

4. Recursion 2.

Important question

- (1) check AB
- (2) merge sort
- (3) quicksort
- (4) All permutation * (backtrack)
- (5) subset of array (backtrack)
- (6) find subset sum to K
- (7) print all code - song (best)
- (8) print All keypad combinations

length of str

```
int length(char input[]) {
```

```
    if (input[0] == '\0')
```

```
        return 0;
```

```
    return 1 + length(input + 1);
```

5

$1 + \overset{0}{\cancel{l("')}} \rightarrow$

$\leftarrow 1 + \overset{1}{\cancel{l("h")}};$

Recursion

eg. Manish 6

$1 + \overset{5}{\cancel{l("anish")}}$

\downarrow
 $1 + \overset{4}{\cancel{l("nish")}}$

\downarrow
 $1 + \overset{3}{\cancel{l("ish")}}$

\downarrow
 $1 + \overset{2}{\cancel{l("sh")}}$

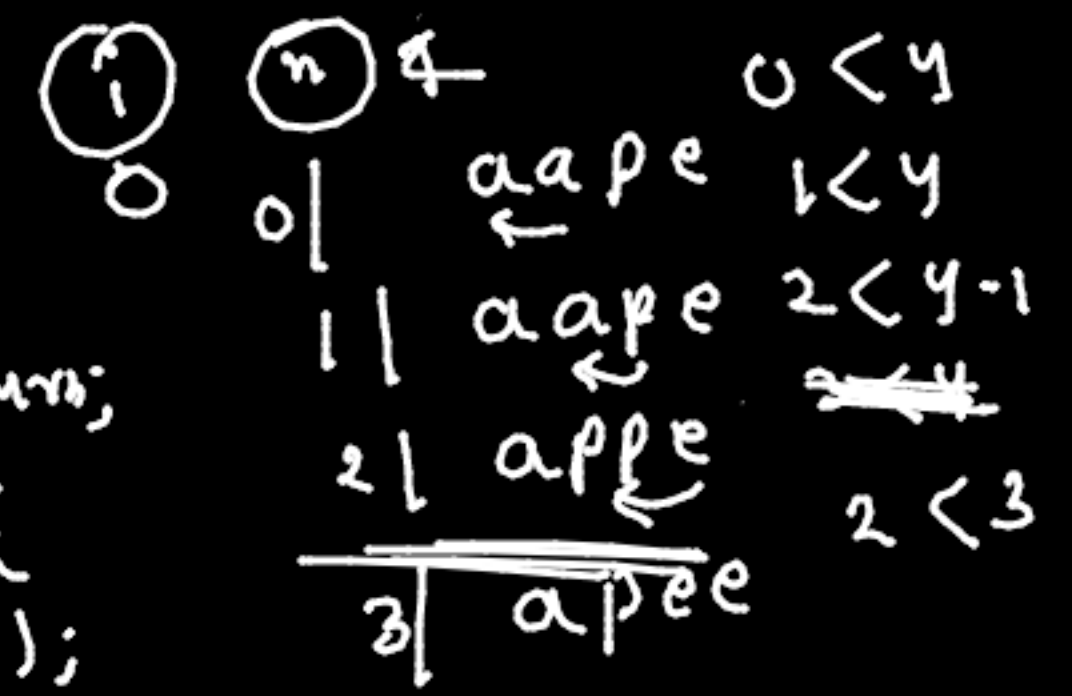
eg. aabccde
→ abcde

```
else {
    fun(input+1);
}
```

shifting

Remove duplicate

```
void fun(char input[])
{
    if (input[0] == '\0') return;
    if (input[0] == input[1]) {
        int i = 0, n = strlen(input);
        [for (; i < n; i++)
            input[i] = input[i+1];
        input[i] = '\0';
        fun(input);
    }
}
```



Condⁿ

- (i) Start with a
- (ii) a followed by a or bb
or nothing
- (iii) bb followed by a

eg. abb
→ true

abbabb

abbabb

→ true

abab

→ false

Check ab

Code

1 or 2 or 3 steps.

Staircase

```
int ways(int n) {  
    if (n <= 2)  
        return n;  
    if (n == 3)  
        return 4;  
    return f(n-1) + f(n-2) + f(n-3);  
}
```

n=4

1,1,1,1

1,2,1

1,3

1,1,2

2,2

2,1,1

3,1

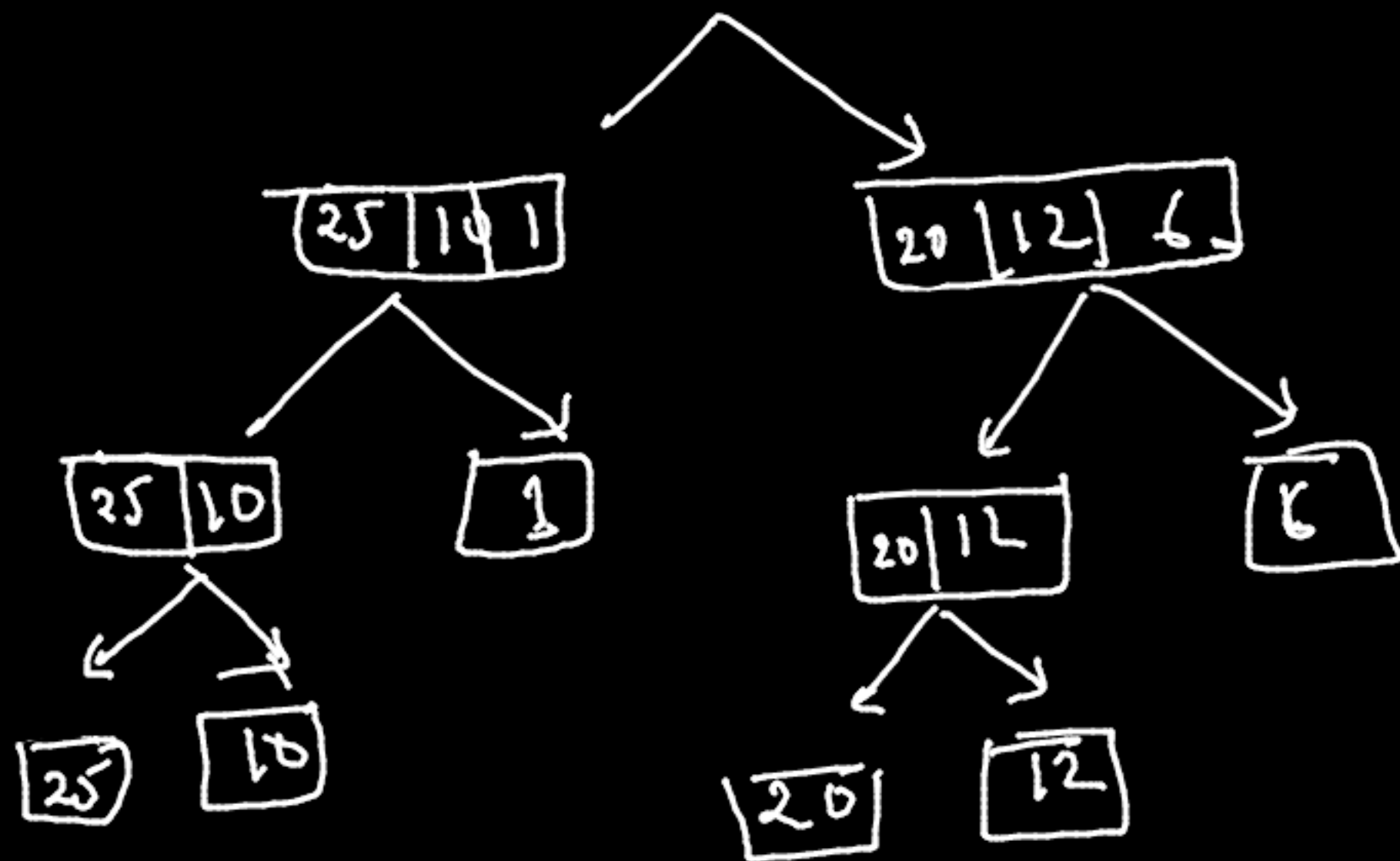
7 Ways.

① → 1

② → 1,1
 → 2

③ → 1,1,1
 → 1,2
 → 2,1
 → 3

Merge Sort

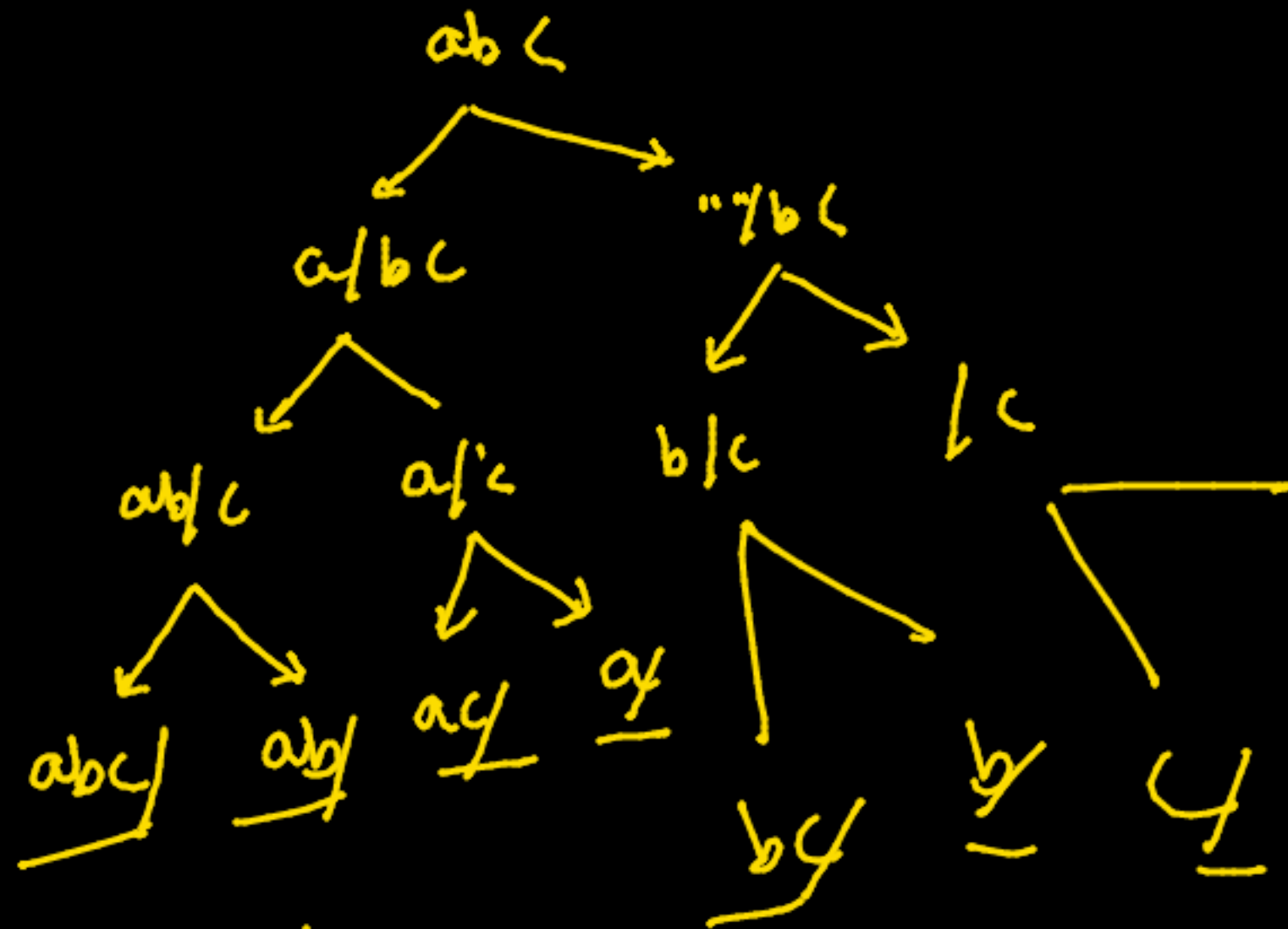


abc subsequence

"
a
b
c
ab
ac
bc
abc

2^n

Subsequence $\rightarrow 2^n$ 4. 3 $2^3 = 8$



↓ code


```
void subsequence(string input, string output)
```

```
{  
    if (input.empty()) {  
        cout << output << endl;  
        return;  
    }
```

pick // including that character ⁱⁿ output and moving one step further
subsequence(input.substr(1), output + input[0]);

Don't pick // not including that character in output and moving one step further
subsequence(input.substr(1), output);

```
}  
  
main() {  
    subsequence("abc", "");  
}
```


Subsequence (Another solⁿ)

```
int subseq ( string input, string output[] ) {  
    if (input.size() == 0) {  
        output[0] = "";  
        return 1;  
    }
```

```
    ↓  
    int smallOutputSize = subseq (input.substr(1), output);
```

```
    for (int i = 0; i < smallOutputSize; i++)  
        output[i + smallOutputSize] = input[0] + output[i];
```

```
    return 2 * smallOutputSize;  
}
```

abc

$\begin{bmatrix} "" \\ c \\ b \\ bc \end{bmatrix}$

a

ac

ab

abc

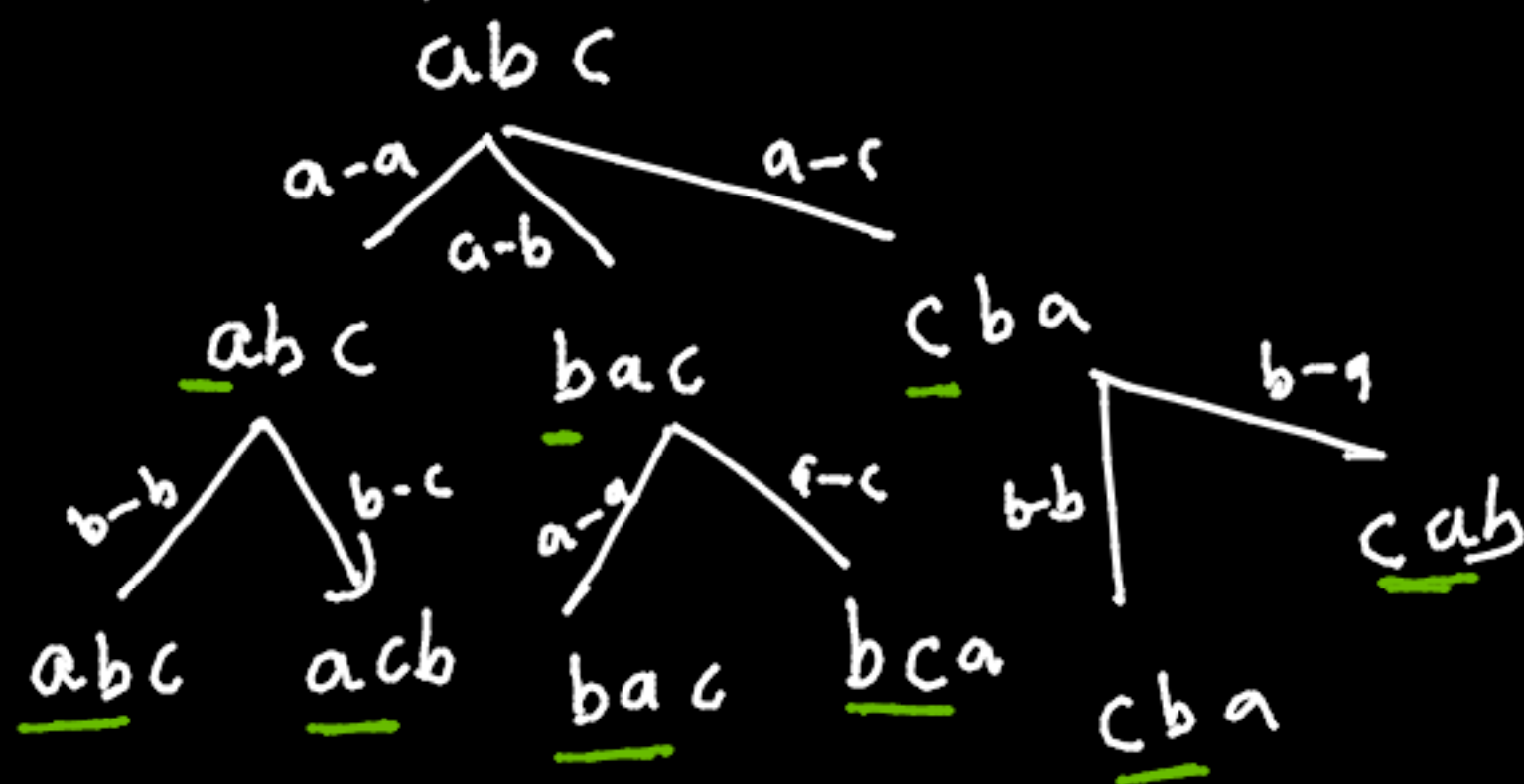
copying and adding

Return permutation

→ $n!$

a-b (a swap b)

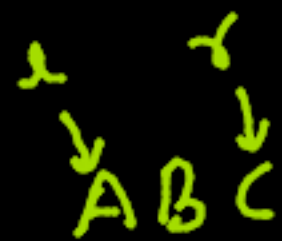
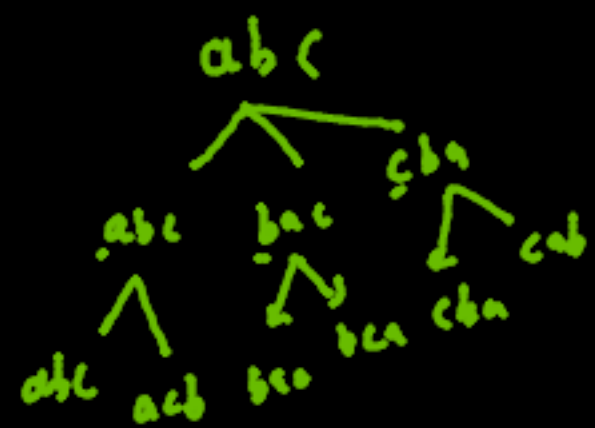
fix



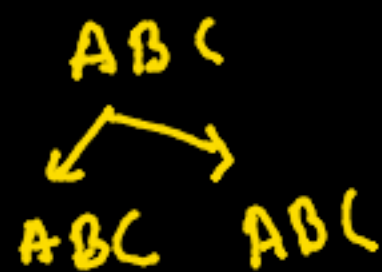
solution

eg. abc

- abc
- acb
- bac
- bca
- cab
- cba



①	②	③
0	2	0
1		1
2		2



```
void permutation (string &s, int l, int r) {
```

```
    if (l == r) {
```

```
        cout << s;
```

```
    }
```

```
    else {
```

```
        for (int i = l; i <= r; i++) {
```

```
            swap (s[l], s[i]);
```

```
            permutation (s, l+1, r)
```

```
            swap (s[l], s[i]);
```

```
    }
```

ABC

eg. [15, 20, 12]

15

26

12

15 20

15 12

20 12

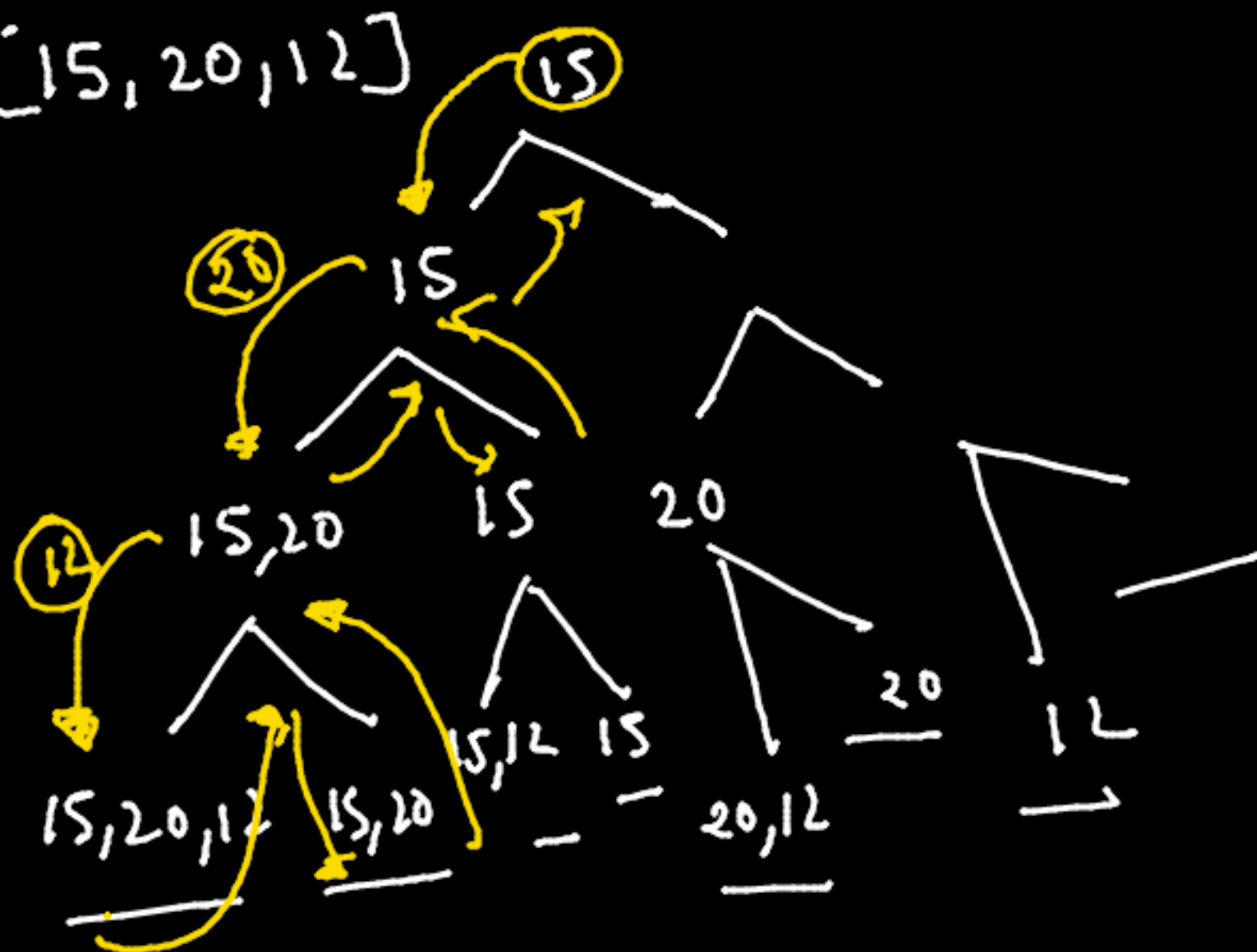
L5 20 12

empty

code

Subset of array

→ $2^n \leftarrow$ length of array.

 $[15, 20, 12]$ 

```
void printSubset(int arr[], int i, int n, vector<int> v) {
```

```
    if (i > n) {
```

```
        for (auto x: v)
```

```
            cout << x << " ";
```

```
        cout << endl;
```

```
        return
```

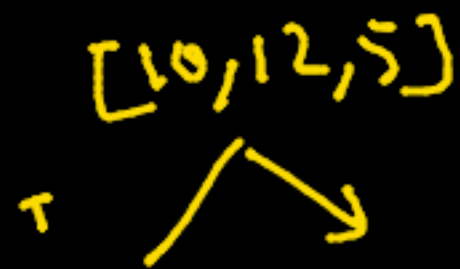
```
    }
```

```
    v.push_back(arr[i]);
```

```
    printSubset(arr, i+1, n, v)
```

```
    v.pop_back();
```

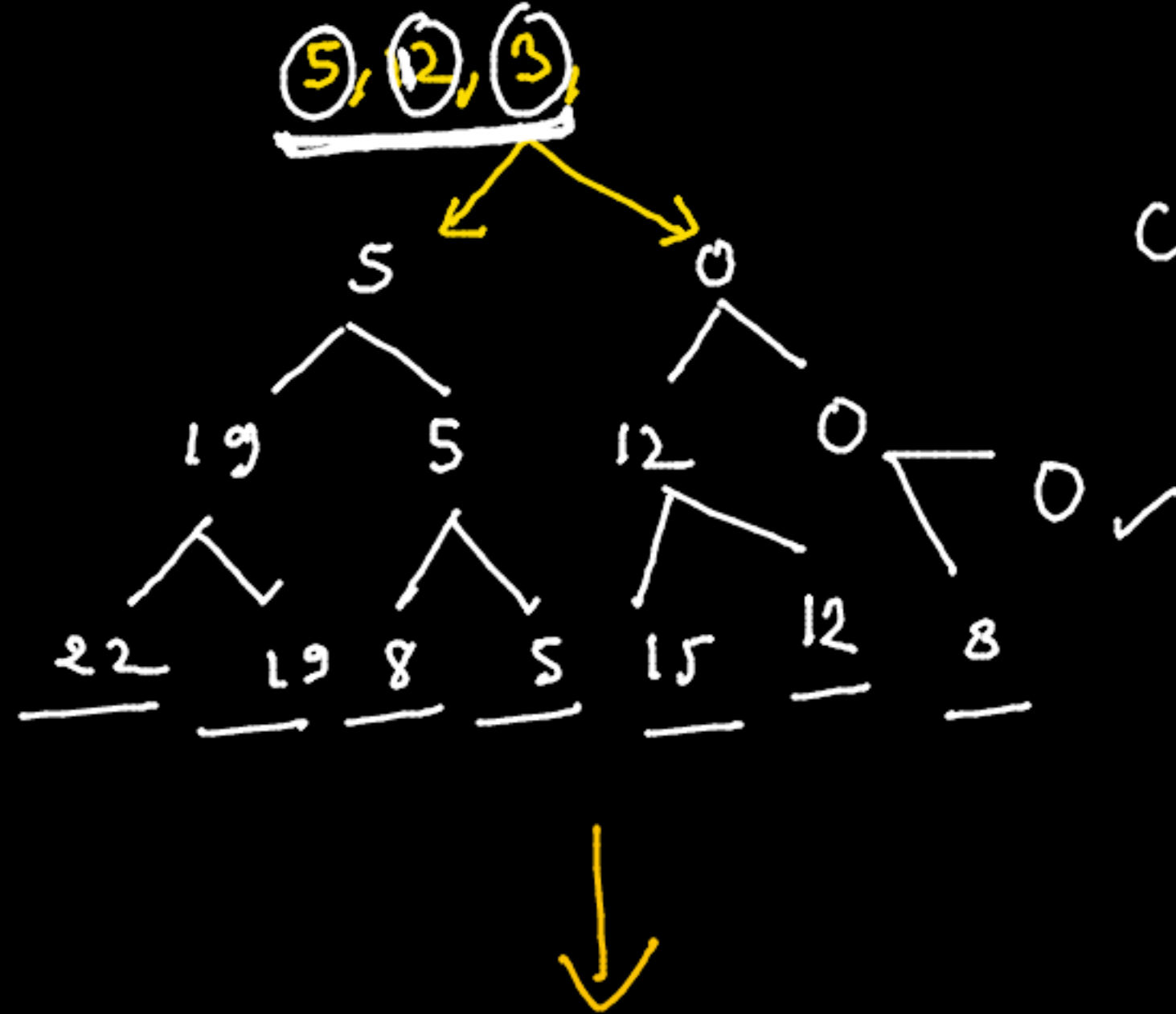
```
    printSubset(arr, i+1, n, v);
```



Including element then calling recursive function to print all subset then pop that particular element

Not including an element.

Return Subset sum To K



Combination.
Taking all possible
subset.

code



4,2


```
void printSubsetsToK(int arr[], int i, int n, vector<int> v, target) {
```

```
    if (i > n) {
```

```
        if (target == 0)
```

```
            for (auto x : v)
```

```
                cout << x << " ";
```

```
            cout << endl;
```

```
        }
```

```
    } return;
```

```
    target -= arr[i];
```

```
    v.push_back(arr[i]);
```

```
    printSubsetsToK(arr, i+1, n, v, target)
```

including not element & target push that
element and move forward.

// Backtrack

```
target += arr[i];
```

```
v.pop_back();
```

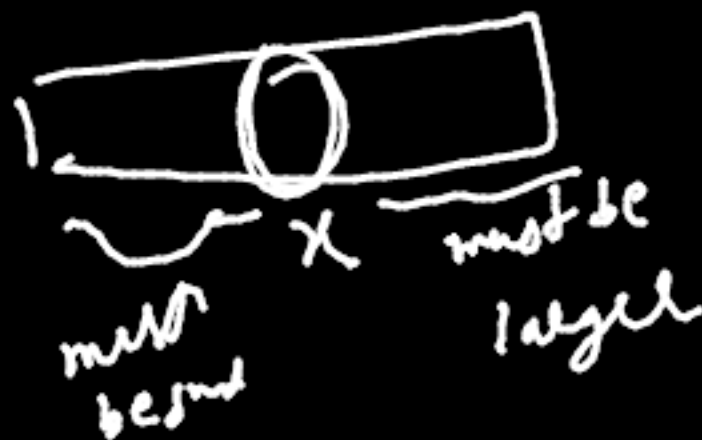
```
printSubsetsToK(arr, i+1, n, v, target)
```

Not including that element

Quick Sort



right
place
me dulo



```
void qs(int arr[], int l, int r)
```

```
if (l > r)
```

```
    return;
```

```
    c = partition(arr, l, r)
```

```
    qs(arr, l, c-1);
```

```
    qs(arr, c+1, r);
```



```

int partition (int arr[], int start, int end) {
    int pivot = arr[start]
    int countSmaller = 0
    for (int i = start; i ≤ end; i++)
        if (pivot > arr[i])
            countSmaller++;
    }

```

```

int pivotIndex = start + countSmaller;
swap(arr[start], arr[pivotIndex]);

```

```

    int i = start, j = end
    while (i < j)
    {
        if (pivot > arr[i])
            i++;
        else if (pivot < arr[j])
            j--;
        else {
            swap(arr[i], arr[j]);
            i++; j--;
        }
    }
    return pivotIndex;
}

```

1-a	16-l
2-b	17-m
3-c	18-n
4-d	19-o
5-e	20-p
6-f	21-q
7-g	22-r
8-h	23-s
9-i	24-t
10-j	25-u
11-k	26-v
12-l	
13-m	
14-n	
15-o	

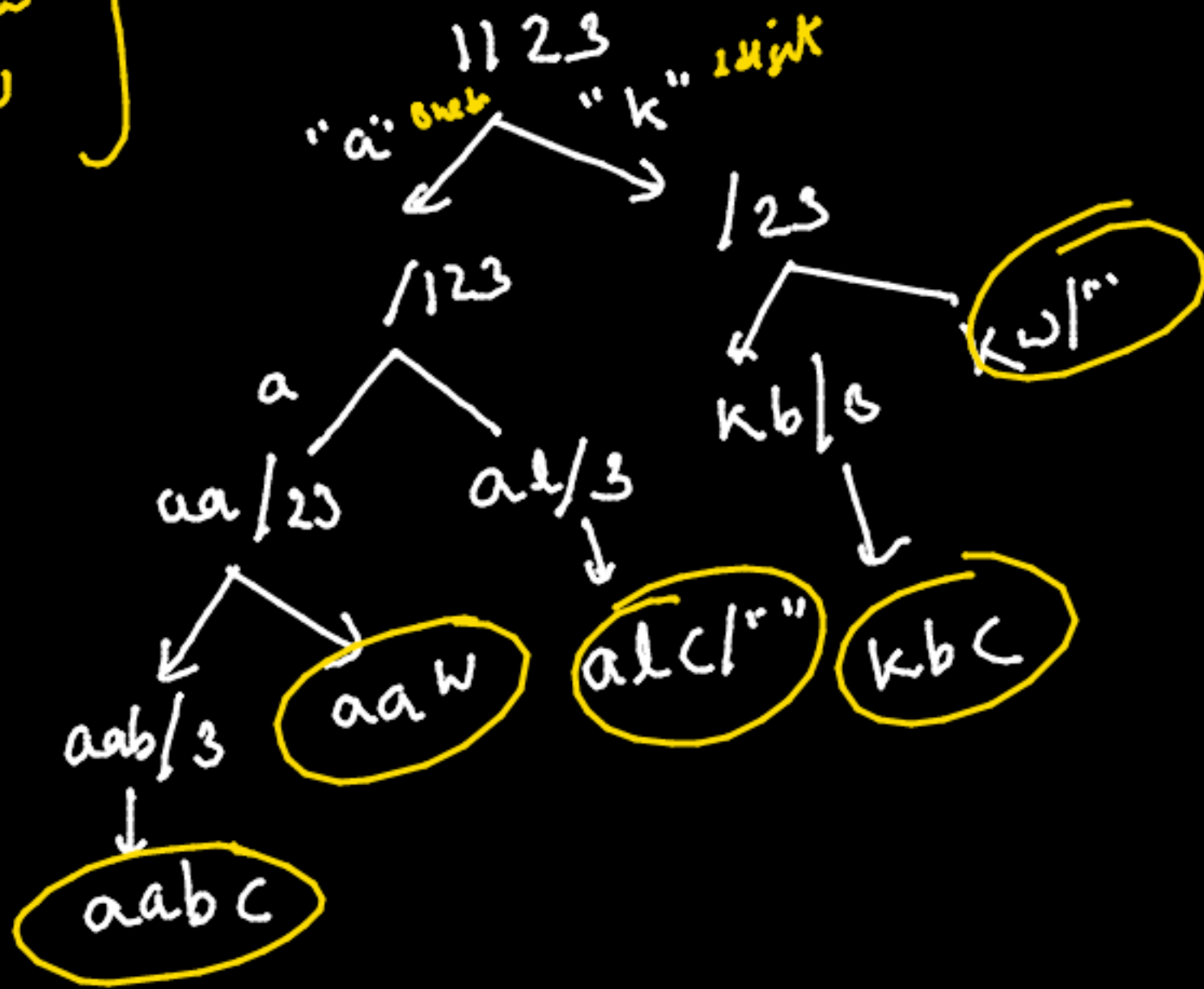
Print all code

"1123"

aabc
alcl
aaw
kw
kbc

5 outputs

Choices → chose 3 digits
① chose 2 digits



```

void printAll ( string input, string output ) {
    if ( input.empty() ) {
        cout << output << endl;
        return;
    }

```

input = "cab"

output = ""

↳

char c1 = input[0] - '0' + 'a' - 1; → first digit to char

int b = stoi(input.substr(0,2)); → first two digit

char c2 = b - 1 + 'a'; → first 2 digit into char.

printAll(input.substr(1), output + c1); → for 1 digit of ""

if (b >= 10 || b <= 26)

{ printAll(input.substr(2), output + c2); → for two digit of ""

! }