

# **Analysis on Manifolds**

**Lecture Notes**

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## 1.0 Algebra and Topology of $\mathbb{R}$

### 1.1 Linear Algebra

Suppose a set  $V$  of *vectors*. We define two operations. The first, called *vector addition*, denotes the sum of vectors  $x$  and  $y$  as  $x + y$ . The second, called *scalar multiplication*, denotes the product of a scalar  $c \in \mathbb{R}$  and a vector  $x$  as  $cx$  as  $cx$ .

**Definition 1.1.** If the following properties hold for all vectors  $x, y, z$  and scalars  $c, d$ , then we call the set  $V$  with these operations a *vector space*.

1.  $x + y = y + x$  (Additive commutativity)
2.  $x + (y + z) = (x + y) + z$
3.  $\exists! 0(x + 0 = x \forall x)$
4.  $x + (-1)x = 0$