

Q3:

$$\frac{75}{100} \times 21 = 15.75 \text{ index } \frac{8+7}{2} = 7.5$$

$$\text{Lower fence} = 7.5 - 1.5(4.5) = -3.65$$

$$\text{Higher fence} = 7.5 + 1.5(4.5) = 14.25$$

so we have to remove the data who not ranging between (-3.65 to 14.25)  
 we remove 27.

[1, 2, 2, 2, 3, 3, 3, 4, 5, 5, 5, 6, 6, 6, 6, 7, 8, 8, 9, 12]

$$\text{minimum} = 1$$

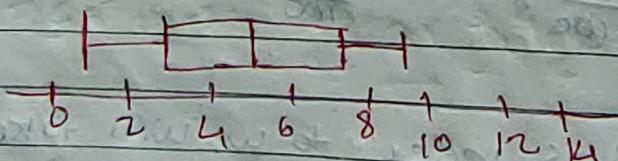
$$\text{Q1} = 3$$

$$\text{median} = 5$$

$$\text{Q3} = 7.5$$

$$\text{max} = 9$$

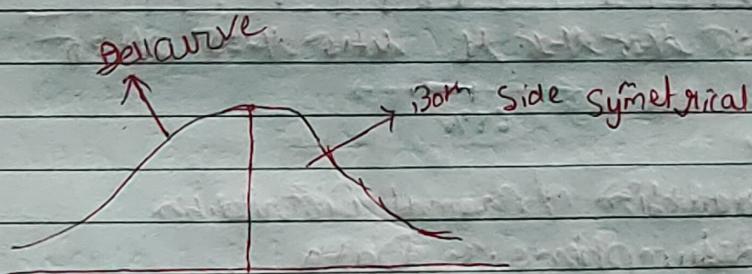
Creating Box plot + to treat outliers



### Topic

- ① Normal distribution
- ② Standard Normal distribution
- ③ Z-score
- ④ Standardization & Normalization

### ① Normal Distribution / Gaussian

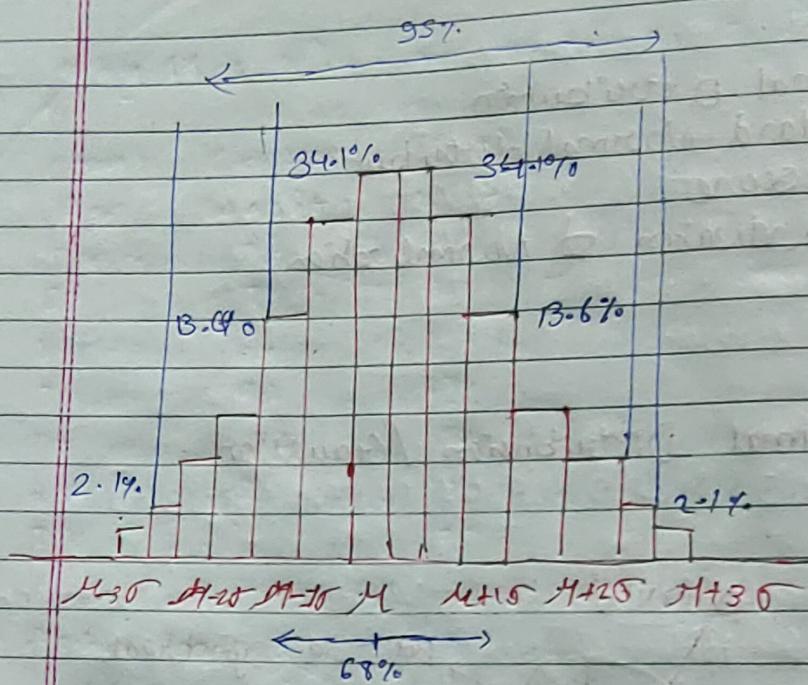


Age, weight, height  $\rightarrow$  Distribution

Domain Expertise

KDE (kernel density estimator)





Normal Distribution  
Assumptions of Data

Within the 1<sup>st</sup> standard deviation to left and right there are around 68% Data

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95% of the Data are falling in 2<sup>nd</sup> Standard deviation

Empirical Rule  
68 - 95 - 99.7%

Note → Q-Q plot

Distribution is Gaussian or Not?

## → Standard Normal Distribution

$x$  = Gaussian distribution

$$y = \text{SN}( \mu = 0, \sigma = 1 )$$

$$x = [1, 2, 3, 4, 5]$$

$$\mu = 3, \sigma = 1.41$$

$$z \text{ score} = \frac{x_i - \mu}{\sigma}$$

$\boxed{\frac{\sigma}{\sqrt{n}}} \Rightarrow \text{Standard Error}$  use in Inferential Stats

$$n = 2$$

$$x = [1, 2, 3, 4, 5]$$

$$\mu = 3, \sigma = 1.414$$

$$y = [-1.414, -0.707, 0, 0.707, 1.414]$$

$$\text{Score } \frac{x_i - \mu}{\sigma}$$

$$= \frac{1 - 3}{1.414} = -1.414$$

$$= \frac{2 - 3}{1.414} = -0.707$$

why AI is O?

(Year)	(kg)	(cm)
Age	Weight	Height
24	72	150
26	78	160
32	84	165
33	92	170
34	87	180
28	83	180
29	80	175

Machine Learning



Algorithm → Mathematical model

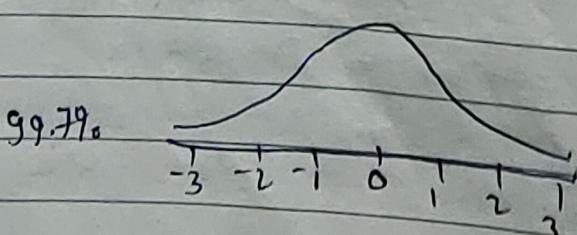
mathematical calculation time

use Z-score formula to convert data into same scale

Normalization  $\Rightarrow$  Standardization [Z-score]

$$\mu = 0, \sigma = 1$$

$[-3 \leftrightarrow 3]$



In normalization we will give the range like  
 $(0-1)$ ,  $(0-4)$ ,  $(0-5)$   
 (lower scale  $\leftrightarrow$  higher scale) -

We will do with formula

min max formula  $[0-1]$

$$x = 12345$$

$$x_{\text{scaled}} = \frac{x - x_{\text{min}}}{x_{\text{max}} - x_{\text{min}}} \quad y = [0.25, 0.5, 0.75, 1]$$

$$= \frac{1-1}{5-1} = 0$$

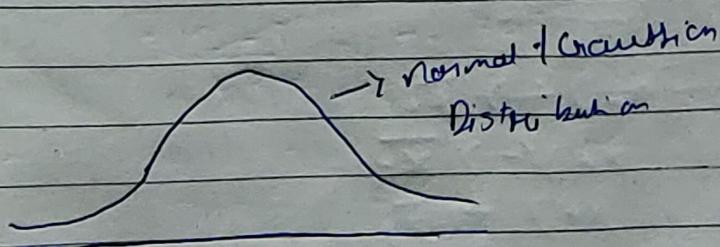
$$= \frac{2-1}{5-1} = \frac{1}{4}$$

$$= \frac{3-1}{5-1} = \frac{2}{4}$$

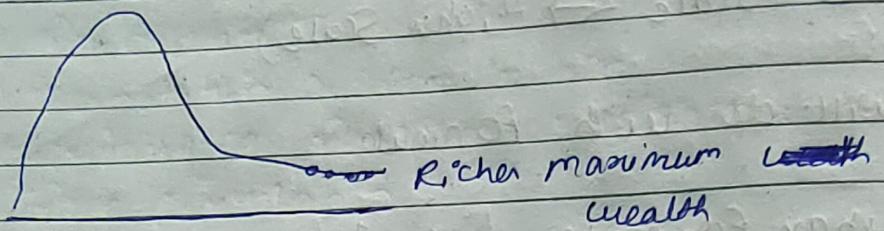
$$= \frac{4-1}{5-1} = \frac{3}{4}$$

We'll apply this in Deep learning

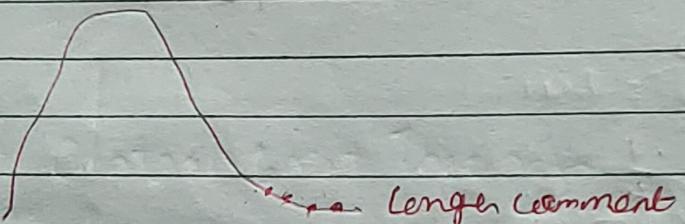
## Log Normal Distribution



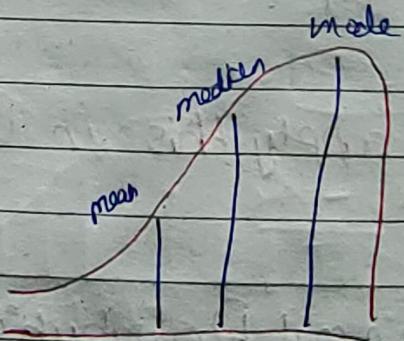
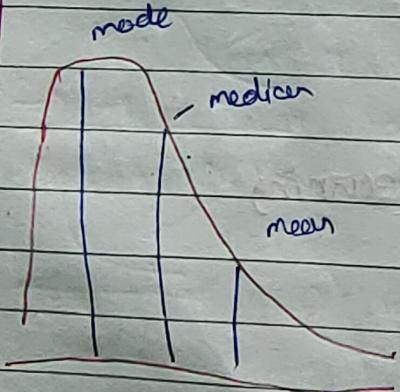
Log Normal Distribution / Right skewed

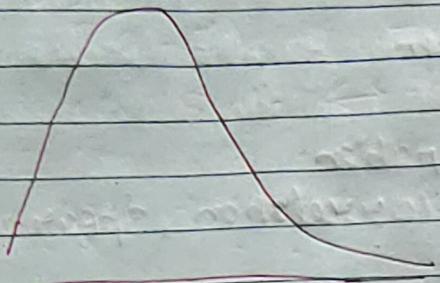


~~wealth~~ wealth Distribution

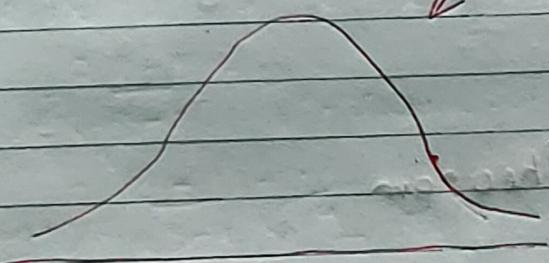


Relation of mean, median, mode





$x = \text{Log Normal Distribution}$   
If we apply:  $y = \ln(x)$

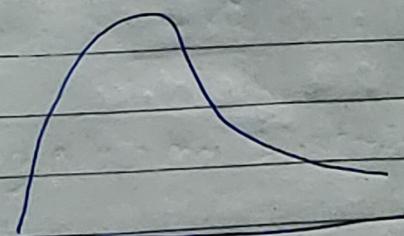


$$x = \text{no}(\mu, \sigma) \Rightarrow \exp(x)$$

$$\downarrow y$$



$$\begin{aligned} &\text{Native Log} \\ &\uparrow \\ &\text{Loge} \\ &= y = \ln(x) \end{aligned}$$



$$x = \text{log normal distribution} \\ (\mu, \sigma)$$

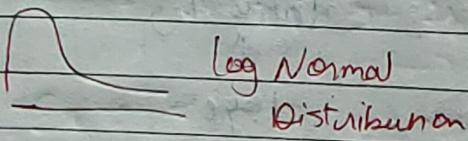
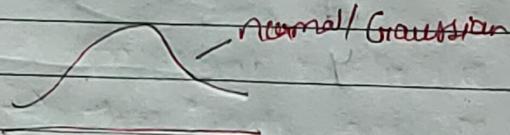
## Day 4 - Stats

Topic

- ① Central Limit Theorem
- ② Probability
- ③ Permutation and combination
- ④ Covariance, Pearson Correlation; Spearman Rank Correlation.
- ⑤ Bernoulli distribution
- ⑥ Binomial Distribution
- ⑦ ~~Power law~~ Pareto Distribution

## → ① Central Limit Theorem

Population

Data ( $N$ )Sample data ( $n$ )

$$S_1 - (x_1, x_2, x_3, \dots, x_n) \rightarrow \bar{x}_1$$

$$S_2 - (x_{11}, x_{12}, x_{13}, \dots, x_n) \rightarrow \bar{x}_2$$

$$S_3 - (x_{21}, x_{22}, x_{23}, \dots, x_n) \rightarrow \bar{x}_3$$

Calculation mean by Sample data

*Date \_\_\_\_\_  
Page \_\_\_\_\_*

$n = \text{size of Sample}$

$m = \text{No. of Sample}$

$\hookrightarrow$  Large the ratio between  
sample size and no. of sample

At any distribution if we probably take  $M$  no of sample and of sample size  $n$

Then

$n > 30$  whenever we take all the sample mean, when we plot this it will follow a gaussian distribution



$\rightarrow$  Gaussian Distribution

$\rightarrow$  The Central limit theorem states that if you have a population with mean  $\mu$  and standard deviation  $\sigma$  and take sufficiently large random samples from the population with replacement, then the distribution of the sample means will be approximately normally distributed.

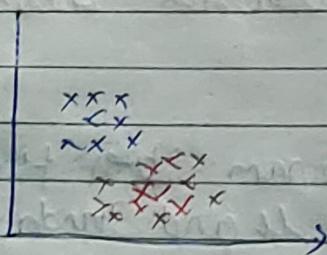
## ② Probability :

Probability is a measure of the likelihood of an event.

Ex : Tossing a fair coin

$$P(H) = 0.5 \quad P(T) = 0.5$$

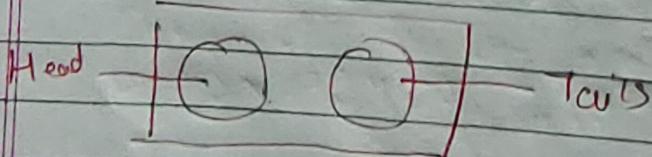
Rolling a Dice :  $P(1) = \frac{1}{6}$   $P(2) = \frac{1}{6}$   $P(3) = \frac{1}{6}$



## ③ Mutual Exclusive Event

→ Two events are mutually exclusive if they cannot occur at the same time

Ex : ① Tossing a coin ② Rolling a dice



## ⑥ Non Mutual Exclusive Events

→ Two events can occur at the same time

Ex: Picking randomly a card from a deck of cards  
two events "heart" and "king" can be selected

Addition Rule for mutual exclusive events.

① What is the probability of coin landing on heads or tails?

$$\rightarrow P(A \text{ or } B) = P(A) + P(B)$$

$$= \frac{1}{2} + \frac{1}{2} = 1$$

② What is the probability of getting 1 or 6 or 3 while rolling a dice?

$$\rightarrow P(1 \text{ or } 6 \text{ or } 3) = P(1) + P(6) + P(3)$$

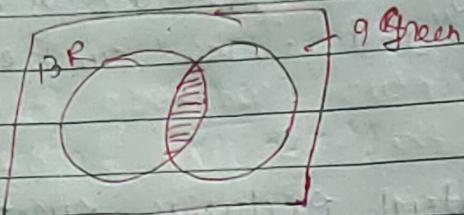
$$= \frac{1}{6} + \frac{1}{6} + \frac{1}{6} = \frac{1}{2}$$

Non Mutual Exclusive Events: Addition Rule  
Bag of marbles: 10 Red, 6 Green, 3 Blue

When picking randomly from Bag of marbles  
what is the probability of choosing a marble  
that is red or green?

$$\rightarrow P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

$$= \frac{13}{19} + \frac{9}{19} - \frac{3}{19} = \frac{19}{19} = 1$$



$$\frac{13}{19} + \frac{9}{19} - \frac{3}{19} = \frac{19}{19} = 1$$

$\rightarrow$  ~~independent~~ multiplication rule

① Dependent Events : Two events are dependent if they affect on another

$\rightarrow$  a Bag of marble [ 0000 ]  
 $\quad \quad \quad$  000

$$P(\omega) = \frac{4}{7} \rightarrow P(4) = \frac{3}{6}$$

one marble is out ↗

$$P(\omega) \times P(4/0)$$

$$= \frac{4}{7} \times \frac{3}{6} = \frac{42}{42} = \frac{2}{7}$$

## Independent Events

What's the probability of rolling a '3' and then a '3' with a normal 6-sided dice?

$$\rightarrow P(1) = \frac{1}{6} \quad P(2) = \frac{1}{6} \quad P(3) = \frac{1}{6} \quad P(4) = \frac{1}{6}$$

multiplication Rule for Independent Events

$$P(A \text{ and } B) = P(A) * P(B)$$
$$= \frac{1}{6} \times \frac{1}{6} = \boxed{\frac{1}{36}}$$

→ permutation :-

School of children

[Dairy milk, kit kat, milky  
Snickers, Star]

$$\frac{5}{5} \times \frac{4}{4} \times \frac{3}{3}$$
$$= 6 \text{ ways} = \text{Permutation}$$

with permutation orders matter

all the possible arrangement

NPR

$n = \text{Total no. of object}$

$r = \# \text{ of selection}$

$$= \frac{n!}{(n-r)!} = \frac{s!}{(s-r)!}$$

$$= \frac{5 \times 4 \times 3 \times 2!}{3!} = \boxed{120}$$

$\Rightarrow$  Combination

Repetition will not occur  
unique combination

[DM KR MB]

[MB KR DM] — X

$$n_c = \frac{n!}{r!(n-r)!} = \frac{3!}{3!(3-3)!}$$

$$= \frac{3! \times 3!}{3! \times 3!}$$

[10]

## Covariance

Age weight

[Feature Selection]

12 40

13 45 Age ↑

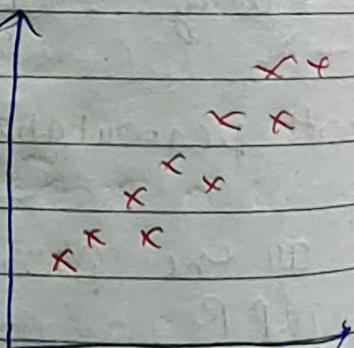
13 48 Age ↓

15 60

19 62

weight ↑

weight ↓



Quantify the relationship  $x \otimes y$  using mathematical question

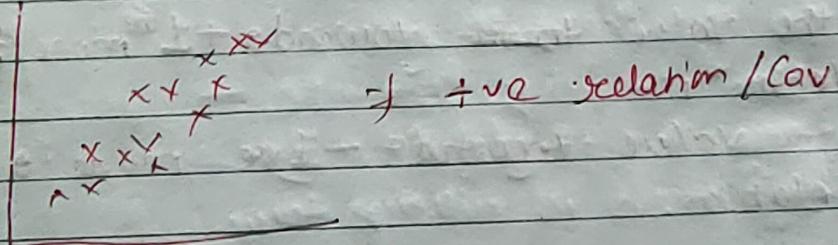
$$\text{Cov}(x, y) = \frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{n-1}$$

$$\sigma^2 = \frac{\sum (x_i - \bar{x})^2}{n-1}$$

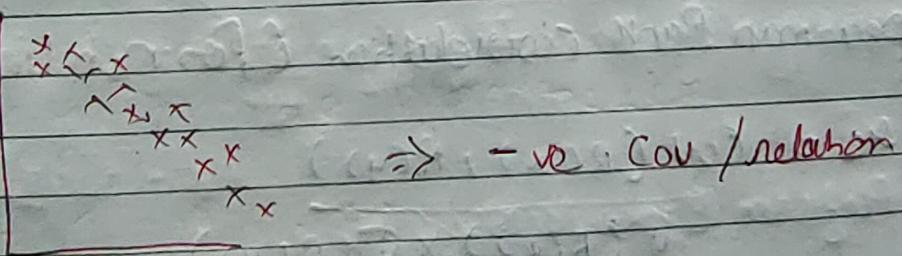
$$\sigma^2 = \frac{\sum (x_i - \bar{x})(x_i - \bar{x})}{n-1}$$

$\boxed{\text{Cov}(x, y) = \text{Var}(x)}$

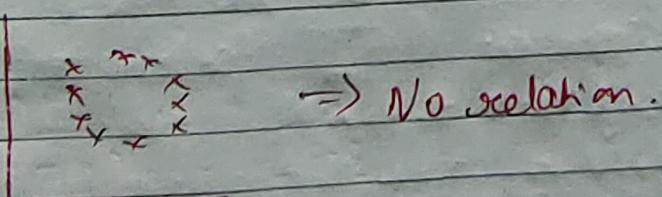
$\text{Cov} = 0$  [No relation between  $x$  &  $y$ ]



$\Rightarrow +ve \text{ relation / Cov}$



$\Rightarrow -ve \text{ Cov / relation}$



$\Rightarrow \text{No relation.}$

x	y
10	5
8	4
7	3.1
6	3
7.5	3.8

→ Pearson Correlation Coefficient (-1 to 1)

$$S(x,y) = \frac{\text{Cov}(x,y)}{\sigma_x \sigma_y}$$

more the value ~~towards~~ towards +1 <sup>more</sup> more the correlation,

more the value ~~towards~~ -1 <sup>more</sup> more -ve correlation.

→ Spearman Rank Correlation (For non linear to

$$s_s = \frac{\text{Cov}(R(x), R(y))}{\sigma(R(x)) \times \sigma(R(y))}$$

Why this corrolamin will be used?

$\text{xyz} \rightarrow \text{exp}$  +ve } good  
-ve }

Day - 5 Stats

Inferential Statistics

- 1) Hypothesis Testing
- 2) P-value
- 3) Confidence Interval
- 4) Significance value

Z test

t test

Chi Square test

Anova test (F-test)

Inferential Stat

- (3) Distribution
- ① Bernoulli
- ② Binomial
- ③ Power Law

Sample

Assumption

Conclusion

Population

Hypothesis Test

→ Hypothesis testing :-

Steps of Hypothesis testing:

① Null Hypothesis: [default one]

Null hypothesis is always true.

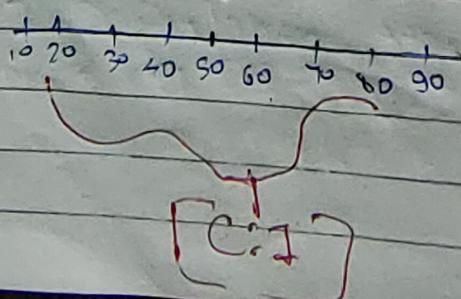
② Alternate Hypothesis: Opposite one of Null Hypothesis

③ Perform Experiments:

We define Some Range  
and that is confidence interval

coin toss / 100 time

↓ 50 times Head



$C-I = [20 - 80]$

coin is fair

to time head (Null hypothesis is Rejected).

↳ we fail to Reject the Null Hypothesis (with in C-I)

↳ we Reject the Null Hypothesis (outside C-I) }  
(Conclusion)

② Person is criminal or not (murder case)

① Null hypothesis :- Person is not criminal

② ~~Hyp~~ Alternate Hypothesis :- Person is Criminal

③ Experiment / Proof : DNA, weapons, eye witness footage.

Based on Proof . we go on conclusions.

→ Confidence Interval :-

Significance Value  
 $1 - 0.95$   
 $[5\%]$  on  $0.05$

95%.

