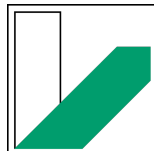


Theoretical Plasmaphysics

Bachelor Thesis

**Size convergence
of the $E \times B$ staircase pattern
in flux tube simulations
of ion temperature gradient driven
turbulence**

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Information

Day	April 9, 2023
Place	Universität Bayreuth
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Abstract

The radial size convergence of the $E \times B$ staircase pattern is addressed in local gradient-driven flux tube simulations of ion temperature gradient (ITG) driven turbulence. It is shown that a mesoscale pattern size of $\sim 57.20 - 76.27 \rho$ is inherent to ITG driven turbulence with Cyclone Base Case parameters in the local limit.

Zusammenfassung

Dedication

Contents

1	Introduction	11
2	Theory	13
3	Methods and Material	17
3.1	Simulation Setup	18
3.2	btrzx1 Cluster	18
3.3	Restart Script for Simulation btrzx1 Cluster	18
4	Results and Discussion	19
4.1	Variation of Computational Resolution	20
4.1.1	Benchmark	20
4.1.2	Reduction of parallel velocity grid points $N_{v_{\parallel}}$	21
4.1.3	Reduction of magnetic moment grid points N_{μ}	22
4.1.4	Reduction of magnetic field grid points N_s	23
4.1.5	Final Resolution for Simulation	24
4.2	Size Convergence of $E \times B$ staircase pattern	25
4.2.1	Radial increased Box Size	25
4.2.2	Isotropic increased Box Size	27
4.2.3	Binormal increased Box Size	28
4.2.4	Staircase structures in Comparison	29
4.3	The finite heat flux threshold	30
5	Closure	31
6	Append A	33
6.1	Append A	33

Bibliography	35
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Introduction

Ion temperature gradient driven turbulence close to marginal stability exhibits zonal flow pattern formation on mesoscales, so-called $E \times B$ staircase structures³. Such pattern formation has been observed in local gradient-driven flux-tube simulations^{11,20,14} as well as global gradient-driven^{9,16,15} and global flux-driven^{3,4,19,7,8} studies. In global studies, spanning a larger fraction of the minor radius, multiple radial repetitions of staircase structures are usually observed, with a typical pattern size of several ten Larmor radii. By contrast, in the aforementioned local studies the radial size of $E \times B$ staircase structures is always found to converge to the radial box size of the flux tube domain. The above observations lead to the question:

Does the basic pattern size always converges to the box size, or is there a typical mesoscale size inherent to staircase structures also in a local flux-tube description?

The latter case would imply that it is not necessarily global physics, i.e., profile effects, that set

- (i) the radial size of the $E \times B$ staircase pattern
- (ii) the scale of avalanche-like transport events.

These transport events are usually restricted to $E \times B$ staircase structures and considered as a nonlocal transport mechanism³.

In this bachelor thesis the above question is addressed through a box size convergence scan of the same cases close to the nonlinear threshold for turbulence generation as studied in Ref. 11.

Theory

2

In the following the box size is increased relative to the standard box size $(L_x, L_y) = (76.27, 89.76) \rho$ in the radial and binormal direction. Here, x is the radial coordinate that labels the flux surfaces normalized by the thermal Larmor radius ρ , y labels the field lines and is an approximate binormal coordinate. Together with the coordinate s which parameterizes the length along the field lines and is referred to as the parallel coordinate these quantities form the Hamada coordinates⁶. The increased box sizes are indicated by the real parameter N_R for radial and N_B for the binormal direction with the nomenclature $N_R \times N_B$ throughout this work. Note that, the number of modes in the respective direction, i.e., N_x and N_m , respectively, is always adapted accordingly to retain a spatial resolution compliant to the standard resolution [Tab. 4.1] and standard box size.

The $E \times B$ staircase pattern is manifest as radial structure formation in the $E \times B$ shearing rate defined by^{13,12,11}

$$\omega_{E \times B} = \frac{1}{2} \frac{\partial^2 \langle \phi \rangle}{\partial x^2}, \quad (2.1)$$

where $\langle \phi \rangle$ is the zonal electrostatic potential normalized by $\rho_* T / e$ ($\rho_* = \rho / R$ is the thermal Larmor radius normalized with the major radius R , T is the temperature, e is the elementary charge). The zonal potential is calculated from the electrostatic potential ϕ on the two-dimensional x - y -plane at the low field side according to¹⁴

$$\langle \phi \rangle = \frac{1}{L_y} \int_0^{L_y} dy \phi(x, y, s = 0). \quad (2.2)$$

The $E \times B$ shearing rate $\omega_{E \times B}$ is the radial derivative of the advecting zonal flow velocity^{5,17} and quantifies the zonal flow induced shearing of turbulent structures^{1,5,2}.

Consistent with Ref. 11 the turbulence level is quantified by the turbulent heat conduction coefficient χ , which is normalized by $\rho^2 v_{th} / R$ ($v_{th} = \sqrt{2T/m}$ is the thermal velocity and m is the mass). Furthermore, quantities ρ , R , T , v_{th} and m are referenced quantities from Ref. 11,10.

In order to diagnose the temporal evolution of the staircase pattern and to obtain an estimate of its amplitude the radial Fourier transform of the $\mathbf{E} \times \mathbf{B}$ shearing rate is considered. It is defined by

$$\omega_{\mathbf{E} \times \mathbf{B}} = \sum_{k_{\text{ZF}}} \hat{\omega}_{\mathbf{E} \times \mathbf{B}}(k_{\text{ZF}}, t) \exp(ik_{\text{ZF}}x), \quad (2.3)$$

where $\hat{\omega}_{\mathbf{E} \times \mathbf{B}}$ is the complex Fourier coefficient and $k_{\text{ZF}} = 2\pi n_{\text{ZF}}/L_x$ defines the zonal flow wave vector with the zonal flow mode number n_{ZF} ranging in $-(N_x - 1)/2 \leq n_{\text{ZF}} \leq (N_x - 1)/2$. Based on the definitions above, the shear carried by the zonal flow mode with wave vector k_{ZF} is defined by $|\hat{\omega}_{\mathbf{E} \times \mathbf{B}}|_{n_{\text{ZF}}} = 2|\hat{\omega}_{\mathbf{E} \times \mathbf{B}}(k_{\text{ZF}}, t)|$. In general, the zonal flow mode that dominates the $\mathbf{E} \times \mathbf{B}$ staircase pattern, also referred to as the *basic mode* of the pattern in this work, exhibits the maximum amplitude in the spectrum $|\hat{\omega}_{\mathbf{E} \times \mathbf{B}}|_{n_{\text{ZF}}}$.

Methods and Material

3

3.1 Simulation Setup

The gyrokinetic simulations are performed with the non-linear flux tube version of Gyrokinetic Workshop (GKW)¹⁰ with adiabatic electron approximation. In agreement with Ref. 11, Cyclone Base Case (CBC) like parameters are chosen with an inverse background temperature gradient length $R/L_T = 6.0$ and circular concentric flux surfaces. The numerical resolution is compliant to the "Standard resolution with 6th order (S6)" set-up of the aforementioned reference, with a somewhat lowered number of parallel velocity grid points. It has been carefully verified that this modification preserves the same physical outcome as the original study. A summary of the numerical parameters is given in Tab. 4.1 and for more details about the definition of individual quantities the reader is referred to Refs. 10,11.

	N_m	N_x	N_s	$N_{\nu_{\parallel}}$	N_{μ}	D	ν_d	$D_{\nu_{\parallel}}$	D_x	D_y	Order	$k_y\rho$	$k_x\rho$
S6	21	83	16	64	9	1	$ \nu_{\parallel} $	0.2	0.1	0.1	6	1.4	2.1

Table 3.1: Resolution used in this paper: Number of toroidal modes N_m , number of radial modes N_x , number of grid points along the magnetic field N_s , number of parallel velocity grid points $N_{\nu_{\parallel}}$, number of magnetic moment grid points N_{μ} , dissipation coefficient used in convection along the magnetic field D , the velocity in the dissipation scheme ν_d , dissipation coefficient used in the trapping term $D_{\nu_{\parallel}}$, damping coefficient of radial modes D_x , damping coefficient of toroidal modes D_y , order of the scheme used for the zonal mode, maximum poloidal wave vector $k_y\rho$, and maximum radial wave vector $k_x\rho$

3.2 btrzx1 Cluster

3.3 Restart Script for Simulation btrzx1 Cluster

Results and Discussion

4.1 Variation of Computational Resolution

At the beginning of this work the goal is to estimate the minimal resolution needed to run the simulation without fearing numerical dissipation. Numerical dissipation can therefore result to no formation of zonal flow stuctures, which cause an permanent turbulent state of the simulation. The goal behind this testing is to reduce **calculation time** and **costs** of the simulation.

Because of that, the criteria for the best resolution should be:

- (1) Subdued turbulence after **short** time periods
- (2) Stability for **long** time periods

and the following procedure will be applied for verification:

1. Reduce only one number of grid points and look if criterias (1), (2) are satisfied
2. Reduce to knowm minimum number of grid points to verify result in general.

4.1.1 Benchmark

Starting from the “Standard resolution with 6th order (S6)” [Tab. 3.1] the first step is to reproduce the result of Ref. 11 in Section IV. Note that, because of selected circular geometry the used gradient length is $R/L_T = 6.0$ instead of $R/L_T = 7.0$. In Fig. 4.1 the obtained data is similar to the results from Ref. 11 with subdued turbulence after $\sim 3000R/v_{\text{th}}$.

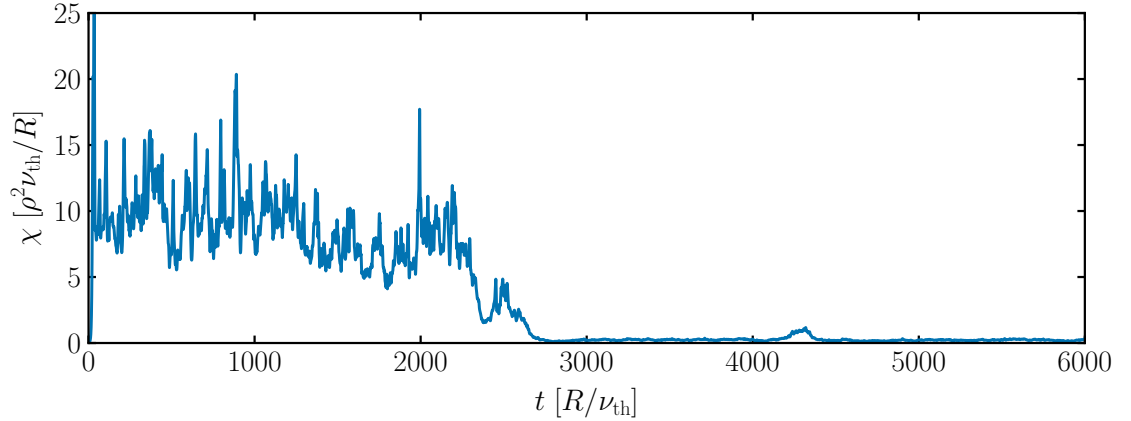


Figure 4.1: Time traces of the heat conduction coefficient χ for $R/L_T = 6.0$ for benchmark

As next step an approach to the finite heat flux threshold were made to verify the selection of the gradient length R/L_T . As in Ref. 11 in Section V conclude is the finite

heat flux threshold approximately located at a gradient length of $R/L_T = 6.3$ for circular geometry [FIG. 4 of Ref. 11]. Therefore following parameters were used:

$$R/L_T \in [6.0, 6.3] .$$

As seen in Fig. 4.2 for $R/L_T = 6.3$ no suppression of turbulence occur in the whole time domain, which is in agreement with Ref. 11.

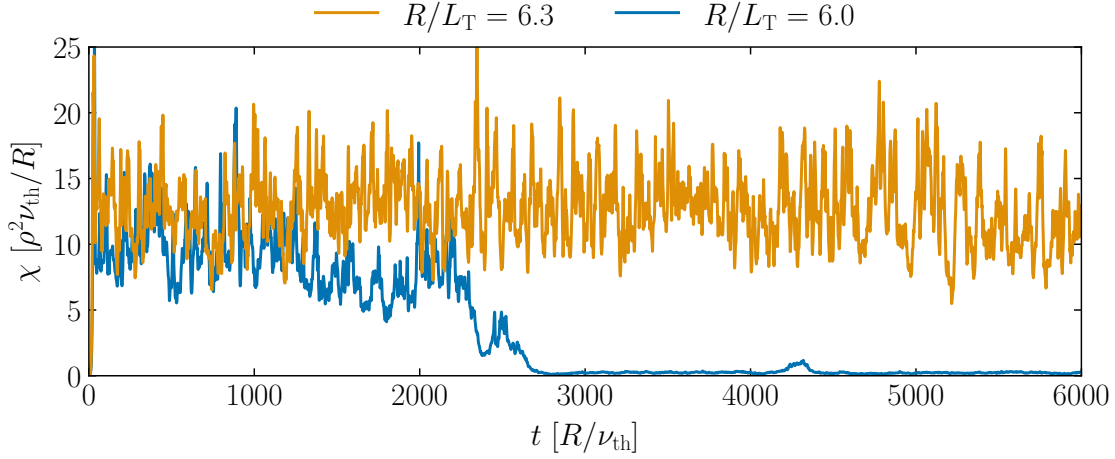


Figure 4.2: Time traces of the heat conduction coefficient χ for $R/L_T = 6.0$ and $R/L_T = 6.3$ for benchmark

4.1.2 Reduction of parallel velocity grid points $N_{\nu_{\parallel}}$

In the following the number of grid points for the parallel velocity $N_{\nu_{\parallel}}$ is reduced to:

$$N_{\nu_{\parallel}} \in [16, 32, 48, 64] .$$

In Fig. 4.3 is clearly visible that the resolution with $N_{\nu_{\parallel}} = 16$ is not suitable for criteria **(1)** because here the turbulence is not subdued after a long time period. But resolution $N_{\nu_{\parallel}} = 32$ is as well not acceptable according to criteria **(2)** since the suppressed turbulence state gain instability after $\sim 3000R/v_{th}$.

So to conclude only grid points with $N_{\nu_{\parallel}} = 48, 64$ are satisfying the set criteria. Due to criteria **(1)** the selected resolution will be:

$N_{\nu_{\parallel}} = 48$

With this number of grid points the time till turbulence subdued is halved compared to the benchmark case, i.e., turbulence suppression occur after $\sim 1500R/v_{th}$.

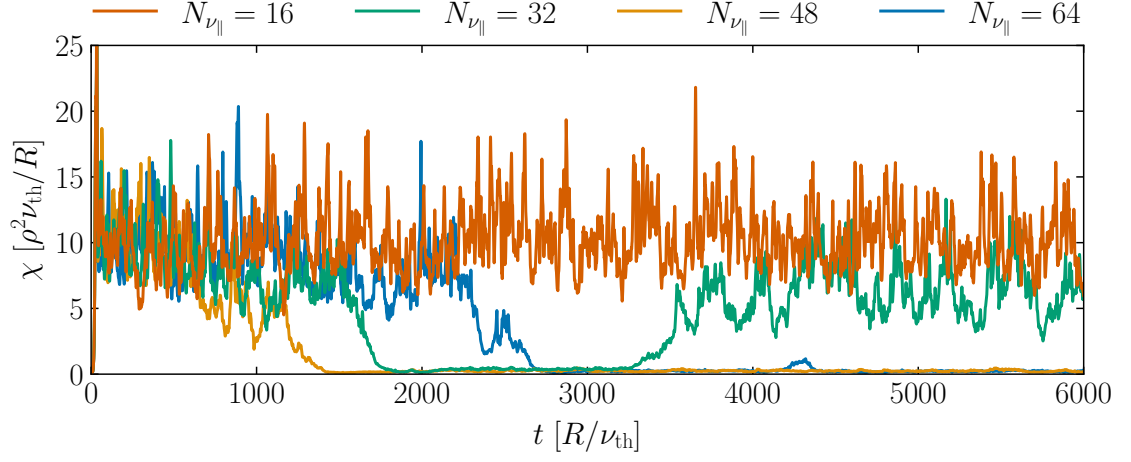


Figure 4.3: Time traces of the heat conduction coefficient χ for $R/L_T = 6.0$ for reduced parallel velocity grid points $N_{\nu_{\parallel}}$

4.1.3 Reduction of magnetic moment grid points N_{μ}

As next step the number of grid points for the magnetic moment N_{μ} were reduced with:

$$N_{\mu} \in [6, 9] .$$

As in Fig. 4.4 shown, the reduction of grid points for the magnetic moment does not significantly impact the suppression of turbulence. The turbulence enters the stationary state in both cases after $\sim 3000 R/\nu_{th}$.

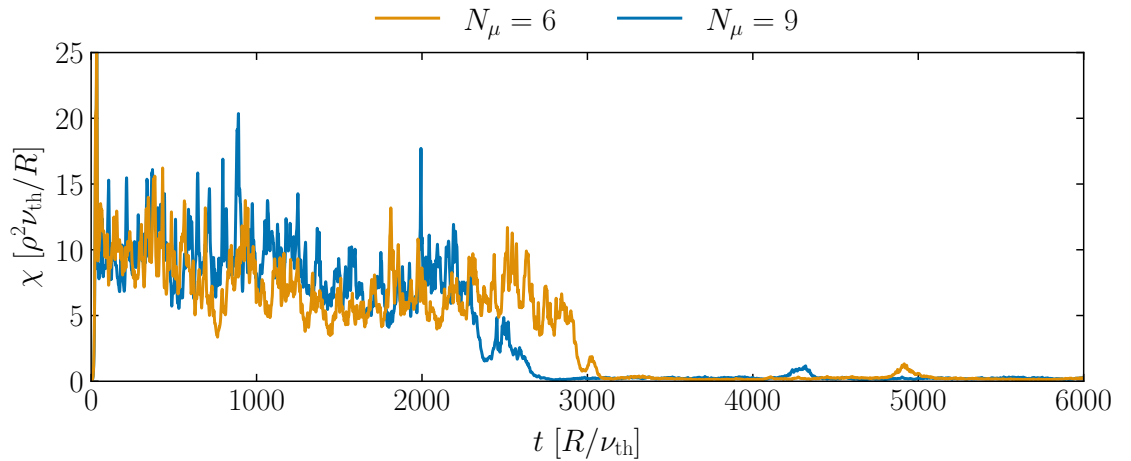


Figure 4.4: Time traces of the heat conduction coefficient χ for $R/L_T = 6.0$ for reduced magnetic moment grid points N_μ

To conclude a curial result the number of grids point for the parallel velocity got reduced to $N_{\nu_\parallel} = 48$ according to Chapter 4.1.2. In this case the turbulence does not subdue for the resolution $N_\mu = 6$ which leads, with the both criteria in mind, to the following resolution:

$$N_\mu = 9$$

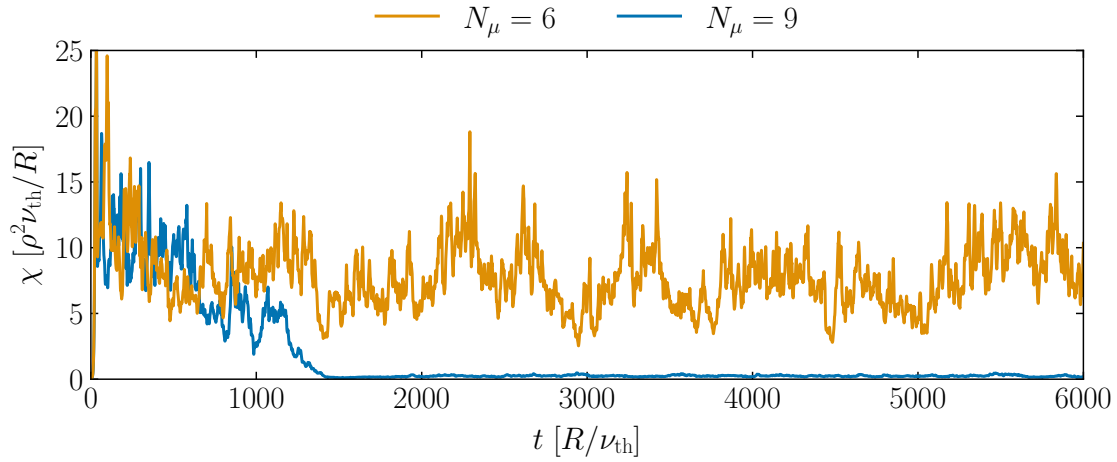


Figure 4.5: Time traces of the heat conduction coefficient χ for $R/L_T = 6.0$ and $N_{\nu_\parallel} = 48$ for reduced magnetic moment grid points N_μ

4.1.4 Reduction of magnetic field grid points N_s

In the final step the number of grid points for the magnetic field N_s get reduced with the following parameters:

$$N_s \in [12, 16] .$$

In Fig. 4.6 is clearly visible that the reduction to $N_s = 12$ does not satisfy the criteria (2) because the the stationary state of the turbulence gets instabil after $\sim 2500R/\nu_{th}$. This concludes to the following resolution:

$$N_s = 16$$

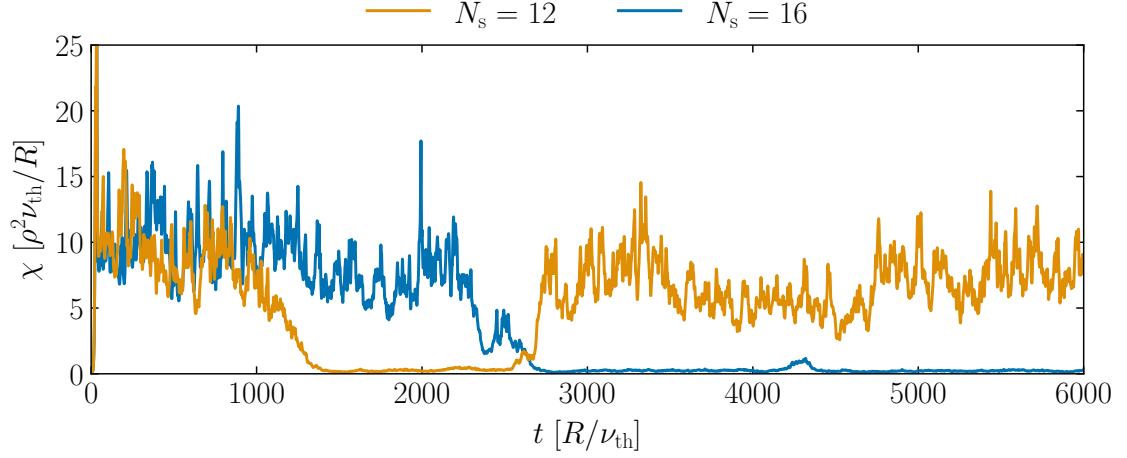


Figure 4.6: Time traces of the heat conduction coefficient χ for $R/L_T = 6.0$ for reduced magnetic field grid points N_s

4.1.5 Final Resolution for Simulation

Together with the results of Chapter 4.1.2, 4.1.3 and 4.1.4 the final resolution used in the upcoming simulations are displayed in Tab. 4.1 with reduced number of grid points for the parallel velocity $N_{\nu_{\parallel}}$.

	N_m	N_x	N_s	$N_{\nu_{\parallel}}$	N_{μ}	D	ν_d	$D_{\nu_{\parallel}}$	D_x	D_y	Order	$k_y\rho$	$k_x\rho$
S6	21	83	16	48	9	1	$ \nu_{\parallel} $	0.2	0.1	0.1	6	1.4	2.1

Table 4.1: Resolution used in this paper: Number of toroidal modes N_m , number of radial modes N_x , number of grid points along the magnetic field N_s , number of parallel velocity grid points $N_{\nu_{\parallel}}$, number of magnetic moment grid points N_{μ} , dissipation coefficient used in convection along the magnetic field D , the velocity in the dissipation scheme ν_d , dissipation coefficient used in the trapping term $D_{\nu_{\parallel}}$, damping coefficient of radial modes D_x , damping coefficient of toroidal modes D_y , order of the scheme used for the zonal mode, maximum poloidal wave vector $k_y\rho$, and maximum radial wave vector $k_x\rho$

4.2 Size Convergence of $E \times B$ staircase pattern

This chapter is a further iteration of the brief communication published in “Physics of Plasma”. It provides additional plots and paragraphs that were not necessary for the publication. the format was changed as well because the publication was written in REVTeX 4.1 and this bachelor thesis in `scrcpr`. The brief communication can be found in the appendix of this thesis or under **REF PAPER GITHUB**.

4.2.1 Radial increased Box Size

In the first test the radial box size is increased while the binormal box size is kept fixed to the standard size. The scan covers the realizations:

$$N_R \times N_B \in [1 \times 1, 2 \times 1, 3 \times 1, 4 \times 1] .$$

Each realization exhibits an initial quasi-stationary turbulent phase and a second final¹¹ phase with almost suppressed turbulence [Fig. 4.7 (a)]. The latter state is indicative for the presence of a fully developed staircase pattern as depicted in Fig. 4.10. This type of structure is characterized by intervals of almost constant shear with alternating sign satisfying the Waltz criterion $|\omega_{E \times B}| \approx \gamma^{18,17}$ (γ is the growth rate of the most unstable linear ITG driven Eigenmode), connected by steep flanks where $\omega_{E \times B}$ crosses zero. Fig. 4.10 (a) shows a striking repetition of the staircase structure, with the number of repetitions equal to N_R . Hence, the basic size of the pattern not only converges with increasing radial box size, the converged radial size turns out to at least roughly agree with the standard radial box size of Ref. 11.

Due to the lack of a substantial turbulent drive in the final suppressed state no further zonal flow evolution is observed [Fig. 4.7 (b)] and one might critically ask whether the structures shown in Fig. 4.10 represent the real converged pattern in a statistical sense. Note that in the 3×1 case the initial quasi-stationary turbulent state extends up to a few $\sim 10^4 R/v_{th}$. During this period the zonal flow mode with $n_{ZF} = 3$, i.e., the mode that dominates the staircase pattern in final suppressed phase, undergoes a long-term evolution with a typical time scale of several $\sim 10^3 R/v_{th}$.

Hence, several of such cycles are covered by the initial turbulent phase, which is evident from the occurrence of phases with reduced amplitude around $t \approx 8000 R/v_{th}$ and $t \approx 18000 R/v_{th}$. It is the $n_{ZF} = 4$ zonal flow mode, i.e., the next shorter radial scale mode, that dominates the shear spectrum $|\hat{\omega}_{E \times B}|_{n_{ZF}}$ in the latter two phases (not shown). This demonstrates a competition between the $n_{ZF} = 3$ and $n_{ZF} = 4$ modes. Most importantly, no secular growth of the $n_{ZF} = 1$ (box scale) zonal flow mode is observed during the entire quasi-stationary turbulent phase [Fig. 4.7 (b) dotted line]. The above discussion indicates that although the $n_{ZF} = 3, 4$ zonal modes compete, the pattern scale

does not converge to the radial box scale but rather to a mesoscale of $\sim 57.20 - 76.27 \rho$ (i.e., $n_{\text{ZF}} = 4, 3$ in the 3×1 case).

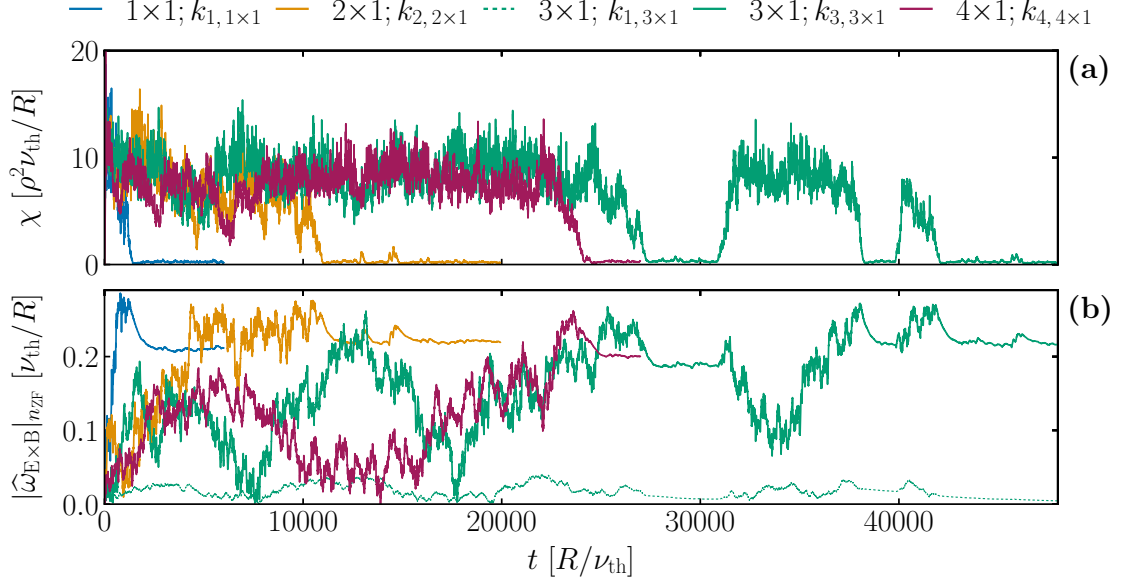


Figure 4.7: **(a)** Time traces of the heat conduction coefficient χ for $R/L_T = 6.0$ for radial increased box sizes
(b) Time traces of $|\hat{\omega}_{\text{E} \times \text{B}}|_{n_{\text{ZF}}}$ for radial increased box sizes

4.2.2 Isotropic increased Box Size

Since the radially elongated simulation domain might inhibit the development of isotropic turbulent structures, in the second test the radial and binormal box size is increased simultaneously. This scan covers the realizations:

$$N_R \times N_B \in [1 \times 1, 2 \times 2, 3 \times 3] .$$

Interestingly, suppression of the turbulence by the emergence of a fully developed staircase pattern always occurs after $\sim 1000 R/\nu_{th}$ [Fig. 4.8 (a)], i.e., significantly faster compared to the 3×1 and 4×1 realizations. As shown in Fig. 4.10 (b) also this test confirms the convergence of the staircase pattern size to a typical mesoscale that is distinct from the radial box size in the $N_R > 1$ realizations.

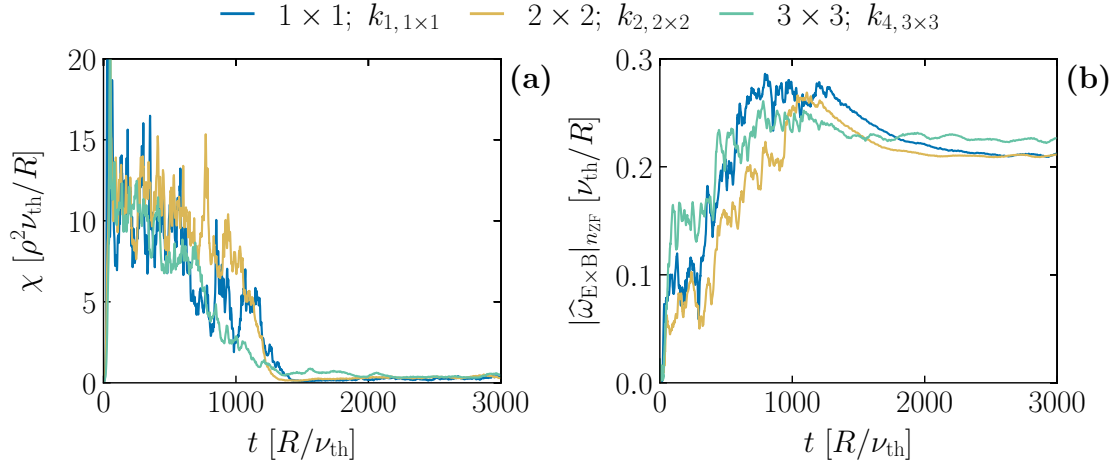


Figure 4.8: **(a)** Time traces of the heat conduction coefficient χ for $R/L_T = 6.0$ for isotropic increased box sizes
(b) Time traces of $|\hat{\omega}_{E \times B}|_{n_{ZF}}$ for isotropic increased box sizes

By contrast to the radial box size scan the 3×3 realization shows a stationary pattern with four repetitions of the fully developed staircase structure, i.e., a somewhat smaller pattern size [Fig. 4.8 (b), Fig. 4.10 (b)]. Whether this is related to a possible pattern size dependence on the binormal box size or to the competition between patterns with the two sizes $\lambda \in [57.20, 76.27] \rho$ as observed in the first test is addressed in the next paragraph.

4.2.3 Binormal increased Box Size

In a third test the binormal box size is varied with the radial box size fixed to $N_R = 3$. This test covers the realizations:

$$N_R \times N_B \in [3 \times 1.5, 3 \times 2.5, 3 \times 3, 3 \times 5] .$$

As in the isotropic scan the turbulence subdued and a fully developed staircase pattern forms after $\sim 2000 R/\nu_{th}$ [Fig. 4.9 (a)]. The convergence of staircase pattern can be seen in Fig. 4.10 (c) and confirms again a size of a typical mesoscale. Fig. 4.10 (c) also confirms that indeed a competition between patterns with two sizes $\lambda \in [57.20, 76.27] \rho$ causing the different results for 3×1 and 3×3 . The zonal flow mode number varies between $n_{ZF} = 3, 4$ which can be seen in Fig. 4.10 (c) in the 3×2.5 realization. The staircase structure has a pattern between 3 and 4 repetitions which get represented in the second repetition with no significant plateau at positive shear. Instead the pattern returns immediately after reaching the maximum shear ($+\gamma$) to the minimum shear ($-\gamma$) of the third repetition in a steep flank. The Fourier analysis of this case yields no definitely basic mode rather two dominating modes with $n_{ZF} = 3, 4$ with a fraction of the maximum amplitude $|\hat{\omega}_{E \times B}|_{n_{ZF}}$ each [Fig. 4.9 (b)].

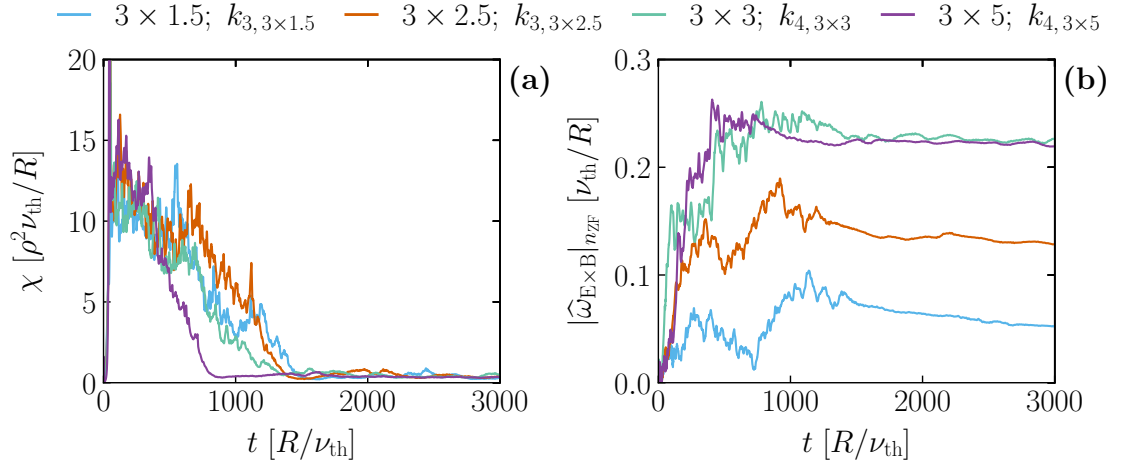


Figure 4.9: (a) Time traces of the heat conduction coefficient χ for $R/L_T = 6.0$ for binormal increased box sizes
 (b) Time traces of $|\hat{\omega}_{E \times B}|_{n_{ZF}}$ for binormal increased box sizes

4.2.4 Staircase structures in Comparison

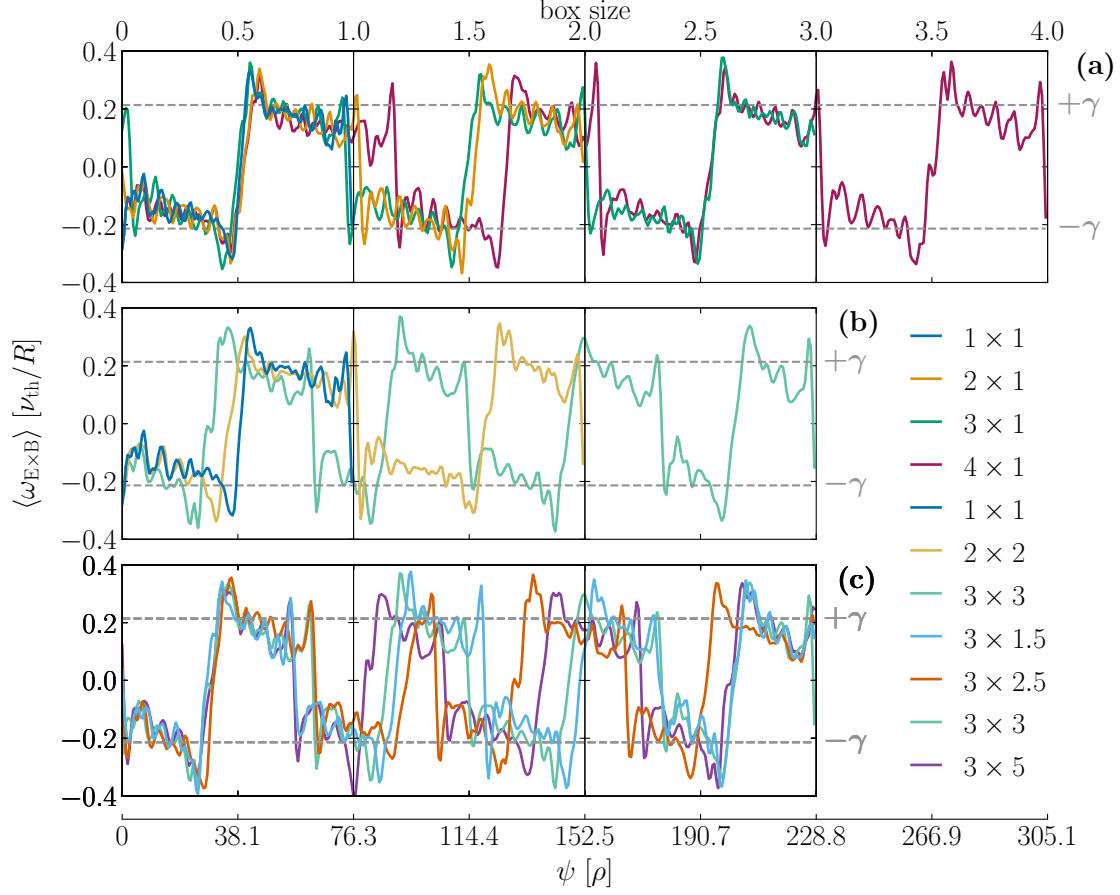


Figure 4.10: Comparison of shearing rate $\omega_{E \times B}$ for each box sizes scan averaged over given time interval and the growth rate $\pm\gamma$ of the most unstable linear ITG driven Eigenmode. The staircase structures are radially shifted with respect to each other till alignment for better visibility.

(a) radial:	$t_{1 \times 1}$	$\in [2000, 5000]$,	$t_{2 \times 1}$	$\in [15000, 18000]$,
	$t_{3 \times 1}$	$\in [43000, 45000]$,	$t_{4 \times 1}$	$\in [26000, 28000]$
(b) isotropic:	$t_{1 \times 1}$	$\in [2000, 5000]$,	$t_{2 \times 2}$	$\in [2000, 3000]$,
	$t_{3 \times 3}$	$\in [2000, 3000]$		
(c) binormal:	$t_{3 \times 1.5}$	$\in [2000, 3000]$,	$t_{3 \times 2.5}$	$\in [2000, 3000]$,
	$t_{3 \times 3}$	$\in [2000, 3000]$	$t_{3 \times 5}$	$\in [1000, 3000]$

4.3 The finite heat flux threshold

In the final test the inverse background temperature gradient length R/L_T is varied at fixed 3×3 box size. Since suppression of turbulence usually occurs at later times when approaching the finite heat flux threshold from below¹¹, the analysis aims to lengthen the phase during which the zonal flow varies in time due to turbulent Reynolds stresses. This scan covers realizations with:

$$R/L_T \in [6.0, 6.2, 6.4] .$$

In the case of $R/L_T = 6.2$ turbulence suppression is observed for $t > 11000 R/\nu_{\text{th}}$, while stationary turbulence during the entire simulation time trace of $12000 R/\nu_{\text{th}}$ is found for $R/L_T = 6.4$ [Fig. 4.11]. The finite heat flux threshold, hence, is:

$$R/L_T|_{\text{finite}} = 6.3 \pm 0.1$$

in accordance to Ref. 11. Although the initial quasi-stationary turbulence in the former case is significantly longer compared to the $R/L_T = 6.2$ realization discussed in the second test, a stationary pattern with basic zonal flow mode $n_{\text{ZF}} = 3$ establishes. Again, the $n_{\text{ZF}} = 1$ (box scale) zonal flow mode does not grow secularly during the entire turbulent phase. Also, this test confirms the statistical soundness of the converged pattern size of $\sim 57.20 - 76.27 \rho$.

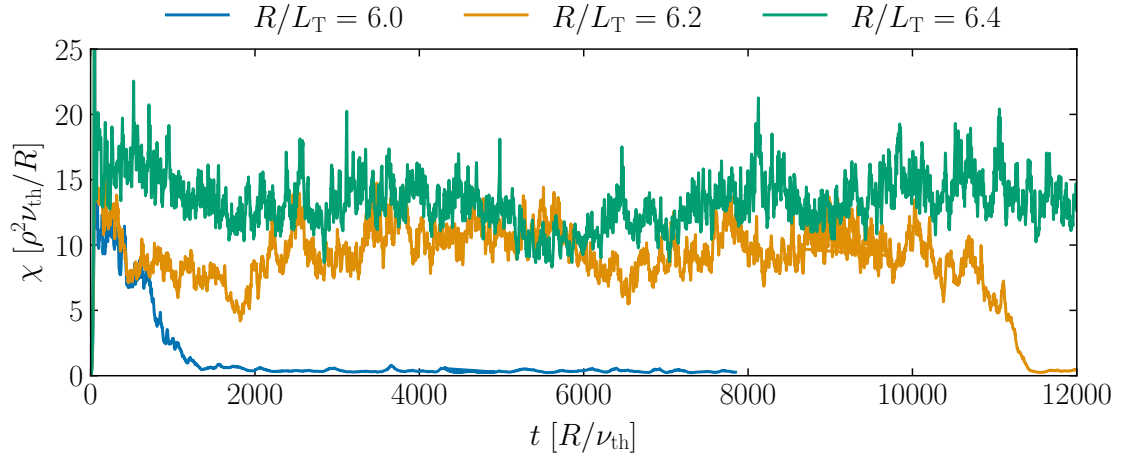


Figure 4.11: Time traces of the heat conduction coefficient χ for different gradient lengths R/L_T

Closure

Through careful tests this brief communication confirms the radial size convergence of the $\mathbf{E} \times \mathbf{B}$ staircase pattern in local gyrokinetic flux tube simulations of ion temperature gradient (ITG) driven turbulence. A mesoscale pattern size of $\sim 57.20 - 76.27 \rho$ is found to be intrinsic to ITG driven turbulence for Cyclone Base Case parameters. This length scale is somewhat larger compared to results from global studies with finite ρ_* , which report of a few $10 \rho^3$, and has to be considered the proper mesoscale in the local limit $\rho_* \rightarrow 0$. The occurrence of this mesoscale implies that non-locality, in terms of Ref. ³, is inherent to ITG driven turbulence, since avalanches are spatially organized by the $\mathbf{E} \times \mathbf{B}$ staircase pattern^{9,3,13,11}.

Append A

6.1 Append A

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