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Effects of $E \times B$ velocity shear and magnetic shear on turbulence and transport in magnetic confinement devices*

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One of the scientific success stories of fusion research over the past decade is the development of the $E \times B$ shear stabilization model to explain the formation of transport barriers in magnetic confinement devices. This model was originally developed to explain the transport barrier formed at the plasma edge in tokamaks after the L (low) to H (high) transition. This concept has the universality needed to explain the edge transport barriers seen in limiter and divertor tokamaks, stellarators, and mirror machines. More recently, this model has been applied to explain the further confinement improvement from H (high) mode to VH (very high) mode seen in some tokamaks, where the edge transport barrier becomes wider. Most recently, this paradigm has been applied to the core transport barriers formed in plasmas with negative or low magnetic shear in the plasma core. These examples of confinement improvement are of considerable physical interest; it is not often that a system self-organizes to a higher energy state with reduced turbulence and transport when an additional source of free energy is applied to it. The transport decrease that is associated with $E \times B$ velocity shear effects also has significant practical consequences for fusion research. The fundamental physics involved in transport reduction is the effect of $E \times B$ shear on the growth, radial extent, and phase correlation of turbulent eddies in the plasma. The same fundamental transport reduction process can be operational in various portions of the plasma because there are a number of ways to change the radial electric field E_r . An important theme in this area is the synergistic effect of $E \times B$ velocity shear and magnetic shear. Although the $E \times B$ velocity shear appears to have an effect on broader classes of microturbulence, magnetic shear can mitigate some potentially harmful effects of $E \times B$ velocity shear and facilitate turbulence stabilization. Considerable experimental work has been done to test this picture of $E \times B$ velocity shear effects on turbulence; the experimental results are generally consistent with the basic theoretical models. © 1997 American Institute of Physics. [S1070-664X(97)93605-3]

I. INTRODUCTION

One of the scientific success stories of fusion research over the past decade is the development of the $E \times B$ velocity shear model to explain the formation of transport barriers in magnetic confinement devices. This model was originally developed to explain the transport barrier formed at the plasma edge in tokamaks after the L (low) to H (high) transition. As has been discussed previously,1 this concept has the universality needed to explain the edge transport barriers seen in limiter and divertor tokamaks, stellarators, and mirror machines. More recently, this model has been applied to explain the further confinement improvement from H (high) mode to VH (very high) mode seen in some tokamaks, 2-4 where the edge transport barrier becomes wider. Most recently, this paradigm has been applied to the core transport barriers formed in plasmas with negative or low magnetic shear in the plasma core. 1,5-8

These examples of confinement improvement are of considerable physical interest; it is not often that a system self-organizes to a higher energy state with reduced turbulence

and transport when an additional source of free energy is applied to it. In addition to its intrinsic physics interest, the transport decrease that is associated with $E \times B$ velocity shear effects has significant practical consequences for fusion research. For example, the best fusion performance to date in the DIII-D9 and JT-60U10 tokamaks has been obtained under conditions where transport reduction through $E \times B$ velocity shear decorrelation of turbulence is almost certainly taking place. 11,12 The performance of these discharges represents a revolutionary step forward in the control of plasma turbulence and transport. In the DIII-D case, for example, the ion thermal transport is at the minimum level set by interparticle collisions over the whole discharge. ¹¹ In other words, at least in the ion channel, it appears that anomalous transport is much smaller than collision-induced transport.

The fundamental physics involved in transport reduction is the effect of $E \times B$ velocity shear on the growth of and radial extent of turbulent eddies in the plasma. Both nonlinear decorrelation^{13–17} and linear stabilization^{18–23} effects have been considered. The basic nonlinear effect is the reduction in radial transport owing to a decrease in the radial correlation length and the change in the phase between den-

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sity, temperature, and potential fluctuations. There are a multitude of linear effects specific to various modes; however, one general feature of linear stabilization is coupling to more stable modes caused by the $E \times B$ velocity shear.

The same fundamental transport reduction process can be operational in various portions of the plasma because there are a number ways to change the radial electric field E_r . The radial force balance equation

$$E_r = (Z_i e n_i)^{-1} \nabla P_i - v_{\theta i} B_{\phi} + v_{\phi i} B_{\theta}, \qquad (1)$$

indicates that there is a connection between E_r and the cross field heat and particle transport (∇P_i) , cross field angular momentum transport $(v_{\varphi i})$, and poloidal flow $(v_{\theta i})$. Since sheared $E \times B$ flow also affects turbulence and transport, there are several feedback loops whereby E_r and its shear can change, allowing the plasma access to different confinement regimes. For example, both $v_{\theta i}$ and ∇P_i are important in the H-mode edge¹ while $v_{\varphi i}$ appears to play the major role in the VH mode. He had both $v_{\varphi i}$ (Ref. 6) and ∇P_i (Ref. 7) appear to play a role in the core transport barriers. This multiplicity of feedback loops ultimately provides a number of possibilities for active control of transport. Neutral beam injection, for example, has been used to alter $v_{\varphi i}$ (Refs. 2–7) while ion Bernstein wave input may have produced effects consistent with a change in $v_{\theta i}$.

One of the important themes in this area is the synergistic effects of $E \times B$ velocity shear and magnetic shear. Although the $E \times B$ velocity shear appears to have an effect on broader classes of microturbulence, magnetic shear can mitigate some potentially harmful effects of $E \times B$ velocity shear and facilitate turbulence stabilization. For example, there are many similarities in velocity shear effects in magnetized

plasmas and neutral fluids;²⁵ however, in neutral fluids, the increased turbulent drive owing to the free energy provided by the velocity shear usually overcomes the stabilizing effects of reduced radial correlation length to drive Kelvin–Helmholtz instabilities. In a plasma with magnetic shear, both in the ideal case²⁶ and the resistive case,¹⁴ Kelvin–Helmholtz modes are rendered ineffectual. As a second example, in the case of core transport barriers, the magnetic shear effects play a role by linearly stabilizing several modes (e.g., sawteeth and ideal ballooning modes) while reducing the growth rates of others,^{11,27,28} thus allowing the core gradients to steepen. A transport bifurcation, similar to those previously discussed,^{29,30} results and the core transport barrier forms.^{27–30}

Considerable experimental work has been done to test this picture of $E \times B$ velocity shear effects on turbulence. As will be discussed in detail in this paper, the experimental results are consistent with the basic theoretical models. The $E \times B$ velocity shear model has the universality needed to explain: (1) H-mode edge confinement improvement seen in limiter and divertor tokamaks, stellarators, torsatrons, and mirror machines produced with a variety of heating and plasma biasing schemes; (2) the confinement improvement in the outer-half of the plasma seen in VH-mode and high internal inductance discharges³¹ and (3) the formation of core transport barriers in a number of tokamaks. In addition, there is both qualitative and quantitative agreement between theory and the experimental results. Finally, in the last several years, there have been several rigorous tests of causality; the experimental results are consistent with $E \times B$ velocity

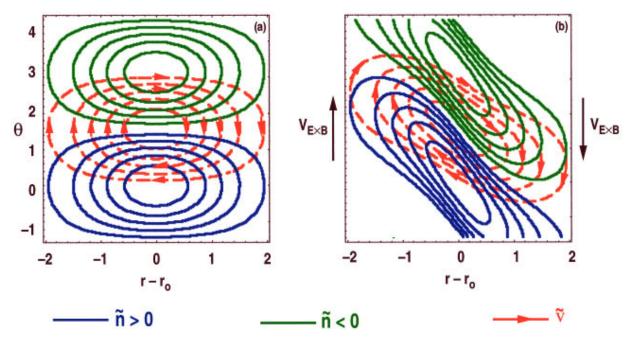


FIG. 1. Results of a simple model of turbulence which treats density as a passive scalar, convected by the eddy velocity field. The calculation is done in a cylindrical (r, θ) geometry. In (a) there is no shear in the average velocity while in (b) an average velocity with a linear gradient is imposed on the system. The sheared average flow distorts the turbulent eddies and leads to decorrelation between the density and velocity perturbations. This decorrelation is manifested in the sheared case in the difference in the angle that the major axes of the density and velocity ellipses make with each other and by the twisting in the density ellipses as one moves away from the density maximum or minimum.

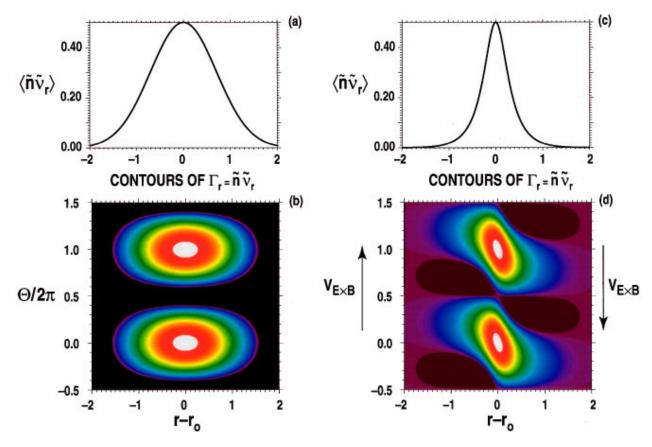


FIG. 2. The radial particle flux n V_r for the model shown in Fig. 1. The (a) and (b) plots are for no shear in the average velocity while (c) and (d) are for the sheared case. The (b) and (d) plots are color coded contours of the radial flux in the (r, θ) plane while the (a) and (c) plots are the radial flux averaged over the theta coordinate. The distortion of the eddies in (d) compared to (b) shows the effect of velocity shear on the radial flux. In addition, at points away from the maximum, the radial flux decreases strongly in the sheared case. The net radial flux [the integral under the curves in (a) and (c)] decreases significantly owing to the velocity shear.

shear causing the reduction in turbulence and transport in both the plasma edge and the core.

The goal of this paper is to give a summary of the theoretical picture of $E \times B$ velocity shear decorrelation and suppression of turbulence and then to review experimental results which provide tests of this model. The theory is reviewed in Sec. II while the experimental results are considered in the remaining sections.

II. THEORY

A. Basic theoretical model

There are two themes which wind through the theory of $E \times B$ velocity shear effects on turbulence. The first is (nonlinear) decorrelation of turbulence, leading to a reduction in transport ^{13–17} even though the underlying turbulence is not completely suppressed. The second is (linear) stabilization of modes leading to transport reduction through complete stabilization. Examples of the latter effect are given in Refs. 18–23.

An illustration of turbulence decorrelation is given in Figs. 1 and 2. In this simple model,³² density is treated as a passive scalar, affected by the velocity field of turbulent eddies. As is illustrated in Fig. 1, with no velocity shear, the eddies coupled with a linear background density profile produce hills and valleys in the density spatial distribution. As is

shown in Fig. 2, the correlation between the density and velocity perturbations then leads to radial transport. When a shear in the average velocity is added to the problem, the eddies are distorted and, as is shown in Fig. 2, radial transport is reduced. This reduction is due both to changes in the phase relationship between the density and velocity perturbations and to decreases in the amplitude of the turbulent fluctuations.

The simple model shown in Figs. 1 and 2 is highly idealized. However, it retains the important features first discussed in the analytic models¹⁴ and that are also seen in much more elaborate numerical calculations. ^{22,33–35} The ability of $E \times B$ velocity shear to affect even nonlinearly saturated turbulence is important in the overall picture, since it provides a mechanism whereby the plasma can start in a highly turbulent, poor confinement state and move to an improved confinement state with reduced turbulence.

The linear stability effects of $E \times B$ velocity shear are more difficult to discuss in general, since much of the physics is mode specific. ^{18–23} However, there is one general effect that appears to persist across a number of different modes. The presence of $E \times B$ velocity shear results in enhanced damping by coupling the unstable modes to other, nearby, stable modes, thus improving the overall stability of the system. Often, this coupling leads to increased Landau damping of the modes. ^{20,22} Magnetic shear is often helpful in

this process; however, complete $E \times B$ velocity shear stabilization is possible even in the absence of magnetic shear.¹⁸

B. Frequently asked questions

There are several key questions about $E \times B$ velocity shear effects which cause confusion. The first of these concerns the central role that $E \times B$ velocity shear is assigned in the theory. In general, one might think that shear in any component of any species' velocity could be significant. The central role of $E \times B$ velocity shear can be looked at in two ways. The formal mathematical answer has been provided by Kim *et al.*³⁶ through a careful, general toroidal geometry derivation of the equations governing electrostatic, flute-like modes. This work clearly shows that, for such modes, the only convective term in the equations is the $E \times B$ drift. Accordingly, the $E \times B$ velocity acquires a special place in the theory. What measurements there are in tokamaks ^{37,38} indicate that fluctuations are indeed flute-like, although these measurements were made near the plasma edge.

There is another way to understand why $E \times B$ shear is fundamental. For any particular mode in the plasma, the actual phase and group velocities of the turbulence can be complicated functions of the plasma parameters. However, all particles move with the $E \times B$ velocity, regardless of their charge or mass. Accordingly, the $E \times B$ velocity contributes to all modes. Consequently, any mode that can be affected by sheared velocity will be affected by sheared $E \times B$ velocity provided the $E \times B$ velocity shear is sufficiently large. In this sense, $E \times B$ velocity shear provides a universal mechanism for affecting turbulence.

A second confusing point has to do with the difference between the poloidal rotation of the various ions in the plasma and the $E \times B$ flow velocity. This confusion comes about partially because the initial theories of velocity shear effects on the H mode were done in cylindrical geometry^{14,15} for a plasma with one ion species. For this case, there is little distinction between the fluid velocity perpendicular to **B** and the $E \times B$ velocity. In addition, this confusion may partially have resulted from the initial H-mode observations of changes in the radial electric field E_r across the L to H transition which were based on observations of changes in the poloidal flow of impurity ions.^{39,40} However this confusion came about, as is shown in Fig. 3, the $E \times B$ drift speed is very different from the poloidal rotation speed of the main ions and the poloidal rotation speed of the most significant impurity ion. 41 The main ion and impurity poloidal rotation speeds do not even have the same sign. Furthermore, the shear in the three different speeds are also clearly different. Accordingly, since the theory speaks in terms of shear in the $E \times B$ velocity, one really cannot substitute the ion poloidal rotation speed for this.

The final frequently asked question has to do with the velocity shear itself driving turbulence. Although there are several instances in neutral fluids of velocity shear reducing transport, ^{25,42–44} in neutral fluid dynamics one usually thinks of sheared velocity as a source of free energy which can drive turbulence through Kelvin–Helmholtz instabilities. ⁴⁵ Fortunately, in a plasma, magnetic shear is capable of rendering Kelvin–Helmholtz modes ineffectual. One can think

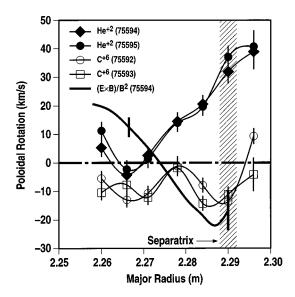


FIG. 3. The poloidal rotation speed of the main plasma ion (He⁺²), the most significant impurity ion (C⁺⁶), and the $E \times B$ drift speed in the edge of a H-mode plasma in DIII-D showing the significant difference in the three speeds. Data are from Ref. 41. Plasma conditions are 1.0 MA plasma current, 2.0 T toroidal field, 6.7 MW injected deuterium neutral beam power, and 2.2×10^{19} m⁻³ line averaged density. Discharge is a single-null divertor with the ∇B drift towards the X-point.

of this problem in analogy to other plasma instabilities (e.g., ballooning modes or drift waves) as having possibilities for both ideal and resistive instabilities. For the ideal case, 26 the stability criterion can be stated as $(\nabla E_r/B) < (V_A/L_s)$, where B is the magnitude of the magnetic field, V_A is the Alfvén speed, and L_s is the magnetic shear length. The physical basis for the stabilization is that shear in the magnetic field prevents coupling of the various modes across the velocity gradient so that they are unable to extract energy from the $E \times B$ velocity shear and grow. The steepest gradients in E_r are observed at the edge of H-mode plasma; however, even there the $\nabla E_r/B$ is insufficient for ideal instability for typical parameters. If finite resistivity η is assumed, then the modes can slip past the magnetic field and still extract energy from the velocity shear. However, the presence of $E \times B$ velocity shear also acts as a decorrelation mechanism. Accordingly, the criterion for preventing significant Kelvin-Helmholtz instability is 14

$$\frac{\nabla E_r}{E_r} < \left(\frac{1}{\eta \Delta \omega_D}\right)^{1/4} (V_A k_y / L_s c)^{1/2},$$

where $\Delta \omega_D$ is the turbulence decorrelation rate and k_y is the poloidal wave number of the turbulent mode. Again, this criterion would be most easily violated at the plasma edge in H mode, where ∇E_r and η are the largest. Using typical H-mode tokamak edge parameters shows that there is no significant instability.

C. General geometry and decorrelation and stabilization criteria

Early theory on $E \times B$ shear stabilization of turbulence was done in cylindrical geometry. ^{14,15} Recently, in order to deal with the true geometry of tokamaks, the two-point

analysis has been extended to general tokamak flux surface geometry, 46 yielding an expression for the $E \times B$ shearing rate for flute-like modes

$$\omega_{E\times B} = \frac{\Delta\psi_0}{\Delta\phi} \left(\frac{\partial}{\partial\psi}\right) \frac{E_r}{RB_{\theta}},\tag{2}$$

where $L_r = \Delta \psi_0 / RB_\theta$ is the radial correlation length, $R\Delta \varphi$ is the toroidal correlation length of the ambient turbulence, R is the major radius, and B_θ is the poloidal magnetic field. For flute-like modes, the poloidal correlation length is $L_\theta = RB_\theta \Delta \phi / B_\phi$ while the correlation length perpendicular to the field line but in the flux surface is $L_\perp = RB_\theta \Delta \phi / B$; here, B_ϕ is the toroidal magnetic field and B is the magnitude of the magnetic field. In many cases, measurements of L_r and L_\perp are not available. Motivated by numerical simulations which show $L_\perp \cong L_r$, 33,47,48 the assumption $L_\perp = L_r$ can be used to reduce Eq. (2) to

$$\omega_{E\times B} = \frac{(RB_{\theta})^2}{B} \left(\frac{\partial}{\partial \psi}\right) \frac{E_r}{RB_{\theta}}.$$
 (3)

There is also experimental evidence that L_{\perp} and L_{r} are nearly equal. ⁴⁹ The $E \times B$ shearing rate actually enters into the various theories quadratically; ^{14,46} accordingly, the sign of $\omega_{E \times B}$ is irrelevant. Indeed, H-mode edge barriers have been seen with both signs of E_{r} and its derivative. ¹

The functional forms in Eqs. (2) and (3) have several interesting features. The combination E_r/RB_θ in the formula shows that both electric field and magnetic field shear are contributing to the final result. Second, under the usual neoclassical assumptions, E_r/RB_θ is constant on a flux surface because the lowest order electrostatic potential is a flux function. However, since $(RB_{\theta})^2/B$ varies on a flux surface, so does $\omega_{E\times B}$. Third, E_r/RB_θ is the toroidal angular speed due to the equilibrium flow driven by E_r in standard neoclassical theory. This suggests, and the basic equations confirm, 46 that the basic shearing is in the toroidal direction for flute-like modes in toroidal geometry. Finally, the form in Eq. (3) agrees with the results of previous, large aspect ratio derivations 18,50,51 in that limit, although some diamagnetic drift terms must be neglected to produce exact agreement with Refs. 18 and 50.

As is illustrated in Fig. 4, the differences between the shear in E_r/B and in E_r/RB_{θ} has great practical significance. As is shown there, E_r has a local maximum around ρ =0.5 in this particular plasma, indicating that the shear in E_r/B would vanish near that point. E_r/RB_{θ} , on the other hand, has its maximum on the magnetic axis and has a significant derivative throughout the plasma, as is illustrated by the plot of $\omega_{E\times B}$. Indeed, this particular plasma shows confinement improvement across the whole minor radius.⁶

For $E \times B$ shear decorrelation of turbulence, $\omega_{E \times B}$ must be comparable to $\Delta \omega_D$, the nonlinear turbulence decorrelation rate in the absence of $E \times B$ shear. Although $\Delta \omega_D$ can be calculated for some cases, 22,35 it is not routinely available for comparison with experiment. Recent nonlinear gyro-Landau fluid simulations have also shown complete turbulence stabilization when $\omega_{E \times B}$ is comparable to γ_{MAX} , the maximum linear growth rate of all the unstable modes in the plasma. This rule $\omega_{E \times B} = \gamma_{MAX}$ has thus been used in

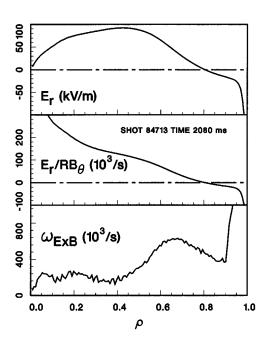


FIG. 4. Plot of radial electric field E_r , toroidal angular speed E_r/RB_θ , and the $E\times B$ shearing rate defined in Eq. (3) as a function of flux surface label ρ for a high performance, deuterium VH-mode plasma in DIII-D. Here, ρ is proportional to the square root of the toroidal flux inside a given flux surface. Although the derivative of E_r vanishes near ρ =0.5, the $E\times B$ shearing rate is appreciable across the whole plasma. Plasma conditions are 1.2 MA plasma current, 1.6 T toroidal field, 9.8 MW injected deuterium neutral beam power, and $4.7\times 10^{19}~{\rm m}^{-3}$ line averaged density. Discharge is a double-null divertor.

several comparisons between theory and experiment^{6,7} and will be used later in this paper. It should be noted, however, that even the original numerical calculations on which this rule is based¹⁸ showed up to factors of 2.5 deviation from this rule for turbulence stabilization. In other words, in some cases it took an $\omega_{E\times B}$ a factor of 2 smaller than γ_{MAX} for complete stabilization while in other cases $\omega_{E\times B}$ had to exceed γ_{MAX} by a factor of 2.5. Accordingly, this rule can only be taken as a rough rule of thumb. Equation (3) shows that $\omega_{E\times B}$ is not constant on a magnetic surface. Accordingly, there is a question of where to make the comparisons between $\omega_{E\times B}$ and γ_{MAX} . The stability codes used to evaluate $\gamma_{\rm MAX}$ (Refs. 52–55) typically find the fastest growing modes along the low toroidal field side of a given flux surface. The $\omega_{E\times R}$ quoted in comparisons in this paper, unless otherwise noted, is evaluated at that point on the flux surfaces.

Finally, in comparing $\omega_{E\times B}$ to $\Delta\omega_D$ or γ_{MAX} , we end up confronting the relative roles of a large number of plasma parameters. For example, for trapped electron modes and/or ion temperature gradient driven modes, γ_{MAX} depends at least on magnetic shear, ion to electron temperature ratio T_i/T_e , impurity concentration in the plasma, and the Shafranov shift of the magnetic axis. Accordingly, in a given situation, all of these can influence how much $E\times B$ velocity shear is needed to affect the turbulence. In that sense, any quantity which significantly affects the $\Delta\omega_D$ or γ_{MAX} can be important in the physics. On the other hand, there is evidence, presented in Sec. IV, that it is the $E\times B$ velocity shear that is the important feature in producing the reduced trans-

port, since there are many cases where γ_{MAX} is observed to increase in the region where transport and fluctuations are reduced.

D. Curvature effects

Much of the theoretical work on $E \times B$ shear stabilization effects only considers the effect of the first derivative of the $E \times B$ velocity. However, as has been considered by several authors^{20,23,56–58} stabilization effects due to a nonzero second derivative (curvature) of the $E \times B$ velocity are also possible. Unlike the first derivative case, the stabilization effects of curvature depend on the sign of the curvature. Furthermore, whether a given sign is stabilizing or destabilizing is mode specific. For example, calculations for ion temperature gradient (ITG)^{20,23} and dissipative trapped electron modes (DTE) indicate that positive E_r curvature (an E_r well) is stabilizing for ITG modes and destabilizing for DTE modes. Positive E_r curvature is destabilizing for electron drift waves provided that the E_r well is deep enough. ^{56,57}

The nonlinear effects of E_r curvature result in a radial squeezing or broadening of the turbulent eddies, depending on the sign of the curvature. Squeezing produces reduced radial correlation lengths and reduced transport, similar to a linear variation in the $E \times B$ flow.

III. H-MODE EDGE RESULTS

H-mode edge transport barrier studies provide the largest body of data for testing the $E \times B$ velocity shear theory. The results show qualitative and quantitative agreement with the theory. In addition, in the last few years, several results have been produced which are consistent with $E \times B$ shear causing changes in turbulence and transport.

The H mode was first discovered in the Axisymmetric Divertor Experiment (ASDEX) a divertor tokamak, ⁵⁹ but has now been seen in a wide variety of magnetic confinement devices. H mode has been obtained in all auxiliary heated divertor tokamaks that have operated since 1982, in limiter discharges in several tokamaks, ^{60–63} in a current-free stellarator, ^{64,65} in a heliotron/torsatron, ^{66,67} and in a linear tandem mirror machine. ^{68,69} H mode has also been produced with a wide variety of techniques: heating with neutral beam injection on many machines, electron cyclotron heating, ^{64,65,70,71} ion cyclotron heating, ^{60,72} lower hybrid heating, ⁷³ and Ohmic heating. ^{74–77} Furthermore, H mode has also been produced by biasing the plasma using an external electrode ^{75,78,79} or by biasing the limiter. ^{68,69} Since the advent of biased H modes, ^{75,78,79} H modes produced by heating the plasma have been referred to as spontaneous H mode.

Because the H-mode confinement improvement appears in many magnetic configurations and has been produced by many means, it is clear that the explanation of the results requires some mechanism with significant universality. A theory that is specific to a given magnetic configuration or to a specific heating mechanism would not be consistent with the experimental results. The reduction in turbulence-driven transport by $E \times B$ velocity shear has this universality.

There is a set of common features that are seen in all devices which obtain H mode. The first to be identified was the formation of a transport barrier at the plasma edge⁸⁰ where the density and temperature gradients steepen after the transition. The formation of this barrier is associated with a drop in the D_{α} radiation all around the plasma, indicating a significant decrease in the particle outflux. In addition, later work showed that the density fluctuation amplitude decreases in the region where the transport barrier forms. 81-83 Finally. at the same time as the formation of the transport barrier and the reduction in fluctuations, a steep gradient region develops in E_r at the plasma edge. ^{39,40} These features have been seen in all tokamak discharges where diagnostics capabilities allow it 84,85 and have also been seen in the stellarator 86-88 and mirror results.^{68,69} This spatial and temporal correlation between increased $E \times B$ shear, turbulence reduction, and transport reduction demonstrates qualitative consistency between the theory of $E \times B$ velocity shear stabilization of turbulence and the experimental results.

Theory predicts that radial, fluctuation-driven transport should be reduced if the $E \times B$ shearing rate is large enough. Langmuir probe measurements in the plasma edge in spontaneous H modes^{89,90} and biased H mode^{91,92} in tokamaks and in the Wendelstein 7-AS stellarator⁸⁸ show large decreases in the fluctuation-driven particle flux, consistent with the theoretical expectation.

The functional form in Eq. (3) predicts that $\omega_{E\times B}$ is not constant on a flux surface, being significantly larger on the low toroidal field side of the flux surface. Accordingly, one might expect significant poloidal variation in the effect of $E\times B$ shear on turbulent fluctuations. Experimental measurements at the inner and outer midplane of the edge plasma in H mode have indeed shown such differences, ^{84,93} which are qualitatively consistent with the factor of 6 variation in $\omega_{E\times B}$ between the two sides of the flux surface seen in the experiments.

In addition to qualitative agreement, there is quantitative agreement between the $E \times B$ velocity shear stabilization theory and L to H transition experiments. The $\omega_{E\times B}$ values from Eq. (2) have been compared with the measured turbulence decorrelation rates in several devices. 84,89,93-95 The results show that $\omega_{E\times B}$ increases significantly as the plasma goes from L mode to H mode and $\omega_{E\times B}$ significantly exceeds $\Delta \omega_D$ in the H mode. $\omega_{E \times B}$ significantly exceeding $\Delta\omega_D$ has also been seen in the Ohmic shear layer in the edge of the Texas Experimental Tokamak (TEXT)³⁷ where turbulence and transport are reduced. An example of such a comparison is given in Fig. 5. For this comparison, the radial correlation length and intrinsic turbulence decorrelation time is obtained from phase contrast imaging⁹⁶ while the estimate of the poloidal correlation length is derived from far infrared scattering. 97 As can be seen in Fig. 5, the $E \times B$ shearing rate is comparable to the intrinsic turbulence decorrelation rate in the L mode but is much larger than it in the H mode. This is what the theory would predict. 14,46

A key prediction of the $E \times B$ velocity shear theory is the prediction that $E \times B$ velocity shear causes the reduction in turbulence and transport. Causality can be quite difficult to pin down in spontaneous H modes, since the E_r shear also

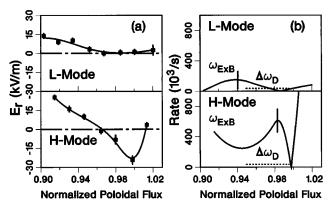


FIG. 5. Comparison of L-mode and H-mode edge profiles in DIII-D near the time of the L to H transition. The L-mode time is about 25 ms prior to the start of the dithering transition while the H-mode time is 50 ms later in the quiescent H-mode phase. In (a), the E_r profiles are shown; notice the characteristic E_r well at the plasma edge in H mode. In (b) the $E \times B$ shearing rate from Eq. (2) is compared to the intrinsic turbulence decorrelation rate. Because of the need to use several phase contrast chords to obtain the radial correlation length, the value is plotted as the average value over the region sampled. Plasma conditions are 1.5 MA plasma current, 2.2 T toroidal field, 8.6 MW injected deuterium neutral beam power, and 3.6×10^{19} m⁻³ line averaged density. Plasma is a double-null divertor operated in deuterium.

participates in a number of feedback loops in which changes in transport lead to changes in E_r . One way to test causality for the spontaneous H-mode transition is to look for cases where the E_r evolves significantly prior to the L to H transition. Over the past two years, the DIII-D group has published several papers showing that the $E \times B$ shear changes prior to changes in the turbulence and transport. 90,98–100 This observation is consistent with causality.

Another way to approach the causality question is to look at H modes produced by biasing the plasma. 75,78,79,91,92 In these cases, the experimenter controls E_r and causality is easier to determine, since the E_r can be varied at will. The existence of a biased H mode itself is a strong argument for $E \times B$ shear causing turbulence reduction and transport improvement, since it is the $E \times B$ shear that the experimenter is changing. A recent experiment on TEXTOR (Tokamak Experiment for Technology Oriented Research)¹⁰¹ has produced some very clear evidence that $E \times B$ shear influences transport. In this experiment, the electrode bias is increased slowly over a period of 2 s. The typical radial current bifurcation of the biased H mode occurs after about 1 s. However, even prior to this, there is clear evidence that the density gradient in the plasma edge has local maxima where the radial derivative of E_r is maximum. These density gradient maxima become higher after the radial current bifurcation, since the E_r gradient increases further at that time. The fact that these maxima are seen even prior to the radial current bifurcation shows that it is the E_r change, not the current bifurcation itself, which leads to reduced transport. Changes in the fluctuation level 95,102,103 and in the radial correlation of turbulence⁹⁵ have also been seen during direct biasing of the scrape-off layer in a tokamak⁹⁵ and during direct biasing of the main plasma in a mirror machine. 102,103 All of these results are consistent with $E \times B$ velocity shear causing changes in turbulence.

IV. $E \times B$ VELOCITY SHEAR EFFECTS IN THE PLASMA CORE

In addition to evidence of $E \times B$ velocity shear effects in the edge of H-mode plasmas, there is also evidence that these effects are active in the core plasma in tokamaks. There are data here both from discharges in which the $E \times B$ shear effects appear to grow in from the H-mode edge and in others in which the transport improves first near the magnetic axis. Most important, the evidence from the plasma core is also consistent with the $E \times B$ shear causing changes in turbulence and transport.

A. VH-mode and high I_i discharges

The VH mode, an improved confinement H mode, has been identified on both DIII-D^{2,104–107} and the Joint European Torus (JET).^{2,108,109} A key feature of the VH mode is the penetration of the H-mode edge transport barrier deeper into the plasma. Although a magnetic configuration giving second stable ballooning access at the plasma edge facilitates formation of the VH mode,^{2,108} it is clear from the experimental results that the region of improved confinement is much wider than the second stable region.^{106,107} Indeed, in DIII-D,^{106,107} the width of the second stable region changes little between the L mode, H mode, and VH mode. The wider transport barrier in the VH mode occurs naturally at high power once the local bifurcation condition is satisfied.³⁰

Initial work on the VH mode on DIII-D^{106,107,110} established a spatial and temporal correlation between the change in the $E \times B$ velocity shear and the change in local thermal transport. The region where the local thermal diffusivity changes most is between $\rho = 0.6$ and 0.9, which is the same region where the $E \times B$ velocity shear changes the most. This is also the region where density fluctuations, measured by FIR (far infrared) scattering, ^{111,112} change the most. Furthermore, there is evidence ¹¹⁰ that the change in the $E \times B$ velocity begins 20–40 ms prior to the first change in thermal transport.

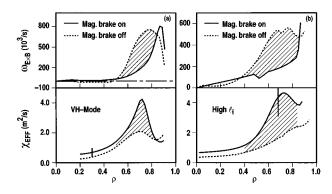


FIG. 6. Comparison of the change in the $E \times B$ shearing rate and the local single fluid thermal diffusivity inferred from power balance analysis in shots with and without magnetic braking. The magnetic braking was used to directly alter the $E \times B$ shearing rate. (a) VH-mode discharges with plasma conditions 1.3 MA plasma current, 1.7 T toroidal field, 4.7 MW injected deuterium neutral beam power, and 5.2×10^{19} m⁻³ line averaged density. (b) Elongation-ramp, high l_i discharges with plasma conditions 1.0 MA plasma current, 1.4 T toroidal field, 6.0 MW injected deuterium neutral beam power, and 6.0×10^{19} m⁻³ line averaged density. At the times presented, all discharges are double-null divertors operated in deuterium.

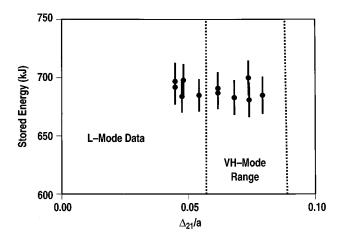


FIG. 7. Plot of the global stored energy in an L-mode plasma in DIII-D versus the amplitude of the nonaxisymmetric perturbation used to change toroidal rotation. Also shown on the figure is the range of the perturbation used in the VH-mode experiment discussed in Fig. 6. Note that the stored energy in L mode is essentially unchanged over the range of amplitudes used, indicating no direct effect of the perturbation on confinement. Note also that the range of values covered on the y axis does not include zero. Plasma conditions are 1.8 T toroidal field, 6.9 MW injected deuterium neutral beam power, and 6.2×10^{19} m⁻³ line averaged density. Results are from Ref. 116.

The high internal inductance (l_i) discharges are created in DIII-D by starting with a nearly circular cross section discharge and ramping the vertical elongation from 1.3 to 2.2 in about 200 ms.³¹ Since this time is short compared to the current diffusion time, the current density profile in the elongated plasma is transiently very peaked. Energy confinement improves by a factor of up to 1.8 relative to a discharge with the constant, higher elongation. A correlation has been seen between the increased $E \times B$ shear and the confinement improvement.³¹

In order to test whether increased $E \times B$ velocity shear is causing improved confinement in VH-mode and high l_i shots, magnetic braking of the plasma^{113,114} was used to alter the toroidal plasma rotation and change the $E \times B$ velocity shear without changing the neutral beam input to the plasma. This means that the rotation can be changed without changing the other plasma parameters, giving a fairly clean test of causality. As is illustrated in Fig. 6, the experimental results^{3,4,114} are clearly consistent with the idea that changes in the $E \times B$ velocity shear cause the changes in local thermal transport. Transport rates increase in the region where the $E \times B$ shearing rate decreases, consistent with the theory. In addition, the density fluctuation amplitude increases when the transport increases.^{3,112}

When using magnetic braking to investigate the effects of $E \times B$ shear on confinement, one must take care that there are no direct effects of the nonaxisymmetric magnetic perturbation itself on transport. As has been discussed previously, ¹¹⁵ no direct effects are expected. That none occur is illustrated in Fig. 7. This figure shows that the stored energy and, hence, the energy confinement time in L-mode divertor plasmas is essentially unchanged for the range of amplitudes of the magnetic braking used in the VH-mode experiment. ¹¹⁶ No $E \times B$ velocity shear effects are expected

in an L-mode plasma with this neutral beam input power, since the toroidal rotation and, hence, E_r are small. Any change in the energy confinement in the L-mode case is within the error bars of the measurement. These are much smaller than the 30% change in global confinement seen with magnetic braking for the data in Fig. 6.³ Accordingly, both the arguments presented previously 115 and the L-mode data in Fig. 7 are consistent with no direct effect of the nonaxisymmetric perturbation on transport.

B. Discharges with central transport barriers

Over the past two years, the routine achievement of reduced transport in the central region of tokamak plasmas has generated enormous excitement in the field. Record fusion performance in DIII-D and JT-60U has been achieved utilizing these improved confinement discharges. Although this routine achievement of improved confinement utilizes target plasmas with negative central magnetic shear, it appears that the key physics for the transport reduction is the $E \times B$ velocity shear.

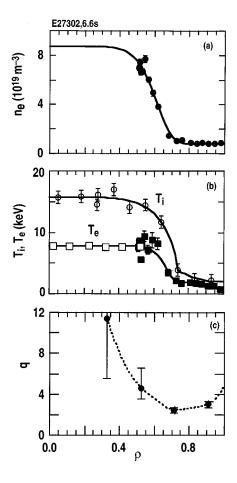


FIG. 8. Radial profiles for a high performance, negative central shear discharge in JT-60U. (a) Electron density n_e measured by Thomson scattering. Solid curve is obtained by fitting interferometer data (one tangential and two vertical chords). (b) T_i from charge exchange recombination spectroscopy and T_e . In the T_e profile, closed points are measured by Thomson scattering and open points are by electron cyclotron emission. (c) q profile from motional Stark effect measurements. Data are from Ref. 137.

Initial techniques for creating core transport barriers were restricted to narrow parameter ranges. 117-120 Although it was not realized during the initial experiments, 117 a common feature of these improved core confinement modes is profiles of the magnetic safety factor q with q > 1 on axis and low¹²¹ or, in some cases^{118,119} negative central magnetic shear. Routine achievement of core transport barriers required developing a means of shaping the current density profile. This development actually had two parts. First, experimentalists had developed the technique of heating the plasma during the initial current ramp^{122–124} or of a subsidiary current ramp¹²⁵ as a technique for slowing current diffusion and broadening the q profile. Second, improvements in measurements of the magnetic field line pitch inside the plasma^{126–129} allowed them to rapidly and reliably determine the q profile so that the response to this technique could be accurately determined. Heating during the initial current ramp is the technique used on most machines; 5,6,8,130-132 offaxis current drive has also been used to produce133,134 or sustain the negative central shear. 135

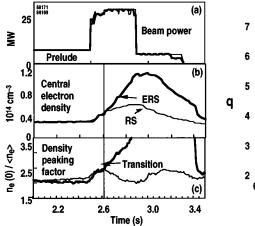
As is illustrated in Fig. 8, impressively steep core gradients can be produced in these types of discharges. These lead to quite low inferred ion thermal diffusivities and particle diffusivities on most of the machines which have studied this mode of operation. ^{5–8,130,136–138} On the other hand, the steepest core gradients are also associated with magnetohydrodynamic (MHD) stability problems; ^{136,137} the best compromise appears to be shots where the gradient scale lengths are never as locally steep, but where transport is reduced across the whole plasma. ¹¹

The model which has evolved to understand these results in the negative magnetic shear discharges includes synergistic effects of magnetic shear and $E \times B$ velocity shear. The negative or low magnetic shear allows stabilization of high n MHD modes (e.g., ballooning modes). In addition, the magnetic configuration with q > 1 everywhere stabilizes sawtooth MHD oscillations. A lack of these instabilities plus application of additional heat and, possibly, angular momentum input allows pressure and toroidal rotation gradients to

build, thus starting the feedback process discussed with Eq. (1). A local transport bifurcation can occur based on $E \times B$ shear decorrelation of turbulence as discussed by Staebler and Hinton. 29,30 As pointed out by Diamond et al., 27,28 the local transport bifurcation starts first in the plasma core because magnetic shear effects, $T_i/T_e > 1$ and the Shafranov shift all give the lowest threshold (microinstability growth rate) there. The transport barrier propagates outward into the region of increased microinstability growth rate until the local $E \times B$ shearing rate can no longer overcome the instability growth rate. Because E_r can be influenced by particle, angular momentum, and heat input [see Eq. (1)], various of these terms can be active in various machines. In the Tokamak Fusion Test Reactor (TFTR), for example, the pressure gradient term is dominant and $E_r < 0$ in the plasma core¹³⁹ while the toroidal rotation term is dominant and, as is shown in Fig. 4, $E_r > 0$ in the plasma core in DIII-D.

There are a number of testable predictions which this theory makes:

- (1) Sawteeth and ballooning modes are turned off by the *q* value and profile shape.
- (2) Negative magnetic shear alone is not sufficient for transport barrier formation.
- (3) The theory is a local bifurcation theory, accordingly, there should be spatial and temporal correlation between increased $E \times B$ shearing rate, transport reduction, and fluctuation decrease.
- (4) $\omega_{E\times B}$ should be comparable to γ_{MAX} before barrier formation and should increase more than γ_{MAX} after formation.
- (5) As can be seen in Eq. (3), the $(RB_{\theta})^2/B$ factor will make $\omega_{E\times B}$ bigger on the low toroidal field side of a flux surface, especially in cases with large Shafranov shift; accordingly, turbulence stabilization is easier there and harder on the high toroidal field side.
- (6) Since the theory contains a local transport bifurcation when $\omega_{E\times B}$ is big enough, there must be a threshold in the heat, particle, or angular momentum input required



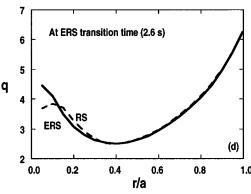


FIG. 9. Plots from two discharges in TFTR showing that the q profile is identical at the time of the RS-ERS transition. (a) Deuterium neutral beam input power, (b) central electron density, (c) density peaking factor all plotted as a function of time, (d) q profile at the time of the transition. The RS plasma trace is the dashed line. Data are from Ref. 7.

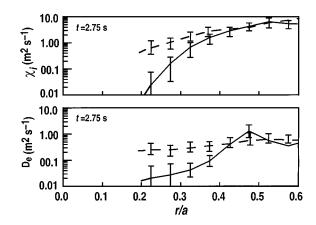


FIG. 10. Plots of electron particle diffusivity (D_e) and ion thermal diffusivity in the ERS (solid line) and the RS plasmas of Figs. 9 and 11 at t = 2.75 s into the two discharges. Data are from Ref. 7.

to create the transport barrier. This has four corollaries. First, it is the amount of input inside a given flux surface which matters, not the total power. Second, since the source has to drive pressure gradients and/or rotation, the source strength required must increase at least linearly with the local density. Third, the barrier should expand from the inside out when the source is increased and contract from the outside in when it is decreased. Fourth. destruction of the $E \times B$ velocity shear by changing the momentum input should lead to barrier collapse even at constant input power.

(7) Hot ion modes should be favorable for barrier formation, since many of the key unstable modes in the plasma core (e.g., collisionless trapped electron modes and ion temperature gradient modes) are stabilized by increasing T_i/T_e .

Consider first the experimental evidence for the effects of the q profile. The importance of having discharges with-

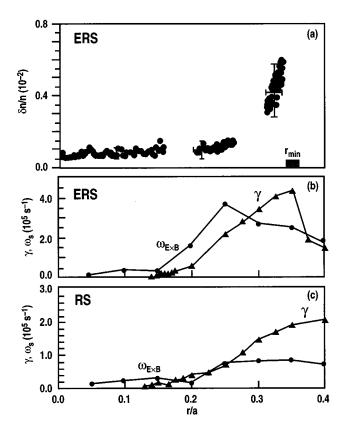
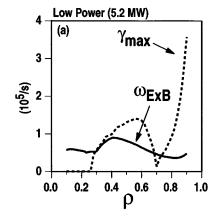


FIG. 11. (a) Amplitude of density fluctuations in ERS mode at t =2.72-2.78 s in TFTR for the same ERS shot used in Figs. 9 and 10. (b) Comparison of the $E \times B$ shearing rate $\omega_{E \times B}$ with the linear growth rate $\gamma_{\rm MAX}$ for the ERS shot in Figs. 9 and 10. (c) $\omega_{E \times B}$ vs $\gamma_{\rm MAX}$ comparison for the RS shot in Figs. 9 and 10. Data are from Ref. 7.

out sawteeth is clear in the case of the high β_p mode in JT-60U; 120,121 the improved core confinement does not happen in sawtoothing discharges. The negative magnetic shear configuration also removes the limits imposed by ballooning



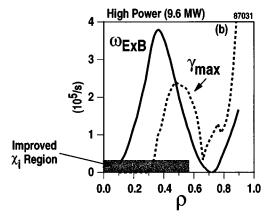


FIG. 12. Plots of the E×B shearing rate and the maximum turbulence growth rate for two times in a negative central magnetic shear shot on DIII-D (87031). (a) During the early formation of the transport barrier in the plasma core, the $E \times B$ shearing rate equals or exceeds the turbulence growth rate over only a small region in the center of the plasma. (b) During the later, higher input power phase, the $E \times B$ shearing rate has increased so that it exceeds the turbulence growth rate over a much wider region. As is indicated on the plot, this is the region over which transport has been reduced. Plasma conditions are 1.6 MA plasma current and 2.1 T toroidal field for both cases. In (a) there is 5.2 MW injected deuterium neutral beam input power and 2.0×10¹⁹ m⁻³ line averaged density while for (b) the corresponding figures are 9.6 MW and 2.4×10^{19} m⁻³. Results are from Ref. 146.

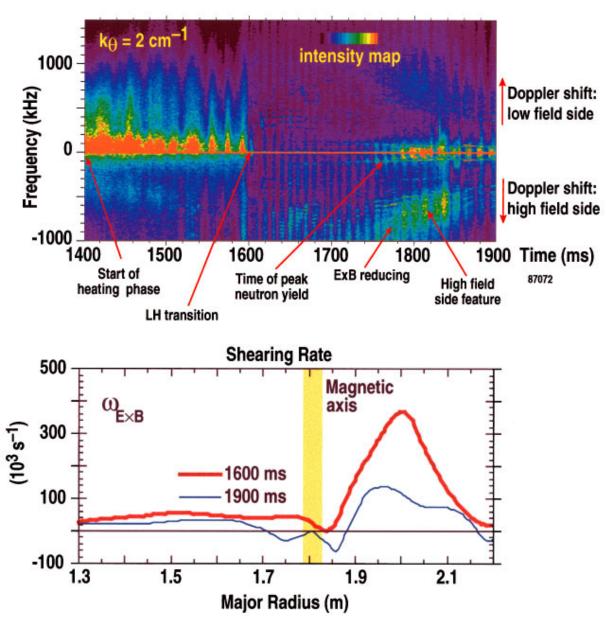


FIG. 13. Upper plot shows the scattered signal from the DIII-D far infrared scattering system for a shot with a negative central shear core transport barrier. Lower plot shows $\omega_{E\times B}$ from Eq. (3) for two different time during this shot. Because of the $E\times B$ Doppler shift of the FIR signals, the more negative frequency side of the upper plot corresponds to the core plasma region inside the magnetic axis, the more positive frequency side corresponds to the core region outside the magnetic axis, while the portion near zero frequency is an overlap of the signals from the near the plasma edge and the magnetic axis. Note that most of the turbulence is quenched near 1600 ms, at the time of the L to H transition, indicating that this portion the signal came from near the plasma edge. Small, bursting turbulence is left only on the negative frequency side, which corresponds to the portion of the plasma inside the magnetic axis. As the plasma approaches the peak performance phase, this high-field-side turbulence increases first before there is any sign of activity on the low field side.

modes, as is shown in DIII-D⁵ and TFTR¹³⁰ where the measured pressure profiles are shown to be in the second stable ballooning mode regime.

Although the q profile plays a role in achieving the core confinement improvement, there is considerable evidence that, even with the proper q profile, some other factor is needed to create the confinement improvement. Some of the clearest evidence comes from the comparison of RS (reverse shear) and ERS (enhanced reverse shear) transition data in TFTR.⁷ The transition between the RS (unimproved confinement) and the ERS (improved confinement) states has the nature of a bifurcation. As is shown in Fig. 9, at the time of the bifurcation, the q profiles in the two discharges are es-

sentially identical. This indicates that some other factor is needed to explain the transition. The difference is the time evolution of $\omega_{E\times B}$. Other evidence is also consistent with this conclusion. If negative magnetic shear were the only factor needed for the transport reduction, then all negative magnetic shear discharges should exhibit improved confinement during the current ramp phase when the magnetic shear reversal is even stronger. However, except for some observations of slow confinement improvements during this phase on DIII-D, 140 most machines report no confinement improvement until the high power phase is reached. $^{130-132}$

Additional evidence that negative magnetic shear is not the key factor in core transport barrier formation comes from high β_p mode discharges in JT-60U.¹⁴¹ Core particle and ion thermal transport barriers can be formed even in discharges with positive magnetic shear, ¹⁴¹ although, as mentioned previously, sawtooth-free discharges are required. ^{120,121}

Spatial and temporal correlation between increased $E \times B$ velocity shear, turbulence reduction, and transport reduction has been established on DIII-D^{6,11,140,142} and TFTR. ^{7,139,143–145} The spatial correlation is illustrated in Figs. 10 and 11, which shows that the low turbulence level determined by reflectometry in the core of an ERS discharge exists in the same region where the $E \times B$ shearing rate is increased and the transport decreased over the comparable RS case.

There is also a significant amount of data from DIII-D^{6,140,142,146} and TFTR^{7,139,143–145} showing that $\omega_{E\times B}$ is comparable to γ_{MAX} prior to the formation of the transport barrier and significantly exceeds it after formation. An example of the DIII-D data is shown in Fig. 12; some of the TFTR results are in Fig. 11. An important feature to notice in both Figs. 11 and 12 is that the γ_{MAX} values actually increase in the reduced transport phase over a significant portion of the region where the transport reduction occurs. This is not surprising, since the gradients which drive the turbulence have increased. However, this increase indicates that the fluctuation and transport reduction are not caused by stabilization of the turbulence by any of the factors which are included in the $\gamma_{\rm MAX}$ calculation. Accordingly, although other factors (e.g., $T_i/T_e > 1$, Shafranov shift, etc.) may help to reduce γ_{MAX} initially so that the $E \times B$ shearing rate can exceed the growth rate, they themselves are not sufficient to explain the reduced fluctuations and transport.

The poloidal variation of $\omega_{E\times B}$ and its correlation with turbulence are shown in Fig. 13. In this particular shot, the large Shafranov shift gives a variation in the $(RB_{\theta})^2/B$ factor in Eq. (3) of about a factor of 7 between the high and low field sides of a given flux surface. This produces the distinct in–out asymmetry in $\omega_{E\times B}$ seen in Fig. 13. Also shown in Fig. 13 is the scattered power from a FIR scattering system. The distinct in–out asymmetry in the turbulence near the end of the high performance phase in this shot is qualitatively consistent with the much reduced $E\times B$ shearing rate on the high toroidal field side of the flux surfaces relative to the low toroidal field side, as is shown in Fig. 13. Poloidally, these modes clearly have the largest amplitude in the region where $\omega_{E\times B}$ is the smallest.

The power threshold observations are also consistent with the idea of $E \times B$ shear stabilization. In order for the transport bifurcation process to first start, gradients and rotation must be big enough to produce the required $E \times B$ shear. A power threshold for the formation of the core transport barrier is seen on most machines. ^{6,120,130} Experiments on JT-60U¹⁴⁷ show that it is the power inside a given flux surface that is essential for creating the core barrier in the high β_p mode. In the experiment shown in Fig. 14, the power near the magnetic axis was altered by changing the particular neutral beams used. In this experiment, the total heating power was kept fixed. The discharge with the higher on-axis power input showed the formation of the transport barrier.

As has been discussed, 27,28 one would expect the power

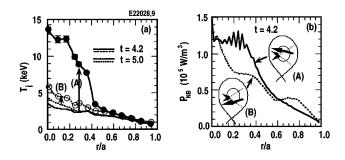


FIG. 14. Effect of beam power deposition profile on the internal transport barrier formation in JT-60U from Ref. 147. As shown in the insets in (b), the power deposition profile was changed by changing the particular neutral beams used. Total input power was kept fixed. As is shown in (a), the shot with the higher on-axis power exhibited formation of the core transport barrier.

required to form the transport barrier to increase with the plasma density provided that the energy and angular momentum confinement times do not increase faster than linearly with the density. Since energy and angular momentum confinement in tokamaks depends, at best, weakly on density, the form for the pressure gradient and rotation contributions to E_r in Eq. (1) shows that E_r should decrease as $1/n_i$ when the power and angular momentum input are constant. This is because the pressure gradient term has $1/n_i$ as a coefficient and because the rotation speed is proportional to $1/n_i$ at constant angular momentum content. In addition, if increasing density diminishes the local input near the axis, the same effect as shown in Fig. 14 could play a role. A power threshold increasing with plasma density has been seen in the high β_p mode in JT-60U. ^{148,149} As is shown in Fig. 15, the threshold power for the creation of the core transport barrier in high β_p discharges increases faster than linearly with the plasma density. High β_p mode is perhaps one of the best cases to check the intrinsic density scaling, since it does not require negative magnetic shear for its formation. Accordingly, the change in current penetration that occurs when higher density lowers the plasma temperature should not play a major role.

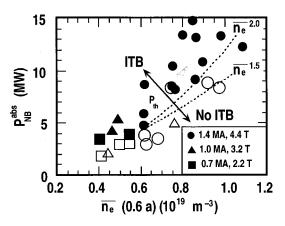


FIG. 15. Change of power input needed for core transport barrier formation with plasma line averaged density for JT-60U high β_p mode discharges. The figure is from Ref. 149.

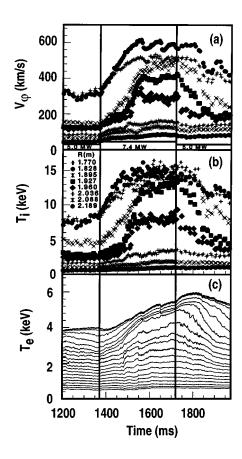


FIG. 16. Expansion and contraction of a core transport barrier in DIII-D due to changes in the neutral beam input power. (a) Toroidal rotation of C VI ions from charge exchange recombination spectroscopy; (b) ion temperature at the locations shown, and (c) electron temperature from electron cyclotron emission. The electron temperature measurements are spaced 2.5 cm apart in major radius. After the beam power shown in (a) is stepped up, the centermost ion temperatures and toroidal rotation respond immediately but there is a time delay for the outer locations to manifest the improved confinement, indicating the time it takes for the transport barrier to expand. Improve confinement is indicated by the change in slope of the curves. The inverse process happens when the power is stepped down; the temperature and rotation further out in the plasma respond first.

Barrier expansion and contraction with changing input power has been studied in DIII-D. As can be seen in Fig. 16, the transport barrier expands from the middle outwards when the power is stepped up. This agrees with the expectation from the $E \times B$ shear stabilization model that the core barrier forms first near the axis and then, as the $E \times B$ shear increases, can move out into regions where γ_{MAX} is greater. The inverse process is seen to happen when the power is stepped down. As can be seen in Figs. 11 and 12, the E $\times B$ shearing rate is well above γ_{MAX} further into the core, so it takes a bigger decrease before $\omega_{E \times B}$ reaches the marginal point. Accordingly, the transport barrier is destroyed in the outer regions first, where the plasma is closer to marginal stability. Transport analysis of this shot 140 supports this interpretation of the raw temperature and rotation data shown in Fig. 16.

Recently, a key test of causality has been performed on TFTR. ^{139,143–145} As is illustrated in Fig. 17, this experiment studied the collapse of the core transport barrier in the lower power, postlude phase. The beam power was stepped down

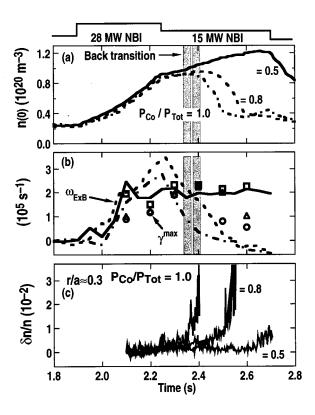


FIG. 17. Plot showing variation of time of back transition in postlude phase of a set of ERS shots in TFTR: (a) central density versus time for different fractions of power from the coinjected neutral beams showing that the back transition is earlier for greater coinjection. (b) $E \times B$ shearing rate and maximum turbulence growth rate for the same shots; turbulence growth rates are the open symbols; notice that the $E \times B$ shearing rate begins to change before the density in (a) shows that the transport barrier collapses. (c) Density fluctuation amplitude from reflectometry showing that the density fluctuations increase when the transport barrier collapses.

from the peak 28 MW used to form the barrier to 14 MW. During the 14 MW phase, the angular momentum input to the plasma was changed by changing the fraction of the beam power which came from neutral beams injecting parallel to (co) and antiparallel to (counter) the plasma current. This allowed the experimenters to directly change the toroidal rotation. Since the E_r in the ERS phase is negative ^{139,145} and since a corotation of the plasma contributes a positive E_r according to Eq. (1), it was possible to change the E $\times B$ shear in the plasma without changing the total input power. Accordingly, it was possible to change the $E \times B$ shear without changing many of the other quantities which contribute to γ_{MAX} , such as the Shafranov shift. As the beam mix is shifted toward co, $\omega_{E\times B}$ decreases more quickly and the back transition occurs sooner. In addition, as is shown in Fig. 17, the fluctuations measured by reflectometry¹⁴³ grow back up at the same time that the density trace indicates that the transport barrier is being destroyed. Transport analysis 139,145 shows that the transport rates increase at the same time that the fluctuations return. Accordingly, there is a clear temporal correlation between the decrease in $\omega_{E \times B}$, the increase in the fluctuations, and the increase in transport. In this case, as in the VH mode and high l_i magnetic braking, the experimenters have directly changed the $E \times B$ shearing rate. These results, then, are a strong test of causality and are consistent with $E \times B$ velocity shear causing the suppression of turbulence and transport.

Comparison of the TFTR and DIII-D results shows how the $E \times B$ shear stabilization hypothesis can unify the experimental results. The toroidal rotation profiles in the TFTR balanced injection cases are very different than those in the DIII-D coinjection cases. Had one tried to explain the core barrier formation in the two machines through shear in the toroidal rotation speed, the TFTR cases would have been incomprehensible, since the toroidal rotation is essentially zero. However, when considered from the standpoint of sheared $E \times B$ flow, the results from both machines are clearly part of the same basic physics.

Finally, there has been no systematic study of the role of the T_i/T_e ratio in core transport barrier creation. Most experiments have worked in the hot ion mode. 5-8,130-132,135-149 However, it is possible to create a core transport barrier in cases with almost equal T_i and T_e . 150

Although a considerable amount of the data on core transport barriers is consistent with the $E \times B$ velocity shear decorrelation hypothesis, there are still at least two outstanding puzzles. First, there is the puzzle of the lack of change in electron thermal transport in some machines. Both JT-60U^{137,138} and Tore Supra¹³⁴ see significant reduction in the electron thermal diffusivity in the core transport barrier region under cases of negative central shear. However, JT-60U sees no significant change in the electron thermal diffusivity in the high β_p mode, which has almost no magnetic shear in the plasma core. DIII-D sees modest changes in electron thermal diffusivity in some cases and large changes in others¹⁴⁰ while TFTR sees little if any change.¹³⁰ A naive model in which one thought of complete turbulence suppression would predict large changes in all cases. However, the experimental results show that turbulence is reduced but not completely suppressed.^{7,11} This variability in the electron thermal transport reduction indicates that there is still something to learn about $E \times B$ velocity shear effects on the electron transport channel.

A second result provides a cautionary note about trusting the $\omega_{E\times B} = \gamma_{\text{MAX}}$ stabilization criterion too exactly. As is shown in Fig. 18, formation of the ERS mode in TFTR can occur at values of $\omega_{E\times B}$ as much as a factor of 3 below γ_{MAX} . This range of values is similar to the range seen in the gyro-Landau fluid calculation. The fact that there is this range indicates a need for improved theory in this area.

V. TRANSPORT REDUCTION ACROSS THE WHOLE PLASMA

Most of the devices discussed in Sec. IV, have achieved particle and ion thermal diffusivities that are at or below standard neoclassical values in the plasma core. In addition, H-mode plasmas discussed in Sec. III have significant transport reduction in the plasma edge. A key question is whether the H-mode edge confinement improvement and the core confinement improvement can be combined to yield reduced transport across the whole plasma radius. Two devices have achieved results like this. In JT-60U, the high β_p H-mode discharges tart out with the high β_p mode core trans-

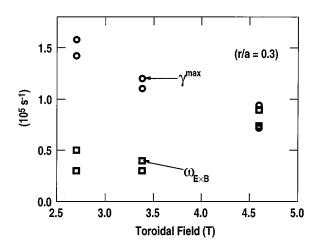


FIG. 18. Linear growth rates (circles) and $E \times B$ shearing rates (squares) for various toroidal magnetic fields at the time of formation of the ERS core transport barrier on TFTR (Ref. 144). This scan is done at constant q; hence, plasma current is varying in proportion to toroidal field. At low toroidal field, the $E \times B$ shearing rate needed to stabilize turbulence is only about 1/3 of the linear growth rate.

port barrier and then acquire an H-mode edge transport barrier later in the shot. In DIII-D controlled manipulation of the time of the L to H transition yields discharges with ion thermal diffusivity at the standard neoclassical value across the whole minor radius. This is accompanied by significant reduction in the density fluctuations across the whole plasma. Shown in Fig. 19, the $E \times B$ shearing rate

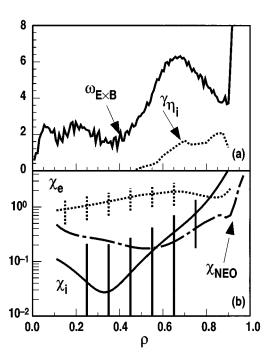


FIG. 19. The ion thermal diffusivity is at or below the standard neoclassical value across the whole minor radius of this discharge: (a) comparison of $E \times B$ shearing rate and linear growth rate showing shearing rate significantly exceeding growth rate across the whole minor radius; (b) comparison of inferred electron and ion thermal diffusivities with the Chang–Hinton neoclassical value. Results are from Ref. 6.

significantly exceeds the linear growth rate across the whole plasma in another DIII-D discharge where the ion thermal diffusivity is at or below standard neoclassical across the whole minor radius.⁶ Indeed, in these sorts of discharges, the term transport barrier is a bit of a misnomer, since the transport is reduced throughout the plasma and the radial profiles show no sign of a local barrier.

VI. SUGGESTIONS FOR FUTURE WORK

The results discussed in this paper show that the fusion plasma physics community has made significant strides in the past decade in its ability to control plasma turbulence and reduce turbulent transport. Although we have achieved a significant level of theoretical understanding of the $E \times B$ velocity shear decorrelation mechanism, there is still a considerable amount to do to make that understanding quantitative and predictive.

If one wishes to consider linear stability, the data in Fig. 18 and the initial theoretical results¹⁸ indicate a need for more exact predictions of the actual stabilization conditions required for the $E \times B$ shear to reduce the turbulence and transport. Theory and experiment show factors of 2–3 deviation from the simple rule of thumb $\omega_{E \times B} = \gamma_{\text{MAX}}$. A fundamental problem here is that inclusion of the $E \times B$ shearing rate directly in the stability codes requires a major reformulation of the underlying model. However, given the experimental success in this area in reducing turbulence and transport, a significant effort to improve the theory is appropriate.

The more fundamental point is that the plasma usually starts in a highly turbulent state and then, if the $E \times B$ shearing rate is large enough, moves towards a state with reduced turbulence and transport. Accordingly, the more fundamental comparison is between $\omega_{E \times B}$ and $\Delta \omega_D$. This means that, in order to understand the fundamental physics of $E \times B$ shear stabilization, we really need to understand the parametric dependence of $\Delta \omega_D$. Indeed, it is somewhat surprising that the comparison of $\omega_{E \times B}$ with γ_{MAX} is as good as it is, since γ_{MAX} only contains information on linear stability.

The differing observations of changes in the electron thermal transport motivate further experimental work to isolate the factors which permit this improvement in some machines but not in others. This work would benefit from theoretical suggestions about which factors are important.

Since we are now seeing ion thermal and particle diffusivities at or below the standard neoclassical values, it is clear that the neoclassical theory of cross-field transport is finally relevant to fusion plasmas. In order to understand the cases where transport is apparently below the minimum, collisional level, there is a clear need to improve the neoclassical theory. This theory has never been properly derived for the very core of tokamak plasmas, where the size of the banana orbits is bigger than the distance to the magnetic axis. In addition, density and temperature gradient scale lengths in H-mode edge barriers and in core transport barriers are comparable to the poloidal gyroradius. Since the analytical version of the theory was derived under the assumption that poloidal gyroradii were much smaller than the scale lengths, we need to improve the derivation of the theory to relax this

assumption. Finally, it is possible that orbit squeezing effects due to the shear in E_r (Refs. 151 and 152) could also be affecting the transport.

As always, improved comparisons between theory and experiment require improved plasma diagnostics. For example, in the H-mode edge area, some theories of the transition (e.g., fluctuation-driven Reynolds stress¹⁵³) have still not been tested some four years after their original suggestion, because of a lack of diagnostic capability. There are potential techniques using Langmuir probes in this area; however, the actual development has yet to start. Another example is the need for more direct measurements of E_r , both in the plasma edge and the core to see if there are any turbulence effects. The recent realization that the motional Stark effect measurements $^{126-129}$ are directly sensitive to E_r (Refs. 154 and 155) provides a possible avenue to attack this problem. Furthermore, the field in general would benefit from techniques to directly measure the fluctuation-driven heat and particle fluxes in the core of hot plasmas. (The Langmuir probe techniques employed at the edge are not suitable for the high temperatures in the core.) Finally, the understanding of turbulence in neutral fluids has advanced greatly with the advent of techniques to directly visualize the two-dimensional turbulent fluctuations. Since the fusion plasma community now has direct ways of altering turbulence, development of such techniques for plasmas could fuel even greater progress.

Most of the work that has been done to date developing improved core confinement in tokamaks has been done with techniques that are transient. The field in general needs to work on means of producing and controlling the $E \times B$ shear that can be used in steady state situations. A particular need in this area is to develop techniques which can be used in a fusion power plant.

VII. CONCLUSIONS

The $E \times B$ shear decorrelation model has the universality needed to explain the turbulence reduction and confinement improvement seen under a number of conditions: (1) H-mode edge confinement improvement seen in limiter and divertor tokamaks, stellarators, torsatrons, and mirror machines produced with a variety of heating and plasma biasing schemes; (2) the confinement improvement in the outer-half of the plasma seen in the VH mode and high internal inductance discharges and (3) the formation of core transport barriers in a number of tokamaks. In addition, there is significant qualitative agreement between theory and experiment. For example, there are spatial and temporal correlations between the changes in the $E \times B$ velocity shear, turbulence, and transport reduction in both the H-mode edge and in the plasma core. This spatial correlation is even manifested in the poloidal variation of $E \times B$ shear and turbulence seen in Fig. 13. Furthermore, there is quantitative agreement between theory and experiment. Both in the H-mode edge and in the plasma core, the $E \times B$ shearing rate is large enough according to theory to be affecting the turbulence. Finally, there have been a number of tests of causality over the past several years; the results are consistent with the $E \times B$ velocity shear causing the reduction in turbulence and transport. In the H-mode edge, the $E \times B$ shear changes prior to the change in turbulence and transport in spontaneous transitions in DIII-D. Directly altering the $E \times B$ shear at the plasma edge alters turbulence and transport even prior to the radial current bifurcation in TEXTOR. Directly changing the $E \times B$ shear in the VH-mode and elongation ramp, high l_i discharges with magnetic braking changes the turbulence and transport in DIII-D. The postlude ERS experiments in TFTR also demonstrate that direct changes of E_r at otherwise constant plasma parameters change turbulence and transport.

As has been mentioned several times in this paper, there are synergistic effects between $E \times B$ velocity shear and magnetic shear. Equations (2) and (3) show that both can play a role in determining the value of $\omega_{E \times B}$. In addition, magnetic shear can stabilize the Kelvin–Helmholtz modes which might otherwise be driven by $E \times B$ velocity shear. Finally, negative central magnetic shear facilitates the core transport barrier formation.

Looking over the $E \times B$ shear effects on turbulence and transport in various parts of the plasma, it is clear that the fusion community has entered a new era in plasma confinement. We now have the ability to control turbulence and reduce turbulence-driven transport substantially. In many ways, this amounts to a revolution in our ability to confine energy in a hot, fusion-grade plasma. This achievement is particularly surprising because many of the techniques used to provoke the formation of the transport barriers (e.g., extra heat input) are ones that provide extra free energy to the plasma. In general, the greater the free energy source, the worse the turbulence gets. However, in the case of a magnetized plasma, the $E \times B$ velocity shear provides a mechanism for the plasma to self-organize itself into a state with reduced turbulence and transport. This is a very fundamental result in fluid dynamics. How this revolution in confinement will ultimately affect fusion as an energy source for the future remains to be seen.

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