$$g_{\phi}(\mathbf{x}_{\mathcal{C}_j}) = [\mathbf{z}_1, \dots, \mathbf{z}_n] = \mathbf{z}_{\mathcal{C}_j}$$