

Assignment #1

1.

Binary	Decimal	Octal	Hexadecimal
1011011.101	91.625	133.5	5B.A
1100010	98	142	62
11101110	238	356	EE
10101111.11	175.75	257.6	AFC

$$\begin{array}{l} 1.0 \ 11011 \cdot 101_2 \rightarrow 133.5_8 \rightarrow 5B.A_{16} \\ 2^6 + 2^5 + 2^4 + 2^3 + 2^2 + 2^1 + 0.5 + 0.125 \\ = 91.625_{10} \end{array}$$

$$\begin{array}{l} 356_8 \rightarrow 2^2 2^2 2^0 \\ 011 + 101 + 110 \\ = 11101110_2 \\ = 238_{10} \end{array}$$

$$\begin{array}{l} 10101111.11_2 \rightarrow 2^2 2^2 2^0 \\ 1010 + 1111 + .11 \\ = 10101111.11_{10} \\ = 175.75_{10} \end{array}$$

$$\begin{array}{r} 98_{10} \\ - 64 \\ \hline 34 \\ - 32 \\ \hline 2 \end{array} \rightarrow \begin{array}{l} 2^6 2^5 2^4 2^3 2^2 2^1 2^0 \\ 1 \ 1 \ 0 \ 0 \ 0 \ 1 \ 0_2 \end{array} \rightarrow 142_8 \rightarrow 62_{16}$$

$$\begin{array}{l} AF.C_{16} \rightarrow 2^2 2^2 2^0 \\ 1010 + 1111 + .11 \\ = 10101111.11_{10} \\ = 175.75_{10} \end{array}$$

2. $\begin{array}{r} 101101 \\ + 101001 \\ \hline 1100010 \end{array} \rightarrow 45 \quad 98$ Since these numbers are unsigned, their range is 0 to $2^6 - 1$. In a 6 bit location, our range is 0-63. Since the decimal answer of 98 is out of that range, overflow occurs.

$$3. \begin{array}{r} 1000001 \\ - 10111 \\ \hline 110110 \end{array} \rightarrow -23$$

32 16 8 4 2 1

4.

Decimal	Sign-Magnitude	2's Complement
+14	001110	001110
-20	110100	101100
37	0100101 (overflow)	0100101 (overflow)

+14: 001110 sign-mag \rightarrow since positive, 2's-comp is same as sign-mag

-20: 110100 sign-mag

-20: $N = 2^0 \rightarrow 2^{-N} = 2^6 - 20 = 44_{10} \rightarrow 101100_{2\text{-comp}}$

37: 0100101 sign-mag \rightarrow since positive, 2's-comp is same as sign-mag

One difficulty that arises is the fact that in order to represent 37_{10} in binary, we have to use more than 6 bits which causes overflow. Also, the range for signed numbers with 6 bits is $-(2^{k-1} - 1)$ to $+(2^{k-1} - 1)$ which is -31 to 31. 37 is out of that range. Same thing with 2's-comp where the range is $-(2^{k-1})$ to $+(2^{k-1} - 1)$ which is -32 to 31. 37 is also not in that range so overflow occurs.

5. 21 bits \rightarrow 2's-comp: $-(2^{k-1})$ to $+(2^{k-1} - 1)$

$$\begin{array}{l} \downarrow \text{unsigned: } 0 \text{ to } 2^k - 1 \\ = 0 \text{ to } 2^{21} - 1 \\ = 0 \text{ to } 2097151 \end{array}$$

$$= -(2^{20}) \text{ to } +(2^{20} - 1)$$

$$= -1048576 \text{ to } +1048575$$

$$6. A = 9_{10}, B = 19_{10}$$

assume 6-bits

$$(A+B) \quad +9: 001001_2 \quad \left. \begin{array}{l} \\ (+) \end{array} \right\} 2's\text{-comp is same} \quad \left. \begin{array}{l} 001001 \\ +010011 \\ \hline 011100 \end{array} \right\} \begin{array}{l} (+) \\ \text{as unsigned so...} \end{array}$$

$$(A-B) \quad +9: 001001_2 \quad \left. \begin{array}{l} \\ (+) \end{array} \right\} 2's\text{-comp is same}$$

$$\begin{array}{r} -19: 010011_2 \xrightarrow{\text{flip}} 101100 \xrightarrow{\text{add}} \begin{array}{r} 101100 \\ +1 \\ \hline 101101 \end{array} \\ \downarrow \begin{array}{r} 001001 \\ +101100 \\ \hline 110110 \end{array} \\ (-) \end{array}$$

$$(B-A) \quad -9: 001001_2 \xrightarrow{\text{flip}} 110110 \xrightarrow{\text{add}} \begin{array}{r} 110110 \\ +1 \\ \hline 110111 \end{array}$$

$+19: 010011_2 \quad \left. \begin{array}{l} \\ (+) \end{array} \right\} 2's\text{-comp is same}$

$$\begin{array}{r} \begin{array}{r} 1 \\ 0 \\ 0 \\ 0 \\ 1 \\ 1 \end{array} \\ +101100 \\ \hline 001010 \end{array} \quad \begin{array}{l} \text{We discard the final} \\ \text{carry here} \end{array}$$

$$(-A-B) \quad -9: 001001_2 \xrightarrow{\text{flip}} 110110 \xrightarrow{\text{add}} \begin{array}{r} 110110 \\ +1 \\ \hline 110111 \end{array}$$

$-19: 010011_2 \xrightarrow{\text{flip}} 101100 \xrightarrow{\text{add}} \begin{array}{r} 101100 \\ +1 \\ \hline 101101 \end{array}$

$$\begin{array}{r} \begin{array}{r} 1 \\ 0 \\ 1 \\ 1 \\ 0 \\ 1 \end{array} \\ +101100 \\ \hline 100100 \end{array} \quad \begin{array}{l} \text{We discard the} \\ \text{final carry here} \end{array}$$

$$7. A = 32_{10}, B = 31_{10}$$

For 6-bit 2's-comp, the range is $-(2^{k-1})$ to $+(2^{k-1}-1)$
 $= -32$ to $+31$

In this case, A does not fall within this range and so overflow would occur when trying to do all four calculations $A+B$, $A-B$, $B-A$, and $-A-B$.

$$8. Go Jays! \quad \begin{array}{l} \text{Ascii encoding} = 71\ 111\ 32\ 74\ 97\ 121\ 115\ 33 \\ \text{Hexadecimal encoding} = 47\ 6F\ 20\ 4A\ 61\ 79\ 73\ 21 \end{array}$$

$$71_{10} = 100011_2 = 47_{16} \quad 115_{10} = 1110011_2 = 73_{16}$$

$$111_{10} = 110111_2 = 6F_{16} \quad 33_{10} = 100001_2 = 21_{16}$$

$$32_{10} = 100000_2 = 20_{16}$$

$$74_{10} = 1001010_2 = 4A_{16}$$

$$97_{10} = 1100001_2 = 61_{16}$$

$$121_{10} = 111100_2 = 79_{16}$$

9. Character "8" = 00111000_2 (odd parity)

Sender Transmits : After single bit error :

00111000 = 8

$0\bullet111000$ = X

00011000 = "CAN"

00101000 = (

00110000 = 0

00111000 = <

$001110\bullet0$ = :

$0011100\bullet$ = q