

Searching I

- Search Algorithms
- Search Structures: Dictionaries

Searching

Key question: How can we store data (often a set of key-value pairs) so that we can then search for specific items efficiently?

Keys and Values

(K, V)

V - value \rightarrow actual data

$K \rightarrow$ key \rightarrow used for search/insert

Keys may be comparable.

Review of data structures...

Trees

Priority Queues / Binary Heap — insert / del max

Stacks / Queues / Deque

LIFO

FIFO

Linked Lists

Arrays ← indexing

Union - Find

connectivity
→ graphs

(sequential)
linear search
 $O(1)$ if indexes are keys
sorted → binary search

The Dictionary ADT

→ storing (key, value) pairs

operations:

(put) insert (key, value)

(get) search (key)

(remove) delete (key)

Applications of Dictionaries

→ Dictionary

→ Database

→ Symbol Table

Should we allow duplicate keys?

How would you implement a Dictionary?

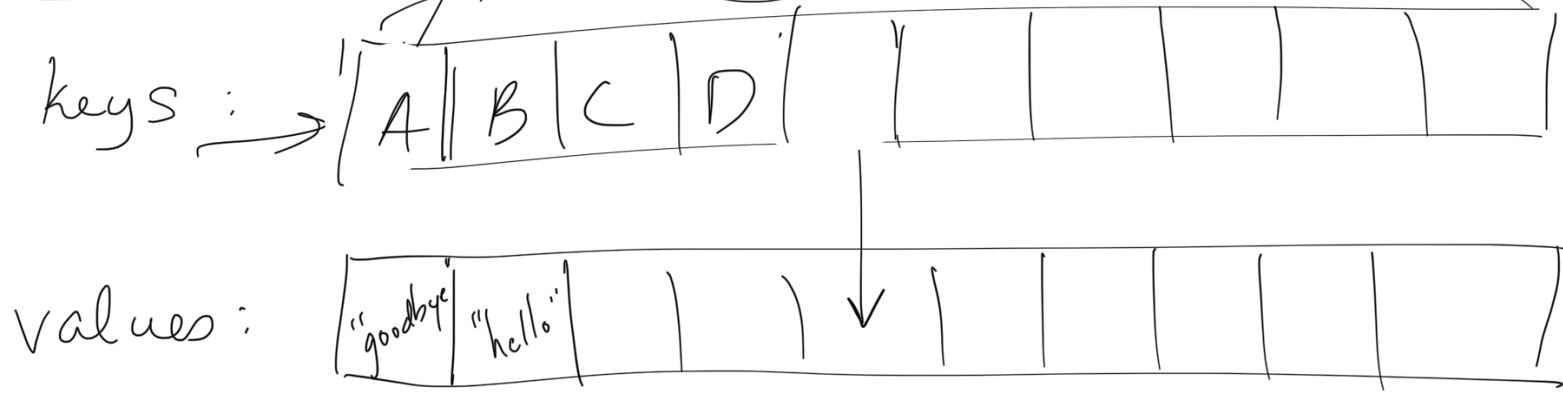
(Hashtable) Array of Linked Lists

two arrays →
keys & values
↑
sorted
↓
binary search

BST

Tree
Trie

2 Arrays



(1, "hello")

(0, "goodbye")

array of pairs

(key, value)

insert : $O(N)$
search : $O(\log N)$

insert : $O(1)$
search : $O(N)^9$

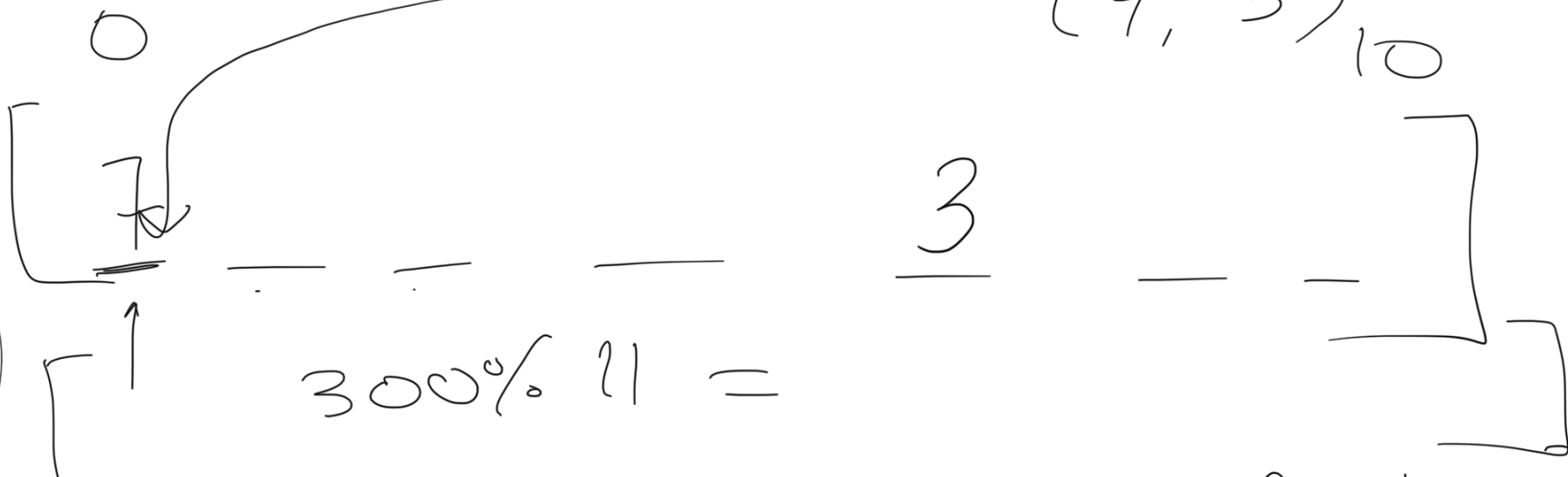
Bin Sort

range of keys

(6, 7)
(4, 3)₁₀

$M=11$

$\frac{N}{11}$



$$300 \% 11 = 3$$

insert ("hello", A)

hash function.

$$\text{hash}(\text{"hello"}) = \text{"h" + "e" + "/" + "/" + "o"} = 300$$

SHA 256

hash(SSN + salt)

Ordered vs. Unordered Dictionary

Ordered Dictionary:

Keeps the keys in order

public class ST <Key extends Comparable<Key>, Value>		
	ST()	<i>create an ordered symbol table</i>
	void put(Key key, Value val)	<i>put key-value pair into the table (remove key from table if value is null)</i>
	Value get(Key key)	<i>value paired with key (null if key is absent)</i>
	void delete(Key key)	<i>remove key (and its value) from table</i>
	boolean contains(Key key)	<i>is there a value paired with key?</i>
	boolean isEmpty()	<i>is the table empty?</i>
	int size()	<i>number of key-value pairs</i>
	Key min()	<i>smallest key</i>
	Key max()	<i>largest key</i>
	Key floor(Key key)	<i>largest key less than or equal to key</i>
	Key ceiling(Key key)	<i>smallest key greater than or equal to key</i>
	int rank(Key key)	<i>number of keys less than key</i>
	Key select(int k)	<i>key of rank k</i>
	void deleteMin()	<i>delete smallest key</i>
	void deleteMax()	<i>delete largest key</i>
	int size(Key lo, Key hi)	<i>number of keys in [lo..hi]</i>
	Iterable<Key> keys(Key lo, Key hi)	<i>keys in [lo..hi], in sorted order</i>
	Iterable<Key> keys()	<i>all keys in the table, in sorted order</i>

References

[1] *Algorithms, Fourth Edition*; Robert Sedgewick and Kevin Wayne (and associated slides)