LING/C SC 581:

Advanced Computational Linguistics

Lecture 23

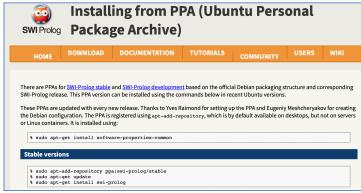
Today's Topic

- Recent Chomsky video lecture (I sent the link around):
 - Possible **HLT-related** questions for Prof. Chomsky?
 - No guarantee he has time, but I can ask...
- Change of topic
 - writing our own grammars
 - but first, we must refamiliarize ourselves with a programming language,
 Prolog

SWI Prolog

- You should already have SWI Prolog installed on your machine
- If not, please install now!
- https://www.swi-prolog.org/download/stable





https://www.swi-prolog.org/build/PPA.html

SWI Prolog Cheatsheet

```
• At the prompt ?-
    1. halt.
                       ^D
    2. listing.
                       listing(name).
   3. [filename].
                       loads filename.pl
   4. trace.
   5. notrace.
   6. debug.
   7. nodebug.
   8. spy(name).
   9.
        pwd.
    10. working_directory(_,Y).
       switch directories to Y

    Anytime

   • ^C (then a(bort) or h(elp) for other
     options)
```

```
Notation:
\+
         negation
         conjunction
         disjunction
         if
Facts:
predicate(Args).
Rules:
p(Args) := q(Args), ..., r(Args).
Data structures:
list: [a,..b]
empty list: []
head/tail: [head|List]
Atom:
name, number
Term:
functor(arguments)
arguments: comma-separated terms/atoms
```

Derivations

- Prolog's computation rule:
 - Try first matching (**grammar**) rule in the database (but remember other possibilities for backtracking)
 - Backtrack if matching rule leads to failure (or if asked by the user typing;)
 - undo variable bindings (i.e. undo assignments) and try next matching rule
- For grammars:
 - Top-down left-to-right derivations
 - **left-to-right** = expand leftmost nonterminal first
 - Leftmost expansion done recursively = depth-first

- a grammar is code, could be a recognizer program:
 - no need to write a separate grammar rule interpreter (in this case)
- Example query
 - ?- s([a,a,b,b,b],[]). Yes
- Note:
 - Syntax of DCGs:
 - ---> "expands to"
 - terminal symbol enclosed in square brackets: [terminal]
 - non-terminal symbol, otherwise
 - Query uses the start symbol s with two arguments:
 - (1) sequence (as a list) to be recognized and
 - (2) the empty list []

Grammar for a*b* apbp.prolog: 1. s --> [a],b. 2. b --> [a],b. 3. b --> [b],c. 4. b --> [b]. 5. c --> [b]. 6. c --> [b].

```
[ling581-21$ swipl
Welcome to SWI-Prolog (threaded, 64 bits, version 8.2.0)
SWI-Prolog comes with ABSOLUTELY NO WARRANTY. This is free software.
Please run ?- license. for legal details.
For online help and background, visit https://www.swi-prolog.org
For built-in help, use ?- help(Topic). or ?- apropos(Word).
[?- [apbp].
true.
[?- s([a,a,b,b,b],[]).
true ;
[?- s([b,a],[]).
[?- s(String,[]).
           Stack sizes: local: 0.8Gb, global: 0.1Gb, trail: 41.8Mb
Stack depth: 5,477,658, last-call: 0%, Choice points: 5,477,650
           Possible non-terminating recursion:

[5,477,658] user:b(_32877284, [])

[5,477,657] user:b([length:1|_32877312], [])
    Exception: (5,477,657) b(_32877212, []) ? abort
 % Execution Aborted
```

Infinite Loop: Doesn't enumerate at all!

Partial enumerator only! Why?

```
[?- [apbp2].
true.

[?- s(String,[]).
String = [a, b];
String = [a, b, b];
String = [a, b, b, b];
String = [a, b, b, b, b];
String = [a, b, b, b, b, b];
String = [a, b, b, b, b, b, b];
String = [a, b, b, b, b, b, b];
String = [a, b, b, b, b, b, b, b];
String = [a, b, b, b, b, b, b, b]
```

```
apbp2.prolog
                                      apbp.prolog
1s --> [a],b.¶
2b --> [b].¶
3b --> [b],c.¶
4b \longrightarrow [a],b.
5c --> [b].¶
6c --> [b].c.¶
-:-- apbp2.prolog All (7,0)
                                  (Prolog[SWI])
1s \longrightarrow [a],b.
2b \longrightarrow [a],b.
3b --> [b],c.¶
4b --> [b].¶
5c --> [b],c.¶
6c --> [b].¶
-:-- apbp.prolog All (1,0)
                                  (Prolog[SWI])
```

type w

```
1s \longrightarrow [a],b.
2b --> [b].¶
3b --> [a].b.
4b --> [b],c.¶
5c --> [b].¶
6c --> [b],c.¶
-:-- apbp3.prolog All (3,0)
                                 (Prolog[SWI])
            apbp2.prolog
1s \longrightarrow [a],b.
2b --> [b].¶
3b --> [b],c.¶
4b --> [a],b.¶
5c --> [b].¶
6c --> [b],c.¶
-:-- apbp2.prolog All (1,0)
                                 (Prolog[SWI])
```

- How to guarantee enumeration?
- Iterative Deepening (ID):
 - Breadth-first search implemented in depth-first search
 - Idea:
 - find all solutions at depth N, remember them,
 - then search (all over) again to depth N+1,
 - and so on...

```
[?- [id meta].
                                      String = [a, a, a, a, a, b];
true.
                                      String = [a, a, a, a, b, b];
                                      String = [a, a, a, b, b, b];
[?- id(s(String,[])).
                                      String = [a, a, b, b, b, b];
String = [a, b];
                                      String = [a, b, b, b, b, b];
String = [a, a, b];
                                      String = [a, a, a, a, a, b] ;
String = [a, b, b];
                                      String = [a, a, a, a, a, b, b];
String = [a, a, a, b];
                                      String = [a, a, a, a, b, b, b];
String = [a, a, b, b];
                                      String = [a, a, a, b, b, b, b];
String = [a, b, b, b];
                                      String = [a, a, b, b, b, b, b];
String = [a, a, a, a, b];
                                      String = [a, b, b, b, b, b, b];
String = [a, a, a, b, b];
                                      String = [a, a, a, a, a, a, b];
String = [a, a, b, b, b];
                                      String = [a, a, a, a, a, a, b, b]
String = [a, b, b, b, b]
```

for strings of length N, there'll be N-1 solutions

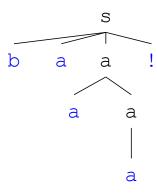
Extra Argument: Parse Tree

- Recovering a parse tree
 - when want Prolog to return more than just true/false answers
 - in case of true, we can compute a syntax tree representation of the parse
 - by adding an extra argument to nonterminals
 - applies to all grammar rules (not just regular grammars)

Example

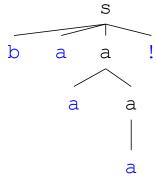
- sheeptalk again
- DCG (non-regular, context-free):

```
s --> [b], [a], a, [!].
a --> [a]. (base case)
a --> [a], a. (recursive case)
```



Extra Argument: Parse Tree

• Tree:



s(b,a,a(a,a(a)),!)

• Prolog term data structure:

- hierarchical
- allows sequencing of arguments
- functor(arg₁,..,arg_n)
- each arg_i could be another term or simple atom

Extra Arguments: Parse Tree

• DCG

```
s --> [b], [a], a, [!].
a --> [a]. (base case)
a --> [a], a. (right recursive case)
```

base case

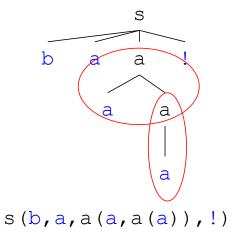
```
- a --> [a].

- a(subtree) --> [a].

- a(a(a)) --> [a].
```

recursive case

```
- a --> [a], a.
- a(subtree) --> [a], a(subtree).
- a(a(a,A)) --> [a], a(A).
```



Idea: for each nonterminal, add an argument to store its subtree

Extra Arguments: Parse Tree

Prolog grammar

```
s --> [b], [a], a, [!].
a --> [a]. (base case)
a --> [a], a. (right recursive case)
```

base and recursive cases

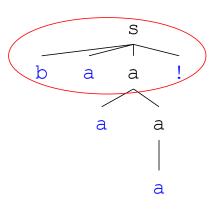
```
- a(a(a)) --> [a].
- a(a(a,A)) --> [a], a(A).
```

start symbol case

```
- s --> [b], [a], a, [!].

- s(tree) --> [b], [a], a(subtree), [!].

- s(s(b,a,A,!)) --> [b], [a], a(A), [!].
```



```
s(b,a,a(a,a(a)),!)
```

Extra Arguments: Parse Tree

Prolog grammar

```
s --> [b], [a], a, [!].
a --> [a]. (base case)
a --> [a], a. (right recursive case)
```

Equivalent Prolog grammar computing a parse

```
- s(s(b,a,A,!)) --> [b], [a], a(A), [!].

- a(a(a)) --> [a].

- a(a(a,A)) --> [a], a(A).
```

- Extra arguments are powerful
 - they allow us to impose (grammatical) constraints and change the expressive power of the system
 - if used as read-able memory
- Example:
 - aⁿbⁿcⁿ n>0 is not a context-free language (type-2)
 - i.e. you cannot write rules of the form X --> RHS that generate this language
 - in fact, it's context-sensitive (type-1)

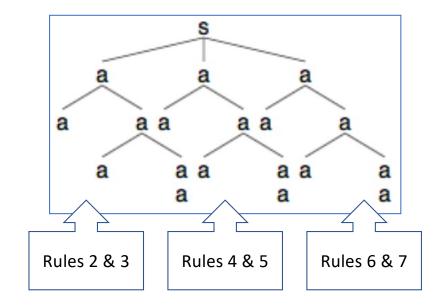
Language {aⁿbⁿcⁿ|n>0}

- 1. CFG (context-free grammar) + extra arguments for grammatical constraints
- 2. CFG + counting, cf. Perl
- 3. CSG (context-sensitive grammar) rules

• A CFG+EA for aⁿbⁿcⁿ n>0: Set membership question

```
[?- [abc_parse].
true.
[?- s(Parse,[a,a,a,b,b,b,c,c,c],[]).
Parse = s(a(a, a(a))), a(a, a(a))), a(a, a(a)));
false.
                                                             S
[?- s(Parse,[a,a,a,b,b,b,c,c],[]).
false.
                                                             а
[?- s(Parse,[a,a,a,b,b,c,c,c],[]).
false.
                                               a
                                                       a a
                                                                 a a
                                                                           a
[?- s(Parse,[a,a,b,b,b,c,c,c],[]).
                                                   a
                                                           a a
                                                                     a a
                                                                               а
false.
                                                           a
                                                                     a
                                                                               a
?-
```

- A context-free grammar (CFG) + extra argument (EA) for the context-sensitive language $\{a^nb^nc^n \mid n>0\}$:
- 1. $s(s(A,A,A)) \longrightarrow a(A), b(A), c(A)$.
- 2. a(a(a)) --> [a].
- 3. $a(a(a,X)) \longrightarrow [a], a(X).$
- 4. b(a(a)) --> [b].
- 5. $b(a(a,X)) \longrightarrow [b], b(X)$.
- 6. $c(a(a)) \longrightarrow [c]$.
- 7. $c(a(a,X)) \longrightarrow [c], c(X).$



• A CFG+EA for aⁿbⁿcⁿ n>0:

```
?- s(_,[a,a,b,b,c,c,c],[]).
false.
?- s(_,[a,a,b,b,c,c],[]).
true .
?- s(_,[a,a,b,b,c],[]).
false.
?- s(_,[a,a,b,b,c,c,c],[]).
false.
?- s(_,[a,a,a,b,b,b,c,c,c],[]).
true .
```

Set membership question

• A CFG+EA grammar for aⁿbⁿcⁿ n>0: