Numerical Descriptive Measures

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To clean the environment variables

```
rm(list=ls(all=T))
```

Defining a Vector

```
vec <- c(20,34,56,23,45,22,60,23,56,78,23,45)
```

$Llarge$Mean of the vector

$$\frac{\sum_{i=1}^{n} x_i}{n}$$

```
mean(vec)
```

```
## [1] 40.41667
```

Median of the vector

$\frac{(n+1)}{2}$ ranked value

```
median(vec)
```

```
## [1] 39.5
```

- For symmetrical distributed data mean, median and mode are almost equal in value
- For asymmetrical distributed data, following relationship holds good approximately
- Mode = 3 * Median - 2 * mean (or)
- Mean - Mode = 3 * (Mean - Median)
- above realtion is called as empirical relation. Using this if two measures are known, it is easy to find out the third measure

Harmonic Mean of a vector

$$\frac{n}{\sum_{i=1}^{n} \frac{1}{x_i}}$$

```
hm_ <- function(vcetor) {
  return(length(vec)/sum(1/vec))
}
```

```
hm_(vec)
```

```
## [1] 32.88149
```

Geometric Mean of a vector

$$\bar{X}_g = (X_1 * X_2 * X_3 * \ .... \ X_n)^{\frac{1}{n}}$$

```
gm_ <- function(vcetor) {
  return(prod(vcetor)^(1/length(vcetor)))
}
```

```
gm_(vec)
```

```
## [1] 36.39962
```

Variation and shape

Range of a vector

$\text{Range} = (x_{max} - x_{min})$

```
range_ <- function(vcetor) {
  return(max(vcetor)-min(vcetor))
}
```

```
range_(vec)
```

```
## [1] 58
```

Variance of a vector

$$\sigma^2 = \frac{\sum_{i=1}^{n}(x_i - \bar{X})^2}{n}$$

```
variance_ <- function(vcetor){
    var_ <-  0
    for (ele in 1:length(vcetor)){
      var_ = var_ + (vcetor[ele] - mean(vcetor))^2
    }
    return (var_/length(vcetor)-1)
}
```

```
variance_(vec)
```

```
## [1] 334.9097
```

Standard deviation of a vector

$$\sigma = \sqrt{\frac{\sum_{i=1}^{n}(x_i - \bar{X})^2}{n}}$$

```
stddev_ <- function(vcetor){
  return (variance_(vcetor) ^ 0.5)
}
```

```
stddev_(vec)
```

```
## [1] 18.30054
```

Coefficient of Variation

It measures the scatter in the data with respect to the mean

$$(\frac{\sigma}{\mu}) * 100$$

```
CoeffVar_ <- function(vcetor){
  return (stddev_(vcetor)/mean(vcetor)) *100
}
```

```
CoeffVar_(vec)
```

```
## [1] 0.4527968
```

Z – Scores

- a Z score of 0 indicates that the value is same as the mean
- Helps in identifying outliers, less than -3 and greater than +3 are considered to be outliers

```
zscore <- function(vcetor){
  temp_ <- c()
  for (ele in 1:length(vcetor)){
    temp_ <- append(temp_, (vcetor[ele]-mean(vcetor))/stddev_(vcetor))
  }
  return (temp_)
}
```

```
zscore(vec)
```

```
##  [1] -1.1156320 -0.3506272  0.8515232 -0.9517024  0.2504480 -1.0063456
##  [7]  1.0700960 -0.9517024  0.8515232  2.0536736 -0.9517024  0.2504480
```

Skewness

- Mean < Median —-> left skewed or negative skew
- Mean = Median —-> symmetrical distribution (zero skewness)
- Mean > Median —-> right skewed or positive skew

Kurtosis

- A distribution that has a sharper-rising center peak than the peak of a normal distribution has positive kurtosis, a kurtosis value that is greater than zero, and is called **lepokurtic**
- A distribution that has a slower-rising (flatter) center peak than the peak of a normal distribution has negative kurtosis, a kurtosis value that is less than zero, and is called **platykurtic**
- A **lepokurtic distribution** has a **higher concentration** of values near the mean of the distribution compared to a normal distribution, while a **platykurtic distribution** has a **lower concentration** compared to a normal distribution