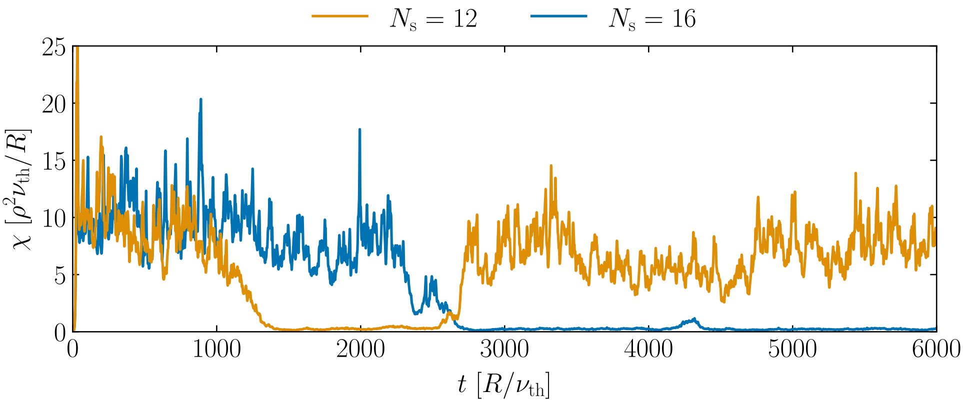

REDUCTION OF GRID POINTS

Final Resolution

	N_m	N_x	N_s	$N_{\nu_\parallel}$	N_μ	D	ν_d	$D_{\nu_\parallel}$	D_x	D_y	Order	$k_y\rho$	$k_x\rho$
S6	21	83	16	48	9	1	$\lvert\nu_\parallel\rvert$	0.2	0.1	0.1	6	1.4	2.1

SIZE CONVERGENCE OF $\mathrm{E} \times \mathrm{B}$ STAIRCASE PATTERN

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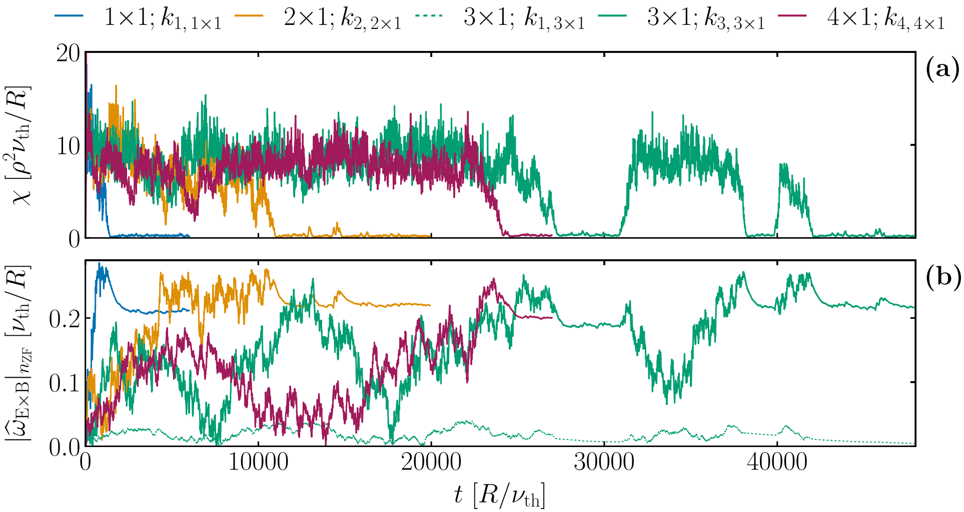
(1) Radial

$$N_{\mathrm{R}} \times N_{\mathrm{B}} \in [1 \times 1,\ 2 \times 1,\ 3 \times 1,\ 4 \times 1]$$

SIZE CONVERGENCE OF $\mathrm{E} \times \mathrm{B}$ STAIRCASE PATTERN



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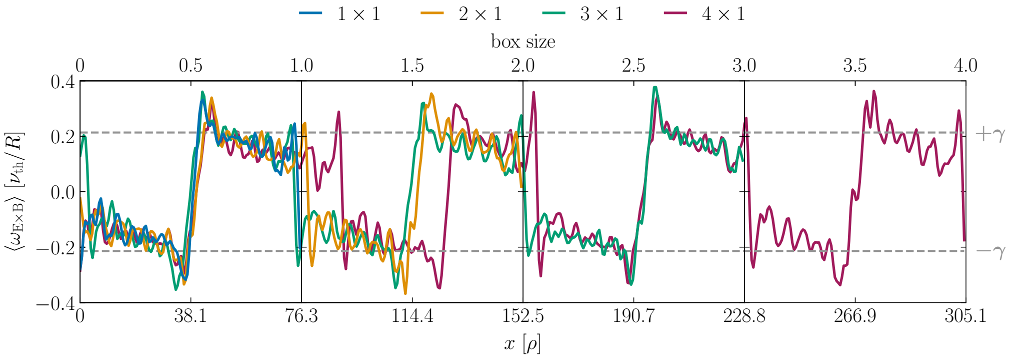
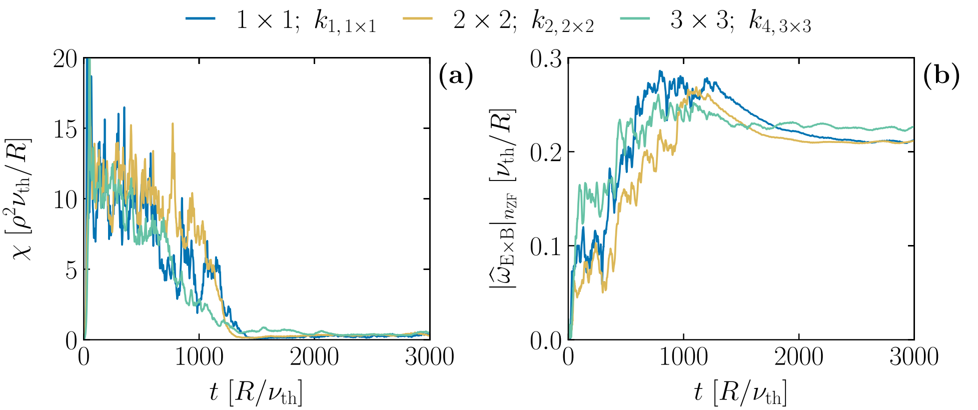


SIZE CONVERGENCE OF $\mathrm{E} \times \mathrm{B}$ STAIRCASE PATTERN

(2) Isotropic

$$N_{\mathrm{R}} \times N_{\mathrm{B}} \in [1 \times 1,\ 1.5 \times 1.5,\ 2 \times 2,\ 2.5 \times 2.5,\ 3 \times 3]$$

SIZE CONVERGENCE OF $\mathrm{E} \times \mathrm{B}$ STAIRCASE PATTERN



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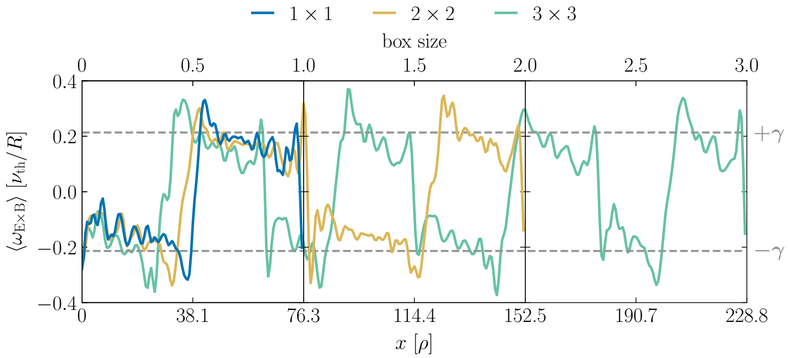

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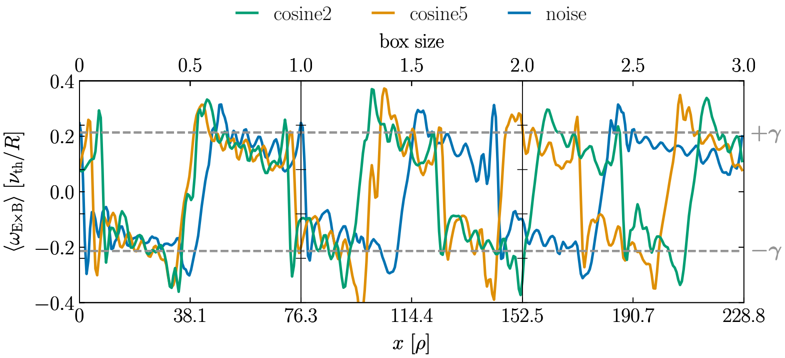

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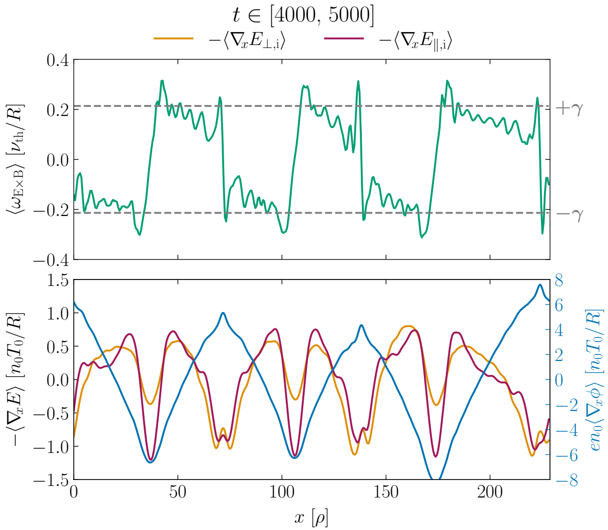
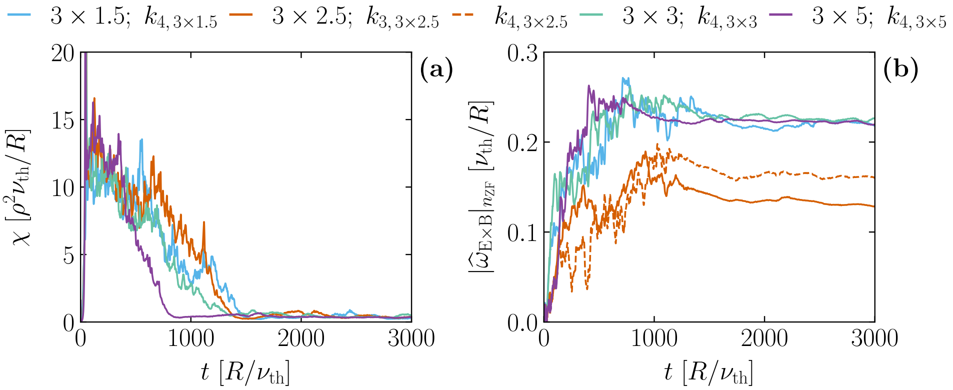


SIZE CONVERGENCE OF $\mathrm{E} \times \mathrm{B}$ STAIRCASE PATTERN

(3) Binormal

$$N_{\mathrm{R}} \times N_{\mathrm{B}} \in [3 \times 1.5,\ 3 \times 2.5,\ 3 \times 3,\ 3 \times 5]$$

SIZE CONVERGENCE OF $\mathrm{E} \times \mathrm{B}$ STAIRCASE PATTERN



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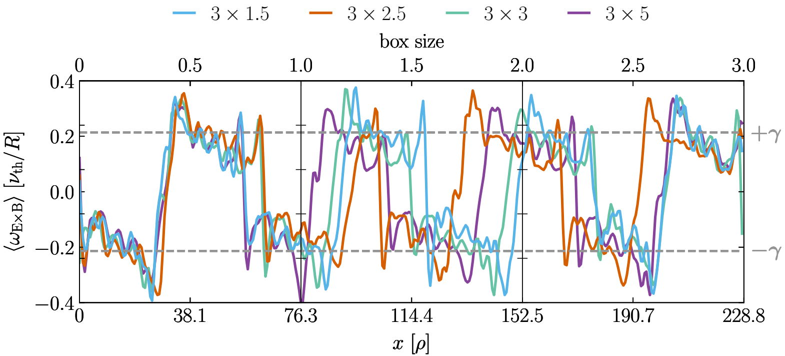

SIZE CONVERGENCE OF $\mathrm{E} \times \mathrm{B}$ STAIRCASE PATTERN

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Does the basic pattern size always converges to the box size, or is there a typical mesoscale size inherent to staircase structures also in a local flux-tube description?

$\Rightarrow$ Mesoscale pattern size of:

$$\boxed{\sim 57 - 76\,\rho}$$

- Non-locality is inherent to ITG-driven turbulence
- Avalanches are spatially organized by the $\mathrm{E} \times \mathrm{B}$ staircase pattern

THE FINITE HEAT FLUX THRESHOLD

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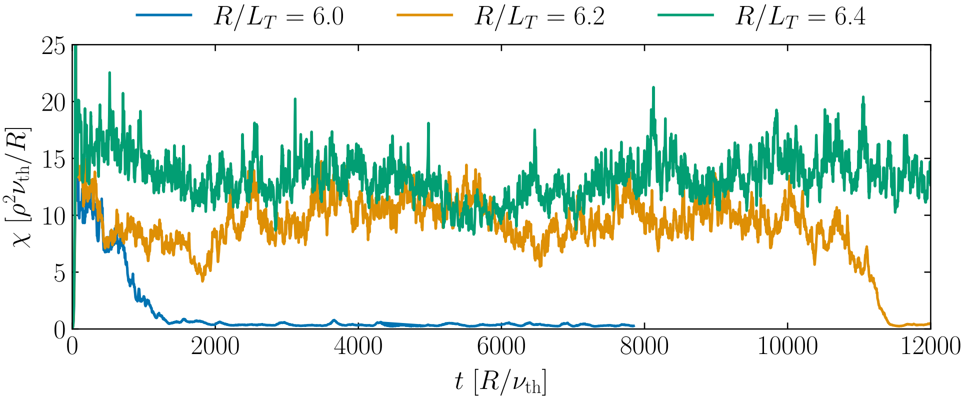

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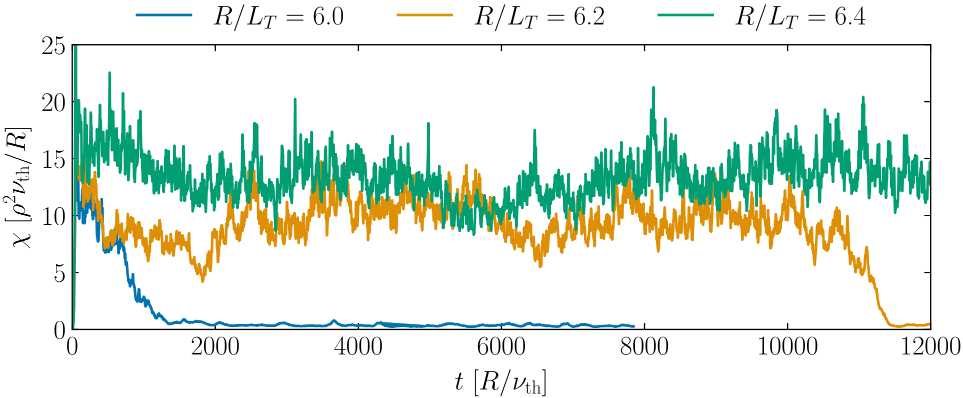

$$\Rightarrow \boxed{R/L_T|_{\mathrm{finite}} = 6.3 \pm 0.1}$$

CONCLUSION

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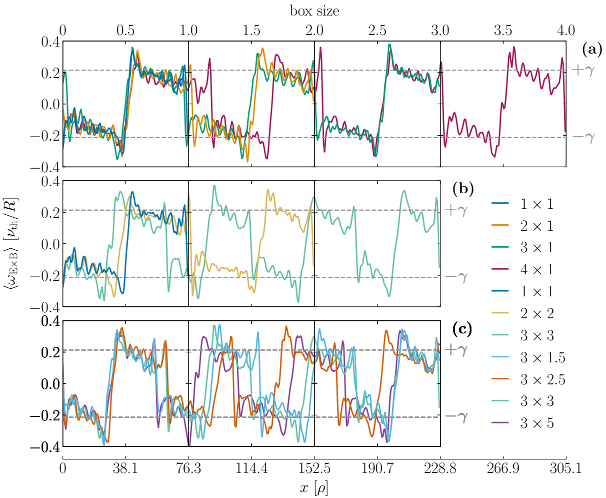

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- Parallel velocity $N_{\nu_{\|}}$ could be reduced from 64 to 48, which halfed the time until suppression of turbulence
- Restart Script with `python` led to further convenience during the task of performing simulations
- Mesoscale pattern size of $\sim 57 - 76\,\rho$ is found to be intrinsic to ITG-driven turbulence for Cyclone Base Case parameters
- Finite heat flux threshold is located at $R/L_T|_{\text{finite}} = 6.3 \pm 0.1$