

Pitfall in relational database design

- A bad design of several properties, including
- Repetition of information
 - Inability to represent certain information
 - Loss of information

lending schema

branch-name	branch-city	assets	customer name	loan no.	amount
downtown	Brooklyn	1,00,000	Jones	L-17	1000
Perryridge	Horseneck	2,00,000	Smith	L-23	3000
Redwood	Palo Alto	1,50,000	Jackson	L-29	5000
downtown	Brooklyn	1,90,000	Jackson	L-11	2000
Perryridge	Horsneck	2,00,000	Glenn	L-16	22000

Repeating of information in our alternative design is undesirable. Repeating information wastes space.

- It complicates updating the databases.

For ex → the assets of Perryridge branch change from 2,00,000 to 3,00,000.

Under our design, many tuples of the lending relation need to be changed. Thus, updates are most costly. We ensure that every tuple consists to the Perryridge branch is updated, else our database will show two different asset values for the Perryridge branch.

Another problem with lending schema design is that we cannot represent directly the information concerning a branch (branch-name, branch-city, assets) unless there exist at least one loan at the branch. This is because tuples in the lending relation require values for loan-number, amount and customer-name.

→ one solⁿ to this problem is to introduce null values but null values are difficult to handle. If we are not willing to deal with null values, then we can create the branch information only when the first loan appⁿ at that branch is made. Worse, we would have to delete this information when all the loans have been paid.

Clearly, this situation is undesirable, under our database design, the branch information would be available regardless of whether or not loans are currently maintained in the branch and without resorting to null values.

Decomposition

- It is the process of breaking down relation into n multiple relation.
- It should be lossless because it confirms that the information in the original relation can be accurately reconstructed based on the decomposed relations.
- If there is no proper decomposition of the relation, then it may lead to problems like loss of information.
- Decomposition helps in eliminating some of the problems of bad design such as redundancy, inconsistencies.

There are two type of decomposition

- lossy → The decomposition of relation R into R_1 and R_2 is lossy when the join of R_1 and R_2 doesn't yield the same relation as in R .

One of the disadvantages of decomposition into two or more relational schemes is that some information is lost during retrieval of original relation or table.

Consider that we have student with three attribute roll-no., s-name, department.

student

Roll-no.	s-name	department
111	paṁmal	Computer
222	paṁmal	Electrical

This relation is decomposed into two relation no-name and name-department

no-name

Roll-no.	Sname
111	Paṁmal
222	Paṁmal

name-department

Sname	dept
paṁmal	comp.
paṁmal	Electrical

In lossy decomposition, spurious tuples are generated when a natural join is applied to the relations in the decomposition.

stu-joined

Roll-no.	Sname	dept
111	paṁmal	Comp.
111	Paṁmal	Electrical
222	"	Comp.
222	"	Electrical

The above decomposition is a bad decomposition or lossy decomposition.

Lossless join decomposition

The decomposition of relation R into R_1 and R_2 is lossless when the join of R_1 and R_2 yield the same relation as R .

The lossless-join decomposition is always defined with respect to a specific set F of dependencies.

stu-name

Roll-no.	s-name
111	parimal
222	parimal

stu-dept

Roll-no.	Dept
111	Comp.
222	Electrical

stu-joined :

<u>Roll-no.</u>	<u>s-name</u>	<u>dept</u>
111	parimal	computer
222	parimal	Electrical

In lossless decomposition, no any spurious tuples are generated when a natural join is applied to the relation in the decomposition.

Properties of decomposition

→ Lossless decomposition → deco

→ dependency preservation

→ Lack of Data Redundancy →

1) It gives a guarantee that the join will result in the same relation as it was decomposed.

2) Dependency Preservation → Every dependency must be satisfied by atleast one decomposed table. If $(A \rightarrow B)$ holds, then two sets are functional dependent. And it become more useful for checking the dependency easily if both sets in a same relation.

$R(A, B, C, D, E)$

$R_1(A, B, C)$

$R_2(C, D, E)$

$A \rightarrow B$

$B \rightarrow C$

$AD \rightarrow E$ ✗

3) Lack of Data Redundancy → The proper decomposition should not suffer from any data redundancy. Lack of data redundancy is also known as a repetition of information.

Functional dependency

It is a relationship that exists when one attribute uniquely determines another attribute.

⇒ If R is a relation with attribute X and Y .

X	Y
a	1
a	2
b	1
b	2

$$X \rightarrow Y$$

Y is functionally dependent on X .

Here X uniquely determines the Y value.

⇒ It is a set of constraints b/w two attributes in a relation.

X
↓
determinant
or
identification
key

Y
dependant

eg → If every attribute B of R dependent of A , then attribute A is a primary key.

<u>ID</u>	<u>Name</u>	<u>Surname</u>
S ₁	Bhanu	P
S ₂	Priya	G
S ₃	Bhanu	M

$\left\{ \begin{array}{l} ID \rightarrow Name \\ ID \rightarrow Surname \end{array} \right\}$

Functional dependencies can be categorized

two types —

Trivial

$AB \rightarrow A$ (dependency is valid)

if $\beta \subseteq \alpha$

Non-trivial

$\beta \not\subseteq \alpha$

$AB \rightarrow ABC$

Closure set of attributes ↓

Attribute closure of an attribute set 'A' can be defined as a set of attributes which can be functionally determined from it. Denoted by F^+

$R(A, B, C, D)$

$A \rightarrow B$

$B \rightarrow D$

$C \rightarrow DE$

$CD \rightarrow AB$

→ The set of all those attributes which can be functionally determined from an attribute set is called as a closure of that attribute set.
→ Closure of attribute set (X) is denoted by $(X)^+$

$A^+ = \{A, B, D\}$

$B^+ = \{B, D\}$

$C^+ = \{C, D, E, A, B\}$

$D^+ = \{D\}$

$E^+ = \{E\}$

$(AB)^+ = \{A, B, D\}$

$(AD)^+ = \{A, D, B\}$

$(ABD)^+ = \{A, B, D\}$

Step-1 Add the attributes contained in the attribute set for which closure is being calculated to the result set.

Step-2 Recursively add the attributes to the result set which can be functionally determined from a.s. already contained in the result set.

Q $R(X, Y, Z, W)$ is decomposed into

Armstrong's Axioms

i) Union Rules

If $A \rightarrow B$ holds and $A \rightarrow C$ holds, then
 $A \rightarrow BC$ holds.

$$\begin{array}{l} A \rightarrow B \\ A \rightarrow C \\ \hline A \rightarrow BC \end{array}$$

ii) Decomposition Rule

If $A \rightarrow BC$ holds
then $A \rightarrow B$ and $A \rightarrow C$ holds

iii) Augmentation Rule

If $A \rightarrow B$ holds and Y is attribute set, then AY and BY also holds.

iv) Transitivity

if $A \rightarrow B$
 $B \rightarrow C$
then
 $A \rightarrow C$

(vi) Reflexivity rule
if X is a set of attributes
and Y is subset of X ,
then we would say
 $X \rightarrow Y$.
(trivial FD)

v) Pseudotransitivity ↓
 if $A \rightarrow B$ holds
 and $BC \rightarrow D$ holds
 $AC \rightarrow D$ holds

Minimal functional dependency set ↓
 (Irreducible set of FD)

Minimal cover → it means to eliminate
 any kind of redundancy from a FD set.

$R(WXYZ)$

$X \rightarrow W$

$WZ \rightarrow XY$

$Y \rightarrow WXZ$

$\alpha \rightarrow \beta$

on α side something
 extra and β side
 something extra and
 worst case full
 dependency extra.

3rd step-1

apply decomposition rule ↓

$X \rightarrow W$

$WZ \rightarrow X$

$WZ \rightarrow Y$

$Y \rightarrow W$

$Y \rightarrow X$

$Y \rightarrow Z$

Now, case is FD may be redundant. We
 don't check right hand side attribute
 because now we write separate here.

$$X^+ = XW$$

again we compute X^+ without seeing $X \rightarrow W$. if we get again XW without seeing this means $X \rightarrow W$ is redundant.

$$X^+ = X$$

I am not getting W here. So $X \rightarrow W$ is essential.

② $WZ \rightarrow X$

$$(WZ)^+ = (WZXY)$$

again

$$(WZ)^+ = (WZYX)$$

so $WZ \rightarrow X$ is redundant.

③ $WZ \rightarrow Y$

$$(WZ)^+ = WZYX$$

again

$$(WZ)^+ = WZ$$

so $WZ \rightarrow Y$ is essential.

④ $Y \rightarrow W$

$$Y^+ = YWXZ$$

again

$$Y^+ = YXZW$$

so $Y \rightarrow W$ is redundant.

$$(5) Y \rightarrow X$$

$$Y^+ = YXWZ$$

again

$$Y^+ = Y \therefore Z$$

so $Y \rightarrow X$ is essential.

$$(6) Y \rightarrow Z$$

$$Y^+ = Y \therefore XW$$

so $Y \rightarrow Z$ is essential.

After that

$$X \rightarrow W$$

$$WZ \rightarrow Y$$

$$Y \rightarrow X$$

$$Y \rightarrow Z$$

But again problem arises. Is there any redundancy on left hand side or not. In this ex. $WZ \rightarrow Y$

$$(WZ)^+ = WZ \therefore X$$

again

$$W^+ = W$$

$$Z^+ = Z$$

so $WZ \rightarrow Y$ is essential.

Finding the keys Using Closure

Super Key → If the closure result of an attribute set contains all the attributes of the relation, then that attribute set is called as a superkey of that relation.

In above example

- The closure of attribute A is the entire relational schema.
- Thus, attribute A is a super key for that relation.

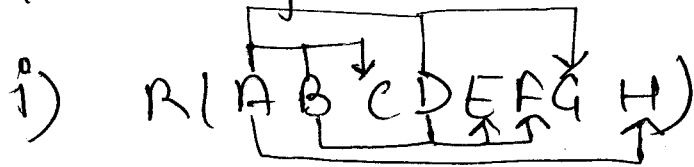
Candidate Key

If there exists no subset of an attribute set whose closure contains all the attributes of the relation, then that attribute set is called as a candidate key of that relation.

Example

- No subset of attribute A contains all the attributes of the relation.
- Thus, attribute A is also a C.K. for that relation.

How to find out a candidate key?



$$AB \rightarrow C$$

$$BD \rightarrow EF$$

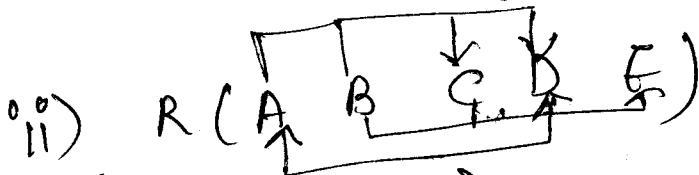
$$AD \rightarrow G$$

$$A \rightarrow H$$

$$(ABD)^+ = (ABDCEFGH)$$

↓

candidate key



$$AB \rightarrow CD$$

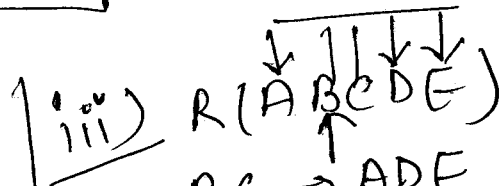
$$D \rightarrow A$$

$$BC \rightarrow DE$$

$$(B)^+ = B$$

$$\left. \begin{aligned} (AB)^+ &= (ABCDE) \\ (BC)^+ &= (ABCDE) \\ (BD)^+ &= BDACE \end{aligned} \right\} \text{C.K.}$$

$$(BE)^+ = BE \times$$



$$BC \rightarrow ADE$$

$$D \rightarrow B$$

$$(C)^+ = ?$$

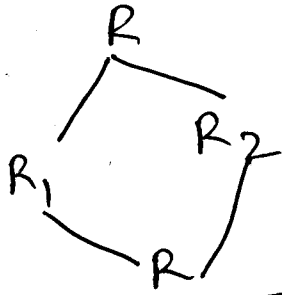
$$(AC)^+ = AC \times$$

$$(BC)^+ = (BCADE) \checkmark$$

$$(CD)^+ = (CD) \\ = (CDBAE) \checkmark$$

$$(CE)^+ = \times$$

Lossless join decomposition



This property guarantees that the extra or less tuple generation problem doesn't occur after decomposition.

A	B	C	D
1	a	p	x

2	b	q	y
3	a	a	x

R ₁		R ₂
A	B	D
1	a	x
2	b	y

R ₁		R ₂	
A	B	C	D
1	a	p	x
2	b	q	y

R ₁ × R ₂			
A	B	C	D
1	a	p	x
1	a	q	y
2	b	p	x
2	b	q	y

→ If a relation R is decomposed into two relations R₁ & R₂, then it will be lossless - if

- i) $\text{attr}(R_1) \cup \text{attr}(R_2) = \text{attr}(R)$
- ii) $\text{attr}(R_1) \cap \text{attr}(R_2) \neq \emptyset$

$$R_1$$

A	B
1	a
2	b
3	a

$$R_2$$

B	C
a	p
b	q
a	r

$$R$$

A	B	C
1	a	p
2	b	q
3	a	r

$R_1 \bowtie R_2$

A	B	C
1	a	p
2	b	q
3	a	r
1	a	r
3	a	p

~~if~~ if I make common attribute candidate key then it will never generate extra tuples.

(iii)

$$\begin{aligned} \text{attr}(R_1) \cap \text{attr}(R_2) &\rightarrow \text{attr}(R_1) \text{ (key Proof)} \\ \text{or} \\ \text{attr}(R_1) \cap \text{attr}(R_2) &\rightarrow \text{attr}(R_2) \end{aligned}$$

example of lossless decomposition

A	B	C	D	E
a	1 2 2	1	p	w
b	2 3 4	2	q	x
a	5 6 8	1	r	y
c	3 4 7	2	s	z

1 condition violate
 $R_1(A, B) \cup R_2(C, D) = R$

(1) $R_1(A, B), R_2(C, D) \rightarrow$ lossy

(2) $R_1(ABC), R_2(DE)$

i) $R_1 \cup R_2 = A, B, C, D, E$

(ii) $R_1 \cap R_2 \neq \emptyset$
 $(A, B, C) \cap (D, E)$ violate // lossy

(3) $R_1(A, B, C), R_2(C, D, E)$

i) $R_1 \cup R_2 = A, B, C, D, E$

(ii) $R_1 \cap R_2 \neq \emptyset$
 "C"

(iii) violate | above table is repeated

(4) $R_1(A, B, C, D), R_2(A, C, D, E)$
 $R_1 \cup R_2 = ABCDE$
 $R_1 \cap R_2 = \{A, C, D\}$
 $R_1 \cap R_2 \Rightarrow \text{attri}(R_1)$

Dependency Preserving

If a table R having FD set F , is decomposed into two tables R_1 and R_2 having FD set F_1 and F_2

$$F_1 \subseteq F^+$$

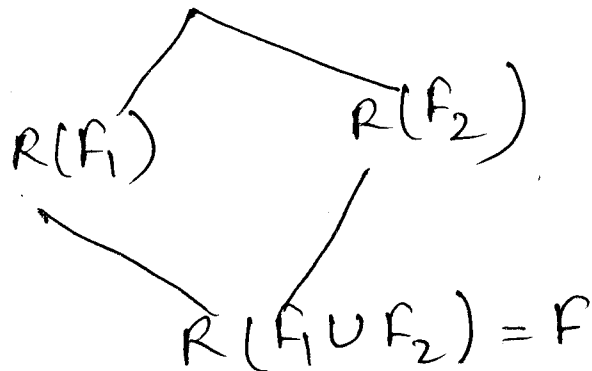
$$F_2 \subseteq F^+$$

$$\overline{(F_1 \cup F_2)^+ = (F)^+}$$

$R(A, B, C)$

$$F) \left[\begin{array}{l} A \rightarrow B \\ B \rightarrow C \\ C \rightarrow A \end{array} \right]$$

$$\begin{array}{c} F_1 \\ R_1(A, B) \end{array} \bigg| \begin{array}{c} R_2(B, C) \\ F_2 \end{array} \quad R(F)$$



$$A^+ = AB$$

$$B^+ = BCA$$

$$\left[\begin{array}{l} A \rightarrow B \checkmark \\ B \rightarrow A \end{array} \right]$$

$$R_2(B, C)$$

$$B^+ = B \text{ } \cancel{B} \text{ } A$$

$$\left[\begin{array}{l} B \rightarrow C \\ B \rightarrow A \end{array} \right]$$

$$C^+ = CAB$$

$$\left[\begin{array}{l} C \rightarrow A \\ C \rightarrow B \end{array} \right]$$

Dependency preserving

$$R(A, B, C, D)$$

$$AB \rightarrow CD$$

$$D \rightarrow A$$

$$R_1(A, D)$$

$$A^+ = A$$

$$D^+ = DA \quad (D \rightarrow A)$$

$$(AD)^+ = AD \times$$

$$R_2(B, C, D)$$

$$B^+ = B$$

$$C^+ = C$$

$$D^+ = DA$$

$$(D \rightarrow A) \times$$

$$(BC)^+ = BC \times$$

$$(BD)^+ = BDAC$$

$$(BD \rightarrow A) \times$$

$$(BD \rightarrow C) \checkmark$$

$$(CD)^+ = CDA \times \quad (CD \rightarrow A) \times$$

Prime attribute

Attributes that form a candidate key of a relation i.e. attributes of candidate key are called prime attributes and rest of the attributes of the relation are non-prime attributes.

Partial FD ↓

Partial dependency means that a non-prime attribute is functionally dependent on a part of a candidate key.

For ex → $R(A, B, C, D)$
 $A \rightarrow B$
 $D \rightarrow C$

$(AD)^+ = (ADBC)$ is

AD is a candidate key.

B & C are non prime attribute
 A & D are prime attribute
so here partial FD exists

Full FD ↓

When a non-prime attribute is fully functional dependent on the candidate key.

$R(A, B, C, D)$

$ABC \rightarrow D$

D is Non Prime attribute

ABC are prime attributes.

So Full FD.

"Normalization"

→ Normalization is the process of decomposing a big relation into smaller relation.

→ The prime objective of normalization is to reduce redundancy.

Redundancy leads the problem of inconsistency.

Goal of Normalization — (Requirement)

To achieve

- i) Functional dependency preservation
- 2) loss less join decomposition

Idea → In the table studentinfo we have tried to store entire data about student.

Result → Entire branch data of a branch must be repeated for every student of the branch.

Redundancy → When same data is stored multiple times unnecessarily in a database.

Student info					
S_id	name	age	Branch	Branch	HODName
1	A	18	101	CS	XYZ
2	B	19	101	CS	XYZ
3	C	18	101	CS	XYZ
4	D	21	102	EC	PQR
5	E	20	102	EC	PQR
6	F	19	103	ME	KLM

Disadvantages → (i) Insertion, deletion and modification anomalies

(ii) Inconsistency (data)

(iii) Increase in database size and increase in time (slow)

Insertion anomalies → When certain data (attribute) cannot be inserted into Database, without the presence of other data.

Deletion anomalies - If we delete some data (unwanted), it causes deletion of some other data (wanted)

Updating/Modification anomalies - When we want to update a single piece of data, but it must be done in a database.

Student info						Student info				Branch info		
S_id	name	age	Br code	Br name	Hod name	S_id	name	age	Br code	Br code	Br name	Hod name
1	A	18	101	CS	XYZ	1	A	18	101	101	C.S	XYZ
2	B	19	101	CS	XYZ	2	B	19	101	102	E.C	POR
3	C	18	101	CS	XYZ	3	C	18	101	103	ME	KLM
4	D	21	102	EC	POR	4	D	21	102			
5	E	20	102	EC	POR	5	E	20	102			
6	F	19	103	ME	KLM	6	F	19	103			

→ As one paragraph contains a single idea similarly one table must contain direct & main data about an Entity

→ Normalization (Decomposition of tables) of table is done of the basis of functional dependencies

First Normal Form ↓

- It is a theoretical discussion.
- Every cell can contain atomic value.
or
you can say that you don't have multivalued attribute.
- Every relation is in 1NF if ^{every cell} it ~~doesn't~~ contain atomic value.
- domains should be same (every column)

Roll No.	name	Course
101	Modi ^o	CN DS
102	Sonia ^a	DBMS CO



Roll No.	name	Course
101	Modi ^o	CN
101	Modi ^o	DS
102	Sonia ^a	DBMS
102	Sonia ^a	CO

Second Normal Form ↓

For a table to be in the Second Normal Form, it must satisfy two conditions—

- 1) The table should be in 1NF.
- 2) There should be no Partial Dependency.

$R(A, B, C, D)$

$AB \rightarrow D$

$B \rightarrow C$

$(AB)^+$ is a candidate key

$A, B \in$ prime attributes

$C, D \in$ non-prime attributes

$B \rightarrow C$ is a partial dependency

When the non-prime attribute is depend on the part of a candidate Key.

So it is not in 2NF.

We have to convert in 2NF.

$R(ABCD)$

$R_1(ABD)$

↓
 $AB \rightarrow C, D$

$R_2(\overline{B} \downarrow C)$

B is a C.K.

How to identify it?
It is in 2NF.

Q → R (A B C D E)
AB → C (P.D.)
D → E (P.D.)

R (A B C D E)
┌───┐
A B C
└───┘
D E

$(ABD)^+ = ABDCE$

So $(ABD)^+$ is a candidate key.
So it is not in 2NF.

R (A B C D E)

├─ R₁ (A B C)

├─ R₂ (D E)

├─ R₃ (A B D)

More detailed discussion on 2NF ↓

$R(A B C)$

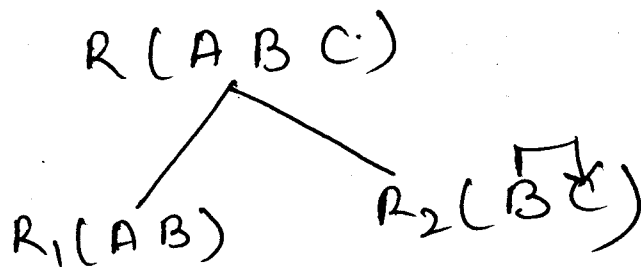
$B \rightarrow C$

so $(AB)^+$ is a candidate key

$A, B \in$ prime attribute

$C \in$ Non Prime attribute

so it has partial dependency.



A	B	C
a	1	x
b	2	y
a	3	z
c	3	z
d	3	z
e	3	z

R_1

A	B
a	1
b	2
a	3
c	3
d	3
e	3

R_2

B	C
1	x
2	y
3	z
3	z
3	z
3	z

3NF ↓

Transitive Dependency → A.F.D. from $\alpha \rightarrow \beta$ is called transitive if $\alpha, \beta \in$ non-prime

3NF ↓

A relation is in 3NF if

- It is in 2NF
- No transitive dependency

every dependency from $\alpha \rightarrow \beta$

- either α is superkey
- or β is a prime attribute

$R(A, B, C)$

$A \rightarrow B$

$B \rightarrow C$

A is a candidate key

— $R_1(B, C)$

— $R_2(A, B)$

R_2

A	B
a	1
b	1
c	1
d	2
e	2
f	3
g	3

R_1

B	C
1	x
2	y
3	z

A	B	C
a	1	x
b	1	x
c	1	x
d	2	y
e	2	y
f	3	z
g	3	z

Q → R (A B C D E)

$A \rightarrow B$

$B \rightarrow E$

$C \rightarrow D$

$(AC)^+ = ABCED$

So $(AC)^+$ is candidate key

$A \rightarrow B$ is P.D.

$C \rightarrow D$ is P.D.

$B \rightarrow E$

$R_1 (A B E)$
 $R_2 (C D)$
 $R_3 (AC)$
 R_4

(transitivity)

③ $R(A B C D E)$

$A \rightarrow B$

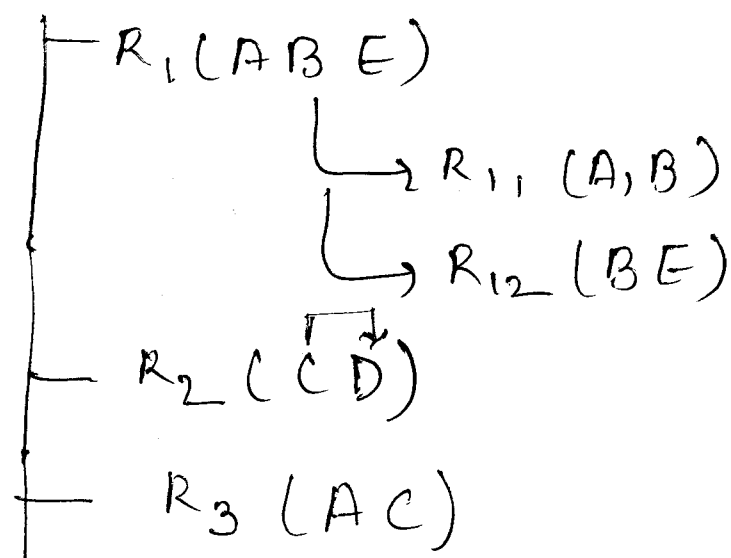
$B \rightarrow E$

$C \rightarrow D$

$(AC)^+$ is a C.K.

B, D, E Non-Prime Attribute

A B C D E



Q → $R(A B C D E F G H I J)$

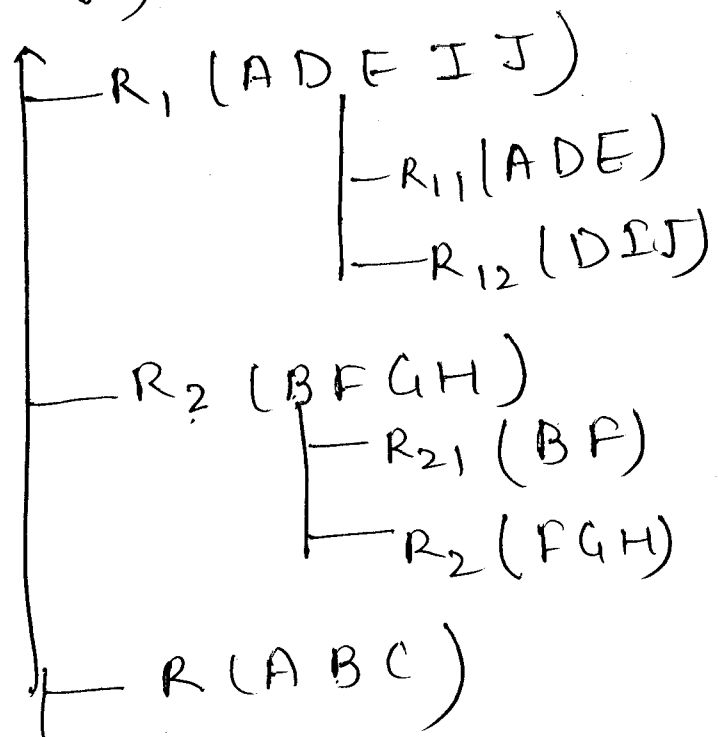
$AB \rightarrow C$

$A \rightarrow DE$

$B \rightarrow F$

$F \rightarrow GH$

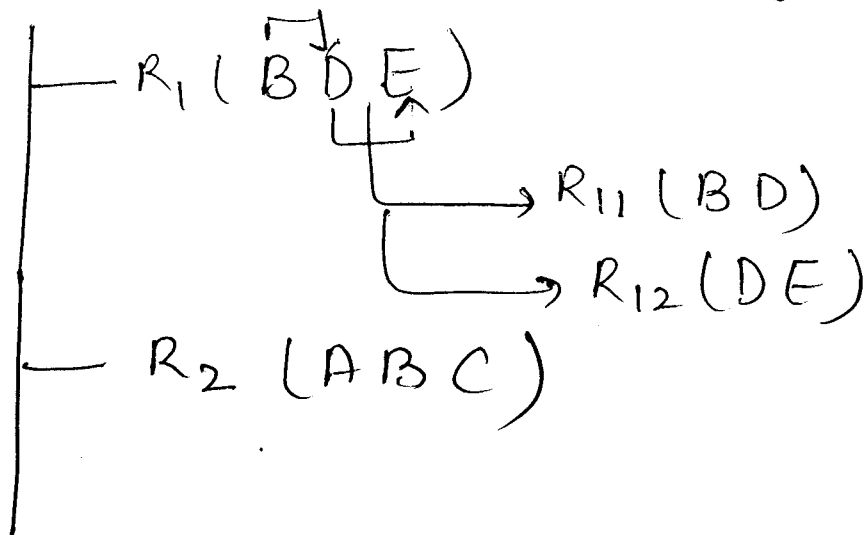
$D \rightarrow IJ$



$(AB)^+$ is a candidate key.

Q → $R(A B C D E)$
 $AB \rightarrow C$
 $B \rightarrow D$
 $D \rightarrow E$

$(AB)^+$ is a candidate key.



BCNF

$\alpha \rightarrow \beta$
 \downarrow
 superkey

$R(ABC)$
 $AB \rightarrow C$
 $C \rightarrow B$

$(AB), (AC)$ is a c.k.

It is 3NF not BCNF.

Identify the Normal Forms:-

① R (A B C D E F G H)

$AB \rightarrow C$

$A \rightarrow DE$

$B \rightarrow F$

$F \rightarrow GH$

(AB) C.K.

1NF

② R (A B C D E)

$CE \rightarrow D$

$D \rightarrow B$

$C \rightarrow A$

(CE) is C.K.

1NF

③ R (A B C D E F)

$AB \rightarrow C$

$DC \rightarrow AE$

$E \rightarrow F$

(ABD) (BCD) C.K.

1NF

④ R (A B C D E G H I)

$AB \rightarrow C$

$BD \rightarrow EF$

$AD \rightarrow GH$

$A \rightarrow I$

1NF

(ABD) is C.K.

Q R (A B C D E)

$AB \rightarrow CD$

$D \rightarrow A$

$BC \rightarrow DE$

(AB) (BD) (BC)

3NF

Q R (A B C D E)

$BC \rightarrow ADE$

$D \rightarrow B$

(BC)

(CD)

3NF

BCNF

• Example (BCNF) :-

$R(A B C)$

$AB \rightarrow C$

$C \rightarrow B$

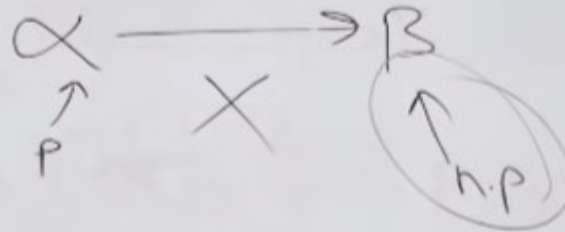
$R_1(CB)$
 $R_2(AC)$

A	B	C
a	1	x
b	2	y
c	2	z
c	3	w
d	3	w
e	3	w

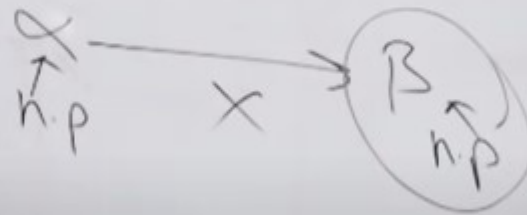
A	C
a	x
b	y
c	z
c	w
d	w
e	w

CB	
C	B
x	1
y	2
z	2
w	3

2NF



3NF



BCNF (Boyce Codd Normal Form)

A Relation R is said to be in BCNF if every FD, $X \rightarrow A$ in F satisfy At least one of following condition held.

- 1) $X \rightarrow A$ must be trivial
- 2) X is a super key.

Note:- 1) In BCNF the FD may not be preserved.
2) BCNF is more stricter than 3NF.

BCNF

• Example (BCNF) :-

$R(A B C)$

$AB \rightarrow C$

$C \rightarrow B$

$R_1(C B)$
 $R_2(A C)$

A	B	C
a	1	x
b	2	y
c	2	z
c	3	w
d	3	w
e	3	w

A	C
a	x
b	y
c	z
c	w
d	w
e	w

C B	
C	B
x	1
y	2
z	2
w	3

Fourth Normal Form (4NF)

A relation 'R' is in 4NF if and only if the following conditions are satisfied -

- i) if 'R' is in 3NF or BCNF
- ii) if it contains no MVD's.

Now What is Multivalued Dependency.

→ For a dependency $x \twoheadrightarrow y$, if for a single value of x , multiple values of y exist, then the relation has multivalued dependency.

→ The relation should have at least three attributes

$$(x \twoheadrightarrow y), (x \twoheadrightarrow z)$$

→ The attributes y and z should be independent of each other.

Note [FD ($\alpha \rightarrow \beta$) says we can't have two tuples with same α value but different β value].

Consider Multivalued Dependency

E-id	ProjectName	D-Name
101	Java/DBMS	Sita/Khushi
102	OS/CN	Geeta/Ram

$E-id \twoheadrightarrow ProjectName$

$E-id \twoheadrightarrow D-Name$

employee-id "multidetermines" D-Name

In this ex - ProjectName and D-Name both are independent attributes and it is dependent on e-id.

ex → Consider the database table of a class which has two relations R1 contains studentID (SID) and student name (SNAME) and R2 contains course id (CID) and course name (CNAME)

R1 (SID, SNAME)

SID	SNAME
S1	A
S2	B

R2 (CID, CNAME)

CID	CNAME
C1	C
C2	D

Table R1XR2

SID	SNAME	CID	CNAME
S1	A	C1	C
S1	A	C2	D
S2	B	C1	C
S2	B	C2	D

Multivalued dependencies (MVD) are-

$SID \twoheadrightarrow CID$; $SID \twoheadrightarrow CNAME$;

$SNAME \twoheadrightarrow CNAME$

Note \rightarrow MVD occurs if two or more independent relations are kept in a single relation

Note - 4NF is a level of a database normalization where there are no non-trivial multivalued dependencies other than a candidate key.

How to decompose it in 4NF?

E_id	ProjectName	D_Name
101	Java/DBMS	Sita/Khushi
102	OS/CN	Geeta/Ram

↓

E_id	ProjectName	D_Name
101	Java	Sita
101	DBMS	Sita
101	Java	Khushi
101	DBMS	Khushi
102	OS	Geeta
102	CN	Geeta
102	OS	Ram
102	CN	Ram

↓

R₁

E_id	ProjectName
101	Java
101	DBMS
102	OS
102	CN

R₂

E_id	D_Name
101	Sita
101	Khushi
102	Geeta
102	Ram

5th NF or Project Join Normal Form

→ 5NF is rarely used practically but it is useful for theoretical study.

→ 5NF is based on Join dependency.

→ Join dependency

— Decompose the relation in multiple relations and it should be lossless and maintain dependencies of original relation.

→ A relation is in 5NF —

i) It must be in 4NF

ii) No Join Dependency exists

for ex →

Dept	subject	student
CSE	DBMS	Shreya
IT	CN	Yug
CSE	DS	Geeta
CSE	COA	Sita
ME	APP	Rini
EC	CSA	Ira

Dept → → subject

Dept → → student

Dept	subject
CSE	DBMS
IT	CN
CSE	DS
CSE	COA
ME	APP
EC	CSA

Dept	student
CSE	Shreya
IT	Yug
CSE	Geeta
CSE	Sita
ME	Rini
EC	Ira

If we perform join here

Dept	subject	student
CSE	DBMS	Shreya ✓
CSE	DBMS	Geeta ✗
CSE	DBMS	Sita ✗
IT	CN	Yug ✓
CSE	DS	Shreya
CSE	DS	Geeta ✓
CSE	DS	Sita ✗
CSE	COA	Shreya ✗
CSE	COA	Geeta ✗
CSE	COA	Sita ✓
ME	APP	Rini ✓
EC	CSE	Dea ✓

so we have to decompose it in 3 table

Dept	subject

dept	student

Sub ect	Student