

Online Homework System

Assignment Worksheet  
11/23/20 - 6:54:38 PM EST

Name: \_\_\_\_\_

Class: Calculus 1 - MATH\*1200 - F20

Class #: \_\_\_\_\_

Section #: \_\_\_\_\_

Instructor: Mihai Nica

Assignment: Practice Term Test #5

**Question 1: (1 point)****Fill in your name on the academic integrity pledge:**

"As a member of the University of Guelph, I pledge to uphold the highest standards of ethics and academic integrity. This means that I will only use my notes, a calculator, and will NOT use any other outside assistance (no internet or other people including my peers). I understand that there are serious consequences, including getting expelled from the course or the university, for violating academic integrity."

Write the phrase "I, --insert name here--, agree to the academic integrity pledge" on the top of your answer for Q1a

**Q1a) Draw a graph of a function that has the following properties:**

- The domain of the function is a finite interval (i.e. the domain of the function is an interval not involving infinity or minus infinity)
- The function is continuous and differentiable everywhere in its domain
- The function has TWO global minima
- The function has NO global maximum

Be sure to clearly indicate what is the domain of the function in your graph.

**Q1b) True or False: Any function which meets all the criteria from Q1a) MUST have a local maximum somewhere in its domain.**

(a) False

(b) True

**Q2 Let  $f(x) = x \ln(x^2)$ . Estimate the value of  $f(1.2)$  using linear approximation.****Q3 Let  $g(x) = x^{\frac{2}{3}}(x - 5)$ . You may use the fact that  $g'(x) = \frac{5(x-2)}{3x^{1/3}}$  and  $g''(x) = \frac{10(x+1)}{9x^{4/3}}$ .**

- Find any x- and y- intercepts
- Determine any vertical or horizontal asymptotes.
- Do a first-derivative analysis. (Find intervals where the function is increasing/decreasing, horizontal/vertical tangents, cusps/corners, any extreme points.)
- Do a second-derivative analysis. (Find intervals where the function is concave up/down, find any points of inflection.)
- Draw a sketch of this function using an appropriate scale. Label some key points that you calculated in parts (a) - (d).

**Q4** A piece of wire which is 10 m long is cut into two pieces at some point along its length. One piece is bent into a square and the other is bent into a circle. The total area enclosed by the shapes is to be optimized.

- a) Set up this problem carefully be sure to clearly explain the variable you are using and what functions you are using.
  - b) How should the wire be cut so that the total area enclosed is a minimum?
  - c) How should the wire be cut so that the total area enclosed is a maximum?
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