hw10

February 1, 2021

```
[]: import os
     import sys
     import time
     import pickle as pk
     from typing import Union, Tuple
     from collections import OrderedDict
     import numpy as np
     import pandas as pd
     import matplotlib.pyplot as plt
     import seaborn as sns
     import torch
     from torch.autograd import grad
     from torch.nn import Parameter
     import torch.nn as nn
     import torch.functional as F
     import torch.optim as optim
     import torchvision
     import torchvision.transforms as transforms
     import torchvision.datasets as datasets
     from torch.utils.data import DataLoader
     from torchsummary import summary
```

```
[]: torch.cuda.is_available()
```

[]: True

```
train_data = datasets.MNIST('data', train=True, download=True, u
      →transform=transform)
       test_data = datasets.MNIST('data', train=False, download=True,_
      →transform=transform)
       yield DataLoader(train_data, batch_size=batch_size, shuffle=True)
       yield DataLoader(test_data, batch_size=batch_size, shuffle=True)
[]: batch size = 64
     train_loader, test_loader = get_mnist_loaders(batch_size)
[]: class SkipConnection(nn.Module):
       def __init__(self, body):
         nn.Module.__init__(self)
         self.body = body
       def forward(self, x):
         y = self.body(x)
         return x + y
[]: class ConvActNorm(nn.Sequential):
       def <u>init</u> (self, in channels, out channels, kernel size, stride, padding):
         nn.Sequential.__init__(self, OrderedDict([
           ('conv', nn.Conv2d(in_channels=in_channels, out_channels=out_channels,
      →kernel_size=kernel_size, stride=stride, padding=padding)),
           ('relu', nn.LeakyReLU()),
           ('bnorm', nn.BatchNorm2d(out_channels)),
         ]))
[]: class ResNet(nn.Module):
       def __init__(self, height, width, n):
         nn.Module.__init__(self)
         layers = []
         layers.append(('can_in', ConvActNorm(in_channels=1, out_channels=16,_
     →kernel_size=3, stride=1, padding=1)))
         chn = 16
         # layers.append(('conv_in', nn.Conv2d(in_channels=1, out_channels=16, u
      →kernel_size=3, stride=1, padding=1)))
         # layers.append(('relu_in', nn.LeakyReLU()))
         # layers.append(('bnorm_in', nn.BatchNorm2d(16)))
         for i in (0, 1, 2):
           for j in range(2 * n):
             first_half = nn.Sequential(
                 ConvActNorm(chn, 16 * 2 ** i, 3, 1, 1),
                 ConvActNorm(16 * 2 ** i, 16 * 2 ** i, 3, 1, 1)
```

```
if chn == 16 * 2 ** 1 and (j != 0 or i == 0):
        first_half = SkipConnection(first_half)
      chn = 16 * 2 ** i
      layers.append((f'firsthalf_{i}_{j}', first_half))
      is_last = j == 2 * n - 1
      second_half = nn.Sequential(
          ConvActNorm(chn, chn, 3, 1, 1),
          ConvActNorm(chn, chn, 3, 2 if is_last else 1, 1)
      )
      if not is_last:
        second_half = SkipConnection(second_half)
        height = (height - 1) // 2 + 1
        width = (width - 1) // 2 + 1
      layers.append((f'secondhalf_{i}_{j}', second_half))
  self.body = nn.Sequential(OrderedDict(layers))
  neck_count = chn * height * width
  self.head = nn.Sequential(
      nn.Linear(neck_count, 10),
      nn.Softmax(1)
  )
  self.neck_count = neck_count
def forward(self, x):
  y = self.body(x)
  return self.head(y.reshape([-1, self.neck_count]))
```

```
[]: def train(
         model: nn.Module,
         optimizer: optim.Optimizer,
         data: Union[DataLoader, Tuple[DataLoader]],
         max_epochs: int,
         cuda=True):
      use_test = False
       if isinstance(data, DataLoader):
         train_loader = data
       elif isinstance(data, tuple):
         if len(data) == 2:
           train_loader, test_loader = data
           if not isinstance(train_loader, DataLoader):
             raise TypeError(f'Expected 1st entry of type DataLoader, but got⊔
      →{type(train_loader)}!')
           if not isinstance(test_loader, DataLoader):
             raise TypeError(f'Expected 2nd entry of type DataLoader, but got
      →{type(test_loader)}!')
```

```
use_test = True
  else:
    raise ValueError(f'Expected tuple of length 2, but got {len(data)}!')
criterion = nn.CrossEntropyLoss()
model.train()
losses = []
batch_total = len(train_loader)
train_accs = dict()
test_accs = dict()
for epoch in range(max_epochs):
  samples_total = 0
  samples_correct = 0
  for batch_idx, batch in enumerate(train_loader):
    x, y = batch
    if cuda:
      x, y = x.cuda(), y.cuda()
    output = model(x)
    loss = criterion(output, y)
    loss.backward()
    optimizer.step()
    yhat = torch.argmax(output, dim=1)
    samples_total += len(y)
    samples_correct += torch.sum(yhat == y)
    losses.append(loss.item())
    if batch_idx % 50 == 0 or batch_idx == batch_total - 1:
      acc = float(samples_correct) / float(samples_total)
      train_accs[epoch + batch_idx / batch_total] = acc
      if use_test:
        model.eval()
        test_x, test_y = next(iter(test_loader))
        if cuda:
          test_x, test_y = test_x.cuda(), test_y.cuda()
        test_output = model(test_x)
        test_loss = criterion(test_output, test_y)
        test_yhat = torch.argmax(test_output, dim=1)
        test_acc = float(torch.sum(test_yhat == test_y)) / float(len(test_y))
        test_accs[epoch + batch_idx / batch_total] = test_acc
```

```
[]: def validate(model: nn.Module, data: DataLoader, cuda=True):
       criterion = nn.CrossEntropyLoss()
       losses = []
       correct_samples = 0
       total_samples = 0
       for x, y in data:
           if cuda:
             x, y = x.cuda(), y.cuda()
           output = model(x)
           loss = criterion(output, y)
           yhat = torch.argmax(output, dim=1)
           losses.append(loss.item())
           correct samples += torch.sum(yhat == y)
           total_samples += len(y)
      mean_losses = np.mean(losses)
       acc = float(correct_samples) / float(total_samples)
       print(f'Validation complete! Validation loss: {mean_losses:.6f}, Validation⊔
      →accuracy: {acc:.2%}')
       return mean_losses, acc
```

```
[]: res_net = ResNet(28, 28, 3) summary(res_net, input_size=(1, 28, 28), device='cpu')
```

Layer (type)	Output Shape	Param #
Conv2d-1	[-1, 16, 28, 28]	160
LeakyReLU-2	[-1, 16, 28, 28]	0
BatchNorm2d-3	[-1, 16, 28, 28]	32
Conv2d-4	[-1, 16, 28, 28]	2,320
LeakyReLU-5	[-1, 16, 28, 28]	0
BatchNorm2d-6	[-1, 16, 28, 28]	32
Conv2d-7	[-1, 16, 28, 28]	2,320

LeakyReLU-8	[-1,				0
BatchNorm2d-9	[-1,				32
Conv2d-10	[-1,				2,320
LeakyReLU-11	[-1,	-	-		0
BatchNorm2d-12	[-1,	16,	28,	28]	32
Conv2d-13	[-1,	16,	28,	28]	2,320
LeakyReLU-14	[-1,	-	-		0
BatchNorm2d-15	[-1,	16,	28,	28]	32
SkipConnection-16	[-1,	16,	28,	28]	0
Conv2d-17	[-1,	16,	28,	28]	2,320
LeakyReLU-18	[-1,	16,	28,	28]	0
BatchNorm2d-19	[-1,	16,	28,	28]	32
Conv2d-20	[-1,	16,	28,	28]	2,320
LeakyReLU-21	[-1,	16,	28,	28]	0
BatchNorm2d-22	[-1,	16,	28,	28]	32
Conv2d-23	[-1,	16,	28,	28]	2,320
LeakyReLU-24	[-1,	16,	28,	28]	0
BatchNorm2d-25	[-1,				32
Conv2d-26	[-1,	16,	28,	28]	2,320
LeakyReLU-27	[-1,	-	-		0
BatchNorm2d-28	[-1,	-	-		32
SkipConnection-29	[-1,	-	-		0
Conv2d-30	[-1,	-	-		2,320
LeakyReLU-31	[-1,	-	-		0
BatchNorm2d-32	[-1,				32
Conv2d-33	[-1,				2,320
LeakyReLU-34	[-1,	-	-		0
BatchNorm2d-35	[-1,	-	-		32
Conv2d-36	[-1,				2,320
LeakyReLU-37	[-1,				0
BatchNorm2d-38	[-1,				32
Conv2d-39	[-1,				2,320
LeakyReLU-40	[-1,				0
BatchNorm2d-41	[-1,				32
SkipConnection-42	[-1,				0
Conv2d-43	[-1,	-	-		2,320
LeakyReLU-44	[-1,				0
BatchNorm2d-45	[-1,	-	-		32
Conv2d-46	[-1,	-	-		2,320
LeakyReLU-47	[-1,	-	-		0
BatchNorm2d-48	[-1,	-	-		32
Conv2d-49	[-1,	-	-		2,320
LeakyReLU-50	[-1,	•	•	_	2,320
•					
BatchNorm2d-51 Conv2d-52	[-1,				32
	[-1, [-1,				2,320
LeakyReLU-53 BatchNorm2d-54	[-1,	-	-		32
SkipConnection-55	[-1,	10,	20,	20]	0

a 01.50	F 4 40 00 007	0.000
Conv2d-56	[-1, 16, 28, 28]	2,320
LeakyReLU-57	[-1, 16, 28, 28]	0
BatchNorm2d-58	[-1, 16, 28, 28]	32
Conv2d-59	[-1, 16, 28, 28]	2,320
LeakyReLU-60	[-1, 16, 28, 28]	0
BatchNorm2d-61	[-1, 16, 28, 28]	32
Conv2d-62	[-1, 16, 28, 28]	2,320
LeakyReLU-63	[-1, 16, 28, 28]	0
BatchNorm2d-64	[-1, 16, 28, 28]	32
Conv2d-65	[-1, 16, 28, 28]	2,320
LeakyReLU-66	[-1, 16, 28, 28]	0
BatchNorm2d-67	[-1, 16, 28, 28]	32
SkipConnection-68	[-1, 16, 28, 28]	0
Conv2d-69	[-1, 16, 28, 28]	2,320
LeakyReLU-70	[-1, 16, 28, 28]	0
BatchNorm2d-71	[-1, 16, 28, 28]	32
Conv2d-72	[-1, 16, 28, 28]	2,320
LeakyReLU-73	[-1, 16, 28, 28]	0
BatchNorm2d-74	[-1, 16, 28, 28]	32
Conv2d-75	[-1, 16, 28, 28]	2,320
LeakyReLU-76	[-1, 16, 28, 28]	0
BatchNorm2d-77	[-1, 16, 28, 28]	32
Conv2d-78	[-1, 16, 14, 14]	2,320
LeakyReLU-79	[-1, 16, 14, 14]	0
BatchNorm2d-80	[-1, 16, 14, 14]	32
Conv2d-81	[-1, 32, 14, 14]	4,640
LeakyReLU-82	[-1, 32, 14, 14]	0
BatchNorm2d-83	[-1, 32, 14, 14]	64
Conv2d-84	[-1, 32, 14, 14]	9,248
LeakyReLU-85	[-1, 32, 14, 14]	0
BatchNorm2d-86	[-1, 32, 14, 14]	64
Conv2d-87	[-1, 32, 14, 14]	9,248
LeakyReLU-88	[-1, 32, 14, 14]	0
BatchNorm2d-89	[-1, 32, 14, 14]	64
Conv2d-90	[-1, 32, 14, 14]	9,248
LeakyReLU-91	[-1, 32, 14, 14]	0
BatchNorm2d-92	[-1, 32, 14, 14]	64
SkipConnection-93	[-1, 32, 14, 14]	0
Conv2d-94	[-1, 32, 14, 14]	9,248
LeakyReLU-95	[-1, 32, 14, 14]	0
BatchNorm2d-96	[-1, 32, 14, 14]	64
Conv2d-97	[-1, 32, 14, 14]	9,248
LeakyReLU-98	[-1, 32, 14, 14]	0
BatchNorm2d-99	[-1, 32, 14, 14]	64
SkipConnection-100	[-1, 32, 14, 14]	0
Conv2d-101	[-1, 32, 14, 14]	9,248
LeakyReLU-102	[-1, 32, 14, 14]	0
BatchNorm2d-103	[-1, 32, 14, 14]	64

Conv2d-104		32,			9,248
LeakyReLU-105		32,			0
BatchNorm2d-106		32,			64
SkipConnection-107		32,			0
Conv2d-108	- •	32,		_	9,248
LeakyReLU-109		32,			0
BatchNorm2d-110		32,			64
Conv2d-111		32,			9,248
LeakyReLU-112		32,			0
BatchNorm2d-113	•	32,	-		64
SkipConnection-114	-	32,	-		0
Conv2d-115		32,			9,248
LeakyReLU-116		32,			0
BatchNorm2d-117		32,			64
Conv2d-118		32,			9,248
LeakyReLU-119		32,			0
BatchNorm2d-120		32,			64
SkipConnection-121		32,			0
Conv2d-122	- •	32,	•	_	9,248
LeakyReLU-123	- •	32,		_	0
BatchNorm2d-124		32,			64
Conv2d-125	[-1,	32,	14,	14]	9,248
LeakyReLU-126	[-1,	32,	14,	14]	0
BatchNorm2d-127	[-1,	32,	14,	14]	64
SkipConnection-128	[-1,	32,	14,	14]	0
Conv2d-129	[-1,	32,	14,	14]	9,248
LeakyReLU-130	[-1,	32,	14,	14]	0
BatchNorm2d-131	[-1,	32,	14,	14]	64
Conv2d-132	[-1,	32,	14,	14]	9,248
LeakyReLU-133	[-1,	32,	14,	14]	0
BatchNorm2d-134	[-1,	32,	14,	14]	64
SkipConnection-135	[-1,	32,	14,	14]	0
Conv2d-136	[-1,	32,	14,	14]	9,248
LeakyReLU-137	[-1,	32,	14,	14]	0
BatchNorm2d-138	[-1,	32,	14,	14]	64
Conv2d-139	[-1,	32,	14,	14]	9,248
LeakyReLU-140	[-1,	32,	14,	14]	0
BatchNorm2d-141	[-1,	32,	14,	14]	64
SkipConnection-142	[-1,	32,	14,	14]	0
Conv2d-143	[-1,	32,	14,	14]	9,248
LeakyReLU-144	[-1,	32,	14,	14]	0
BatchNorm2d-145	[-1,	32,	14,	14]	64
Conv2d-146	[-1,	32,	14,	14]	9,248
LeakyReLU-147	[-1,	32,	14,	14]	0
BatchNorm2d-148	[-1,	32,	14,	14]	64
SkipConnection-149	[-1,	32,	14,	14]	0
Conv2d-150	[-1,	32,	14,	14]	9,248
LeakyReLU-151	[-1,	32,	14,	14]	0
-					

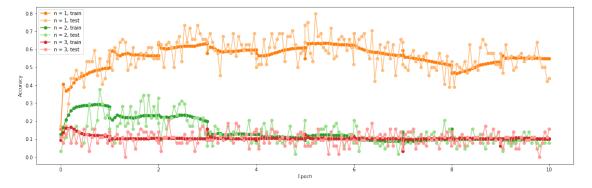
	F	
BatchNorm2d-152	[-1, 32, 14, 14]	64
Conv2d-153	[-1, 32, 14, 14]	9,248
LeakyReLU-154	[-1, 32, 14, 14]	0
BatchNorm2d-155	[-1, 32, 14, 14]	64
SkipConnection-156	[-1, 32, 14, 14]	0
Conv2d-157	[-1, 32, 14, 14]	9,248
LeakyReLU-158	[-1, 32, 14, 14]	0
BatchNorm2d-159	[-1, 32, 14, 14]	64
Conv2d-160	[-1, 32, 7, 7]	9,248
LeakyReLU-161	[-1, 32, 7, 7]	0
BatchNorm2d-162	[-1, 32, 7, 7]	64
Conv2d-163	[-1, 64, 7, 7]	18,496
LeakyReLU-164	[-1, 64, 7, 7]	0
BatchNorm2d-165	[-1, 64, 7, 7]	128
Conv2d-166	[-1, 64, 7, 7]	36,928
LeakyReLU-167	[-1, 64, 7, 7]	0
BatchNorm2d-168	[-1, 64, 7, 7]	128
Conv2d-169	[-1, 64, 7, 7]	36,928
LeakyReLU-170	[-1, 64, 7, 7]	0
BatchNorm2d-171	[-1, 64, 7, 7]	128
Conv2d-172	[-1, 64, 7, 7]	36,928
LeakyReLU-173	[-1, 64, 7, 7]	0
BatchNorm2d-174	[-1, 64, 7, 7]	128
SkipConnection-175	[-1, 64, 7, 7]	0
Conv2d-176	[-1, 64, 7, 7]	36,928
LeakyReLU-177	[-1, 64, 7, 7]	0
BatchNorm2d-178	[-1, 64, 7, 7]	128
Conv2d-179	[-1, 64, 7, 7]	36,928
LeakyReLU-180	[-1, 64, 7, 7]	0
BatchNorm2d-181	[-1, 64, 7, 7]	128
Conv2d-182	[-1, 64, 7, 7]	36,928
LeakyReLU-183	[-1, 64, 7, 7]	0
BatchNorm2d-184	[-1, 64, 7, 7]	128
Conv2d-185	[-1, 64, 7, 7]	36,928
LeakyReLU-186	[-1, 64, 7, 7]	0
BatchNorm2d-187	[-1, 64, 7, 7]	128
SkipConnection-188	[-1, 64, 7, 7]	0
Conv2d-189	[-1, 64, 7, 7]	36,928
LeakyReLU-190	[-1, 64, 7, 7]	0
BatchNorm2d-191	[-1, 64, 7, 7]	128
Conv2d-192	[-1, 64, 7, 7]	36,928
LeakyReLU-193	[-1, 64, 7, 7]	0
BatchNorm2d-194	[-1, 64, 7, 7]	128
Conv2d-195	[-1, 64, 7, 7]	36,928
LeakyReLU-196	[-1, 64, 7, 7]	0
BatchNorm2d-197	[-1, 64, 7, 7]	128
Conv2d-198	[-1, 64, 7, 7]	36,928
LeakyReLU-199	[-1, 64, 7, 7]	0
J	,	v

BatchNorm2d-200	[-1, 64, 7, 7]	128
SkipConnection-201	[-1, 64, 7, 7]	0
Conv2d-202	[-1, 64, 7, 7]	36,928
LeakyReLU-203	[-1, 64, 7, 7]	0
BatchNorm2d-204	[-1, 64, 7, 7]	128
Conv2d-205	[-1, 64, 7, 7]	36,928
LeakyReLU-206	[-1, 64, 7, 7]	0
BatchNorm2d-207	[-1, 64, 7, 7]	128
Conv2d-208	[-1, 64, 7, 7]	36,928
LeakyReLU-209	[-1, 64, 7, 7]	0
BatchNorm2d-210	[-1, 64, 7, 7]	128
Conv2d-211	[-1, 64, 7, 7]	36,928
LeakyReLU-212	[-1, 64, 7, 7]	0
BatchNorm2d-213	[-1, 64, 7, 7]	128
SkipConnection-214	[-1, 64, 7, 7]	0
Conv2d-215	[-1, 64, 7, 7]	36,928
LeakyReLU-216	[-1, 64, 7, 7]	0
BatchNorm2d-217	[-1, 64, 7, 7]	128
Conv2d-218	[-1, 64, 7, 7]	36,928
LeakyReLU-219	[-1, 64, 7, 7]	0
BatchNorm2d-220	[-1, 64, 7, 7]	128
Conv2d-221	[-1, 64, 7, 7]	36,928
LeakyReLU-222	[-1, 64, 7, 7]	0
BatchNorm2d-223	[-1, 64, 7, 7]	128
Conv2d-224	[-1, 64, 7, 7]	36,928
LeakyReLU-225	[-1, 64, 7, 7]	0
BatchNorm2d-226	[-1, 64, 7, 7]	128
SkipConnection-227	[-1, 64, 7, 7]	0
Conv2d-228	[-1, 64, 7, 7]	36,928
LeakyReLU-229	[-1, 64, 7, 7]	0
BatchNorm2d-230	[-1, 64, 7, 7]	128
Conv2d-231	[-1, 64, 7, 7]	36,928
LeakyReLU-232	[-1, 64, 7, 7]	0
BatchNorm2d-233	[-1, 64, 7, 7]	128
Conv2d-234	[-1, 64, 7, 7]	36,928
LeakyReLU-235	[-1, 64, 7, 7]	0
BatchNorm2d-236	[-1, 64, 7, 7]	128
Conv2d-237	[-1, 64, 4, 4]	36,928
LeakyReLU-238	[-1, 64, 4, 4]	0
BatchNorm2d-239	[-1, 64, 4, 4]	128
Linear-240	[-1, 10]	10,250
Softmax-241	[-1, 10]	0
	- , · · •	

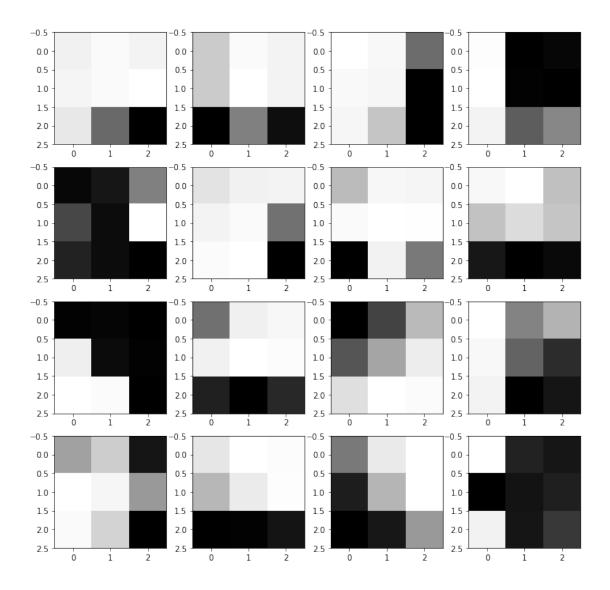
Total params: 1,156,682 Trainable params: 1,156,682 Non-trainable params: 0

Input size (MB): 0.00

```
Forward/backward pass size (MB): 13.05
    Params size (MB): 4.41
    Estimated Total Size (MB): 17.47
[ ]: train_info = {}
[]: %%time
     n = 1
     model = ResNet(28, 28, n).cuda()
     opt = optim.Adam(model.parameters(), lr=1e-3)
     train_info[n] = train(model, opt, tuple(get_mnist_loaders(64)), 10)
    model1 = model
    Epoch: 9/10 Step: 937/938 Loss: 1.711151 Acc: 72.19% Test loss: 1.726776 Test
    acc: 73.44%CPU times: user 4min 42s, sys: 1.1 s, total: 4min 43s
    Wall time: 4min 44s
[]: %%time
    n = 2
    model = ResNet(28, 28, n).cuda()
     opt = optim.Adam(model.parameters(), lr=1e-3)
     train_info[n] = train(model, opt, tuple(get_mnist_loaders(64)), 10)
     model2 = model
    Epoch: 9/10 Step: 937/938 Loss: 2.367401 Acc: 9.89% Test loss: 2.383026 Test
    acc: 7.81%CPU times: user 8min, sys: 1.23 s, total: 8min 2s
    Wall time: 8min 3s
[]: %%time
    n = 3
     model = ResNet(28, 28, n).cuda()
     opt = optim.Adam(model.parameters(), lr=1e-3)
     train_info[n] = train(model, opt, tuple(get_mnist_loaders(64)), 10)
     model3 = model
    Epoch: 9/10 Step: 937/938 Loss: 2.398651 Acc: 10.22% Test loss: 2.304901 Test
    acc: 15.62%CPU times: user 11min 16s, sys: 8.57 s, total: 11min 24s
    Wall time: 11min 26s
[]: with open('train_info.pth', 'wb') as f:
       pk.dump(train_info, f)
[]: colors = plt.cm.tab20(np.linspace(0, 1, 20))
[]: plt.figure(figsize=(20, 6))
     for n, info in train_info.items():
       _, train_accs, test_accs = info
```



```
[]: kernels = model1.body.can_in.conv.weight.cpu().detach().numpy()
   plt.figure(figsize=(12, 12))
   for k in range(kernels.shape[0]):
     plt.subplot(4, 4, k + 1)
     plt.imshow(kernels[k][0], cmap='gray')
```



These kernels seem to detect digit borders oriented in different directions.

```
[75]: def mse4d(y1, y2):
    d = y2 - y1
    shp = d.shape
    return torch.einsum('ijkl,ijkl->', d, d) / (shp[0] * shp[1] * shp[2] * shp[3])

[78]: def mse4d_dict_hook_create(d, name):
    def hook(model, x, y):
        d[name] = mse4d(x[0], y)
        return hook

[82]: hooks = dict()
    mses = dict()
```

```
for k, v in model1.body.named_children():
   if type(v) == SkipConnection:
     hooks[k] = v.register_forward_hook(mse4d_dict_hook_create(mses, k))
```

```
[87]: inimg = tuple(next(iter(tuple(get_mnist_loaders(64))[1])))[0].cuda()
model1(inimg)
pass
```

```
[85]: for k, v in mses.items():
    print(f'{k}:\tMSE = {v}')
```

```
secondhalf_0_0: MSE = 91.04904174804688
secondhalf_1_0: MSE = 101.27399444580078
firsthalf_1_1: MSE = 70.23033905029297
secondhalf_2_0: MSE = 54.97813034057617
```

The layers do not seem to be identity.

```
[86]: for v in hooks.values(): v.remove()
```

For the current configuration and checked n, deeper networks are worse. One of possible causes for the bad results may be too small number of neurons in one of the layers.