

Problem:

The two regression lines of a bivariate distribution are:

$$4x - 5y + 33 = 0 \text{ (line of } y \text{ on } x) \quad 20x - 9y - 107 = 0 \text{ (line of } x \text{ on } y).$$

Estimate the value of x when $y = 7$. Compute the correct answer to one decimal place.

Solution:

We have, line of y on x ,

$$4x - 5y + 33 = 0$$

$$\Rightarrow 5y = 4x + 33$$

$$\Rightarrow \boxed{y = (4/5)x + 33/5}$$

Other one is line of x on y ,

$$20x - 9y - 107 = 0$$

$$\Rightarrow 20x = 9y + 107$$

$$\Rightarrow \boxed{x = (9/20)y + 107/20}$$

Estimating the value of x when $y = 7$,

$$\Rightarrow x = (9/20)y + 107/20$$

$$\Rightarrow x = (9/20) * 7 + 107/20$$

$$\Rightarrow x = 0.45 * 7 + 5.35$$

$$\Rightarrow x = 3.15 + 5.35$$

$$\Rightarrow \boxed{x = 8.5}$$