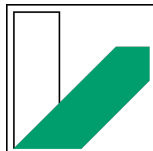


Theoretical Plasmaphysics

Bachelor Thesis

**Size convergence
of the $E \times B$ staircase pattern
in flux tube simulations
of ion temperature gradient driven
turbulence**

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Information

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Dedication

Abstract and Zusammenfassung

The radial size convergence of the $E \times B$ staircase pattern is addressed in local gradient-driven flux tube simulations of ion temperature gradient (ITG) driven turbulence. It is shown that a mesoscale pattern size of $\sim 57.20 - 76.27 \rho$ is inherent to ITG driven turbulence with Cyclone Base Case parameters in the local limit.

Zusammenfassung

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1 Introduction

Ion temperature gradient driven turbulence close to marginal stability exhibits zonal flow pattern formation on mesoscales, so-called $E \times B$ staircase structures [10]. Such pattern formation has been observed in local gradient-driven flux-tube simulations [25, 42, 29] as well as global gradient-driven [22, 35, 31] and global flux-driven [10, 11, 40, 18, 20] studies. In global studies, spanning a larger fraction of the minor radius, multiple radial repetitions of staircase structures are usually observed, with a typical pattern size of several ten Larmor radii. By contrast, in the aforementioned local studies the radial size of $E \times B$ staircase structures is always found to converge to the radial box size of the flux tube domain. The above observations lead to the question: *Does the basic pattern size always converges to the box size, or is there a typical mesoscale size inherent to staircase structures also in a local flux-tube description?* The latter case would imply that it is not necessarily global physics, i.e., profile effects, that set (i) the radial size of the $E \times B$ staircase pattern and (ii) the scale of avalanche-like transport events. These transport events are usually restricted to $E \times B$ staircase structures and considered as a nonlocal transport mechanism [10]. In this brief communication the above question is addressed through a box size convergence scan of the same cases close to the nonlinear threshold for turbulence generation as studied in Ref. [25].

2 Theory

In the following the box size is increased relative to the standard box size $(L_x, L_y) = (76.27, 89.76) \rho$ in the radial and binormal direction. Here, x is the radial coordinate that labels the flux surfaces normalized by the thermal Larmor radius ρ , y labels the field lines and is an approximate binormal or toroidal coordinate. Together with the coordinate s which parameterizes the length along the field lines and represents the poloidal coordinate these quantities form the Hamada coordinates [16]. The increased box sizes are indicated by the real parameter N_R for radial and N_B for the binormal direction with the nomenclature $N_R \times N_B$ throughout this work. Note that, the number of modes in the respective direction, i.e., N_x and N_m , respectively, is always adapted accordingly to retain a spatial resolution compliant to the standard resolution [Tab. 3.1] and standard box size.

The $\mathbf{E} \times \mathbf{B}$ staircase pattern is manifest as radial structure formation in the $\mathbf{E} \times \mathbf{B}$ shearing rate defined by [28, 27, 28, 25]

$$\omega_{\mathbf{E} \times \mathbf{B}} = \frac{1}{2} \frac{\partial^2 \langle \phi \rangle}{\partial x^2}, \quad (2.1)$$

where $\langle \phi \rangle$ is the zonal electrostatic potential normalized by $\rho_* T/e$ ($\rho_* = \rho/R$ is the thermal Larmor radius normalized with the major radius R , T is the temperature, e is the elementary charge). The zonal potential is calculated from the electrostatic potential ϕ on the two-dimensional x - y -plane at the low field side according to [29]

$$\langle \phi \rangle = \frac{1}{L_y} \int_0^{L_y} dy \phi(x, y, s = 0). \quad (2.2)$$

The $\mathbf{E} \times \mathbf{B}$ shearing rate $\omega_{\mathbf{E} \times \mathbf{B}}$ is the radial derivative of the advecting zonal flow velocity [15, 36] and quantifies the zonal flow induced shearing of turbulent structures [2, 15, 3]. Consistent with Ref. [25] the turbulence level is quantified by the turbulent heat conduction coefficient χ , which is normalized by $\rho^2 v_{\text{th}}/R$ ($v_{\text{th}} = \sqrt{2T/m}$ is the thermal velocity and m is the mass). Furthermore, quantities ρ , R , T , v_{th} and m are referenced quantities from Ref. [25, 24].

In order to diagnose the temporal evolution of the staircase pattern and to obtain an estimate of its amplitude the radial Fourier transform of the $\mathbf{E} \times \mathbf{B}$ shearing rate is considered. It is defined by

$$\omega_{\mathbf{E} \times \mathbf{B}} = \sum_{k_{\text{ZF}}} \hat{\omega}_{\mathbf{E} \times \mathbf{B}}(k_{\text{ZF}}, t) \exp(ik_{\text{ZF}}x), \quad (2.3)$$

where $\hat{\omega}_{\mathbf{E} \times \mathbf{B}}$ is the complex Fourier coefficient and $k_{\text{ZF}} = 2\pi n_{\text{ZF}}/L_x$ defines the zonal flow wave vector with the zonal flow mode number n_{ZF} ranging in $-(N_x - 1)/2 \leq n_{\text{ZF}} \leq (N_x - 1)/2$. Based on the definitions above, the shear carried by the zonal flow mode with wave vector k_{ZF} is defined by $|\hat{\omega}_{\mathbf{E} \times \mathbf{B}}|_{n_{\text{ZF}}} = 2|\hat{\omega}_{\mathbf{E} \times \mathbf{B}}|$. In general, the zonal flow mode that dominates the $\mathbf{E} \times \mathbf{B}$ staircase pattern, also referred to as the *basic mode* of the pattern in this work, exhibits the maximum amplitude in the spectrum $|\hat{\omega}_{\mathbf{E} \times \mathbf{B}}|_{n_{\text{ZF}}}$.

3 Methods and Material

3.1 Simulation Setup

The gyrokinetic simulations are performed with the non-linear flux tube version of Gyrokinetic Workshop (GKW) [24] with adiabatic electron approximation. In agreement with Ref. [25], Cyclone Base Case (CBC) like parameters are chosen with an inverse background temperature gradient length $R/L_T = 6.0$ and circular concentric flux surfaces. The numerical resolution is compliant to the "Standard resolution with 6th order (S6)" set-up of the aforementioned reference, with a somewhat lowered number of parallel velocity grid points. It has been carefully verified that this modification preserves the same physical outcome as the original study. A summary of the numerical parameters is given in Tab. 3.1 and for more details about the definition of individual quantities the reader is referred to Refs. [24, 25].

	N_m	N_x	N_s	$N_{\nu_{\parallel}}$	N_{μ}	D	ν_d	$D_{\nu_{\parallel}}$	D_x	D_y	Order	$k_y\rho$	$k_x\rho$
S6	21	83	16	48	9	1	$ \nu_{\parallel} $	0.2	0.1	0.1	6	1.4	2.1

Table 3.1: Resolution used in this paper: Number of toroidal modes N_m , number of radial modes N_x , number of grid points along the magnetic field N_s , number of parallel velocity grid points $N_{\nu_{\parallel}}$, number of magnetic moment grid points N_{μ} , dissipation coefficient used in convection along the magnetic field D , the velocity in the dissipation scheme ν_d , dissipation coefficient used in the trapping term $D_{\nu_{\parallel}}$, damping coefficient of radial modes D_x , damping coefficient of toroidal modes D_y , order of the scheme used for the zonal mode, maximum poloidal wave vector $k_y\rho$, and maximum radial wave vector $k_x\rho$

3.2 btrzx1 Cluster

3.3 Restart Script for Simulation btrzx1 Cluster

4 Results and Discussion

4.1 Variation of Computational Resolution

At the beginning of this work the goal is to change the used resolution to a minimum. The goal behind this research is to reduce Computational time and costs for the computation of the simulation.

4.2 Converge of Wavelength

4.2.1 Radial increased Box Size

In the first test the radial box size is increased while the binormal box size is kept fixed to the standard size. The scan covers the realizations $N_R \times N_B \in [1 \times 1, 2 \times 1, 3 \times 1, 4 \times 1]$. Each realization exhibits an initial quasi-stationary turbulent phase and a second final [25] phase with almost suppressed turbulence [Fig. 4.1 (a)]. The latter state is indicative for the presence of a fully developed staircase pattern as depicted in Fig. 4.2. This type of structure is characterized by intervals of almost constant shear with alternating sign satisfying the Waltz criterion $|\omega_{E \times B}| \approx \gamma$ [38, 36] (γ is the growth rate of the most unstable linear ITG driven Eigenmode), connected by steep flanks where $\omega_{E \times B}$ crosses zero. Fig. 4.2 (a) shows a striking repetition of the staircase structure, with the number of repetitions equal to N_R . Hence, the basic size of the pattern not only converges with increasing radial box size, the converged radial size turns out to at least roughly agree with the standard radial box size of Ref. [25]

Due to the lack of a substantial turbulent drive in the final suppressed state no further zonal flow evolution is observed [Fig. 4.1 (b)] and one might critically ask whether the structures shown in Fig. 4.2 represent the real converged pattern in a statistical sense. Note that in the 3×1 case the initial quasi-stationary turbulent state extends up to a few $\sim 10^4 R/v_{th}$. During this period the zonal flow mode with $n_{ZF} = 3$, i.e., the mode that dominates the staircase pattern in final suppressed phase, undergoes a long-term evolution with a typical time scale of several $\sim 10^3 R/v_{th}$. Hence, several of such cycles are covered by the initial turbulent phase, which is evident from the occurrence of phases with reduced amplitude around $t \approx 8000 R/v_{th}$ and $t \approx 18000 R/v_{th}$. It is the $n_{ZF} = 4$ zonal flow mode, i.e., the next shorter radial scale mode, that dominates the shear spectrum $|\hat{\omega}_{E \times B}|_{n_{ZF}}$ in the latter two phases (not shown). This demonstrates a competition between the $n_{ZF} = 3$ and $n_{ZF} = 4$ modes. Most importantly, no secular growth of the $n_{ZF} = 1$ (box scale) zonal flow mode is observed during the entire quasi-stationary turbulent phase

[Fig. 4.1 (b) dotted line]. The above discussion indicates that although the $n_{ZF} = 3, 4$ zonal modes compete, the pattern scale does not converge to the radial box scale but rather to a mesoscale of $\sim 57.20 - 76.27 \rho$ (i.e., $n_{ZF} = 4, 3$ in the 3×1 case).

4.2.2 Isotropic increased Box Size

Since the radially elongated simulation domain might inhibit the development of isotropic turbulent structures, in the second test the radial and binormal box size is increased simultaneously. This scan covers the realizations $N_R \times N_B \in [1 \times 1, 2 \times 2, 3 \times 3]$. Interestingly, suppression of the turbulence by the emergence of a fully developed staircase pattern always occurs after $\sim 1000 R/\nu_{th}$ [Fig. 4.3], i.e., significantly faster compared to the 3×1 and 4×1 realizations. As shown in Fig. 4.2 (b) also this test confirms the convergence of the staircase pattern size to a typical mesoscale that is distinct from the radial box size in the $N_R > 1$ realizations.

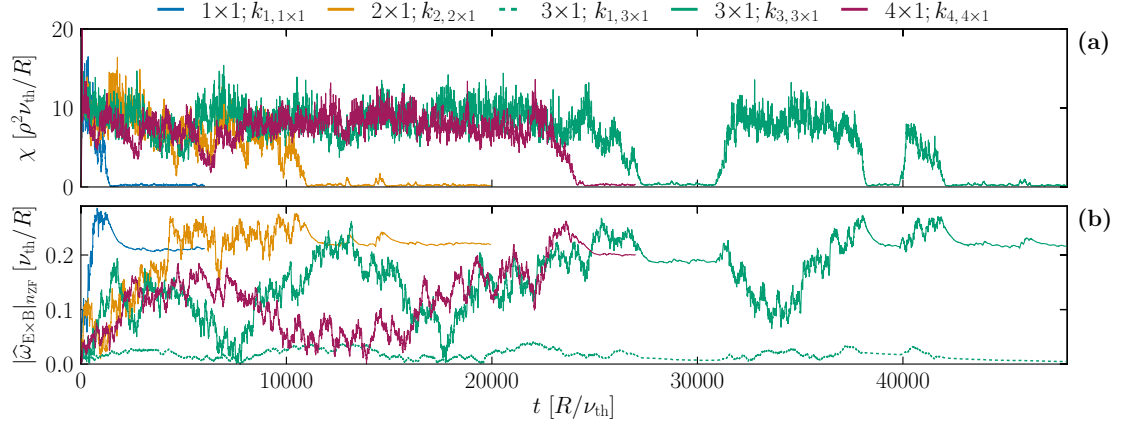


Figure 4.1: (a) Time traces of the heat conduction coefficient χ for $R/L_T = 6.0$ for radial increased box sizes
 (b) Time traces of $|\hat{\omega}_{E \times B}|_{n_{ZF}}$ for radial increased box sizes

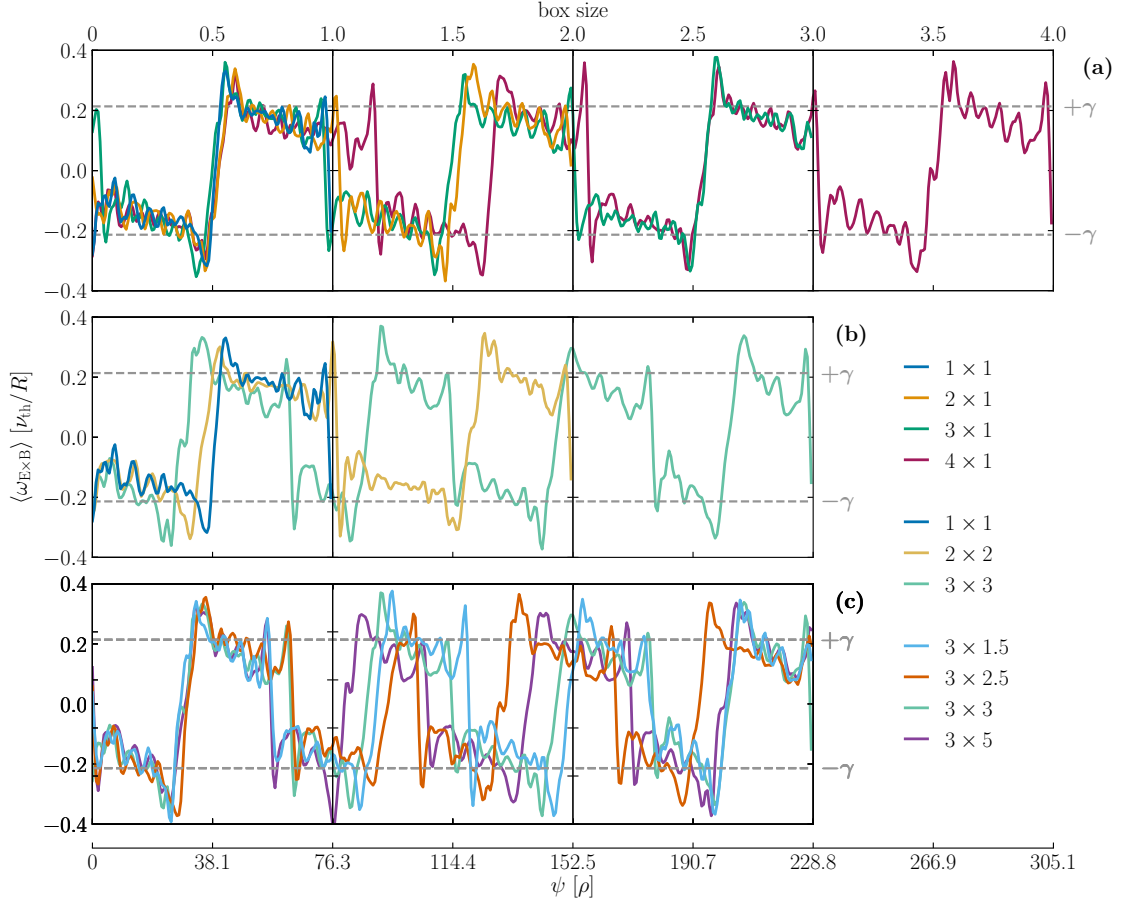


Figure 4.2: Comparison of shearing rate $\omega_{E \times B}$ for each box sizes scan averaged over given time interval and the growth rate $\pm\gamma$ of the most unstable linear ITG driven Eigenmode. The staircase structures are radially shifted with respect to each other till alignment for better visibility.

(a) radial:	$t_{1 \times 1} \in [2000, 5000]$,	$t_{2 \times 1} \in [15000, 18000]$,	$t_{3 \times 1} \in [43000, 45000]$,
(b) isotropic:	$t_{1 \times 1} \in [2000, 5000]$,	$t_{2 \times 2} \in [2000, 3000]$,	$t_{3 \times 3} \in [2000, 3000]$
(c) binormal:	$t_{3 \times 1.5} \in [2000, 3000]$,	$t_{3 \times 2.5} \in [2000, 3000]$,	$t_{3 \times 3} \in [2000, 3000]$

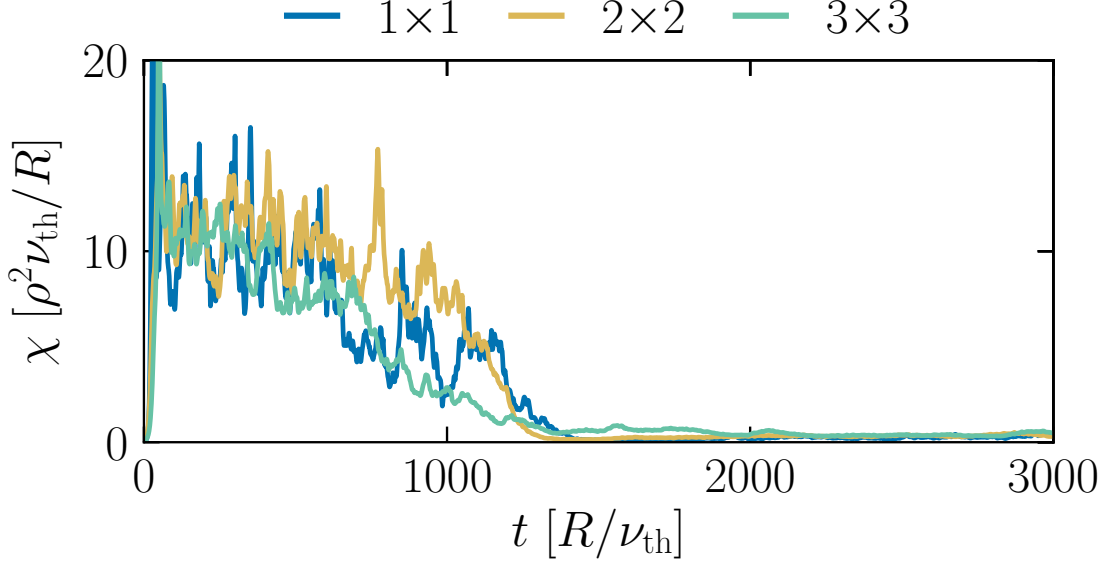


Figure 4.3: Time traces of the heat conduction coefficient χ for $R/L_T = 6.0$ for isotropic increased box sizes

By contrast to the radial box size scan the 3×3 realization shows a stationary pattern with four repetitions of the fully developed staircase structure, i.e., a somewhat smaller pattern size. Whether this is related to a possible pattern size dependence on the binormal box size or to the competition between patterns with the two sizes $\lambda \in [57.20, 76.27] \rho$ as observed in the first test is addressed in the next paragraph.

4.2.3 Binormal increased Box Size

In a third test the binormal box size is varied with the radial box size fixed to $N_R = 3$. This test covers the realizations $N_R \times N_B \in [3 \times 1.5, 3 \times 2.5, 3 \times 3, 3 \times 5]$. As in the isotropic scan the turbulence subdued and a fully developed staircase pattern formats after $\sim 2000 R/v_{th}$ [Fig. 4.4]. The convergence of staircase pattern can be seen in Fig. 4.2 (c) and confirms again a size of a typical mesoscale. Fig. 4.2 (c) also confirms that indeed a competition between patterns with two sizes $\lambda \in [57.20, 76.27] \rho$ causing the different results for 3×1 and 3×3 . The zonal flow mode number varies between $n_{ZF} = 3, 4$ which can be seen in Fig. 4.2 (c) in the 3×2.5 realization. The staircase structure has a pattern between 3 and 4 repetitions which get represented in the second repetition with no positive shear. Instead the pattern returns immediately after reaching the maximum shear ($+\gamma$) to the minimum shear ($-\gamma$) of the third repetition in a steep flank. The Fourier analysis of this case yields no definitely basic mode rather two dominate modes with $n_{ZF} = 3, 4$ with a fraction of the maximum amplitude $|\hat{\omega}_{E \times B}|_{n_{ZF}}$ each (not shown).

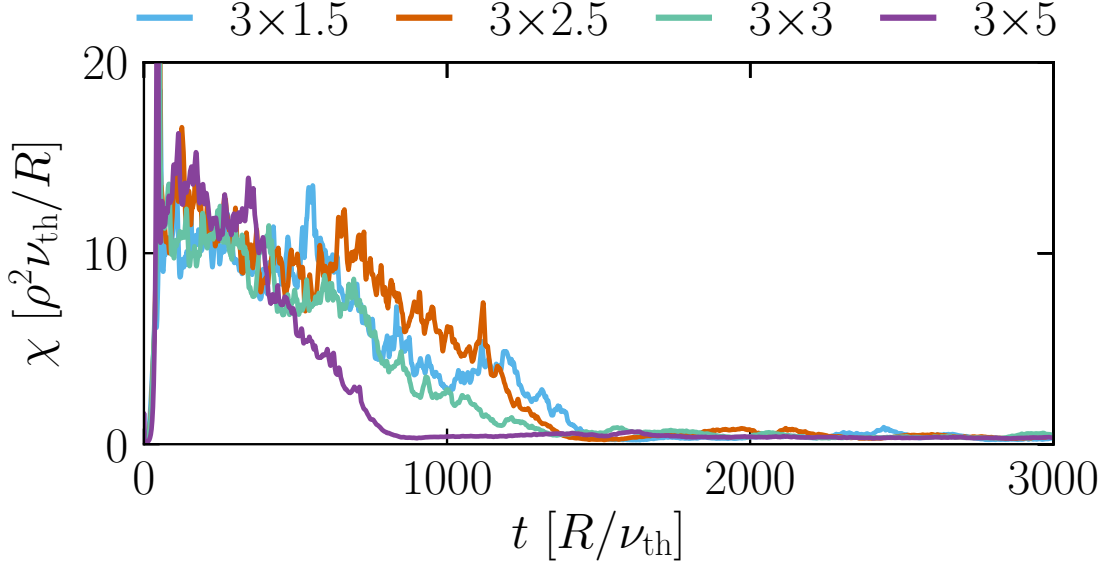


Figure 4.4: Time traces of the heat conduction coefficient χ for $R/L_T = 6.0$ for binormal increased box sizes

4.3 The finite heat flux threshold

In the final test the inverse background temperature gradient length R/L_T is varied at fixed 3×3 box size. Since suppression of turbulence usually occurs at later times when approaching the finite heat flux threshold from below [25], the analysis aims to lengthen the phase during which the zonal flow varies in time due to turbulent Reynolds stresses. This scan covers realizations with $R/L_T \in [6.0, 6.2, 6.4]$. In the case of $R/L_T = 6.2$ turbulence suppression is observed for $t > 12000 R/v_{th}$, while stationary turbulence during the entire simulation time trace of $12000 R/v_{th}$ is found for $R/L_T = 6.4$. The finite heat flux threshold, hence, is $R/L_T|_{\text{finite}} = 6.3 \pm 0.1$. Although the initial quasi-stationary turbulence in the former case is significantly larger compared to the $R/L_T = 6.2$ realization discussed in the second test, a stationary pattern with basic zonal flow mode $n_{ZF} = 3$ establishes. Again, the $n_{ZF} = 1$ (box scale) zonal flow mode does not grow secularly during the entire turbulent phase. Also, this test confirms the statistical soundness of the converged pattern size of $\sim 57.20 - 76.27 \rho$.

5 Closure

Through careful tests this brief communication confirms the radial size convergence of the $\mathbf{E} \times \mathbf{B}$ staircase pattern in local gyrokinetic flux tube simulations of ion temperature gradient (ITG) driven turbulence. A mesoscale pattern size of $\sim 57.20 - 76.27 \rho$ is found to be intrinsic to ITG driven turbulence for Cyclone Base Case parameters. This length scale is somewhat larger compared to results from global studies with finite ρ_* , which report of a few 10ρ [10], and has to be considered the proper mesoscale in the local limit $\rho_* \rightarrow 0$. The occurrence of this mesoscale implies that non-locality, in terms of Ref. [10], is inherent to ITG driven turbulence, since avalanches are spatially organized by the $\mathbf{E} \times \mathbf{B}$ staircase pattern [22, 10, 28, 25].

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