

MATLAB REPORT

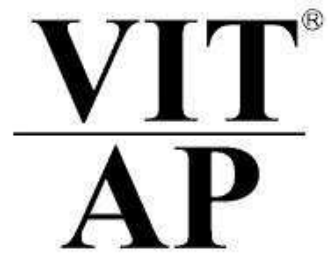
COURSE CODE:MAT 2001
SLOT:L9+L10

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```
%Valiveti Manikanta Bhuvanesh
% %19bcd7088
% %Lab 1
clc
clear all
a=4;
b=5;
c=a+b;
A=[1 2 3 4; 5 6 7 8; 7 6 5 4; 4 3 2 1;9 8 7 6]
```

```
A = 5x4
     1     2     3     4
     5     6     7     8
     7     6     5     4
     4     3     2     1
     9     8     7     6
```

```
B=[4 5 6 7 8; 1 2 3 4 5; 9 8 7 6 5; 3 4 5 6 7]
```

```
B = 4x5
     4     5     6     7     8
     1     2     3     4     5
     9     8     7     6     5
     3     4     5     6     7
```

```
C=A*B
```

```
C = 5x5
    45    49    53    57    61
   113   125   137   149   161
    91   103   115   127   139
    40    46    52    58    64
   125   141   157   173   189
```

```
C(:,3)
```

```
ans = 5x1
    53
   137
   115
    52
   157
```

```
C(2,:)
```

```
ans = 1x5
   113   125   137   149   161
```

```
C(:,4)=[1 2 3 4 5]
```

```
C = 5x5
    45    49    53     1    61
   113   125   137     2   161
    91   103   115     3   139
    40    46    52     4    64
   125   141   157     5   189
```

```
x=[1:10:100]
```

```
x = 1:10
    1    11    21    31    41    51    61    71    81    91
```

```
y=[1:5:100]
```

```
y = 1:20
    1     6    11    16    21    26    31    36    41    46    51    56    61    66    71    7
```

```
z=[1:1:100]
```

```
z = 1:100
    1     2     3     4     5     6     7     8     9    10    11    12    13    14    15    1
```

```
p=[1:0.5:100]
```

```
p = 1:199
    1.0000    1.5000    2.0000    2.5000    3.0000    3.5000    4.0000    4.5000    5.0000    5
```

```
p=linspace(1,100,200)
```

```
p = 1:200
    1.0000    1.4975    1.9950    2.4925    2.9899    3.4874    3.9849    4.4824    4.9799    5
```

```
x=linspace(1,100,10)
```

```
x = 1:10
    1    12    23    34    45    56    67    78    89    100
```

```
y=linspace(1,100,20)
```

```
y = 1:20
    1.0000    6.2105   11.4211   16.6316   21.8421   27.0526   32.2632   37.4737   42.6842   47
```

```
z=linspace(1,100,100)
```

```
z = 1:100
    1     2     3     4     5     6     7     8     9    10    11    12    13    14    15    1
```

```
length(x)
```

```
ans = 10
```

```
length(y)
```

```
ans = 20
```

```
length(z)
```

```
ans = 100
```

```
length(p)
```

```
ans = 200
```

```
Y=x.^2
```

```
Y = 1:10
    1    144    529    1156    2025    3136    4489    608
```

```
plot(x,Y)
hold on
plot(x,Y)
```

```
hold on
Y=x.^2
```

Y = 10

1

144

529

1156

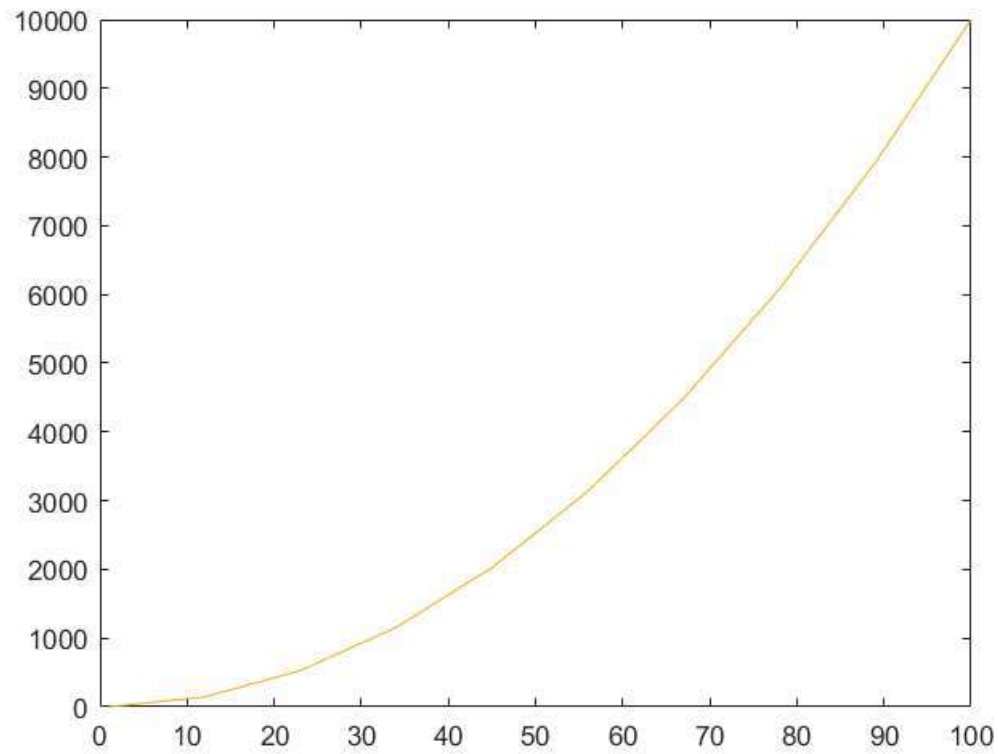
2025

3136

4489

608

```
plot(x,Y)
```



```
%Valiveti Manikanta Bhuvanesh
%19bcd7088
%Lab 2
syms x1 x2 x3 x4
for x1=1:1:2
    x4=3*x1
    x3=4*x1
    x2=0.5*(x3+2*x4)
    disp(x1)
    disp(x2)
    disp(x3)
    disp(x4)
end
```

x4 = 3

x3 = 4

x2 = 5

1

5

4

3

x4 = 6

x3 = 8

x2 = 10

2

10
8
6

```
syms x y z  
a=[-1 3 2;1 2 -3;2 1 -2]
```

```
a = 3x3  
    -1     3     2  
     1     2    -3  
     2     1    -2
```

```
X=[x;y;z]
```

```
X =  
 $\begin{pmatrix} x \\ y \\ z \end{pmatrix}$ 
```

```
b=[1;-9;-3]
```

```
b = 3x1  
     1  
    -9  
    -3
```

```
c=inv(a)
```

```
c = 3x3  
    0.0588   -0.4706    0.7647  
    0.2353    0.1176    0.0588  
    0.1765   -0.4118    0.2941
```

```
p=c*b
```

```
p = 3x1  
    2.0000  
   -1.0000  
    3.0000
```

```
X=p
```

```
X = 3x1  
    2.0000  
   -1.0000  
    3.0000
```

```
%Valiveti Manikanta Bhuvanesh
%19bcd7088
%Lab 3
syms x1 x2 x3
x1=45
```

```
x1 = 45
```

```
x3=35-x1
```

```
x3 = -10
```

```
x2=30-x3
```

```
x2 = 40
```

```
A=[1 0 0;0 1 1;1 0 1;0 1 0]
```

```
A = 4x3
      1      0      0
      0      1      1
      1      0      1
      0      1      0
```

```
B=[45;30;35;40]
```

```
B = 4x1
      45
      30
      35
      40
```

```
C=linsolve(A,B)
```

```
C = 3x1
      45.0000
      40.0000
     -10.0000
```

```
%Valiveti Manikanta Bhuvanesh
%19bcd7088
%Lab 4
syms x y z
eqn=[x+z+30==0,x-y+35==0,y-45==0,z+40==0]
```

```
eqn = (x + z + 30 = 0  x - y + 35 = 0  y - 45 = 0  z + 40 = 0)
```

```
[x,y,z]=solve(eqn,[x,y,z])
```

```
x = 10
y = 45
z = -40
```

```
syms a b c d x
eqn=[c+d==700,a+d==700,a+b==1000,c+b==x+400]
```

```
eqn = (c + d = 700  a + d = 700  a + b = 1000  b + c = x + 400)
```

```
[a,b,c,d,x]=solve(eqn,[a,b,c,d,x])
```

```
a = 700  
b = 300  
c = 700  
d = 0  
x = 600
```

```
syms a b c
```

```
eqn=[3*b-2*c+3==0,5*a-4*c-10==0,a+b==c]
```

```
eqn = (3 b - 2 c + 3 = 0 5 a - 4 c - 10 = 0 a + b = c)
```

```
[a,b,c]=solve(eqn,[a,b,c])
```

```
a =
```

```
 $\frac{2}{7}$ 
```

```
b =
```

```
 $-\frac{17}{7}$ 
```

```
c =
```

```
 $-\frac{15}{7}$ 
```



```
%Valiveti Manikanta Bhuvanesh  
%19bcd7088  
%Lab 5  
A=[3 0 -1;0 1 0;2 0 0]
```

```
A = 3×3  
    3     0    -1  
    0     1     0  
    2     0     0
```

```
P=poly(A)
```

```
P = 1×4  
    1    -4     5    -2
```

```
poly2str(P, 'x')
```

```
ans = '    x^3 - 4 x^2 + 5 x - 2'
```

```
polyvalm(P,A)
```

```
ans = 3×3  
    0     0     0  
    0     0     0  
    0     0     0
```

```
%Valiveti Manikanta Bhuvanesh
%19bcd7088
%Lab 6,7
clc
clear all
M='ILOVELINEARALGEBRA'
```

```
M = 'ILOVELINEARALGEBRA'
```

```
N=double(M)-65
```

```
N = 1×18
     8    11    14    21     4    11     8    13     4     0    17     0    11     6     4
```

```
M=N+7
```

```
M = 1×18
    15    18    21    28    11    18    15    20    11     7    24     7    18    13    11
```

```
L=mod(M,26)
```

```
L = 1×18
    15    18    21     2    11    18    15    20    11     7    24     7    18    13    11
```

```
encrypt_shift=char(L+65)
```

```
encrypt_shift = 'PSVCLSPULHYHSNLIYH'
```

```
L=L-7
```

```
L = 1×18
     8    11    14    -5     4    11     8    13     4     0    17     0    11     6     4
```

```
L=mod(L,26)
```

```
L = 1×18
     8    11    14    21     4    11     8    13     4     0    17     0    11     6     4
```

```
decrypt_shift=char(L+65)
```

```
decrypt_shift = 'ILOVELINEARALGEBRA'
```

```
N=reshape(N,3,[])
```

```
N = 3×6
     8    21     8     0    11     1
    11     4    13    17     6    17
    14    11     4     0     4     0
```

```
key=[-5 -6 -59;1 1 12;2 3 22]
```

```
key = 3×3
    -5    -6   -59
     1     1    12
     2     3    22
```

```
N=key*N
```

```
N = 3x6
```

```
-932 -778 -354 -102 -327 -107
 187  157   69   17   65   18
 357  296  143   51  128   53
```

```
P=mod(N,26)
```

```
P = 3x6
```

```
 4     2    10     2    11    23
 5     1    17    17    13    18
19    10    13    25    24     1
```

```
encrypt_cipher=char(P+65)
```

```
encrypt_cipher = 3x6 char array
```

```
'ECKCLX'
```

```
'FBRRNS'
```

```
'TKNZYB'
```

```
N=reshape(N,1,[])
```

```
N = 1x18
```

```
-932  187  357 -778  157  296 -354   69  143 -102   17   51 -327   65  128 -107
```

```
decrypt=inv(key)*P
```

```
decrypt = 3x6
```

```
103 x
```

```
 0.5280    0.2030    1.0740    1.1180    1.0510    1.1450
-0.0670   -0.0220   -0.1690   -0.1650   -0.1500   -0.1910
-0.0380   -0.0150   -0.0740   -0.0780   -0.0740   -0.0780
```

```
decrypt=int16(decrypt)
```

```
decrypt = 3x6 int16 matrix
```

```
 528    203   1074   1118   1051   1145
 -67    -22   -169   -165   -150   -191
 -38    -15    -74    -78    -74    -78
```

```
decrypt=mod(decrypt,26)
```

```
decrypt = 3x6 int16 matrix
```

```
 8    21    8     0    11     1
11     4    13    17     6    17
14    11     4     0     4     0
```

```
decrypt=char(decrypt+65)
```

```
decrypt = 3x6 char array
```

```
'IVIALB'
```

```
'LENRGR'
```

```
'OLEAEA'
```

```
decrypt_cipher=reshape(decrypt,1,[])
```

```
decrypt_cipher = 'ILOVELINEARALGEBRA'
```



```
%Valiveti Manikanta Bhuvanesh
%19bcd7088
%Lab 8
clc
clear all
a=[0 1 0 0;1/3 0 0 1/2;1/3 0 0 1/2;1/3 0 1 0]
```

```
a = 4x4
    0    1.0000    0    0
    0.3333    0    0    0.5000
    0.3333    0    0    0.5000
    0.3333    0    1.0000    0
```

```
[V,D]=eig(a)
```

```
V = 4x4
   -0.4575   -0.8384    0.6229   -0.8018
   -0.4575    0.1772   -0.4913   -0.0000
   -0.4575    0.1772   -0.4913    0.2673
   -0.6100    0.4841    0.3596    0.5345
D = 4x4
    1.0000    0    0    0
    0   -0.2113    0    0
    0    0   -0.7887    0
    0    0    0   -0.0000
```

```
p=null(a-eye(4,4))
```

```
p = 4x1
    0.4575
    0.4575
    0.4575
    0.6100
```

```
Y=abs(p/norm(p))
```

```
Y = 4x1
    0.4575
    0.4575
    0.4575
    0.6100
```

```
clc
clear all
a=[0 1/3 0 0;1 0 1/2 1/2;0 1/3 0 1/2;0 1/3 1/2 0]
```

```
a = 4x4
    0    0.3333    0    0
    1.0000    0    0.5000    0.5000
    0    0.3333    0    0.5000
    0    0.3333    0.5000    0
```

```
[V,D]=eig(a)
```

```
V = 4x4
    0.3928    0.5880   -0.2357   -0.0000
   -0.8586    0.4034   -0.7071    0.0000
```

```

      0.2329   -0.4957   -0.4714   -0.7071
      0.2329   -0.4957   -0.4714    0.7071
D = 4x4
     -0.7287         0         0         0
         0      0.2287         0         0
         0         0      1.0000         0
         0         0         0     -0.5000

```

```
p=null(a-eye(4,4))
```

```

p = 4x1
     0.2357
     0.7071
     0.4714
     0.4714

```

```
Y=abs(p/norm(p))
```

```

Y = 4x1
     0.2357
     0.7071
     0.4714
     0.4714

```

```
%Valiveti Manikanta Bhuvanesh
%19bcd7088
%Lab 9
clc
clear all
syms x1 x2 x3 X1 X2 X3 t c1 c2 c3
A=[0 1 0;0 0 1;8 -14 7]
```

```
A = 3x3
      0      1      0
      0      0      1
      8     -14      7
```

```
x=[x1;x2;x3]
```

```
x =
      (
      x_1
      x_2
      x_3
      )
```

```
X(t)=[X1;X2;X3]
```

```
X(t) =
      (
      X_1
      X_2
      X_3
      )
```

```
[V,D]=eig(A)
```

```
V = 3x3
      0.5774      0.2182     -0.0605
      0.5774      0.4364     -0.2421
      0.5774      0.8729     -0.9684
D = 3x3
      1.0000      0      0
      0      2.0000      0
      0      0      4.0000
```

```
l1=D(1,1)
```

```
l1 = 1.0000
```

```
l2=D(2,2)
```

```
l2 = 2.0000
```

```
l3=D(3,3)
```

```
l3 = 4.0000
```

```
V1=V(:,1)
```

```
V1 = 3x1
      0.5774
      0.5774
```

0.5774

V2=V(:,2)

V2 = 3×1
0.2182
0.4364
0.8729

V3=V(:,3)

V3 = 3×1
-0.0605
-0.2421
-0.9684

X1(t)=(c1*(exp(l1*t))*V1)

X1(t) =

$$\begin{pmatrix} \frac{\sqrt{3} c_1 e^t}{3} \\ \frac{\sqrt{3} c_1 e^t}{3} \\ \frac{\sqrt{3} c_1 e^t}{3} \end{pmatrix}$$

X2(t)=(c2*(exp(l2*t))*V2)

X2(t) =

$$\begin{pmatrix} \frac{\sqrt{21} c_2 e^{2t}}{21} \\ \frac{2 \sqrt{21} c_2 e^{2t}}{21} \\ \frac{4 \sqrt{21} c_2 e^{2t}}{21} \end{pmatrix}$$

X3(t)=(c3*(exp(l3*t))*V3)

X3(t) =

$$\begin{pmatrix} -\frac{\sqrt{273} c_3 e^{4t}}{273} \\ -\frac{4 \sqrt{273} c_3 e^{4t}}{273} \\ -\frac{16 \sqrt{273} c_3 e^{4t}}{273} \end{pmatrix}$$

X=X1+X2+X3

X(t) =

$$\begin{pmatrix} \frac{\sqrt{21} c_2 e^{2t}}{21} - \frac{\sqrt{273} c_3 e^{4t}}{273} + \sigma_1 \\ \frac{2 \sqrt{21} c_2 e^{2t}}{21} - \frac{4 \sqrt{273} c_3 e^{4t}}{273} + \sigma_1 \\ \frac{4 \sqrt{21} c_2 e^{2t}}{21} - \frac{16 \sqrt{273} c_3 e^{4t}}{273} + \sigma_1 \end{pmatrix}$$

where

$$\sigma_1 = \frac{\sqrt{3} c_1 e^t}{3}$$

```
clc
clear all
syms x1 x2 x3 X1 X2 X3 t c1 c2 c3
A1=[1 -1;2 4]
```

```
A1 = 2x2
      1   -1
      2    4
```

```
x=[x1;x2]
```

```
x =
      (x1)
      (x2)
```

```
X=[X1;X2]
```

```
X =
      (X1)
      (X2)
```

```
[V,D]=eig(A1)
```

```
V = 2x2
     -0.7071    0.4472
      0.7071   -0.8944
D = 2x2
      2    0
      0    3
```

```
l1=D(1,1)
```

```
l1 = 2
```

```
l2=D(2,2)
```

```
l2 = 3
```

$$V1=V(:,1)$$

$$V1 = \begin{matrix} 2 \times 1 \\ -0.7071 \\ 0.7071 \end{matrix}$$

$$V2=V(:,2)$$

$$V2 = \begin{matrix} 2 \times 1 \\ 0.4472 \\ -0.8944 \end{matrix}$$

$$X1(t)=(c1*(\exp(l1*t))*V1)$$

$$X1(t) =$$

$$\begin{pmatrix} -\frac{\sqrt{2} c_1 e^{2t}}{2} \\ \frac{\sqrt{2} c_1 e^{2t}}{2} \end{pmatrix}$$

$$X2(t)=(c2*(\exp(l2*t))*V2)$$

$$X2(t) =$$

$$\begin{pmatrix} \frac{\sqrt{5} c_2 e^{3t}}{5} \\ -\frac{2 \sqrt{5} c_2 e^{3t}}{5} \end{pmatrix}$$

$$X=X1+X2$$

$$X(t) =$$

$$\begin{pmatrix} \frac{\sqrt{5} c_2 e^{3t}}{5} - \frac{\sqrt{2} c_1 e^{2t}}{2} \\ \frac{\sqrt{2} c_1 e^{2t}}{2} - \frac{2 \sqrt{5} c_2 e^{3t}}{5} \end{pmatrix}$$

```
%Valiveti Manikanta Bhuvanesh
%19bcd7088
%Lab 10
clc
clear all
syms y1(t) y2(t) k
A=[-2*k k;k -2*k]
```

$$A = \begin{pmatrix} -2k & k \\ k & -2k \end{pmatrix}$$

```
Dy1=diff(diff(y1))
```

$$Dy1(t) = \frac{\partial^2}{\partial t^2} y_1(t)$$

```
Dy2=diff(diff(y2))
```

$$Dy2(t) = \frac{\partial^2}{\partial t^2} y_2(t)$$

```
[P lambda] = eig(A)
```

$$P = \begin{pmatrix} 1 & -1 \\ 1 & 1 \end{pmatrix}$$

$$\lambda = \begin{pmatrix} -k & 0 \\ 0 & -3k \end{pmatrix}$$

```
if (rank(P)~=length(P))
fprintf('The matrix is not diagonalizable, thus solution is not possible using this method \n')
return
end
D = inv(P)*A*P
```

$$D = \begin{pmatrix} -k & 0 \\ 0 & -3k \end{pmatrix}$$

```
Y = [y1(t);y2(t)]
```

$$Y = \begin{pmatrix} y_1(t) \\ y_2(t) \end{pmatrix}$$

```
for i=1:length(A)
eqs=diff(diff(Y(i),t,1),t,1) - D(i,i)*Y(i) == 0
Sol(i)= dsolve(eqs)
end
```

$$eqs = \frac{\partial^2}{\partial t^2} y_1(t) + k y_1(t) = 0$$

$$Sol = C_3 e^{\sqrt{-k}t} + C_4 e^{-\sqrt{-k}t}$$

$$eqs =$$

$$\frac{\partial^2}{\partial t^2} y_2(t) + 3k y_2(t) = 0$$

$$\text{Sol} = (C_3 e^{\sqrt{-k}t} + C_4 e^{-\sqrt{-k}t} \quad C_5 e^{\sqrt{3}\sqrt{-k}t} + C_6 e^{-\sqrt{3}\sqrt{-k}t})$$

disp(Sol)

$$(C_3 e^{\sqrt{-k}t} + C_4 e^{-\sqrt{-k}t} \quad C_5 e^{\sqrt{3}\sqrt{-k}t} + C_6 e^{-\sqrt{3}\sqrt{-k}t})$$

```
clc
clear all
syms y1(t) y2(t) k G(t) u
Dy1=diff(diff(y1))
```

$$\text{Dy1}(t) = \frac{\partial^2}{\partial t^2} y_1(t)$$

Dy2=diff(diff(y2))

$$\text{Dy2}(t) = \frac{\partial^2}{\partial t^2} y_2(t)$$

A=[0 -1;-1 0]

$$A = 2 \times 2$$

0	-1
-1	0

G(t)=[-101*sin(10*t);101*sin(10*t)]

$$G(t) = \begin{pmatrix} -101 \sin(10t) \\ 101 \sin(10t) \end{pmatrix}$$

```
%cond10=y1(0)==0
%cond11=Dy1(0)==6
%cond20=y2(0)==8
%cond21=Dy2(0)==6
%cond=[cond10;cond20]
[P lambda] = eig(A)
```

$$P = 2 \times 2$$

-0.7071	-0.7071
-0.7071	0.7071

$$\text{lambda} = 2 \times 2$$

-1	0
0	1

```
if (rank(P)~=length(P))
fprintf('The matrix is not diagonalizable, thus solution is not possible using this method \n')
return
end
D = inv(P)*A*P
```

$$D = 2 \times 2$$

-1	0
0	1

Y = [y1(t);y2(t)]

Y =

$$\begin{pmatrix} y_1(t) \\ y_2(t) \end{pmatrix}$$

```
eqs=inv(P)*(diff(diff(Y,t,1),t,1) - D*inv(P)*Y -inv(P)*G(t) == 0)
```

$$\text{eqs} = \begin{pmatrix} \sigma_2 + \sigma_1 = 0 \\ \sigma_2 - \sigma_1 = 0 \end{pmatrix}$$

where

$$\sigma_1 = \frac{\sqrt{2} \left(-\frac{\partial^2}{\partial t^2} y_2(t) + 101 \sqrt{2} \sin(10 t) - \frac{\sqrt{2} y_1(t)}{2} + \frac{\sqrt{2} y_2(t)}{2} \right)}{2}$$

$$\sigma_2 = \frac{\sqrt{2} \left(-\frac{\partial^2}{\partial t^2} y_1(t) + \frac{\sqrt{2} y_1(t)}{2} + \frac{\sqrt{2} y_2(t)}{2} \right)}{2}$$

```
u==inv(P)*Y
```

$$\text{ans} = \begin{pmatrix} u = -\frac{\sqrt{2} y_1(t)}{2} - \frac{\sqrt{2} y_2(t)}{2} \\ u = \frac{\sqrt{2} y_2(t)}{2} - \frac{\sqrt{2} y_1(t)}{2} \end{pmatrix}$$

```
l=inv(P)*G(t)
```

$$l = \begin{pmatrix} 0 \\ 101 \sqrt{2} \sin(10 t) \end{pmatrix}$$

```
for i=1:length(A)
    eqs1=diff(diff(u(i),t,1),t,1) -D(i,i)*u(i)==0
    Sol(i)= dsolve(eqs1)
    pi(i)=l(i)/(-100-D(i,i))
    u(i)=Sol(i)+pi(i)
end
```

```
eqs1 = u = 0
```

```
Error using mupadengine/feval (line 195)
```

```
No differential equations found. Specify differential equations by using symbolic functions.
```

```
Error in dsolve>mupadDsolve (line 340)
```

```
T = feval(symengine,'symobj::dsolve',sys,x,options);
```

```
Error in dsolve (line 194)
```

```
sol = mupadDsolve(args, options);
```

```
Y=P*u
```

```
%Valiveti manikanta bhuvanesh
%19BCD7088
%Solve the DE
% x'(t)=x1-x2
% x2'(t)=2x1+4x2
clc
clear all
syms x1(t) x2(t)
a=diff(x1)==x1-x2;
b=diff(x2)==2*x1+4*x2;
c=[a;b];
[x1(t),x2(t)]=dsolve(c)
```

$$x_1(t) = -C_1 e^{2t} - \frac{C_2 e^{3t}}{2}$$

$$x_2(t) = C_1 e^{2t} + C_2 e^{3t}$$

```
clc
clear all
syms x1(t) x2(t) x3(t)
a=diff(x1)==x2
```

$$a(t) = \frac{\partial}{\partial t} x_1(t) = x_2(t)$$

```
b=diff(x2)==x3
```

$$b(t) = \frac{\partial}{\partial t} x_2(t) = x_3(t)$$

```
c=diff(x3)==8*x1-14*x2+7*x3
```

$$c(t) = \frac{\partial}{\partial t} x_3(t) = 8x_1(t) - 14x_2(t) + 7x_3(t)$$

```
S=[a;b;c];
cond=x1(0)==4;
cond1=x2(0)==6;
cond2=x3(0)==8;
[x1(t) x2(t) x3(t)]=dsolve(S,cond,cond1,cond2)
```

$$x_1(t) = 3e^{2t} - \frac{e^{4t}}{3} + \frac{4e^t}{3}$$

$$x_2(t) = 6e^{2t} - \frac{4e^{4t}}{3} + \frac{4e^t}{3}$$

$$x_3(t) = 12e^{2t} - \frac{16e^{4t}}{3} + \frac{4e^t}{3}$$


```
%Valiveti manikanta bhuvanesh
%19BCD7088
%Program for finding rabbit population in n months
syms f(n) z F
eq = f(n+2) - f(n+1) - f(n)
```

$$eq = f(n+2) - f(n+1) - f(n)$$

```
Zt = ztrans(eq,n,z)
```

$$Zt = z f(0) - z ztrans(f(n),n,z) - z f(1) + z^2 ztrans(f(n),n,z) - z^2 f(0) - ztrans(f(n),n,z)$$

```
Zt = subs(Zt,ztrans(f(n),n,z),F)
```

$$Zt = z f(0) - F z - F - z f(1) + F z^2 - z^2 f(0)$$

```
F = solve(Zt,F)
```

$$F = \frac{-z f(1) - z f(0) + z^2 f(0)}{-z^2 + z + 1}$$

```
pSol = iztrans(F,z,n);
pSol = simplify(pSol)
```

pSol =

$$2 (-1)^{n/2} \cos\left(n \left(\frac{\pi}{2} + \operatorname{asinh}\left(\frac{1}{2}\right) i\right)\right) f(1) + \frac{2^{2-n} \sqrt{5} (\sqrt{5} + 1)^{n-1} \sigma_1}{5} - \frac{2^{1-n} \sqrt{5} (1 - \sqrt{5})^{n-1} \sigma_1}{5}$$

where

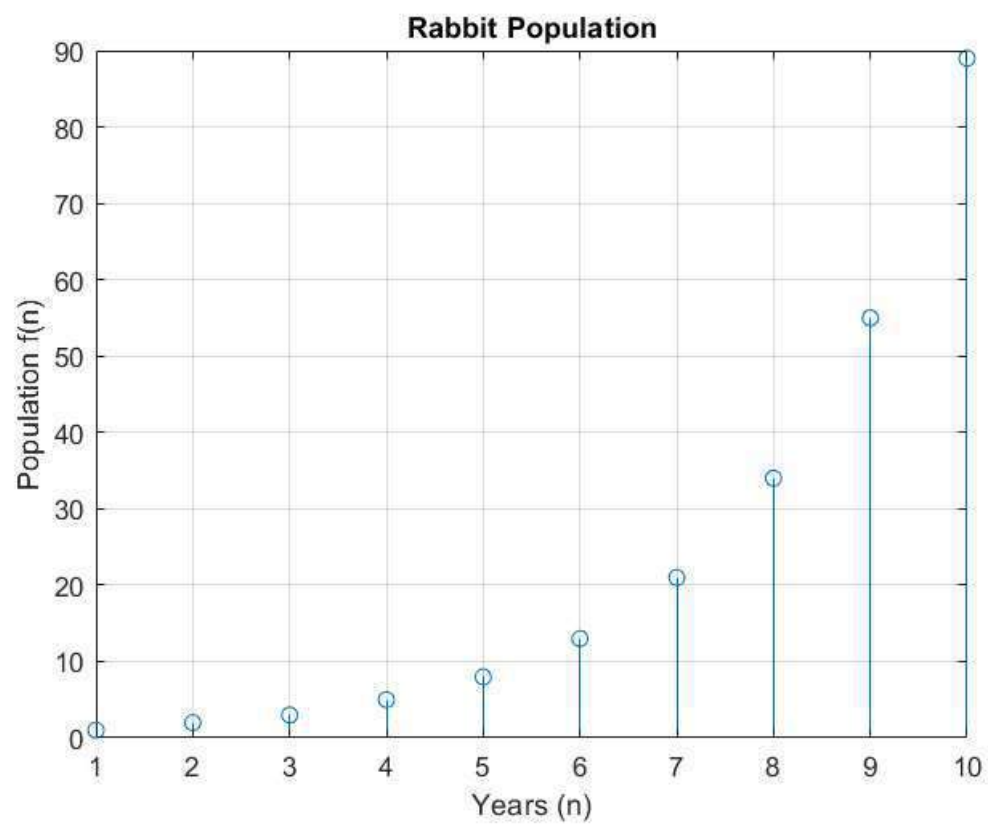
$$\sigma_1 = \frac{f(0)}{2} - f(1)$$

```
pSol = subs(pSol,[f(0) f(1)],[1 1])
```

pSol =

$$2 (-1)^{n/2} \cos\left(n \left(\frac{\pi}{2} + \operatorname{asinh}\left(\frac{1}{2}\right) i\right)\right) - \frac{2^{2-n} \sqrt{5} (\sqrt{5} + 1)^{n-1}}{10} + \frac{2^{1-n} \sqrt{5} (1 - \sqrt{5})^{n-1}}{5}$$

```
nvalues = 1:10;
pSolValues = subs(pSol,n,nvalues);
pSolValues = double(pSolValues);
pSolValues = real(pSolValues);
stem(nvalues,pSolValues)
title('Rabbit Population')
xlabel('Years (n)')
ylabel('Population f(n)')
grid on
```

```
%Valiveti manikanta bhuvanesh
%19BCD7088
%seriesoln
clc
clear all
syms x n
n=50
```

```
n = 50
```

```
a = sym('a',[1 n+1])
```

```
a =
(a1 a2 a3 a4 a5 a6 a7 a8 a9 a10 a11 a12 a13 a14 a15 a16 a17 a18 a19 a20 a21 a22 a2
```

```
y = sum(a.*(x).^[0:n])
```

```
y =
a51 x50 + a50 x49 + a49 x48 + a48 x47 + a47 x46 + a46 x45 + a45 x44 + a44 x43 + a43 x42 + a42 x41 + a41 x40 + a40
```

```
dy = diff(y);
d2y = diff(dy);
ode = collect(d2y-4*y,x)
```

```
ode =
(-4 a51) x50 + (-4 a50) x49 + (2450 a51 - 4 a49) x48 + (2352 a50 - 4 a48) x47 + (2256 a49 - 4 a47) x46 + (2
```

```
coef=coeffs(ode,x)
```

```
coef =
(2 a3 - 4 a1 6 a4 - 4 a2 12 a5 - 4 a3 20 a6 - 4 a4 30 a7 - 4 a5 42 a8 - 4 a6 56 a9 - 4 a7 72 a10 -
```

```
eq1=a(1)==0;
eq2=a(2)==1;
a=solve([eq1, eq2,coef(1:n-1)],a)
```

```
a = struct with fields:
a1: [1 1 sym]
a2: [1 1 sym]
a3: [1 1 sym]
a4: [1 1 sym]
a5: [1 1 sym]
a6: [1 1 sym]
a7: [1 1 sym]
a8: [1 1 sym]
a9: [1 1 sym]
a10: [1 1 sym]
a11: [1 1 sym]
a12: [1 1 sym]
a13: [1 1 sym]
a14: [1 1 sym]
```

```
soln=subs(y,a)
```

```
soln =
4 x49
8644205195683235286768595007647709520704677734375 + 16 x47
58804116977436974739922415018011
```

```
% Solution using dsolve command
syms z(t)
dz = diff(z,t); % First order derivative
d2z = diff(dz,t); % Second order derivative
ode1 = d2z-4*z % given ode in series form
```

$$\text{ode1}(t) = \frac{\partial^2}{\partial t^2} z(t) - 4 z(t)$$

$$\text{ic1}=z(0)=0$$

$$\text{ic1} = z(0) = 0$$

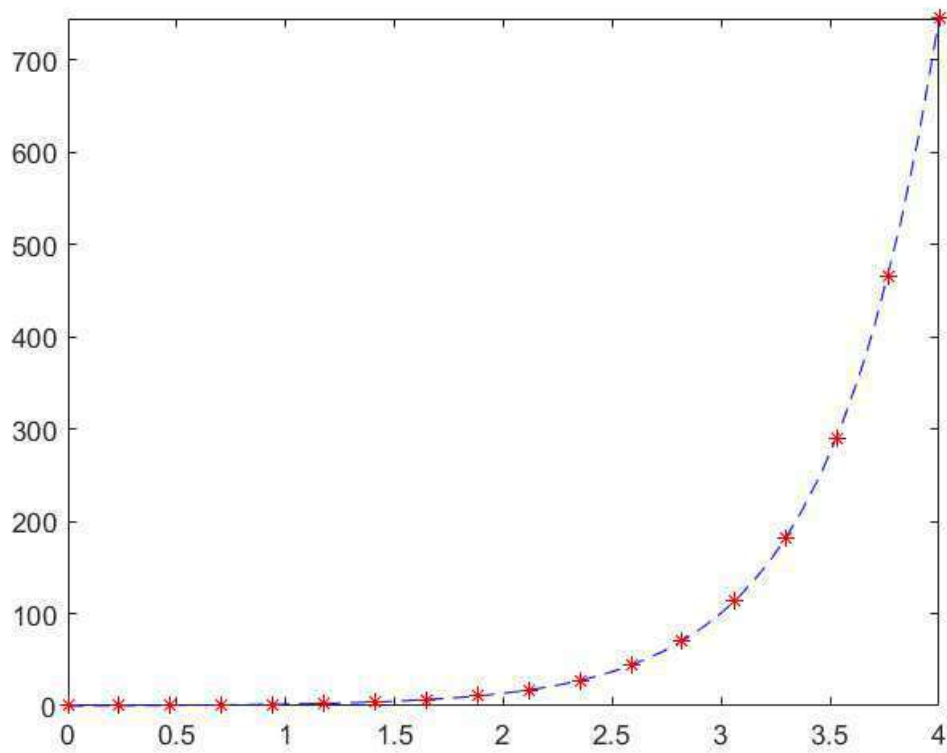
$$\text{ic2}=dz(0)=1$$

$$\text{ic2} = \left(\left(\frac{\partial}{\partial t} z(t) \right) \Big|_{t=0} \right) = 1$$

$$\text{sol1}=(\text{dsolve}(\text{ode1},[\text{ic1} \text{ic2}]))$$

$$\text{sol1} = \frac{e^{-2t} (e^{4t} - 1)}{4}$$

```
% J0=besselj(1,1)
% Y0=bessely(1,1)
% J1=besselj(1,5)
% Y1=bessely(1,5)
% Comparison of exact and series solutions
% soln=subs(sol1)
fplot(soln,[0 4], '--b')
hold on
fplot(sol1,[0 4], '*r')
```



```
% hold on
% fplot(soln(3))
% hold on
% fplot(soln(4))

% xSol = sol.a0
% ySol = sol.a1
% zSol = sol.a2
% a3Sol = sol.a3
% p=taylor(exp(x), x, 1)
```

```

%Valiveti manikanta bhuvanesh
%19BCD7088
%fourierseries
clc
clear all
close all
syms x k L n
% evalin(symengine,'assume(k,Type::Integer)');
a= @(f,x,k,L) int(f*cos(k*pi*x/L)/L,x,-L,L);
b = @(f,x,k,L) int(f*sin(k*pi*x/L)/L,x,-L,L);
fs = @(f,x,n,L) a(f,x,0,L)/2 + ...
symsum(a(f,x,k,L)*cos(k*pi*x/L) + b(f,x,k,L)*sin(k*pi*x/L),k,1,n);
f=abs(x)

```

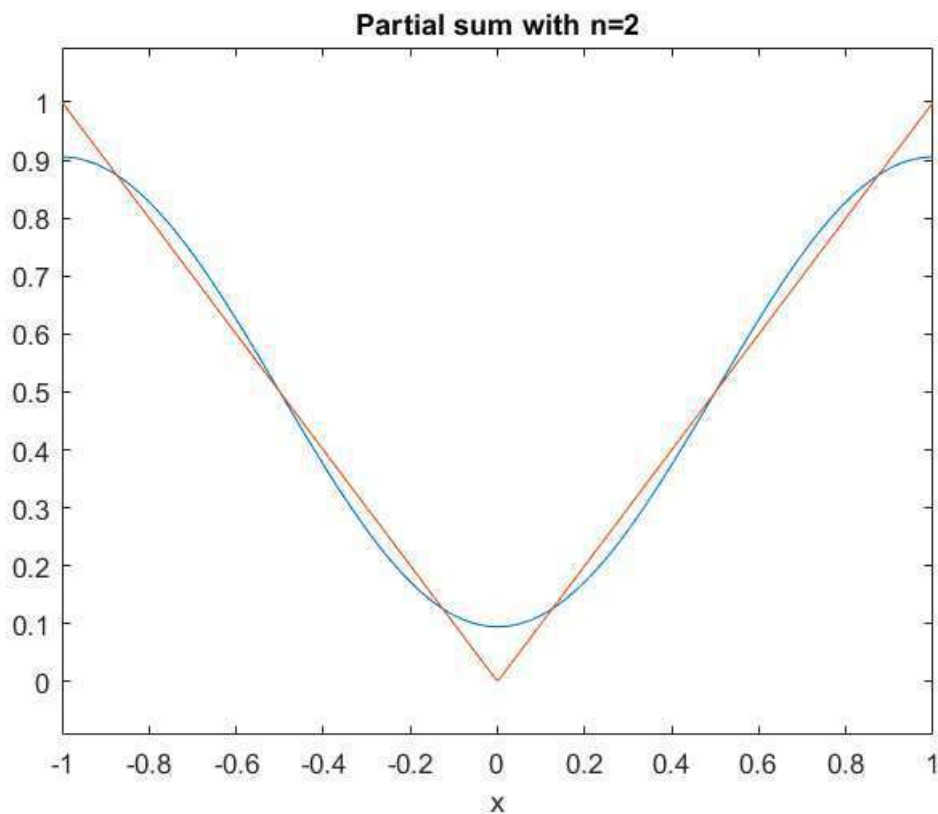
$f = |x|$

```

% pretty(fs(f,x,10,1))

ezplot(fs(f,x,2,1),-1,1)
hold on
ezplot(f,-1,1)
hold off
title('Partial sum with n=2')

```



```

%Valiveti manikanta bhuvanesh
%19BCD7088
%Bessel1st
clc;
clear all;
clf;
r=0:0.1:20;
% J=zeros(10,1)
J0=besselj(1,r);
J1=besselj(1,r);
J2=besselj(2,r);
figure(1)
plot(r,J0,'k','linewidth',2.5);
%hold on
% plot(r,J1,'b','linewidth',2.5);
% plot(r,J2,'r','linewidth',2.5)
grid on
legend('J_0','J_1','J_2')

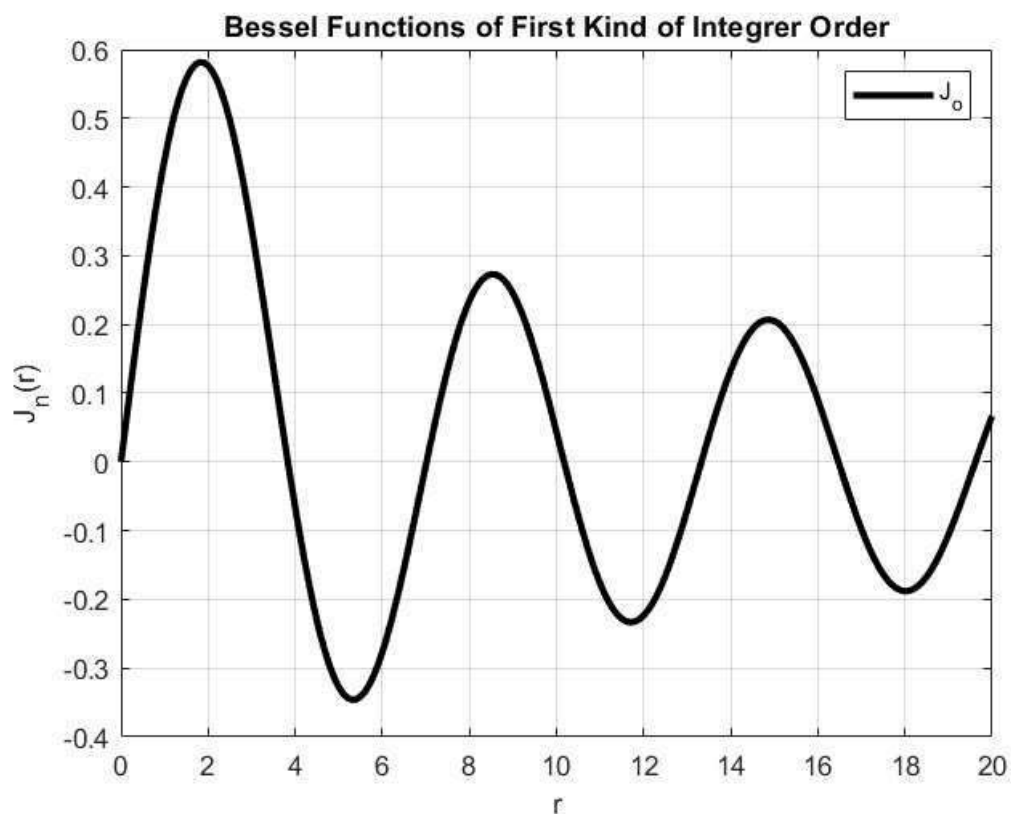
```

Warning: Ignoring extra legend entries.

```

xlabel('r');ylabel('J_n(r)')
title('Bessel Functions of First Kind of Integer Order')

```



```
%Valiveti manikanta bhuvanesh
%19BCD7088
%secondorder_difference_eqn
clc
clear all
syms y(n) r
p= 2%input('Enter the coefficient of y(n+1): ')

```

```
p = 2

```

```
q= 4;
eqn=y(n+2)-p*y(n+1)-q*y(n)==0;
display('The given Difference equation is :')

```

The given Difference equation is :

```
display(eqn)

```

```
eqn = y(n + 2) - 2 y(n + 1) - 4 y(n) = 0

```

```
AE=r^2-p*r-q

```

```
AE = r^2 - 2 r - 4

```

```
r=solve(AE)

```

```
r =
(1 - sqrt(5))
(sqrt(5) + 1)
```

```
% if imag(r(1))~=0

```

```
%Valiveti manikanta bhuvanesh
%19BCD7088
%question 3
syms y(n) z yZT
assume(n>=0 & in(n,'integer'))
f=y(n+2)-(3*(y(n+1)))+2*y(n)-(3^n)
```

$$f = y(n+2) - 3 y(n+1) + 2 y(n) - 3^n$$

```
fZT=ztrans(f,n,z)
```

$$fZT = 3 z y(0) - 3 z \text{ztrans}(y(n), n, z) - \frac{z}{z-3} - z y(1) + z^2 \text{ztrans}(y(n), n, z) - z^2 y(0) + 2 \text{ztrans}(y(n), n, z)$$

```
fZT=subs(fZT,ztrans(y(n),n,z),yZT)
```

$$fZT = 2 yZT - \frac{z}{z-3} + 3 z y(0) - z y(1) - 3 yZT z - z^2 y(0) + yZT z^2$$

```
yZT=solve(fZT,yZT)
```

$$yZT = \frac{\frac{z}{z-3} - 3 z y(0) + z y(1) + z^2 y(0)}{z^2 - 3 z + 2}$$

```
ysol=iztrans(yZT,z,n)
```

$$ysol = y(0) \delta_{n,0} - (\delta_{n,0} - 1) \left(2 y(0) - y(1) + \frac{1}{2} \right) - \left(\frac{2^n}{2} - \frac{\delta_{n,0}}{2} \right) (2 y(0) - 2 y(1) + 2) + \frac{3^n}{2} - \frac{\delta_{n,0}}{2}$$

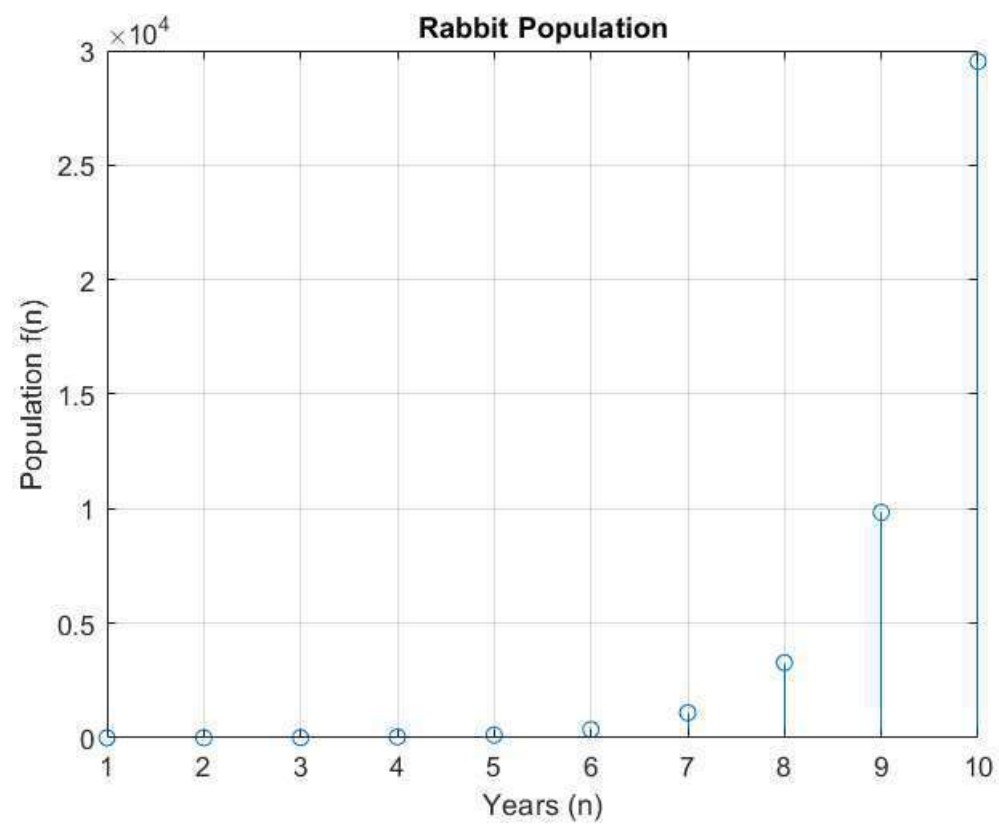
```
ysol=simplify(ysol)
```

$$ysol = 2 y(0) - y(1) - 2^n y(0) + 2^n y(1) - 2^n + \frac{3^n}{2} + \frac{1}{2}$$

```
ysol=subs(ysol,[y(0) y(1)],[0 1])
```

$$ysol = \frac{3^n}{2} - \frac{1}{2}$$

```
nvalues = 1:10;
ySolValues = subs(ysol,n,nvalues);
ySolValues = double(ySolValues);
ySolValues = real(ySolValues);
stem(nvalues,ySolValues)
title('Rabbit Population')
xlabel('Years (n)')
ylabel('Population f(n)')
grid on
```

```
%Valiveti manikanta bhuvanesh
%19BCD7088
%question 4
syms y(n) z yZT
assume(n>=0 & in(n,'integer'))
f=y(n+2)-(4*(y(n+1)))+4*y(n)-(3*n)-2^n
```

$$f = y(n+2) - 4 y(n+1) - 3 n + 4 y(n) - 2^n$$

```
fZT=ztrans(f,n,z)
```

$$fZT = 4 z y(0) - \frac{z}{z-2} - 4 z \text{ztrans}(y(n), n, z) - \frac{3 z}{(z-1)^2} - z y(1) + z^2 \text{ztrans}(y(n), n, z) - z^2 y(0) + 4 \text{ztrans}(y(n), n, z)$$

```
fZT=subs(fZT,ztrans(y(n),n,z),yZT)
```

$$fZT = 4 yZT - \frac{3 z}{(z-1)^2} - \frac{z}{z-2} + 4 z y(0) - z y(1) - 4 yZT z - z^2 y(0) + yZT z^2$$

```
yZT=solve(fZT,yZT)
```

$$yZT = \frac{\frac{3 z}{(z-1)^2} + \frac{z}{z-2} - 4 z y(0) + z y(1) + z^2 y(0)}{z^2 - 4 z + 4}$$

```
ysol=iztrans(yZT,z,n)
```

$$ysol = 3 n + \left(\frac{\delta_{n,0}}{4} + \frac{2^n (n-1)}{4} \right) (2 y(1) - 4 y(0) + 7) + \frac{2^n \binom{n-1}{2}}{4} + y(0) \delta_{n,0} - \frac{25 \delta_{n,0}}{4} + \left(\frac{2^n}{2} - \frac{\delta_{n,0}}{2} \right) (y(1) - y(0))$$

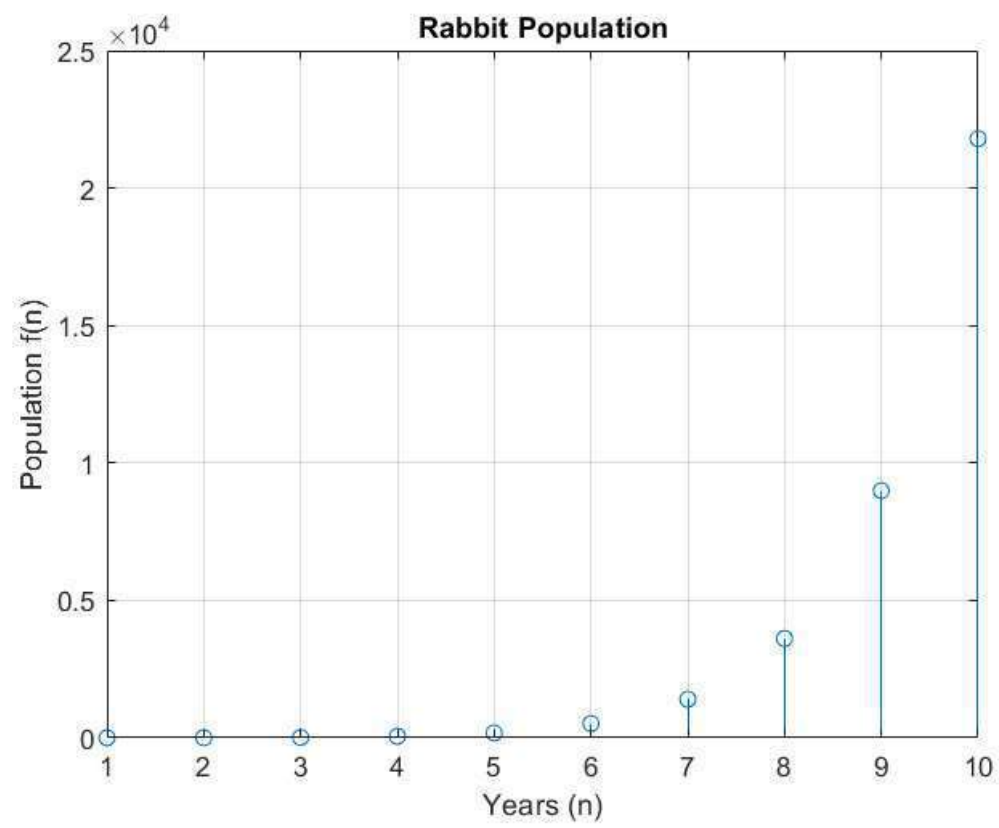
```
ysol=simplify(ysol)
```

$$ysol = 3 n + \frac{2^n \binom{n-1}{2}}{4} + \frac{7 2^n n}{4} + 2^n y(0) - \frac{25 2^n}{4} - 2^n n y(0) + \frac{2^n n y(1)}{2} + 6$$

```
ysol=subs(ysol,[y(0) y(1)],[1 2])
```

$$ysol = 3 n + \frac{2^n \binom{n-1}{2}}{4} + \frac{7 2^n n}{4} - \frac{21 2^n}{4} + 6$$

```
nvalues = 1:10;
ySolValues = subs(ysol,n,nvalues);
ySolValues = double(ySolValues);
ySolValues = real(ySolValues);
stem(nvalues,ySolValues)
title('Rabbit Population')
xlabel('Years (n)')
ylabel('Population f(n)')
grid on
```



```
%Valiveti manikanta bhuvanesh
%19BCD7088
%question 5
syms y(n) z
assume(n>=0 & in(n,'integer'))
f=y(n)+((1/4)^n)*heaviside(n)
```

f =

$$y(n) + \left(\frac{1}{4}\right)^n \text{heaviside}(n)$$

```
fZT=ztrans(f,n,z)
```

fZT =

$$\frac{1}{4z-1} + ztrans(y(n),n,z) + \frac{1}{2}$$

```
fZT=subs(fZT,ztrans(y(n),n,z),yZT)
```

fZT =

$$z + \frac{1}{4z-1} + \frac{1}{2}$$

```
f=(2*z)/(z-1)
```

f =

$$\frac{2z}{z-1}$$

```
inverse=iztrans(f,z,n)
```

inverse = 2

```
%Valiveti manikanta bhuvanesh
%19BCD7088
%question 6
syms y(n) z yZT
assume(n>=0 & in(n,'integer'))
f=y(n+2)-(5*(y(n+1)))+6*y(n)-5^n
```

$$f = y(n+2) - 5 y(n+1) + 6 y(n) - 5^n$$

```
fZT=ztrans(f,n,z)
```

$$fZT = 5 z y(0) - 5 z \text{ztrans}(y(n), n, z) - \frac{z}{z-5} - z y(1) + z^2 \text{ztrans}(y(n), n, z) - z^2 y(0) + 6 \text{ztrans}(y(n), n, z)$$

```
fZT=subs(fZT,ztrans(y(n),n,z),yZT)
```

$$fZT = 6 yZT - \frac{z}{z-5} + 5 z y(0) - z y(1) - 5 yZT z - z^2 y(0) + yZT z^2$$

```
yZT=solve(fZT,yZT)
```

$$yZT = \frac{\frac{z}{z-5} - 5 z y(0) + z y(1) + z^2 y(0)}{z^2 - 5 z + 6}$$

```
ysol=iztrans(yZT,z,n)
```

$$ysol = \left(\frac{2^n}{2} - \frac{\delta_{n,0}}{2} \right) \left(6 y(0) - 2 y(1) + \frac{2}{3} \right) - \left(\frac{3^n}{3} - \frac{\delta_{n,0}}{3} \right) \left(6 y(0) - 3 y(1) + \frac{3}{2} \right) + y(0) \delta_{n,0} + \frac{5^n}{6} - \frac{\delta_{n,0}}{6}$$

```
ysol=simplify(ysol)
```

$$ysol = 3 \cdot 2^n y(0) - 2^n y(1) - 2 \cdot 3^n y(0) + 3^n y(1) + \frac{2^n}{3} - \frac{3^n}{2} + \frac{5^n}{6}$$

```
ysol=subs(ysol,[y(0) y(1)],[1 1])
```

$$ysol = \frac{7 \cdot 2^n}{3} - \frac{3 \cdot 3^n}{2} + \frac{5^n}{6}$$

```
%Valiveti manikanta bhuvanesh
%19BCD7088
%quetion 1
```

```
syms x y
p=1
```

```
p = 1
```

```
q=p/2
```

```
q = 0.5000
```

```
x=0:1:5
```

```
x = 1 6
      0      1      2      3      4      5
```

```
y=[4,8,15,7,6,2]
```

```
y = 1 6
      4      8      15      7      6      2
```

```
k=6
```

```
k = 6
```

```
l=6
```

```
l = 6
```

```
a0=(2/k)*sum(y)
```

```
a0 = 14
```

```
for n=1:l
an=(2/k)*sum(y.*cos(n*pi*x/q))
bn=(2/k)*sum(y.*sin(n*pi*x/q))
end
```

```
an = 14
bn = -7.5928e-15
an = 14
bn = -1.5186e-14
an = 14
bn = -2.7515e-14
an = 14
bn = -3.0371e-14
an = 14
bn = -4.9806e-14
an = 14
bn = -5.5031e-14
```

```
for n=1:l
S=an*cos(n*pi*x/q)+bn*sin(n*pi*x/q);
end
HS=(a0/2)+sum(S)
```

```
HS = 91
```



```
%Valiveti manikanta bhuvanesh
%19BCD7088
%question 2
```

```
syms f(n) z p
assume(n>=0 & in(n,'integer'))
eq =f(n+2)-3*f(n+1)+2*f(n)==0
```

$$\text{eq} = f(n+2) - 3 f(n+1) + 2 f(n) = 0$$

```
Zt = ztrans(eq,n,z)
```

$$\text{Zt} = 3 z f(0) - 3 z \text{ztrans}(f(n), n, z) - z f(1) + z^2 \text{ztrans}(f(n), n, z) - z^2 f(0) + 2 \text{ztrans}(f(n), n, z) = 0$$

```
Zt = subs(Zt,ztrans(f(n),n,z),p)
```

$$\text{Zt} = 2 p + 3 z f(0) - z f(1) - 3 p z - z^2 f(0) + p z^2 = 0$$

```
p = solve(Zt,p)
```

$$p = \frac{z f(1) - 3 z f(0) + z^2 f(0)}{z^2 - 3 z + 2}$$

```
pSol = iztrans(p,z,n);
pSol = simplify(pSol)
```

$$\text{pSol} = 2 f(0) - f(1) - 2^n f(0) + 2^n f(1)$$

```
pSol = subs(pSol,[f(0) f(1)],[200 220])
```

$$\text{pSol} = 20 2^n + 180$$


```
%Valiveti manikanta bhuvanesh
%19BCD7088
%question 3
syms y(n) z yZT
assume(n>=0 & in(n,'integer'))
f=y(n+2)-(3*(y(n+1)))+2*y(n)-(3^n)
```

$$f = y(n+2) - 3 y(n+1) + 2 y(n) - 3^n$$

```
fZT=ztrans(f,n,z)
```

$$fZT = 3 z y(0) - 3 z \text{ztrans}(y(n), n, z) - \frac{z}{z-3} - z y(1) + z^2 \text{ztrans}(y(n), n, z) - z^2 y(0) + 2 \text{ztrans}(y(n), n, z)$$

```
fZT=subs(fZT,ztrans(y(n),n,z),yZT)
```

$$fZT = 2 yZT - \frac{z}{z-3} + 3 z y(0) - z y(1) - 3 yZT z - z^2 y(0) + yZT z^2$$

```
yZT=solve(fZT,yZT)
```

$$yZT = \frac{\frac{z}{z-3} - 3 z y(0) + z y(1) + z^2 y(0)}{z^2 - 3 z + 2}$$

```
ysol=iztrans(yZT,z,n)
```

$$ysol = y(0) \delta_{n,0} - (\delta_{n,0} - 1) \left(2 y(0) - y(1) + \frac{1}{2} \right) - \left(\frac{2^n}{2} - \frac{\delta_{n,0}}{2} \right) (2 y(0) - 2 y(1) + 2) + \frac{3^n}{2} - \frac{\delta_{n,0}}{2}$$

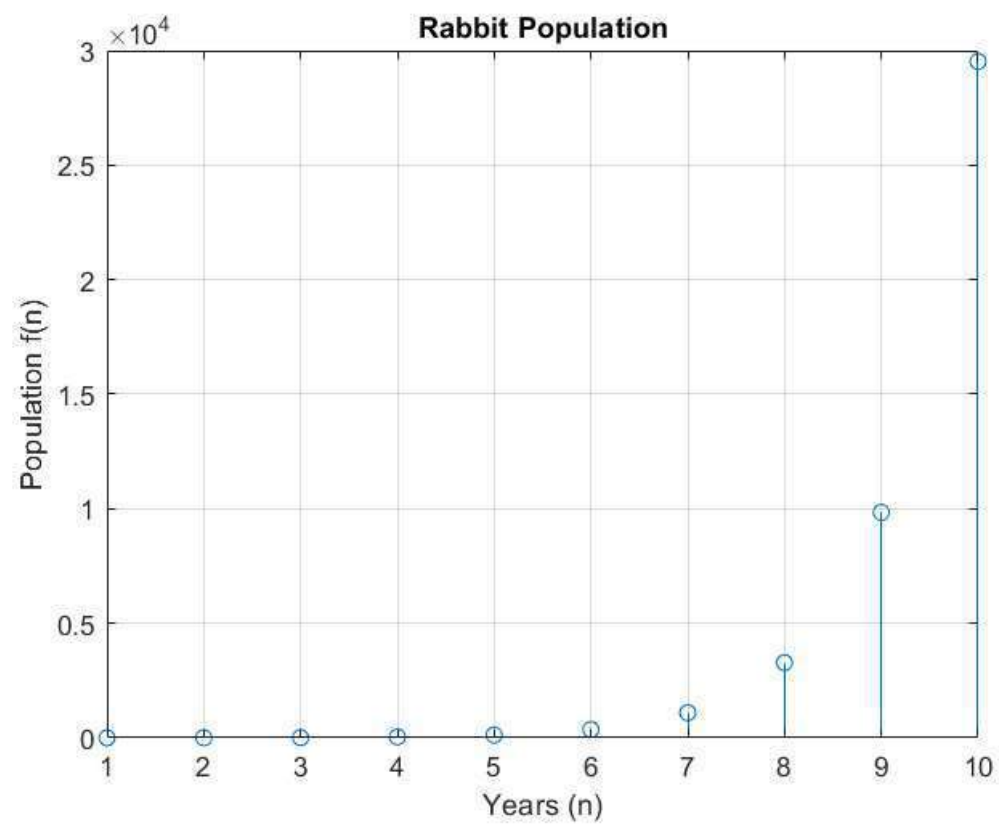
```
ysol=simplify(ysol)
```

$$ysol = 2 y(0) - y(1) - 2^n y(0) + 2^n y(1) - 2^n + \frac{3^n}{2} + \frac{1}{2}$$

```
ysol=subs(ysol,[y(0) y(1)],[0 1])
```

$$ysol = \frac{3^n}{2} - \frac{1}{2}$$

```
nvalues = 1:10;
ySolValues = subs(ysol,n,nvalues);
ySolValues = double(ySolValues);
ySolValues = real(ySolValues);
stem(nvalues,ySolValues)
title('Rabbit Population')
xlabel('Years (n)')
ylabel('Population f(n)')
grid on
```



```
%Valiveti manikanta bhuvanesh
%19BCD7088
%question 4
syms y(n) z yZT
assume(n>=0 & in(n,'integer'))
f=y(n+2)-(4*(y(n+1)))+4*y(n)-(3*n)-2^n
```

$$f = y(n+2) - 4 y(n+1) - 3 n + 4 y(n) - 2^n$$

```
fZT=ztrans(f,n,z)
```

$$fZT = 4 z y(0) - \frac{z}{z-2} - 4 z \text{ztrans}(y(n), n, z) - \frac{3 z}{(z-1)^2} - z y(1) + z^2 \text{ztrans}(y(n), n, z) - z^2 y(0) + 4 \text{ztrans}(y(n), n, z)$$

```
fZT=subs(fZT,ztrans(y(n),n,z),yZT)
```

$$fZT = 4 yZT - \frac{3 z}{(z-1)^2} - \frac{z}{z-2} + 4 z y(0) - z y(1) - 4 yZT z - z^2 y(0) + yZT z^2$$

```
yZT=solve(fZT,yZT)
```

$$yZT = \frac{\frac{3 z}{(z-1)^2} + \frac{z}{z-2} - 4 z y(0) + z y(1) + z^2 y(0)}{z^2 - 4 z + 4}$$

```
ysol=iztrans(yZT,z,n)
```

$$ysol = 3 n + \left(\frac{\delta_{n,0}}{4} + \frac{2^n (n-1)}{4} \right) (2 y(1) - 4 y(0) + 7) + \frac{2^n \binom{n-1}{2}}{4} + y(0) \delta_{n,0} - \frac{25 \delta_{n,0}}{4} + \left(\frac{2^n}{2} - \frac{\delta_{n,0}}{2} \right) (y(1) - y(0))$$

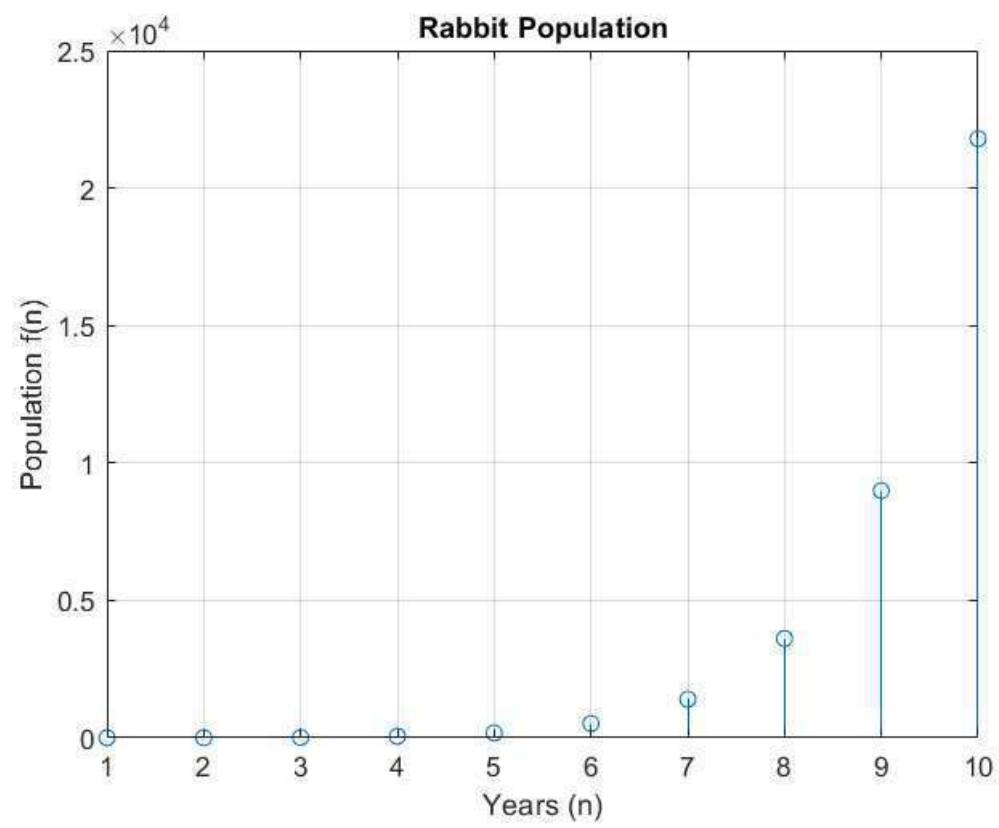
```
ysol=simplify(ysol)
```

$$ysol = 3 n + \frac{2^n \binom{n-1}{2}}{4} + \frac{7 2^n n}{4} + 2^n y(0) - \frac{25 2^n}{4} - 2^n n y(0) + \frac{2^n n y(1)}{2} + 6$$

```
ysol=subs(ysol,[y(0) y(1)],[1 2])
```

$$ysol = 3 n + \frac{2^n \binom{n-1}{2}}{4} + \frac{7 2^n n}{4} - \frac{21 2^n}{4} + 6$$

```
nvalues = 1:10;
ySolValues = subs(ysol,n,nvalues);
ySolValues = double(ySolValues);
ySolValues = real(ySolValues);
stem(nvalues,ySolValues)
title('Rabbit Population')
xlabel('Years (n)')
ylabel('Population f(n)')
grid on
```



```
%Valiveti manikanta bhuvanesh
%19BCD7088
%question 5
syms y(n) z
assume(n>=0 & in(n,'integer'))
f=y(n)+((1/4)^n)*heaviside(n)
```

$$f = y(n) + \left(\frac{1}{4}\right)^n \text{heaviside}(n)$$

```
fZT=ztrans(f,n,z)
```

$$fZT = \frac{1}{4z-1} + ztrans(y(n),n,z) + \frac{1}{2}$$

```
fZT=subs(fZT,ztrans(y(n),n,z),yZT)
```

$$fZT = z + \frac{1}{4z-1} + \frac{1}{2}$$

```
f=(2*z)/(z-1)
```

$$f = \frac{2z}{z-1}$$

```
inverse=iztrans(f,z,n)
```

$$\text{inverse} = 2$$

```
%Valiveti manikanta bhuvanesh
%19BCD7088
%question 6
syms y(n) z yZT
assume(n>=0 & in(n,'integer'))
f=y(n+2)-(5*(y(n+1)))+6*y(n)-5^n
```

$$f = y(n+2) - 5 y(n+1) + 6 y(n) - 5^n$$

```
fZT=ztrans(f,n,z)
```

$$fZT = 5 z y(0) - 5 z \text{ztrans}(y(n), n, z) - \frac{z}{z-5} - z y(1) + z^2 \text{ztrans}(y(n), n, z) - z^2 y(0) + 6 \text{ztrans}(y(n), n, z)$$

```
fZT=subs(fZT,ztrans(y(n),n,z),yZT)
```

$$fZT = 6 yZT - \frac{z}{z-5} + 5 z y(0) - z y(1) - 5 yZT z - z^2 y(0) + yZT z^2$$

```
yZT=solve(fZT,yZT)
```

$$yZT = \frac{\frac{z}{z-5} - 5 z y(0) + z y(1) + z^2 y(0)}{z^2 - 5 z + 6}$$

```
ysol=iztrans(yZT,z,n)
```

$$ysol = \left(\frac{2^n}{2} - \frac{\delta_{n,0}}{2} \right) \left(6 y(0) - 2 y(1) + \frac{2}{3} \right) - \left(\frac{3^n}{3} - \frac{\delta_{n,0}}{3} \right) \left(6 y(0) - 3 y(1) + \frac{3}{2} \right) + y(0) \delta_{n,0} + \frac{5^n}{6} - \frac{\delta_{n,0}}{6}$$

```
ysol=simplify(ysol)
```

$$ysol = 3 \cdot 2^n y(0) - 2^n y(1) - 2 \cdot 3^n y(0) + 3^n y(1) + \frac{2^n}{3} - \frac{3^n}{2} + \frac{5^n}{6}$$

```
ysol=subs(ysol,[y(0) y(1)],[1 1])
```

$$ysol = \frac{7 \cdot 2^n}{3} - \frac{3 \cdot 3^n}{2} + \frac{5^n}{6}$$