

# Multi-layer Perception

## (Draft Version)

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Ph.D. in Computer Science

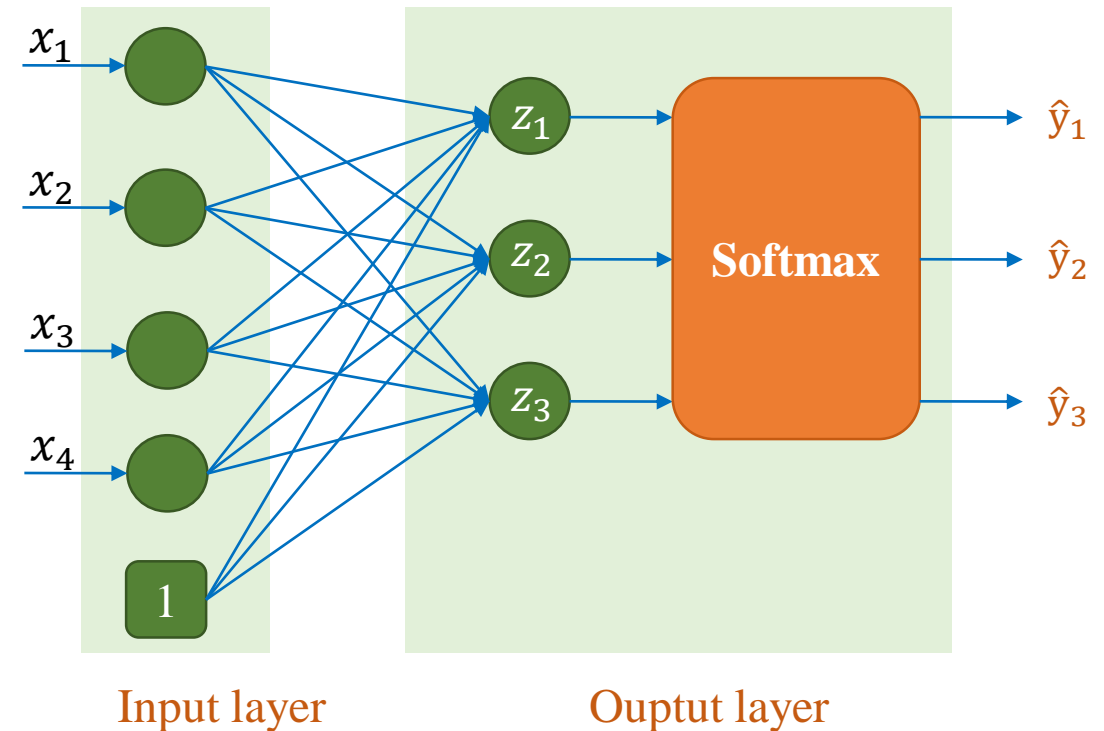
# Outline

- **Multi-layer Perceptron**
- **To-do List for Training**
- **Forward Computation Example**
- **Image Classification: Fashion-MNIST**
- **Image Classification: Cifar-10**
- **Underfitting and Overfitting**

# Multi-layer Perceptron

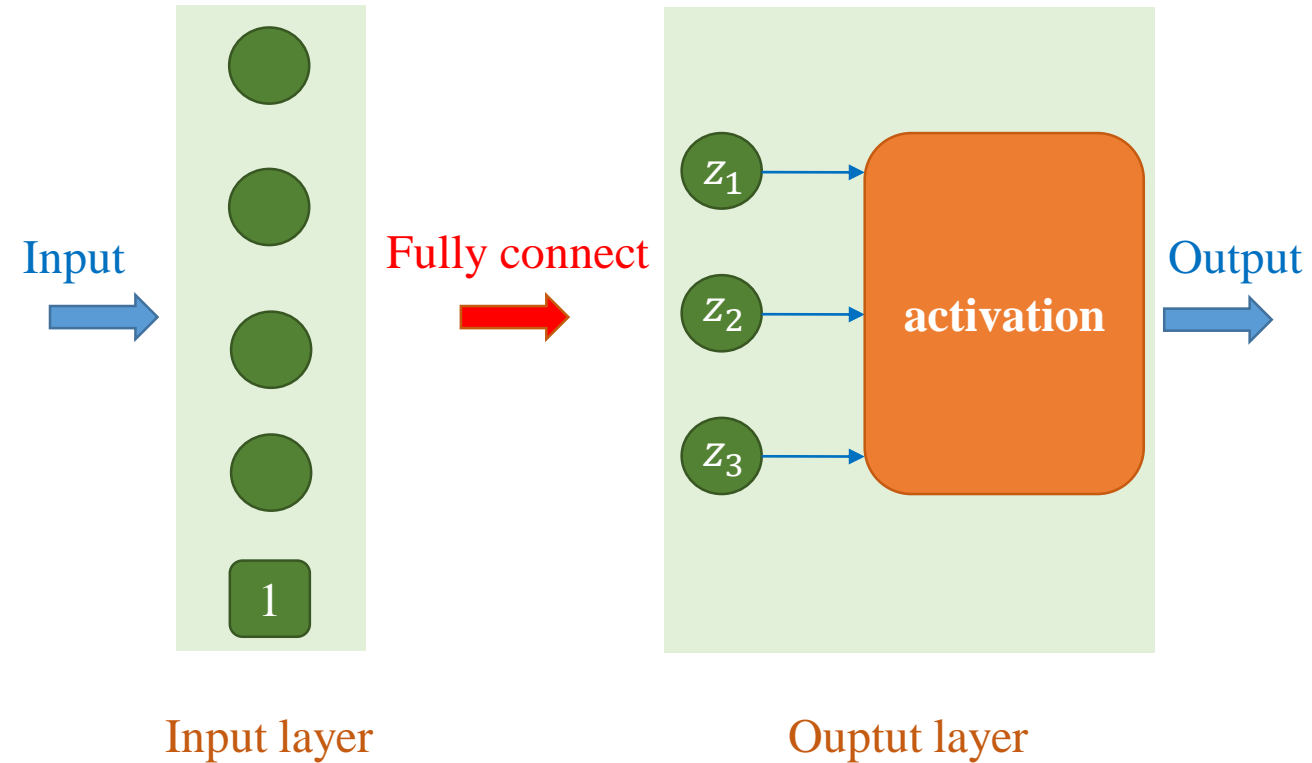
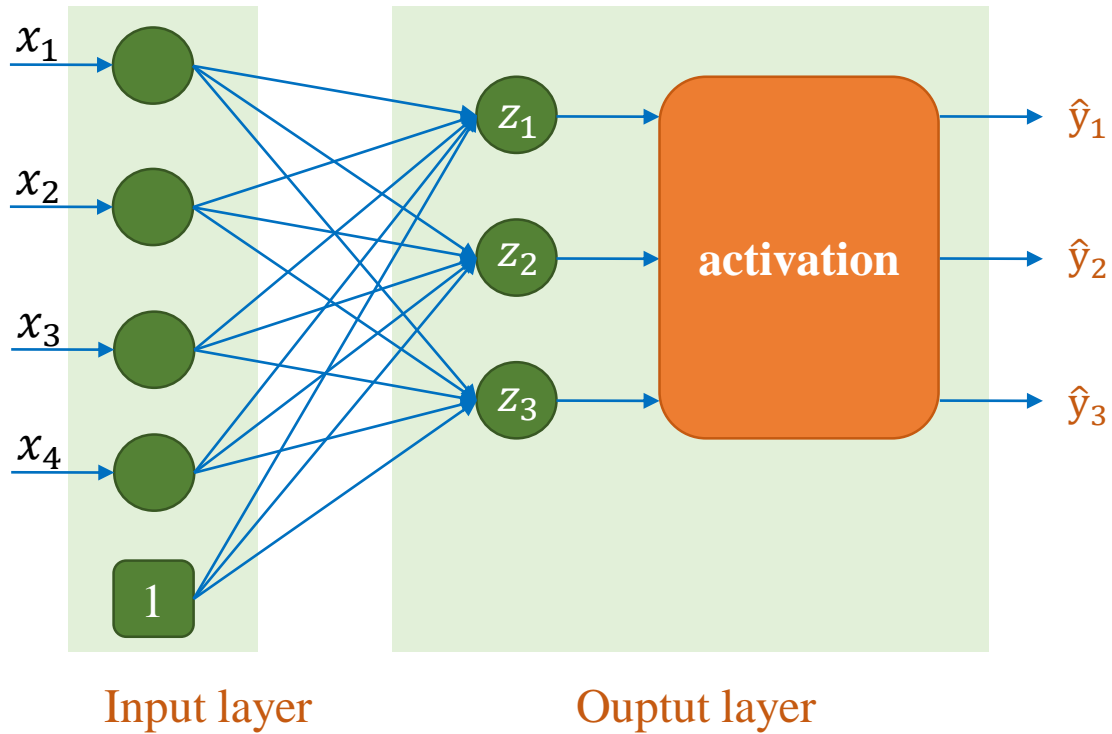
## ❖ Softmax regression

Sepal_Length	Sepal_Width	Petal_Length	Petal_Width	Label
5.2	3.5	1.5	0.2	1
5.2	3.4	1.4	0.2	1
4.7	3.2	1.6	0.2	1
6.3	3.3	4.7	1.6	2
4.9	2.4	3.3	1.1	2
6.6	2.9	4.6	1.3	2
6.4	2.8	5.6	2.2	3
6.3	2.8	5.1	1.5	3
6.1	2.6	5.6	1.4	3



# Multi-layer Perceptron

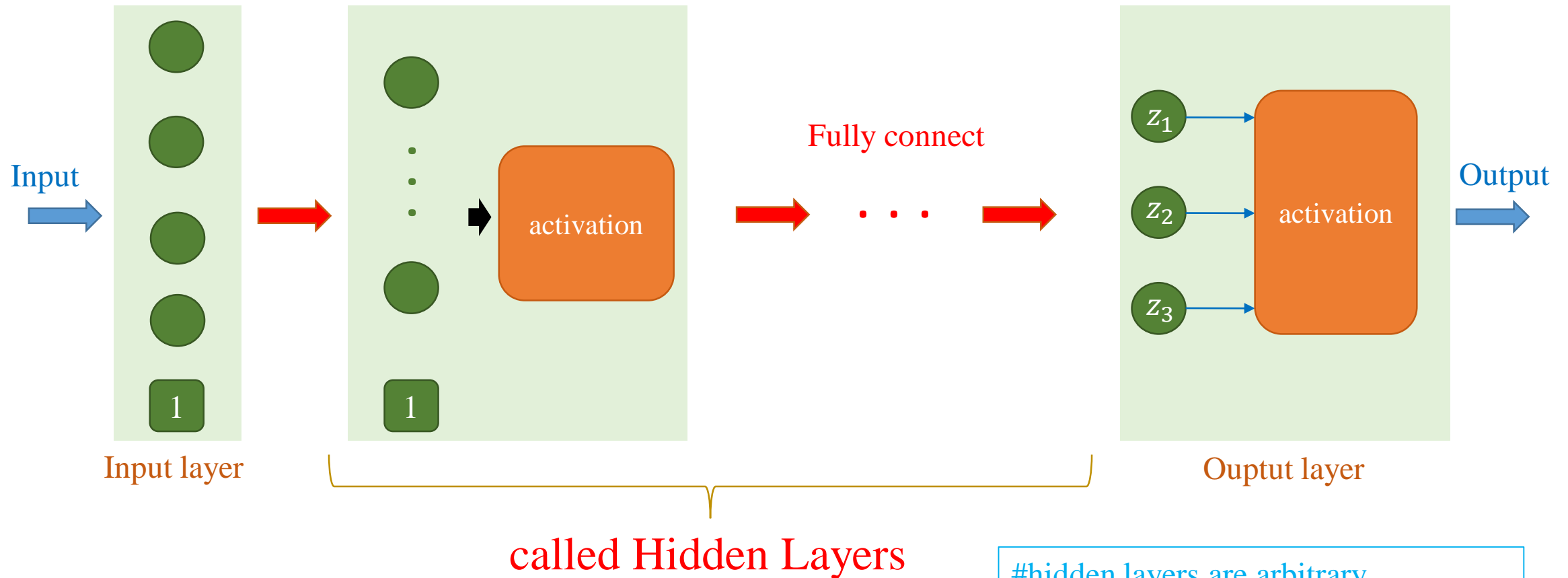
## ❖ Softmax regression



# Multi-layer Perceptron

❖ An idea: More parameters  $\rightarrow$  better capacity (~stronger model)

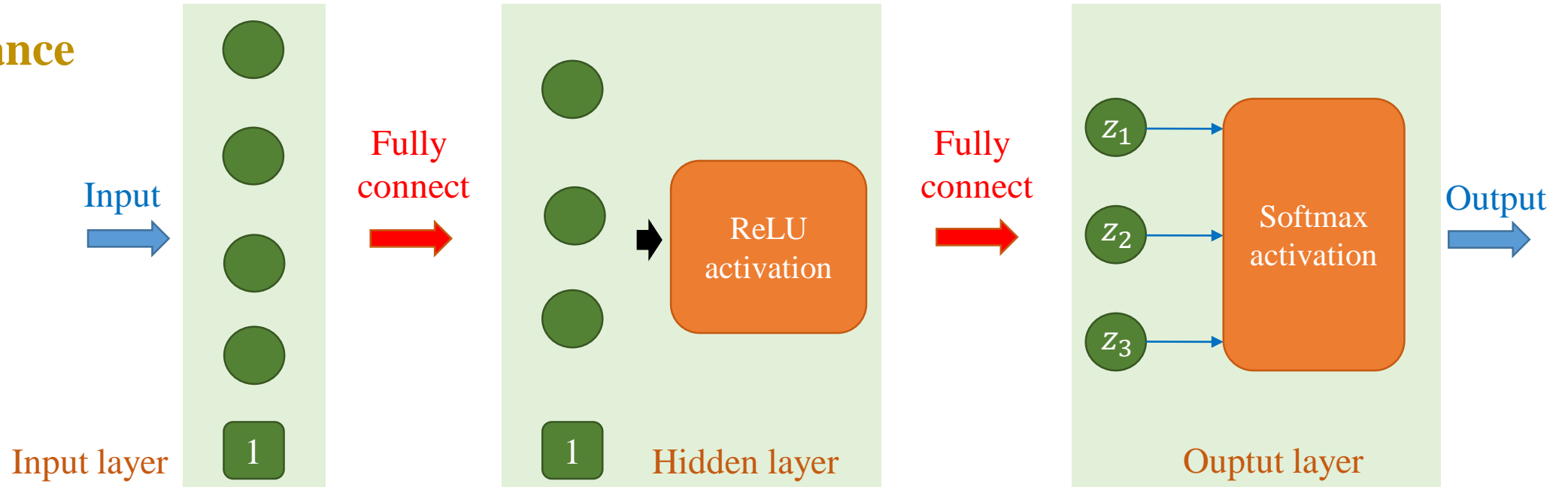
❖ Adding more layers



#hidden layers are arbitrary  
#nodes in a hidden layer are arbitrary

# Multi-layer Perceptron

## An instance

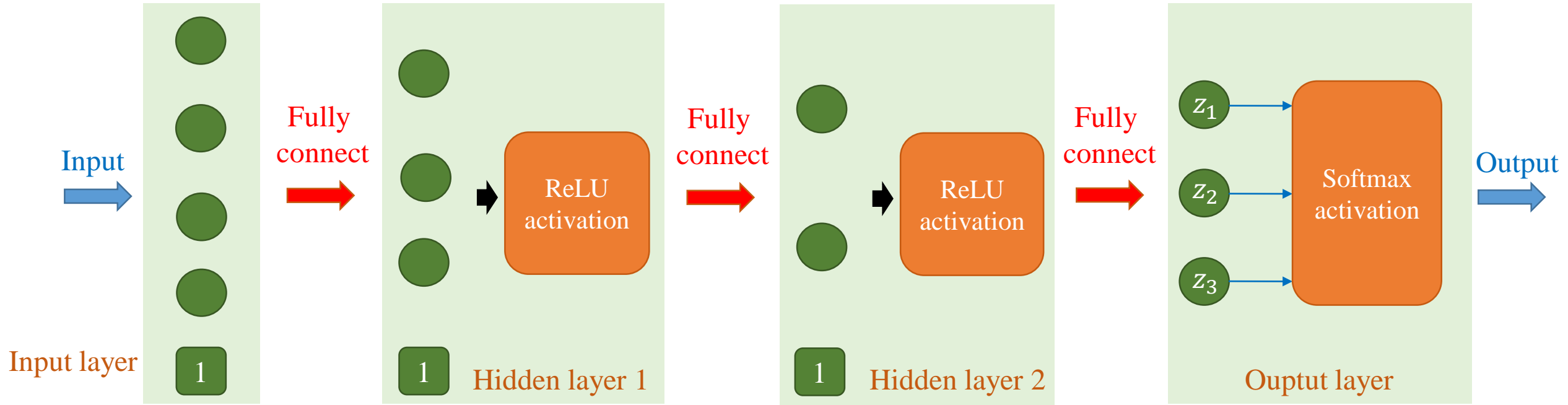


```
1 import tensorflow as tf
2 import tensorflow.keras as keras
3
4 # create model
5 model = keras.Sequential()
6 model.add(keras.Input(shape=(4,)))
7 model.add(keras.layers.Dense(3, activation='relu'))
8 model.add(keras.layers.Dense(3, activation='softmax'))
9
10 model.summary()
```

Model: "sequential"

Layer (type)	Output Shape	Param #
=====		
dense (Dense)	(None, 3)	15
dense_1 (Dense)	(None, 3)	12
=====		
Total params: 27		
Trainable params: 27		
Non-trainable params: 0		

# Multi-layer Perceptron



```
1 import tensorflow as tf
2 import tensorflow.keras as keras
3
4 # create model
5 model = keras.Sequential()
6 model.add(keras.Input(shape=(4,)))
7 model.add(keras.layers.Dense(3, activation='relu'))
8 model.add(keras.layers.Dense(2, activation='relu'))
9 model.add(keras.layers.Dense(3, activation='softmax'))
10
11 model.summary()
```

Model: "sequential"

Layer (type)	Output Shape	Param #
dense (Dense)	(None, 3)	15
dense_1 (Dense)	(None, 2)	8
dense_2 (Dense)	(None, 3)	9

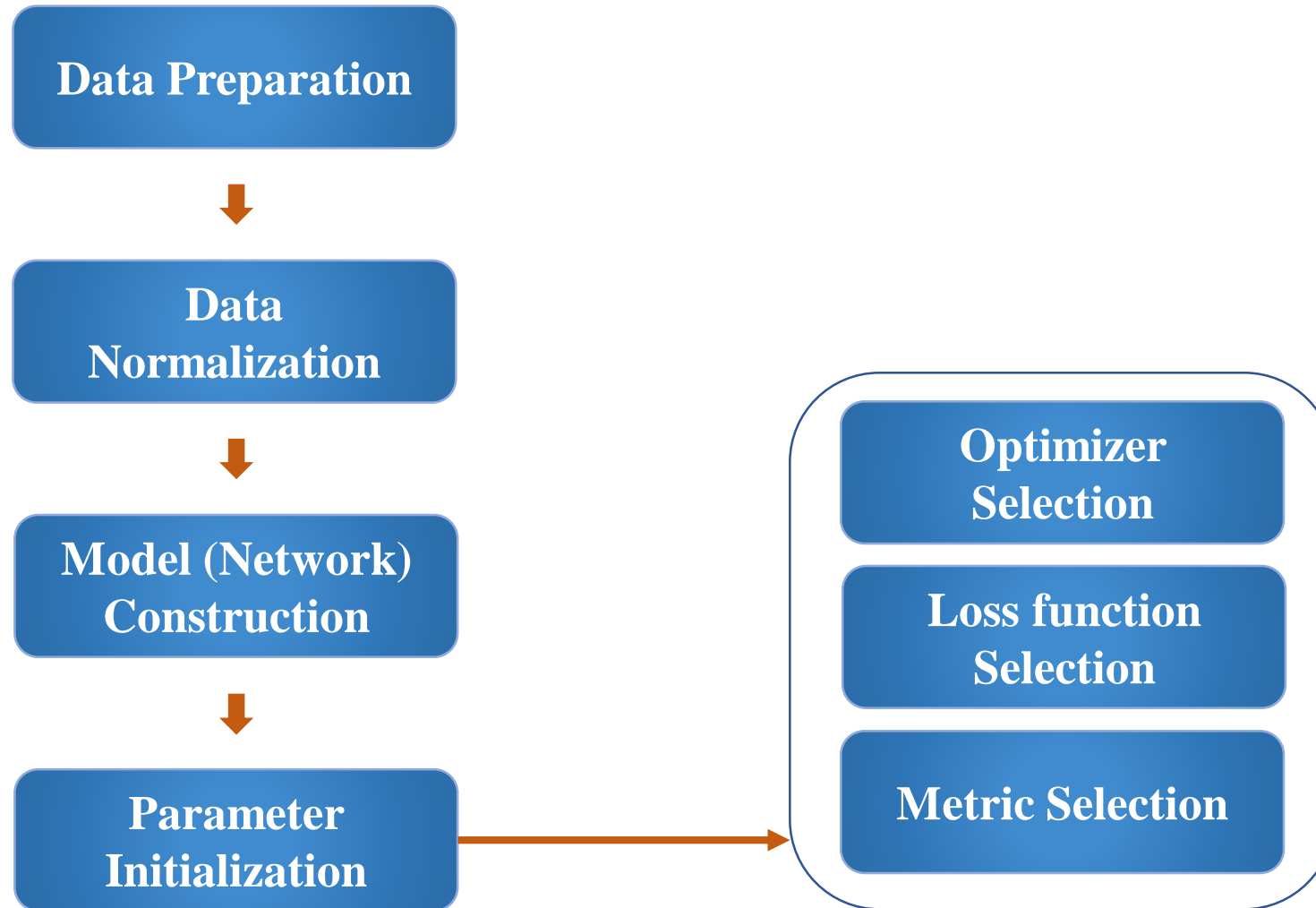
Total params: 32  
Trainable params: 32  
Non-trainable params: 0

# Outline

- **Multi-layer Perceptron**
- **To-do List for Training**
- **Forward Computation Example**
- **Image Classification: Fashion-MNIST**
- **Image Classification: Cifar-10**
- **Underfitting and Overfitting**

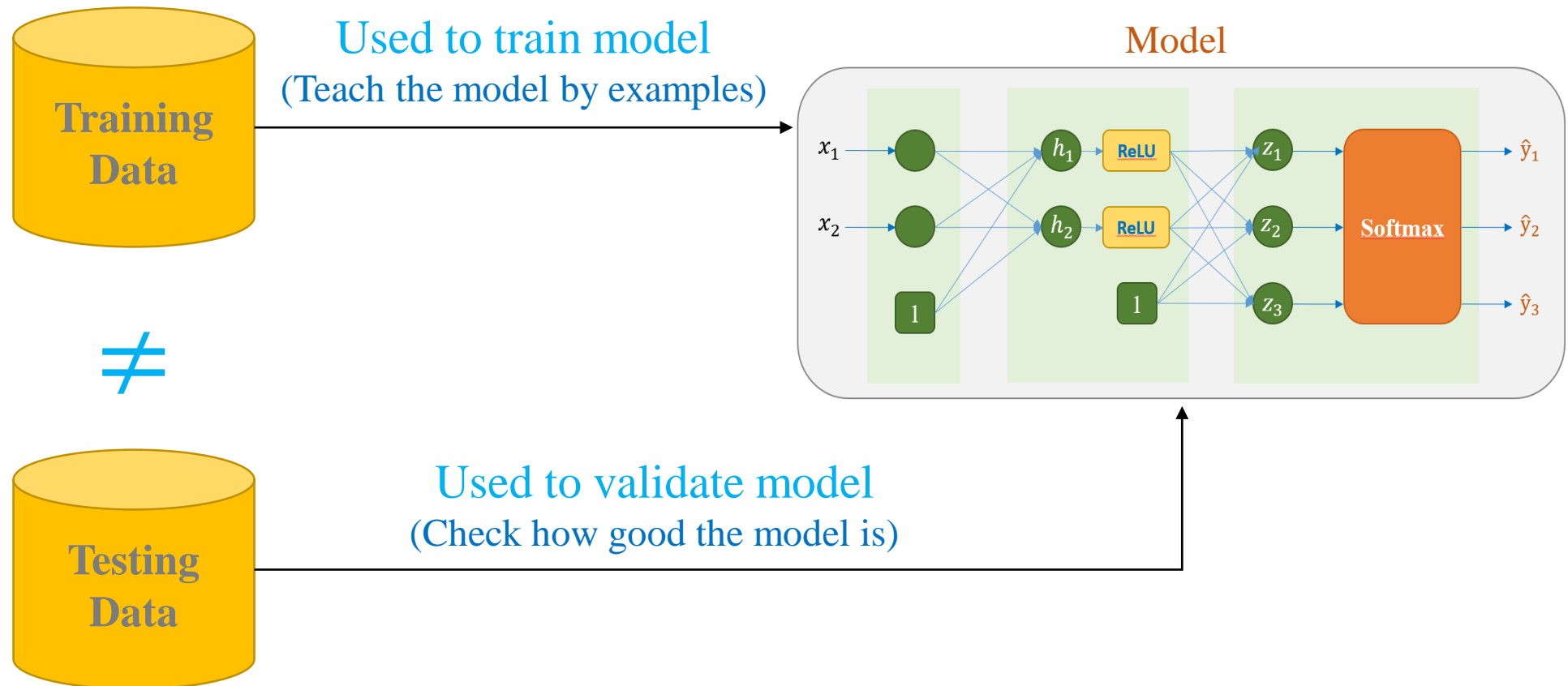


# To-do List for Training



# To-do List for Training

## Data Preparation



# To-do List for Training

## Data Normalization



Convert to the range [0,1]

$$\text{Image} = \frac{\text{Image}}{255}$$

Convert to the range [-1,1]

$$\text{Image} = \frac{\text{Image}}{127.5} - 1$$

Z-score normalization

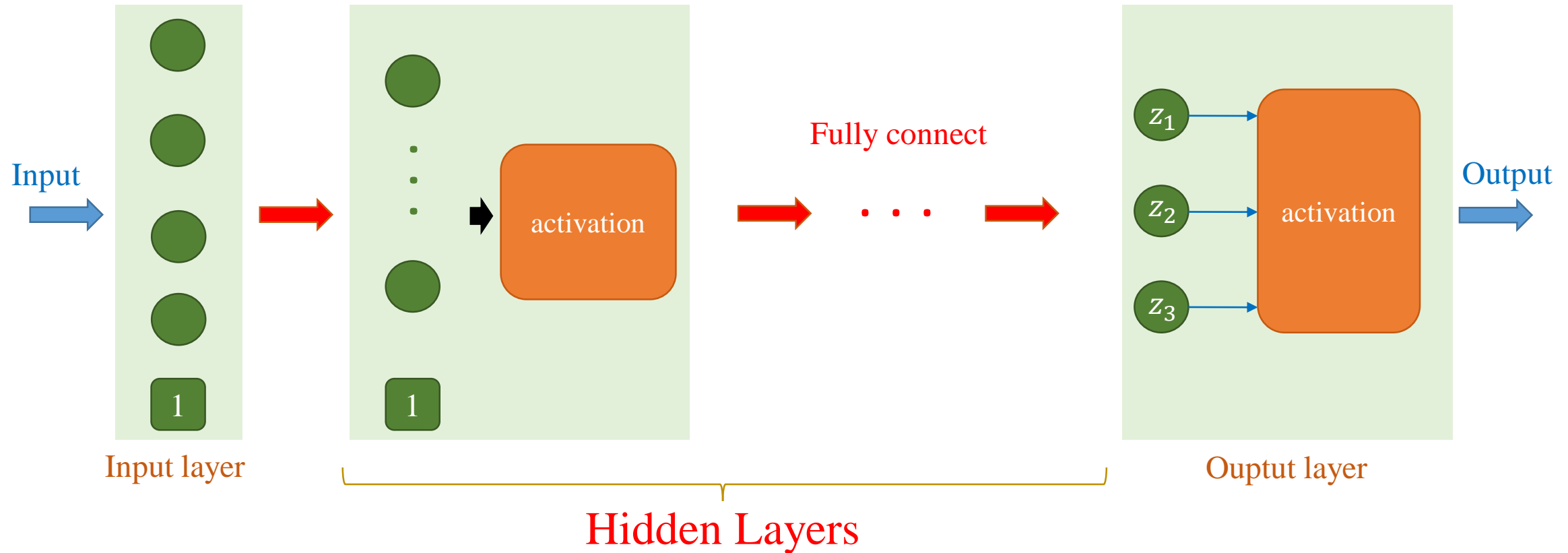
$$\text{Image} = \frac{\text{Image} - \mu}{\sigma}$$

$\mu$  is the mean of  
the image (or training data)

$\sigma$  is the standard deviation  
of the image (or training data)

# To-do List for Training

## Model (Network) Construction



How many hidden layers?  
How many nodes in a hidden layer?

Which activation function?  
Which network components?

# To-do List for Training

## Model (Network) Construction

Which activation function?

$$\tanh(x) = \frac{2}{1 + e^{-2x}} - 1$$

$$\text{sigmoid}(x) = \frac{1}{1 + e^{-x}}$$

$$\text{ELU}(x) = \begin{cases} \alpha(e^x - 1) & \text{if } x < 0 \\ x & \text{if } x \geq 0 \end{cases}$$

$$\text{PReLU}(x) = \begin{cases} \alpha x & \text{if } x < 0 \\ x & \text{if } x \geq 0 \end{cases}$$

$$\text{softplus}(x) = \log(1 + e^x)$$

# To-do List for Training

## ❖ Tanh function

$$\tanh(x) = \frac{2}{1 + e^{-2x}} - 1$$

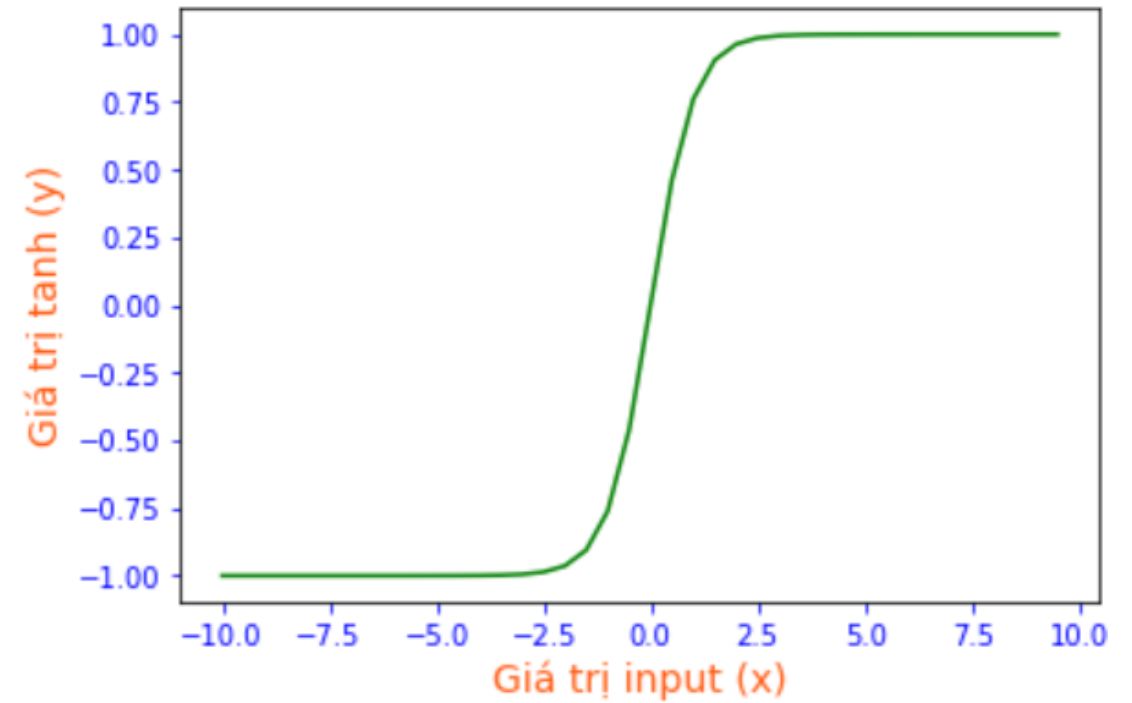
data =

1	5	-4	3	-2
---	---	----	---	----

data\_a = **tanh**(data)

data\_a =

0.761	0.999	-0.999	0.995	-0.964
-------	-------	--------	-------	--------



# To-do List for Training

## ❖ Sigmoid function

$$\text{sigmoid}(x) = \frac{1}{1 + e^{-x}}$$

data =

1

5

-4

3

-2

data\_a = sigmoid(data)

data\_a =

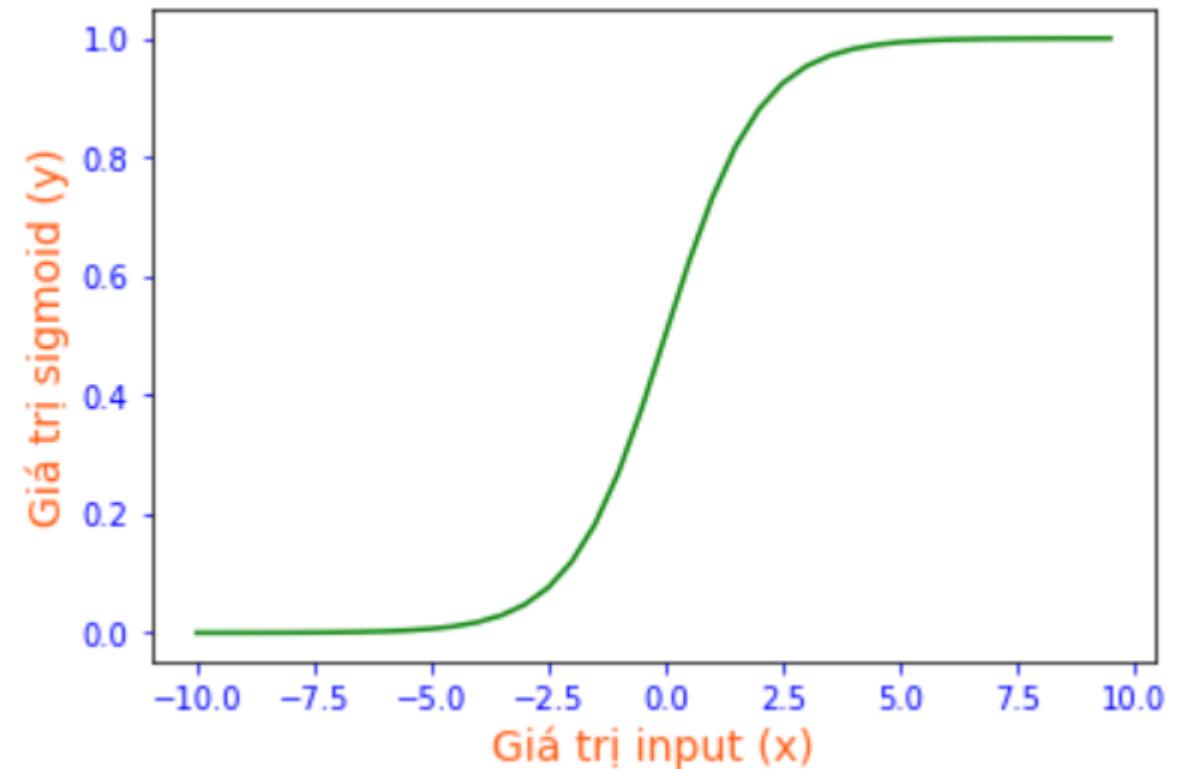
0.731

0.993

0.017

0.95

0.119



# To-do List for Training

## ❖ PReLU function

$$\text{PReLU}(x) = \begin{cases} \alpha x & \text{if } x < 0 \\ x & \text{if } x \geq 0 \end{cases}$$

**data =**

1	5	-4	3	-2
---	---	----	---	----

**data\_a = PReLU(data)**

**data\_a =**

1	5	-0.4	3	-0.2
---	---	------	---	------





# To-do List for Training

## ❖ ELU function

$$\text{ELU}(x) = \begin{cases} \alpha(e^x - 1) & \text{if } x < 0 \\ x & \text{if } x \geq 0 \end{cases}$$

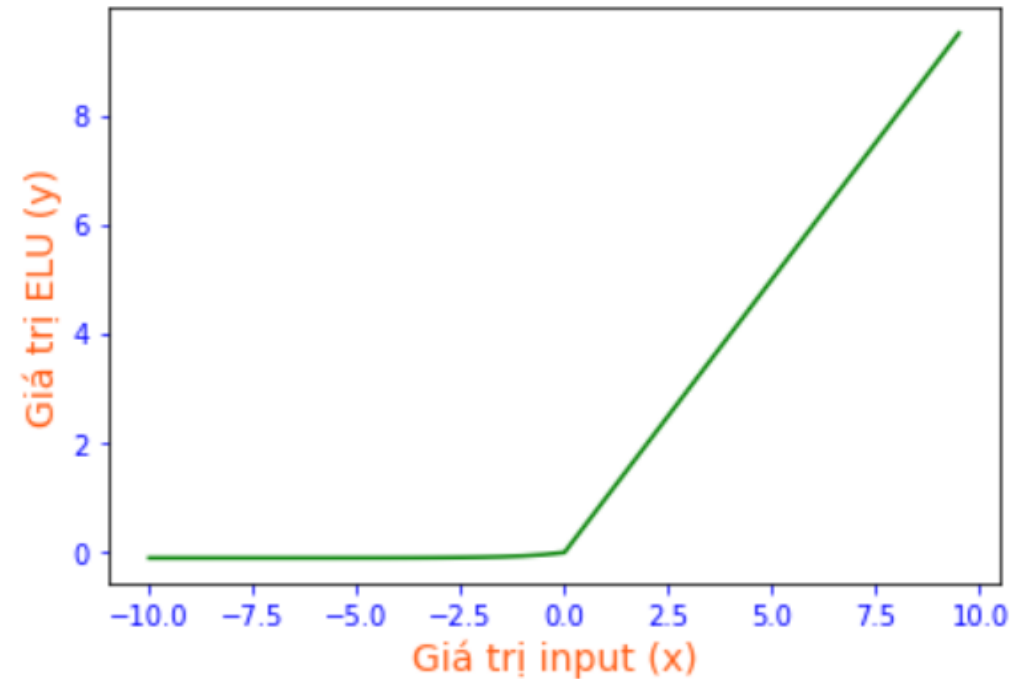
data =

1	5	-4	3	-2
---	---	----	---	----

data\_a = ELU(data)

data\_a =

1	5	-0.098	3	-0.086
---	---	--------	---	--------



# To-do List for Training

## ❖ Softplus function

$$\text{softplus}(x) = \log(1 + e^x)$$

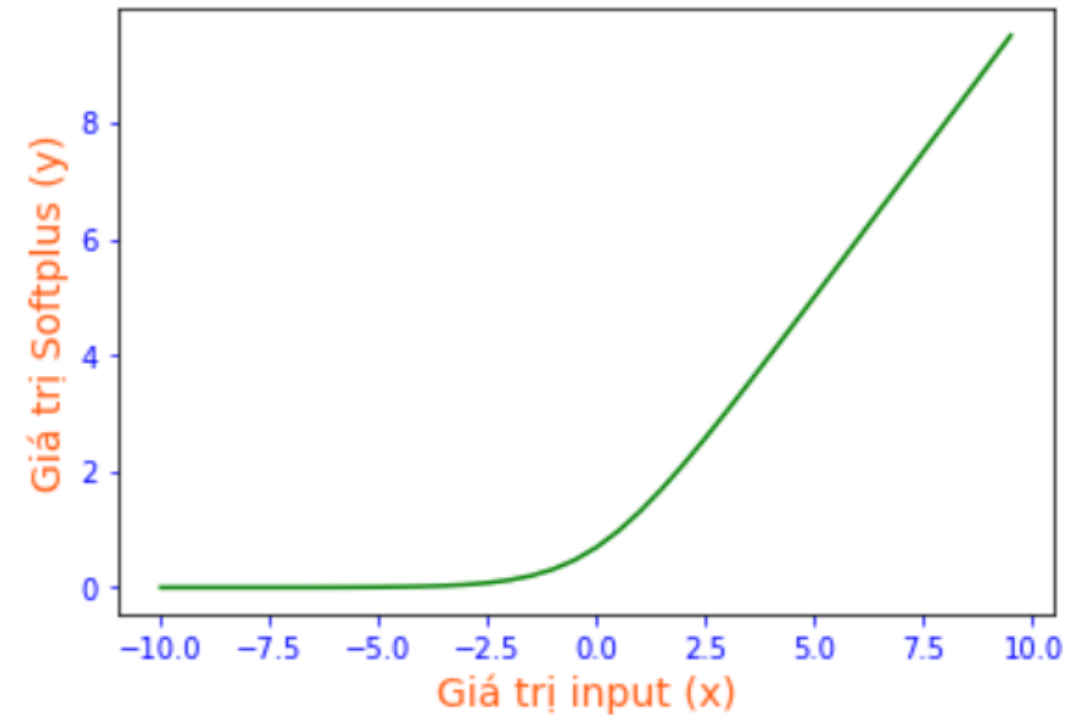
**data =**

1	5	-4	3	-2
---	---	----	---	----

**data\_a = softplus(data)**

**data\_a =**

1.313	5.006	0.018	3.048	0.126
-------	-------	-------	-------	-------



# To-do List for Training

## ❖ ReLU function

$$\text{ReLU}(x) = \begin{cases} 0 & \text{if } x < 0 \\ x & \text{if } x \geq 0 \end{cases}$$

**data =**

1

5

-4

3

-2

**data\_a = ReLU(data)**

**data\_a =**

1

5

0

3

0



# To-do List for Training

## Model (Network) Construction

Which network components?

Dropout

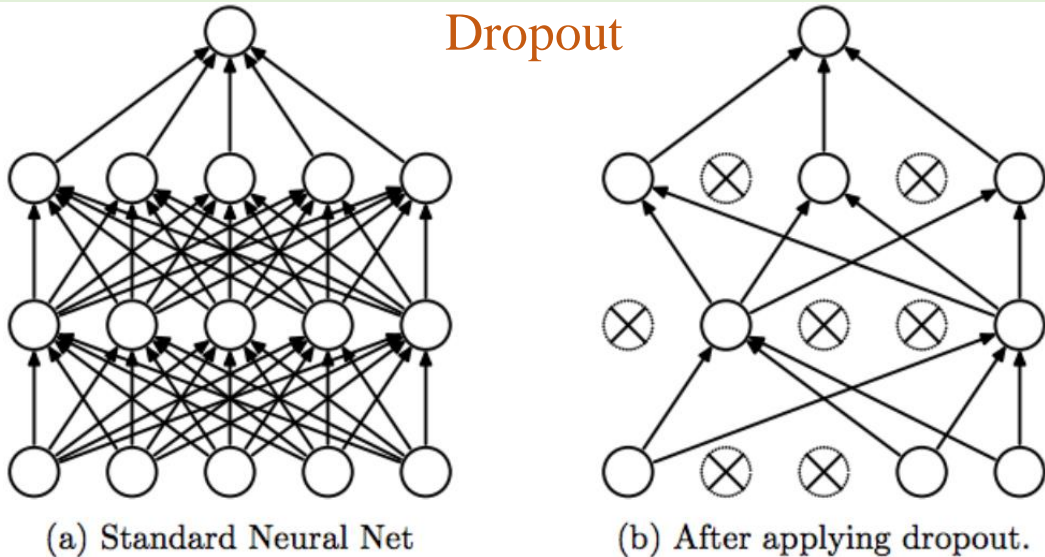


Figure is from (1)

## Batch Normalization

**Input:** Values of  $x$  over a mini-batch:  $\mathcal{B} = \{x_{1...m}\}$ ;  
Parameters to be learned:  $\gamma, \beta$

**Output:**  $\{y_i = \text{BN}_{\gamma, \beta}(x_i)\}$

$$\mu_{\mathcal{B}} \leftarrow \frac{1}{m} \sum_{i=1}^m x_i \quad // \text{ mini-batch mean}$$

$$\sigma_{\mathcal{B}}^2 \leftarrow \frac{1}{m} \sum_{i=1}^m (x_i - \mu_{\mathcal{B}})^2 \quad // \text{ mini-batch variance}$$

$$\hat{x}_i \leftarrow \frac{x_i - \mu_{\mathcal{B}}}{\sqrt{\sigma_{\mathcal{B}}^2 + \epsilon}} \quad // \text{ normalize}$$

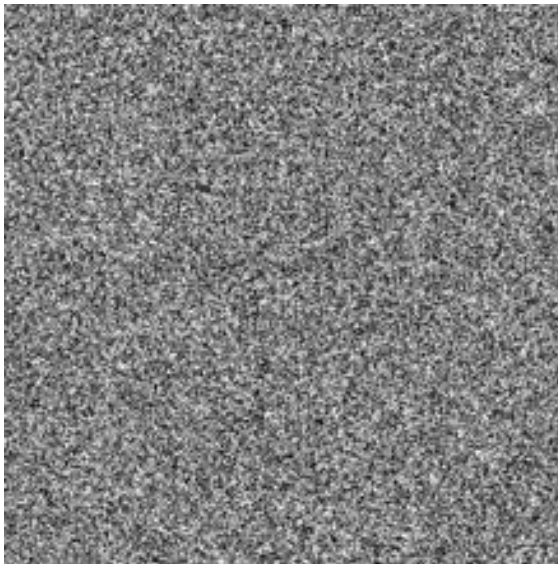
$$y_i \leftarrow \gamma \hat{x}_i + \beta \equiv \text{BN}_{\gamma, \beta}(x_i) \quad // \text{ scale and shift}$$

(1) <https://medium.com/@amarbudhiraja/https-medium-com-amarbudhiraja-learning-less-to-learn-better-dropout-in-deep-machine-learning-74334da4bfc5>

# To-do List for Training

## Parameter Initialization

### Random Initialization



<https://en.wikipedia.org/wiki/Randomness>

#### initializers

##### Overview

deserialize  
get  
GlorotNormal  
GlorotUniform  
he\_normal  
he\_uniform  
Identity  
Initializer  
lecun\_normal  
lecun\_uniform  
Orthogonal  
serialize  
TruncatedNormal  
VarianceScaling

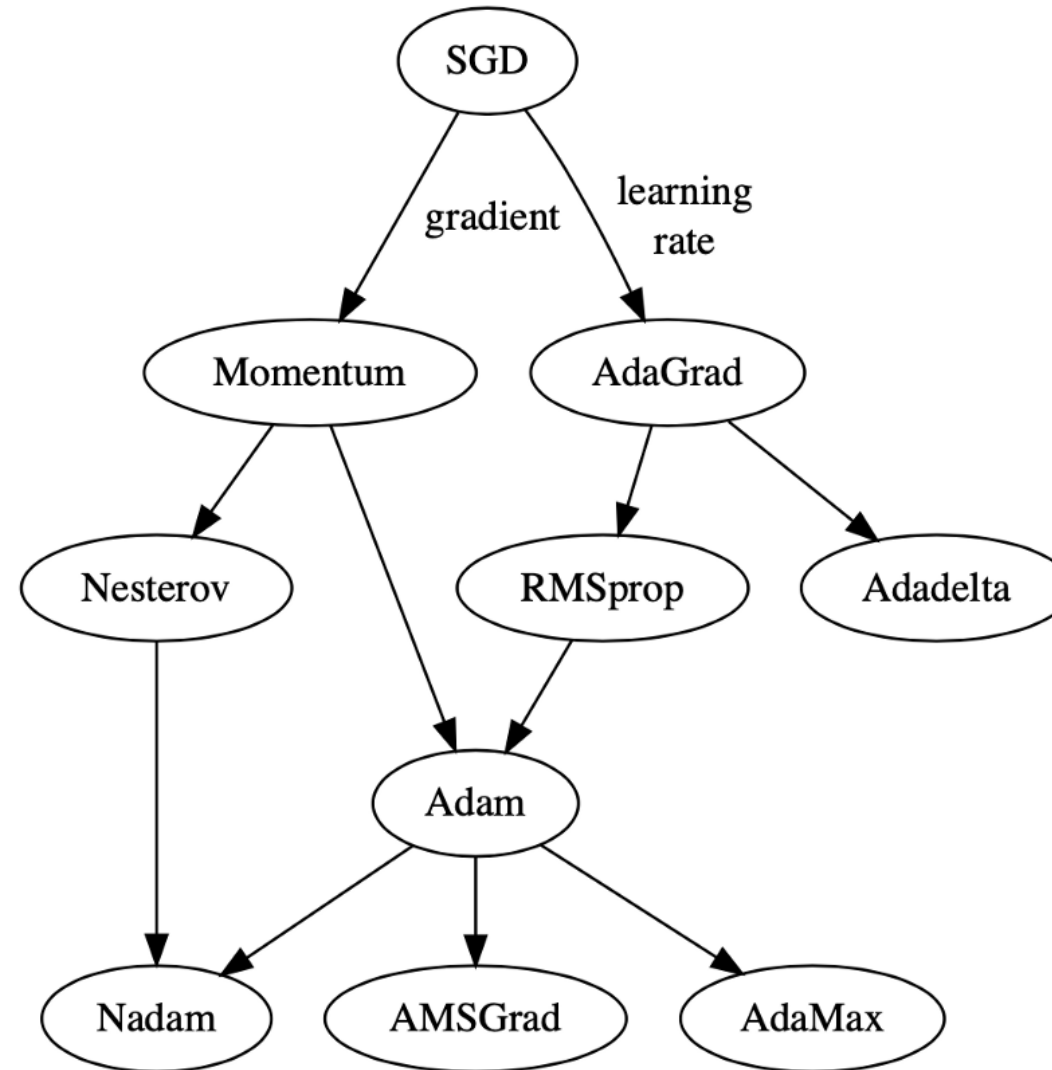
Initialization method  
supported in Tensorflow

[https://www.tensorflow.org/api\\_docs/python/tf/keras/initializers](https://www.tensorflow.org/api_docs/python/tf/keras/initializers)

# To-do List for Training

## Optimizer Selection

Define a way to update parameters



# To-do List for Training

## Loss function Selection

Compute the goodness of the current model

Useful for training

[https://www.tensorflow.org/api\\_docs/python/tf/keras/losses](https://www.tensorflow.org/api_docs/python/tf/keras/losses)

`class BinaryCrossentropy` : Computes the cross-entropy loss between true labels and predicted labels.

`class CategoricalCrossentropy` : Computes the crossentropy loss between the labels and predictions.

`class CategoricalHinge` : Computes the categorical hinge loss between `y_true` and `y_pred` .

`class CosineSimilarity` : Computes the cosine similarity between `y_true` and `y_pred` .

`class Hinge` : Computes the hinge loss between `y_true` and `y_pred` .

`class Huber` : Computes the Huber loss between `y_true` and `y_pred` .

`class KLDivergence` : Computes Kullback-Leibler divergence loss between `y_true` and `y_pred` .

`class LogCosh` : Computes the logarithm of the hyperbolic cosine of the prediction error.

`class Loss` : Loss base class.

`class MeanAbsoluteError` : Computes the mean of absolute difference between labels and predictions.

`class MeanAbsolutePercentageError` : Computes the mean absolute percentage error between `y_true` and `y_pred` .

`class MeanSquaredError` : Computes the mean of squares of errors between labels and predictions.

`class MeanSquaredLogarithmicError` : Computes the mean squared logarithmic error between `y_true` and `y_pred` .

`class Poisson` : Computes the Poisson loss between `y_true` and `y_pred` .

`class Reduction` : Types of loss reduction.

`class SparseCategoricalCrossentropy` : Computes the crossentropy loss between the labels and predictions.

`class SquaredHinge` : Computes the squared hinge loss between `y_true` and `y_pred` .

# To-do List for Training

## Metric Selection

Compute the goodness of the current model

Useful for developers

Precision True Positives False Positives

True Negatives Recall

False Negatives Accuracy

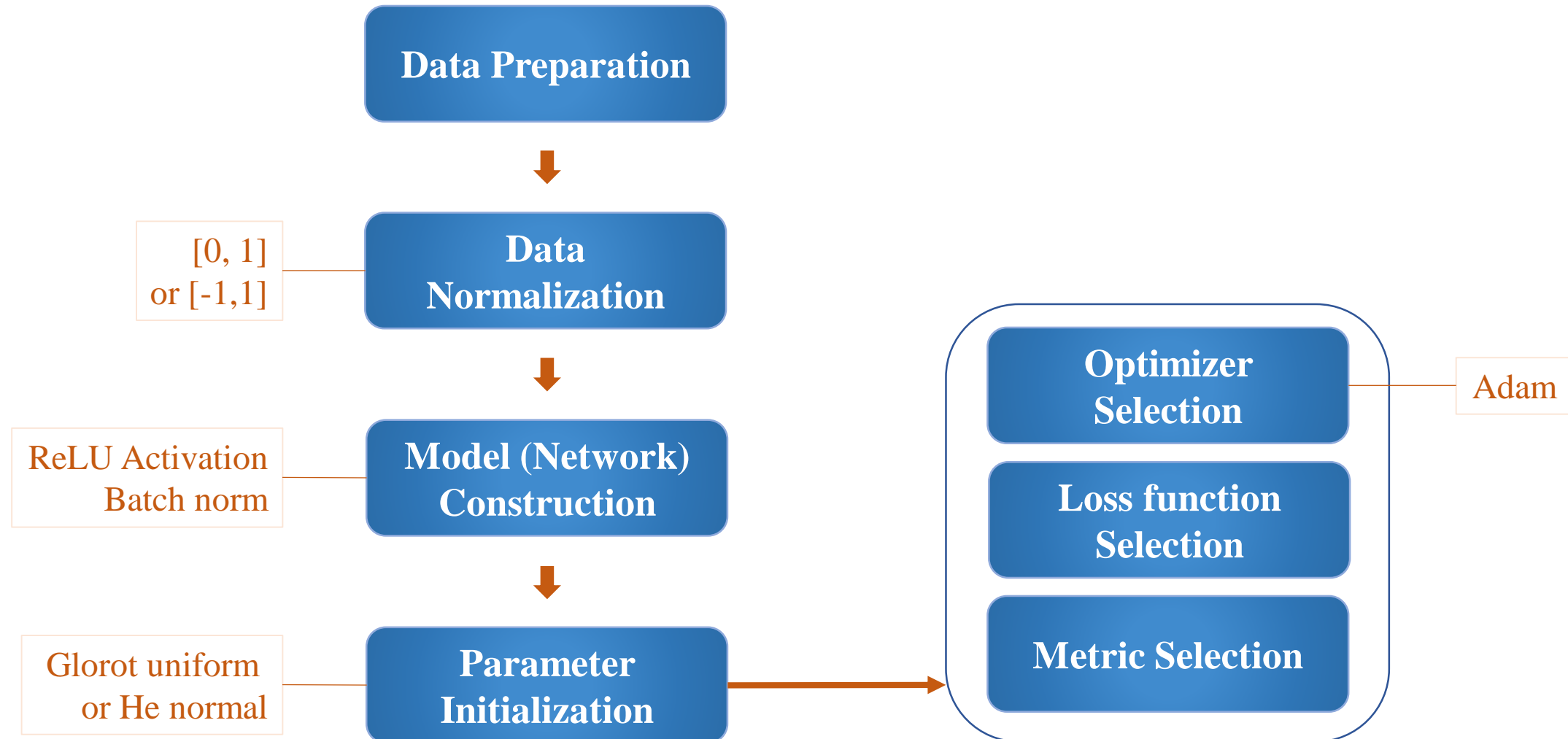
Root Mean Squared Error

Precision At Recall Mean Absolute Error



# To-do List for Training

## Recommendation



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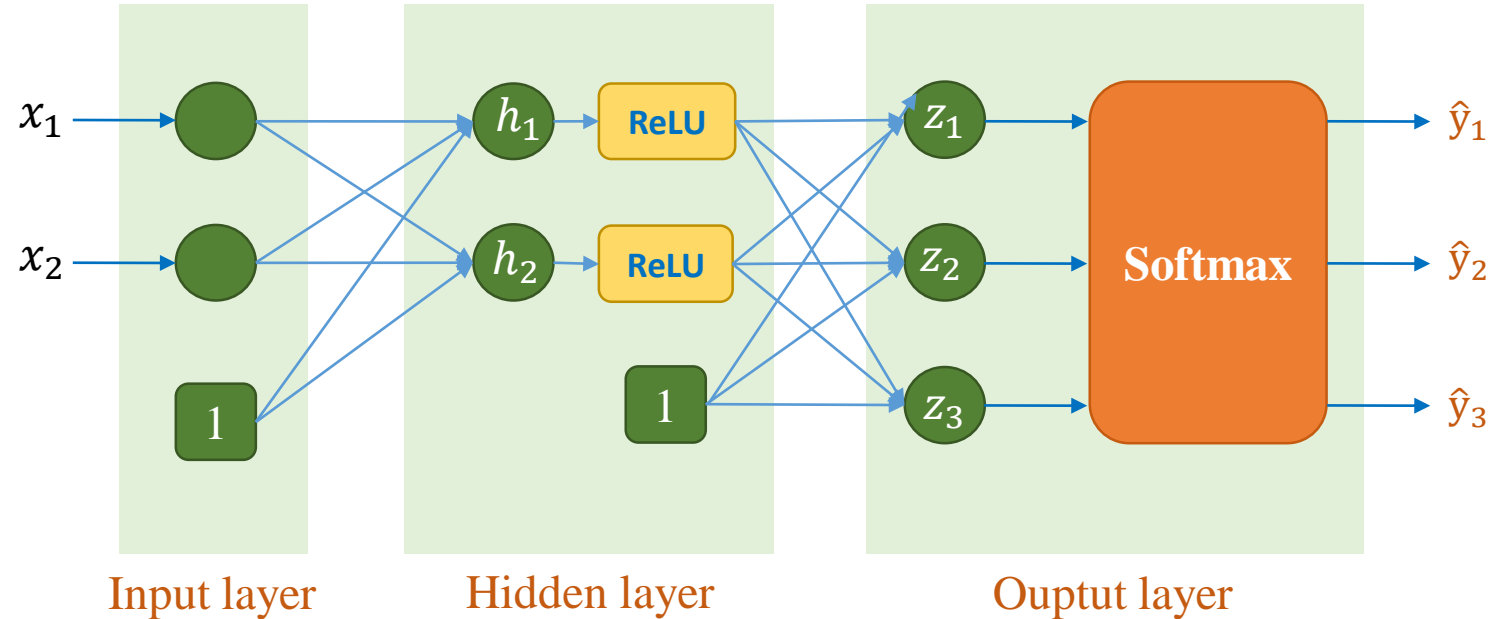
# Example

Feature		Label
Petal Length	Petal Width	Label
1.5	0.2	0
1.4	0.2	0
1.6	0.2	0
4.7	1.6	1
3.3	1.1	1
4.6	1.3	1
5.6	2.2	2
5.1	1.5	2
5.6	1.4	2

$$x = [x^{(1)} \quad x^{(2)} \quad x^{(3)}]$$

$$x = \begin{bmatrix} 1.5 & 4.7 & 5.6 \\ 0.2 & 1.6 & 2.2 \end{bmatrix}$$

$$y = \begin{bmatrix} 0 \\ 1 \\ 2 \end{bmatrix}$$



$$W_h = [W_{h1} \quad W_{h2}]$$

$$= \begin{bmatrix} 0.0 & 0.0 \\ 0.86 & -1.04 \\ 0.41 & -0.65 \end{bmatrix}$$

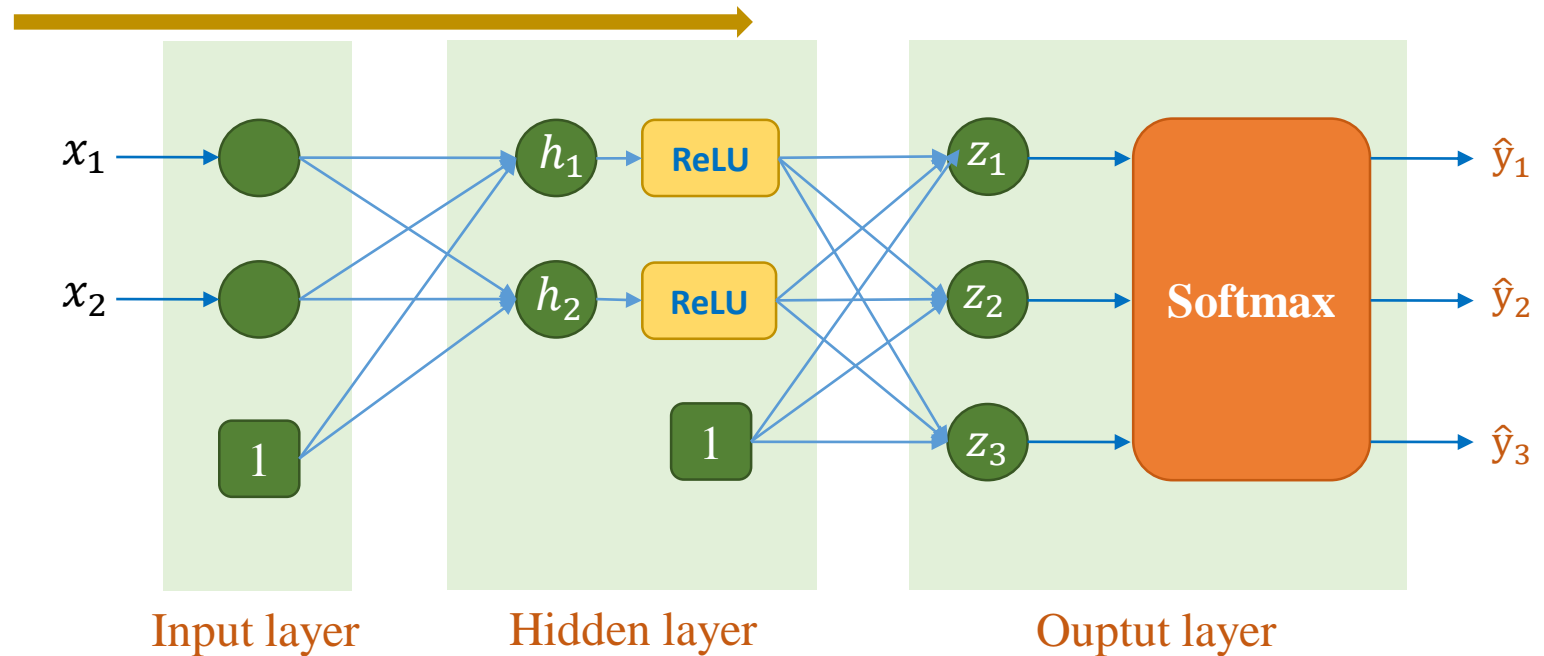
$$W_z = [W_{z1} \quad W_{z2} \quad W_{z3}]$$

$$= \begin{bmatrix} 0.0 & 0.0 & 0.0 \\ 0.32 & 0.25 & 0.14 \\ -0.47 & -1.06 & 0.063 \end{bmatrix}$$

$$\mathbf{h} = \mathbf{W}_h^T \mathbf{x} = \begin{bmatrix} 0.0 & 0.86 & 0.41 \\ 0.0 & -1.04 & -0.65 \end{bmatrix} \begin{bmatrix} 1 & 1 & 1 \\ 1.5 & 4.7 & 5.6 \\ 0.2 & 1.6 & 2.2 \end{bmatrix} = \begin{bmatrix} 1.373 & 4.708 & 5.731 \\ -1.696 & -5.951 & -7.281 \end{bmatrix}$$

$$\text{ReLU}(\mathbf{h}) = \begin{bmatrix} 1.373 & 4.708 & 5.731 \\ 0.0 & 0.0 & 0.0 \end{bmatrix}$$

Feature		Label
Petal Length	Petal Width	Label
1.5	0.2	0
1.4	0.2	0
1.6	0.2	0
4.7	1.6	1
3.3	1.1	1
4.6	1.3	1
5.6	2.2	2
5.1	1.5	2
5.6	1.4	2



$$\mathbf{x} = [\mathbf{x}^{(1)} \quad \mathbf{x}^{(2)} \quad \mathbf{x}^{(3)}]$$

$$= \begin{bmatrix} 1 & 1 & 1 \\ 1.5 & 4.7 & 5.6 \\ 0.2 & 1.6 & 2.2 \end{bmatrix}$$

$$\mathbf{y} = \begin{bmatrix} 0 \\ 1 \\ 2 \end{bmatrix}$$

$$\mathbf{W}_h = [\mathbf{W}_{h1} \quad \mathbf{W}_{h2}]$$

$$= \begin{bmatrix} 0.0 & 0.0 \\ 0.86 & -1.04 \\ 0.41 & -0.65 \end{bmatrix}$$

$$\mathbf{W}_z = [\mathbf{W}_{z1} \quad \mathbf{W}_{z2} \quad \mathbf{W}_{z3}]$$

$$= \begin{bmatrix} 0.0 & 0.0 & 0.0 \\ 0.32 & 0.25 & 0.14 \\ -0.47 & -1.06 & 0.063 \end{bmatrix}$$

$$\text{ReLU}(\mathbf{h}) = \begin{bmatrix} 1.373 & 4.708 & 5.731 \\ 0.0 & 0.0 & 0.0 \end{bmatrix}$$

$$\begin{bmatrix} \mathbf{1} \\ \text{ReLU}(\mathbf{h}) \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 \\ 1.373 & 4.708 & 5.731 \\ 0.0 & 0.0 & 0.0 \end{bmatrix}$$

$$\mathbf{z} = \mathbf{W}_z^T \begin{bmatrix} \mathbf{1} \\ \text{ReLU}(\mathbf{h}) \end{bmatrix} = \begin{bmatrix} 0.0 & 0.32 & -0.47 \\ 0.0 & 0.25 & -1.06 \\ 0.0 & 0.14 & 0.063 \end{bmatrix} \begin{bmatrix} 1 & 1 & 1 \\ 1.373 & 4.708 & 5.731 \\ 0.0 & 0.0 & 0.0 \end{bmatrix}$$

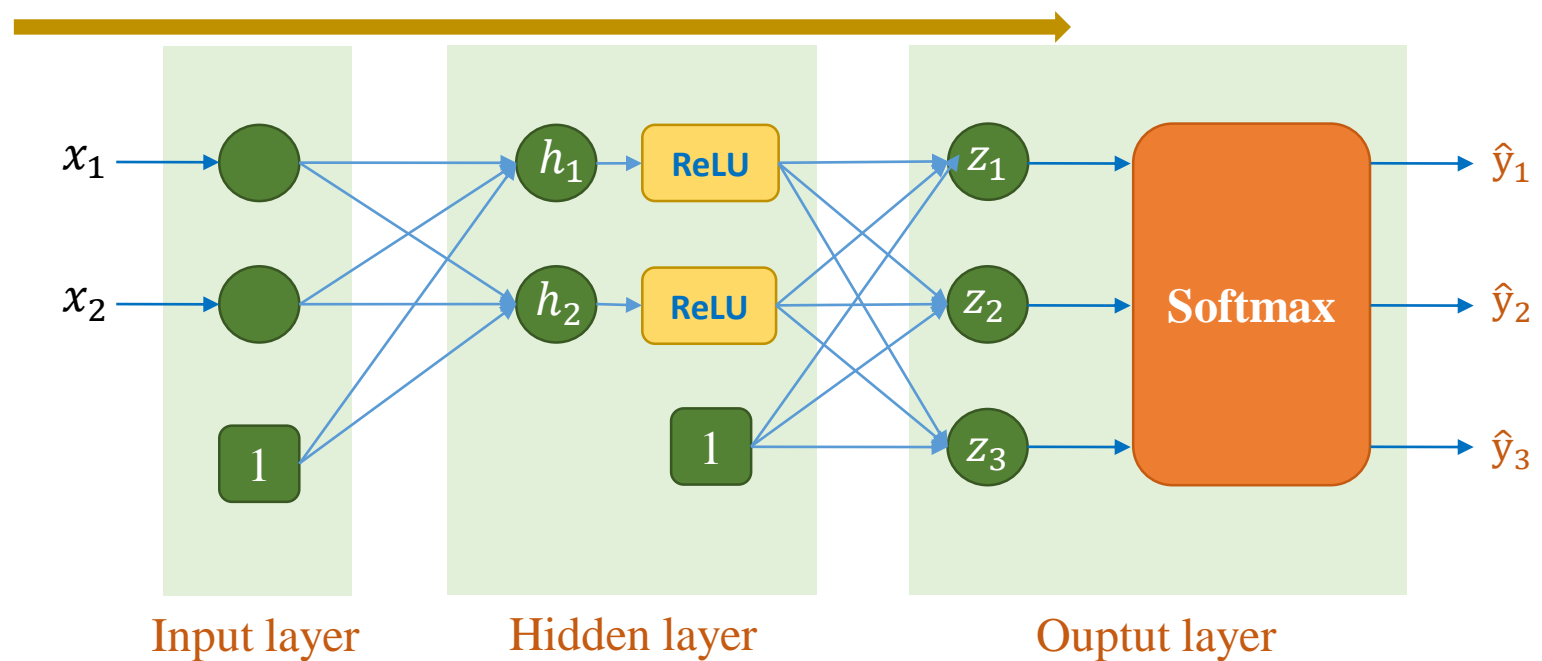
$$= \begin{bmatrix} 0.439 & 1.507 & 1.835 \\ 0.356 & 1.220 & 1.485 \\ 0.195 & 0.670 & 0.816 \end{bmatrix}$$

Feature		Label
Petal Length	Petal Width	Label
1.5	0.2	0
1.4	0.2	0
1.6	0.2	0
4.7	1.6	1
3.3	1.1	1
4.6	1.3	1
5.6	2.2	2
5.1	1.5	2
5.6	1.4	2

$$\mathbf{x} = [\mathbf{x}^{(1)} \quad \mathbf{x}^{(2)} \quad \mathbf{x}^{(3)}]$$

$$= \begin{bmatrix} 1 & 1 & 1 \\ 1.5 & 4.7 & 5.6 \\ 0.2 & 1.6 & 2.2 \end{bmatrix}$$

$$\mathbf{y} = \begin{bmatrix} 0 \\ 1 \\ 2 \end{bmatrix}$$



$$\mathbf{W}_h = [\mathbf{W}_{h1} \quad \mathbf{W}_{h2}]$$

$$= \begin{bmatrix} 0.0 & 0.0 \\ 0.86 & -1.04 \\ 0.41 & -0.65 \end{bmatrix}$$

$$\mathbf{W}_z = [\mathbf{W}_{z1} \quad \mathbf{W}_{z2} \quad \mathbf{W}_{z3}]$$

$$= \begin{bmatrix} 0.0 & 0.0 & 0.0 \\ 0.32 & 0.25 & 0.14 \\ -0.47 & -1.06 & 0.063 \end{bmatrix}$$

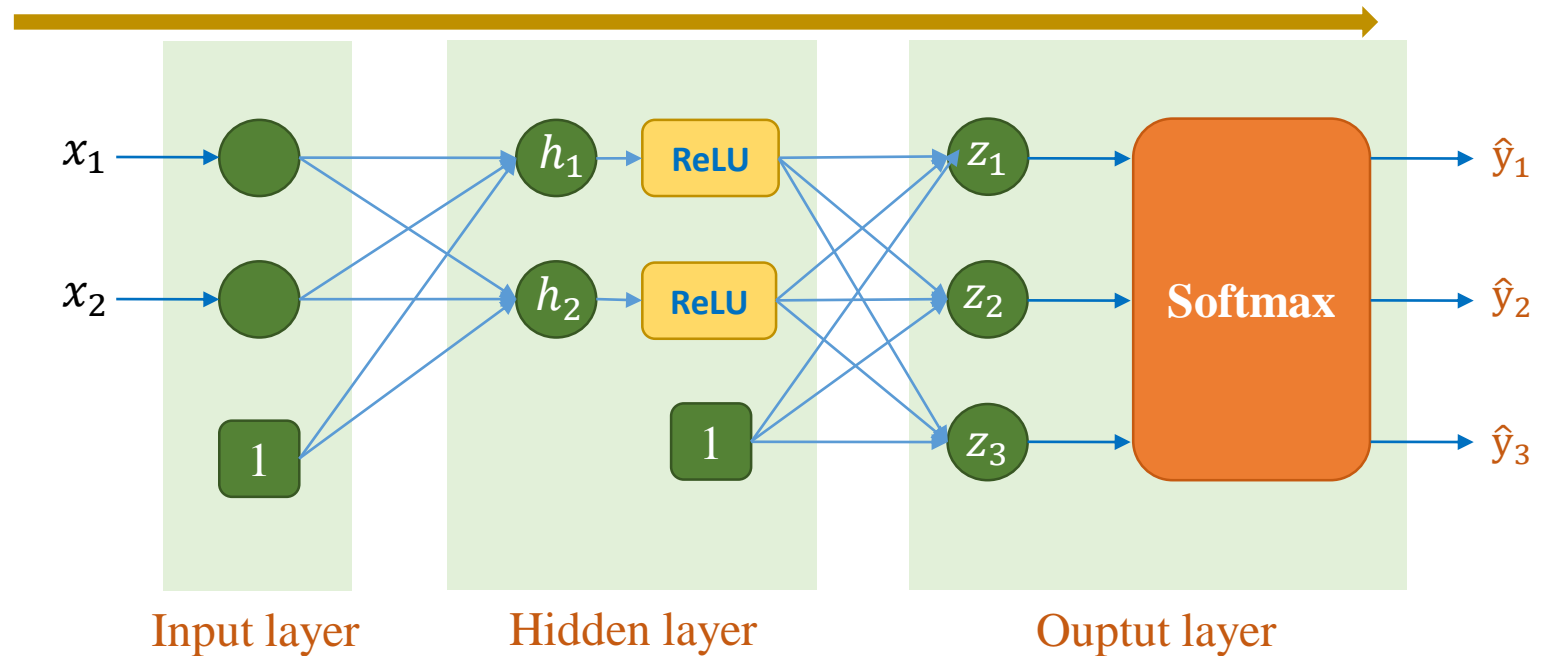
$$\mathbf{z} = \begin{bmatrix} 0.439 & 1.507 & 1.835 \\ 0.356 & 1.220 & 1.485 \\ 0.195 & 0.670 & 0.816 \end{bmatrix}$$

$$\begin{aligned} \hat{\mathbf{y}} = \text{softmax}(\mathbf{z}) &= \begin{bmatrix} \hat{y}^{(1)} & \hat{y}^{(2)} & \hat{y}^{(3)} \end{bmatrix} \\ &= \begin{bmatrix} 0.369 & 0.458 & 0.484 \\ 0.340 & 0.343 & 0.341 \\ 0.289 & 0.198 & 0.174 \end{bmatrix} \end{aligned}$$

$$\text{loss} = 1.269$$

Feature		Label
Petal Length	Petal Width	Label
1.5	0.2	0
1.4	0.2	0
1.6	0.2	0
4.7	1.6	1
3.3	1.1	1
4.6	1.3	1
5.6	2.2	2
5.1	1.5	2
5.6	1.4	2

$$\begin{aligned} \mathbf{x} &= [\mathbf{x}^{(1)} \quad \mathbf{x}^{(2)} \quad \mathbf{x}^{(3)}] \\ &= \begin{bmatrix} 1 & 1 & 1 \\ 1.5 & 4.7 & 5.6 \\ 0.2 & 1.6 & 2.2 \end{bmatrix} \end{aligned} \quad \mathbf{y} = \begin{bmatrix} 0 \\ 1 \\ 2 \end{bmatrix}$$



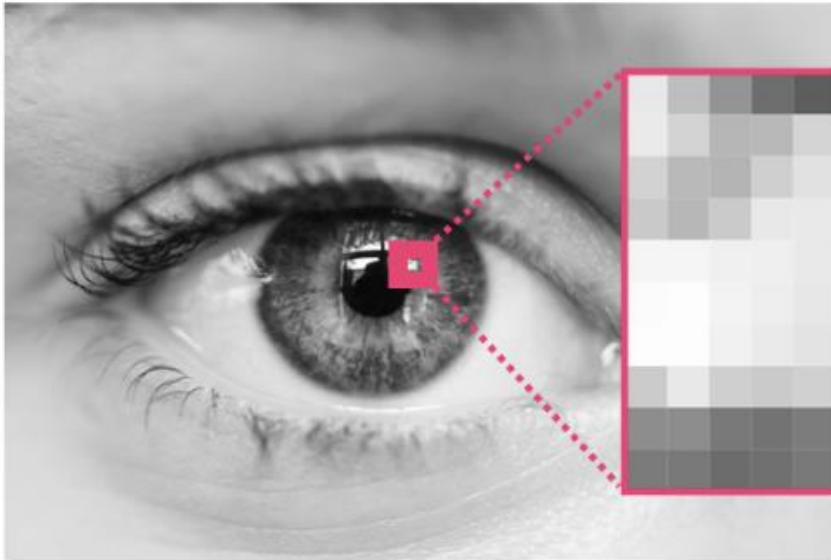
$$\begin{aligned} \mathbf{W}_h &= [\mathbf{W}_{h1} \quad \mathbf{W}_{h2}] & \mathbf{W}_z &= [\mathbf{W}_{z1} \quad \mathbf{W}_{z2} \quad \mathbf{W}_{z3}] \\ &= \begin{bmatrix} 0.0 & 0.0 \\ 0.86 & -1.04 \\ 0.41 & -0.65 \end{bmatrix} & &= \begin{bmatrix} 0.0 & 0.0 & 0.0 \\ 0.32 & 0.25 & 0.14 \\ -0.47 & -1.06 & 0.063 \end{bmatrix} \end{aligned}$$

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# Image Classification: Image Data

## ❖ Grayscale images



230	194	147	108	90	98	84	96	91	101
237	206	188	195	207	213	163	123	116	128
210	183	180	205	224	234	188	122	134	147
198	189	201	227	229	232	200	125	127	135
249	241	237	244	232	226	202	116	125	126
251	254	241	239	230	217	196	102	103	99
243	255	240	231	227	214	203	116	95	91
204	231	208	200	207	201	200	121	95	95
144	140	120	115	125	127	143	118	92	91
121	121	108	109	122	121	134	106	86	97

(Height, Width)

Pixel  $p$  = scalar

$$0 \leq p \leq 255$$

Resolution: #pixels

Resolution = Height $\times$ Width





# Image Data

## Fashion-MNIST dataset

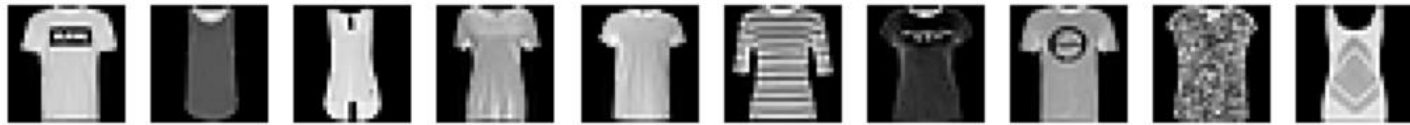
Grayscale images

Resolution=28x28

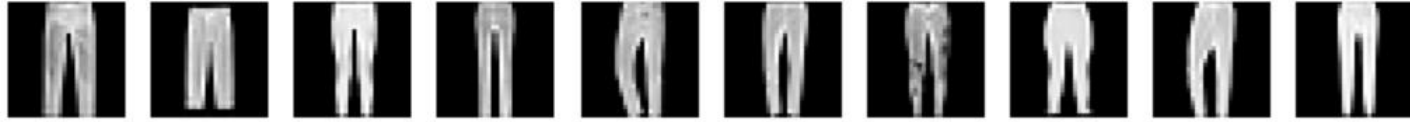
Training set: 60000 samples

Testing set: 10000 samples

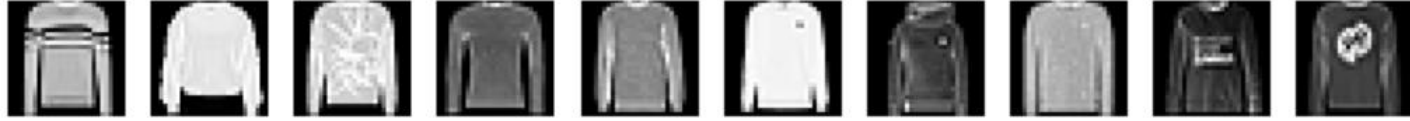
T-shirt



Trouser



Pullover



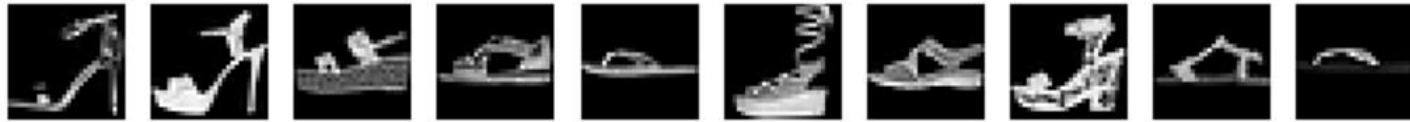
Dress



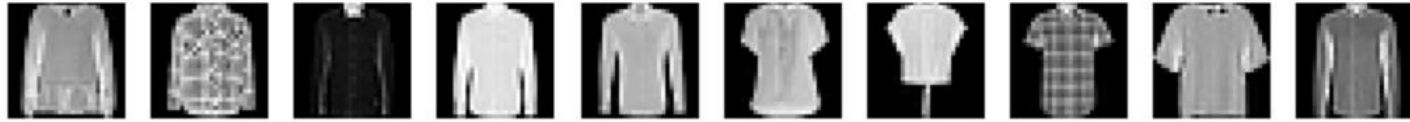
Coat



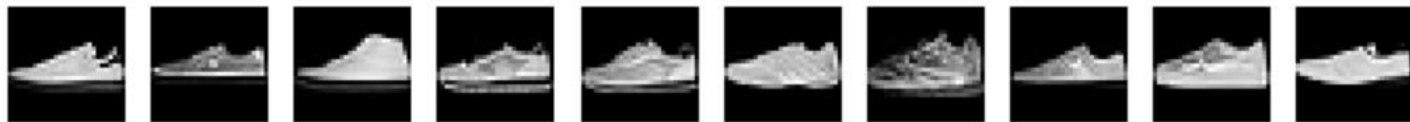
Sandal



Shirt



Sneaker



Bag







Ankle  
Boot



# Image Classification

## ❖ Fashion-MNIST data

### Download data

Name	Size
 t10k-images-idx3-ubyte.gz	4.4 MB
 t10k-labels-idx1-ubyte.gz	5.1 kB
 train-images-idx3-ubyte.gz	26.4 MB
 train-labels-idx1-ubyte.gz	29.5 kB

```
1 import numpy as np
2 from urllib import request
3 import gzip
4 import pickle
5
6 filename = ["training_images", "train-images-idx3-ubyte.gz"],
7            ["test_images", "train-labels-idx1-ubyte.gz"],
8            ["training_labels", "t10k-images-idx3-ubyte.gz"],
9            ["test_labels", "t10k-labels-idx1-ubyte.gz"]]
10
11 # function to download data
12 def download_fashion_mnist(folder):
13     base_url = "http://fashion-mnist.s3-website.eu-central-1.amazonaws.com/"
14     for name in filename:
15         print("Downloading " + name[1] + "...")
16
17         # lưu vào folder data_fashion_mnist
18         request.urlretrieve(base_url + name[1], folder + name[1])
19     print("Download complete.")
20
21 # download dataset và save to folder 'data_fashion_mnist/'
22 folder = 'data_fashion_mnist/'
23 download_fashion_mnist(folder)
```

# Image Classification

## Fashion-MNIST data

```
X_train: (60000, 784)
y_train: (60000,)
X_test: (10000, 784)
y_test: (10000,)
```



784

### Read data

```
1 import os
2 import gzip
3 import numpy as np
4
5 def load_fashion_mnist(path, kind='train'):
6     """Load fashion_MNIST data from `path`"""
7     labels_path = os.path.join(path, '%s-labels-idx1-ubyte.gz' % kind)
8     images_path = os.path.join(path, '%s-images-idx3-ubyte.gz' % kind)
9
10    with gzip.open(labels_path, 'rb') as lbpath:
11        labels = np.frombuffer(lbpath.read(), dtype=np.uint8, offset=8)
12    with gzip.open(images_path, 'rb') as imgpath:
13        images = np.frombuffer(imgpath.read(),
14                                dtype=np.uint8, offset=16).reshape(len(labels), 784)
15
16    return images, labels
17
18
19 X_train, y_train = load_fashion_mnist('C:/Data/data_fashion_mnist/')
20 print('X_train:', X_train.shape)
21 print('y_train:', y_train.shape)
22
23 X_test, y_test = load_fashion_mnist('C:/Data/data_fashion_mnist/', kind='t10k')
24 print('X_test:', X_test.shape)
25 print('y_test:', y_test.shape)
```

# Image Classification

## Fashion-MNIST data

```
X_train: (60000, 784)
y_train: (60000,)
X_test: (10000, 784)
y_test: (10000,)
```

```
1 import tensorflow as tf
2 import tensorflow.keras as keras
3
4 # create model
5 model = keras.Sequential()
6 model.add(keras.Input(shape=(784,)))
7 model.add(keras.layers.Dense(128, activation='sigmoid'))
8 model.add(keras.layers.Dense(10, activation='softmax'))
9
10 # optimizer and loss
11 model.compile(optimizer='sgd',
12               loss='sparse_categorical_crossentropy',
13               metrics=['accuracy'])
14
15 # training
16 model.fit(X_train, y_train, epochs=10)
17
18 # testing
19 test_loss, test_acc = model.evaluate(X_test, y_test, verbose=2)
20 print('Test accuracy:', test_acc)
```

# Image Classification: Another Model

## Fashion-MNIST data

```
1 import tensorflow as tf
2 from tensorflow import keras
3
4 # Data Preparation - Use built-in function for Fashion_MNIST in Tensorflow
5 fashion_mnist = keras.datasets.fashion_mnist
6 (train_images, train_labels), (test_images, test_labels) = fashion_mnist.load_data()
7
8 # Data Normalization [0,1]
9 train_images = train_images / 255.0
10 test_images = test_images / 255.0
11
12 # model: Use relu activation
13 # Glorot uniform is used by default in Tensorflow
14 model = keras.Sequential([
15     keras.layers.Flatten(input_shape=(28, 28)),
16     keras.layers.Dense(128, activation='relu'),
17     keras.layers.Dense(10, activation='softmax')
18 ])
19
20 # Use Adam optimizer, cross-entropy loss and accuracy metric
21 model.compile(optimizer='adam',
22               loss=tf.keras.losses.SparseCategoricalCrossentropy(),
23               metrics=['accuracy'])
24
25 # training
26 model.fit(train_images, train_labels, epochs=20)
27
28 # testing
29 test_loss, test_acc = model.evaluate(test_images, test_labels, verbose=2)
30 print('Test accuracy:', test_acc)
```



# Outline

- **Multi-layer Perceptron**
- **To-do List for Training**
- **Forward Computation Example**
- **Image Classification: Fashion-MNIST**
- **Image Classification: Cifar-10**
- **Underfitting and Overfitting**

# Image Classification

## Cifar-10 dataset

Color images

Resolution=32x32

Training set: 50000 samples

Testing set: 10000 samples

airplane



automobile



bird



cat



deer



dog



frog



horse



ship



truck





# Image Classification

## Cifar-10 dataset

Color images

Resolution=32x32

Training set: 50000 samples

Testing set: 10000 samples

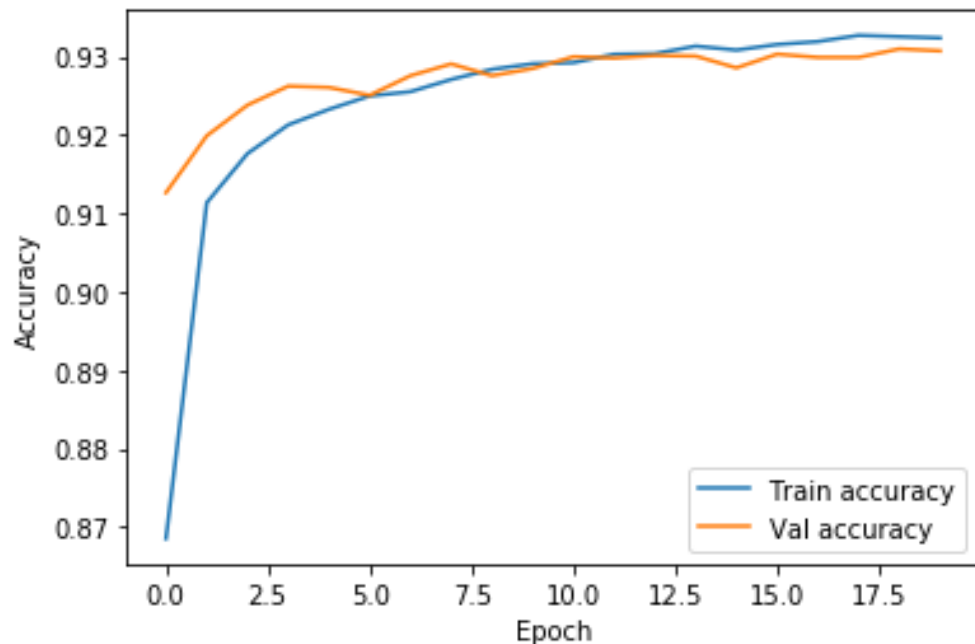
```
1 import tensorflow as tf
2 from tensorflow import keras
3
4 # Data Preparation - Use built-in function for Fashion_MNIST in Tensorflow
5 cifar10 = keras.datasets.cifar10
6 (train_images, train_labels), (test_images, test_labels) = cifar10.load_data()
7
8 # Data Normalization [0,1]
9 train_images = train_images / 255.0
10 test_images = test_images / 255.0
11
12 # model: Use relu activation
13 # Glorot uniform is used by default in Tensorflow
14 model = keras.Sequential([
15     keras.layers.Flatten(input_shape=(32, 32, 3)),
16     keras.layers.Dense(512, activation='relu'),
17     keras.layers.Dense(10, activation='softmax')
18 ])
19
20 # Use Adam optimizer, cross-entropy loss and accuracy metric
21 model.compile(optimizer='adam',
22               loss=tf.keras.losses.SparseCategoricalCrossentropy(),
23               metrics=['accuracy'])
24
25 # training
26 model.fit(train_images, train_labels, epochs=20)
27
28 # testing
29 test_loss, test_acc = model.evaluate(test_images, test_labels, verbose=2)
30 print('Test accuracy:', test_acc)
```

# Outline

- **Multi-layer Perceptron**
- **To-do List for Training**
- **Forward Computation Example**
- **Image Classification: Fashion-MNIST**
- **Image Classification: Cifar-10**
- **Underfitting and Overfitting**

# Underfitting

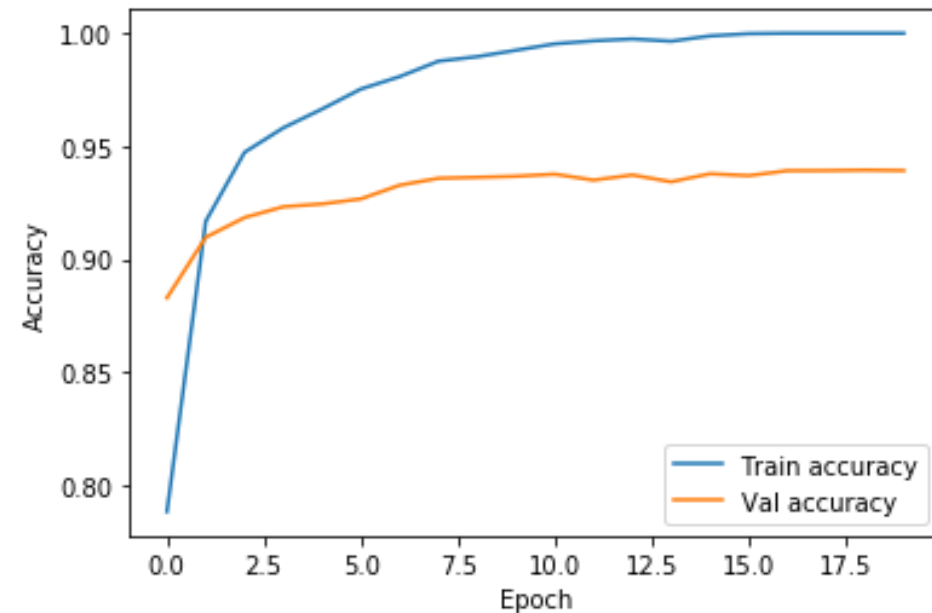
Happen when model is not strong enough



```
1 import tensorflow as tf
2 from tensorflow import keras
3
4 # load data
5 mnist = keras.datasets.fashion_mnist
6 (x_train, y_train), (x_test, y_test) = mnist.load_data()
7
8 # normalize
9 x_train, x_test = x_train / 255.0, x_test / 255.0
10 m_train = x_train.shape[0]
11
12 # model construction
13 model = tf.keras.Sequential([
14     tf.keras.layers.Flatten(input_shape=(28, 28)),
15     tf.keras.layers.Dense(10, activation='softmax')
16 ])
17
18 # compile and train
19 model.compile(optimizer='adam',
20               loss='sparse_categorical_crossentropy',
21               metrics=['accuracy'])
22 history = model.fit(x_train, y_train,
23                     validation_split=0.2, epochs=20, verbose=0)
```

# Overfitting

Model performance is 'quite' different between training and test sets



```
1 import tensorflow as tf
2 from tensorflow import keras
3
4 # load data
5 mnist = keras.datasets.fashion_mnist
6 (x_train, y_train), (x_test, y_test) = mnist.load_data()
7
8 # normalize
9 x_train, x_test = x_train / 255.0, x_test / 255.0
10 m_train = x_train.shape[0]
11
12 # model construction
13 model = tf.keras.Sequential([
14     tf.keras.layers.Flatten(input_shape=(28, 28)),
15     tf.keras.layers.Dense(64, activation='relu'),
16     tf.keras.layers.Dense(64, activation='relu'),
17     tf.keras.layers.Dense(10, activation='softmax')
18 ])
19
20 # model compile and train
21 model.compile(optimizer='adam',
22               loss='sparse_categorical_crossentropy',
23               metrics=['accuracy'])
24 history = model.fit(x_train, y_train,
25                     validation_split=0.9, epochs=20, verbose=0)
```

# Multi-layer Perceptron

## ❖ Demo

```
Python 3.7.3 (default, Apr 24 2019, 15:29:51) [MSC v.1915 64 bit (AMD64)] ::
Type "help", "copyright", "credits" or "license" for more information.
>>>
>>>
>>>
>>>
>>>
>>>
>>>
>>> for epoch in range(n_epochs):
...     sum_of_losses = 0
...     gradients = np.zeros((2,1))
...
...     for index in range(4):
...         xi = X_b[index:index+1]
...         yi = y[index:index+1]
```

