

# ***Preparation for $D^+ \rightarrow K\pi\pi$ analysis***

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**based on E. Bruna PhD thesis**

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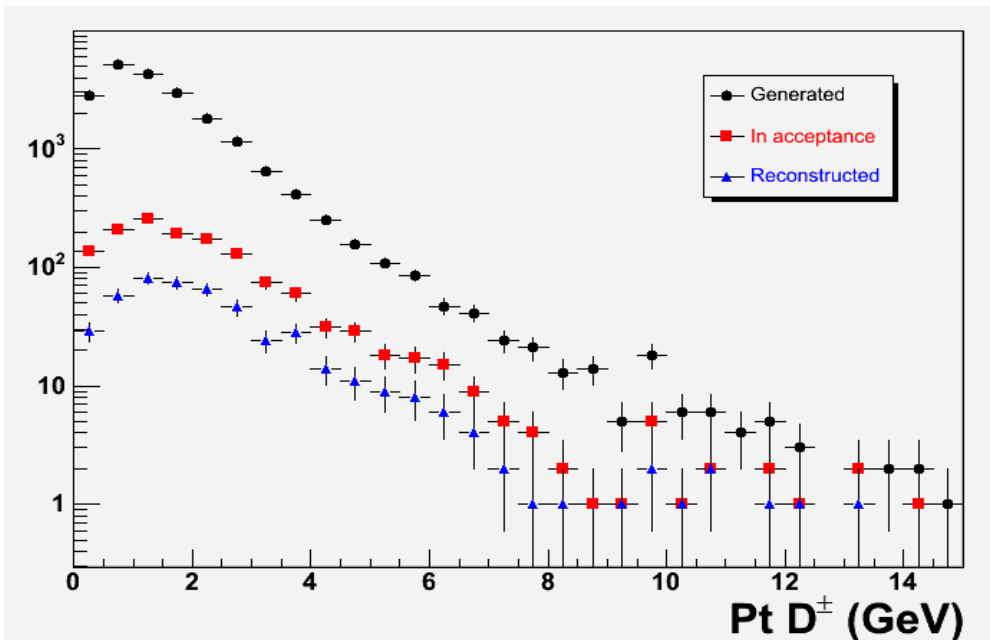
# $D^+ \rightarrow K^- \pi^+ \pi^+$ : *motivation*

- Accurate determination of charm production cross section by measuring as many charmed hadrons as possible
- Ratios like  $D^0/D^+$  ,  $D_s/D^+$  bring information about the hadronization mechanism
- Different systematics w.r.t. the benchmark study  $D^0 \rightarrow K\pi$ 
  - $D^+$  fully reconstructable from a 3-charged body decay instead of the 2 body decay  $D^0 \rightarrow K\pi$ 
    - ✓ *Larger combinatorial background*
    - ✓ *Softer decay products ( $\langle p_T \rangle \sim 0.7 \text{ GeV}/c$  compared to  $\sim 1 \text{ GeV}/c$  of  $D^0$  daughters)*
  - $D^+$  has a “longer” mean proper length ( $c\tau \sim 312\mu\text{m}$  compared to  $\sim 123 \mu\text{m}$  of the  $D^0$ )
  - Possibility to exploit the resonant decay through  $K\bar{K}^*0$  to enhance the S/B ratio

# ***$D^\pm$ statistics in PbPb***

$b_{\min}\text{-}b_{\max}$ (fm)	$\sigma$ (%)	$N_{cc}/\text{ev.}$	$D^\pm$ yield/ev.
0-3	3.6	118	45.8
3-6	11	82	31.8
6-9	18	42	16.3
9-12	25.4	12.5	4.85
12-18	42	1.2	0.47

- $N_{cc}$  = number of c-cbar pairs
  - MNR cross-section calculation
  - Includes shadowing (EKS98)
  - Shadowing centrality dependence from Emelyakov et al., PRC 61, 044904
- $D^\pm$  yield calculated from  $N_{cc}$ 
  - Fraction  $N^{D^\pm}/N_{cc}$  ( $\approx 0.38$ ) from PYTHIA fragmentation
  - $D^+$  less abundant than  $D^0$  by about a factor 3
- Geometrical acceptance and reconstruction efficiency
  - Extracted from 1 event with 20000  $D^\pm$  in full phase space
- B. R.  $D^\pm \rightarrow K\pi\pi = 9.2\%$ 
  - Larger than the B.R.  $D^0 \rightarrow K\pi$  ( $=3.8\%$ )



# ***Simulation and analysis strategy***

- Pb-Pb events generated in 2005 on the italian grid
  - SIGNAL: 5000 events with  $\approx 9000 D^{\pm} \rightarrow K\pi\pi$  (PYTHIA)
  - BACKGROUND: 20000 central Hijing events
- Starting points for Pb-Pb analysis:
  - Huge combinatorial background:  $10^9$  triplets in central Hijing event
  - Three studies with different PID information:
    - ✓ *Perfect PID - No PID - Combined Bayesian PID (ITS+TPC+TRD+TOF+HMPID)*
- pp events with parametrized TPC response generated in 2006 on the italian grid (PWG3 production)
  - Statistics = Physics run of  $5.4 \cdot 10^6$  events
  - Extra events with charmed mesons forced to decay hadronically to increase the signal statistics
- Starting points for pp analysis
  - Much smaller combinatorial background (on average 100 triplets/event)
  - Much worser resolution on primary vertex position
  - For each candidate triplet, primary vertex must be recalculated removing the candidate secondary tracks
  - PID information not used

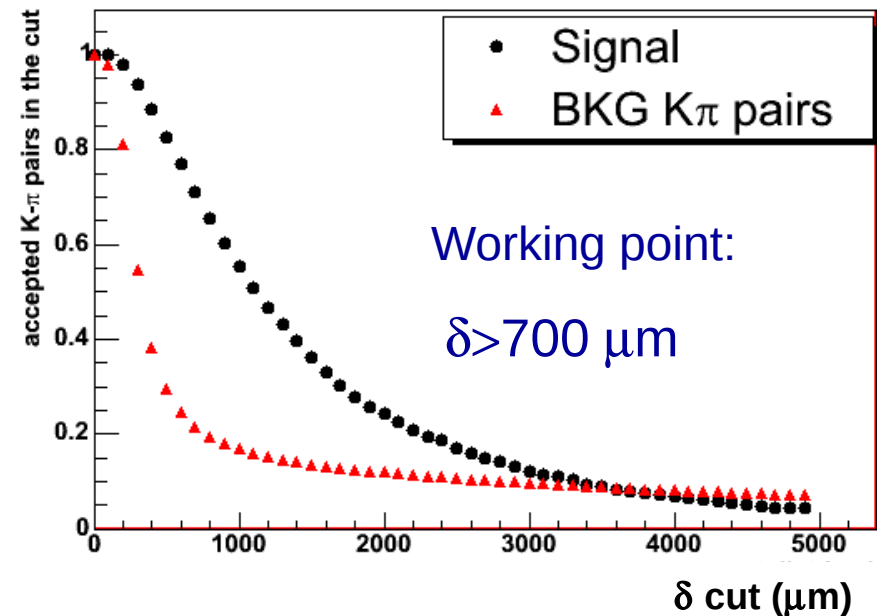
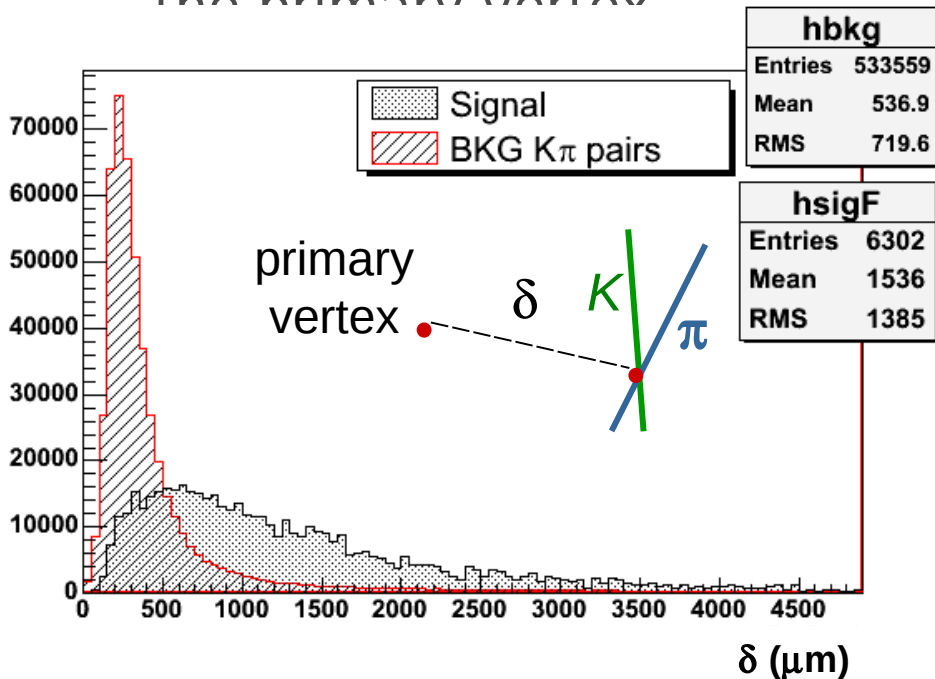
# ***Pre-selection steps***

- Cuts on single tracks (  $p_T$ ,  $d_0^{r\phi}$  )

- In Pb-Pb reduce the combinatorial background from  $10^9$  to  $10^6$  triplets per event keeping  $\approx 10\%$  of the signal
- $p_T$  cut different for K and  $\pi$  (identified by the charge sign)

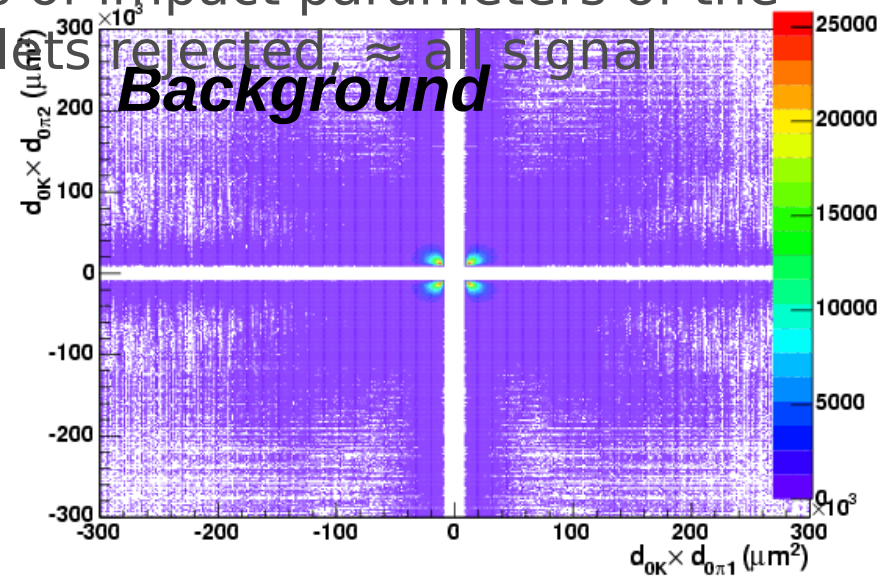
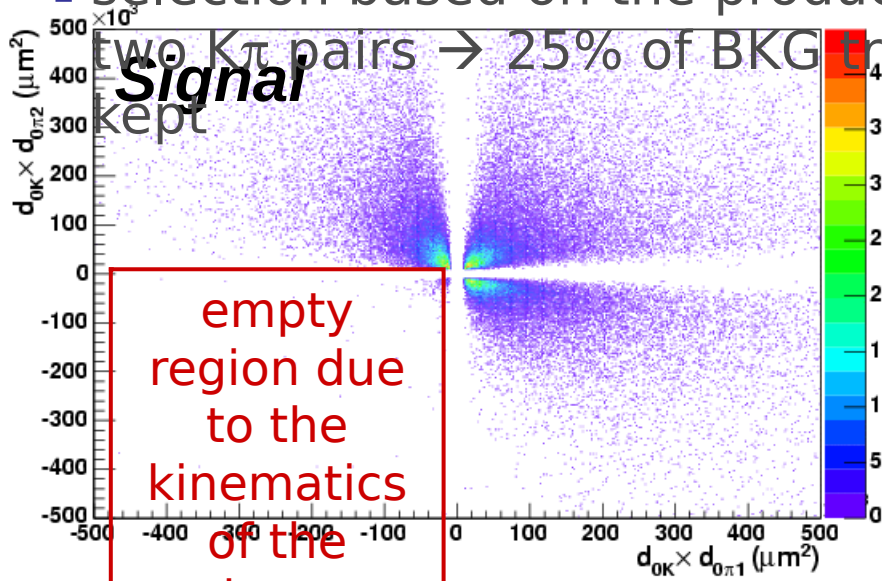
- Cuts on  $K\pi$  candidate pairs

- K and  $\pi$  have opposite charge sign
- Cut on the distance  $\delta$  between the vertex of the 2 tracks and the primary vertex



# ***Pre-selection steps***

- Cuts on single tracks (  $p_T$ ,  $d_0^{r\phi}$  )
- Cuts on  $K\pi$  candidate pairs
  - distance  $\delta$  between the 2 track vertex and the primary vertex
- Build the triplets starting from two selected  $K\pi$  pairs
  - both  $K\pi$  pairs with vertex displaced from the primary vertex
- Cuts on  $K\pi\pi$  candidate triplets of tracks
  - selection based on the products of impact parameters of the



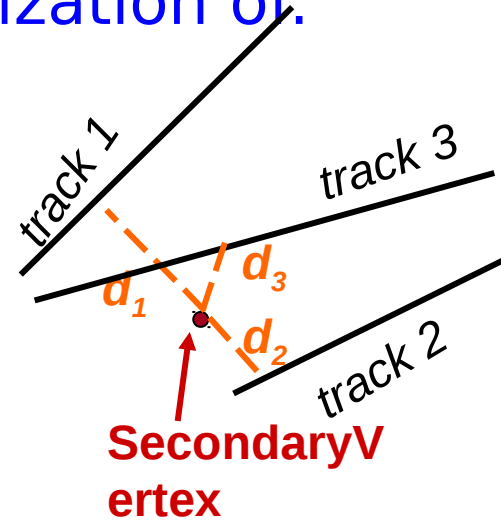
# ***Decay vertex reconstruction*** ***(AliVertexerTracks::VertexForSelectedTracks)***

- Tracks (helices) approximated with Straight Lines
- Vertex coordinates  $(x_0, y_0, z_0)$  from minimization of:

$$D^2 = d_1^2 + d_2^2 + d_3^2$$

with

$$d_k^2 = \left( \frac{x_k - x_0}{\sigma_x} \right)^2 + \left( \frac{y_k - y_0}{\sigma_y} \right)^2 + \left( \frac{z_k - z_0}{\sigma_z} \right)^2$$



□  $\sigma_{xi}$ ,  $\sigma_{yi}$ ,  $\sigma_{zi}$  are the errors on the track parameters

- Calculate track dispersion around the found vertex:

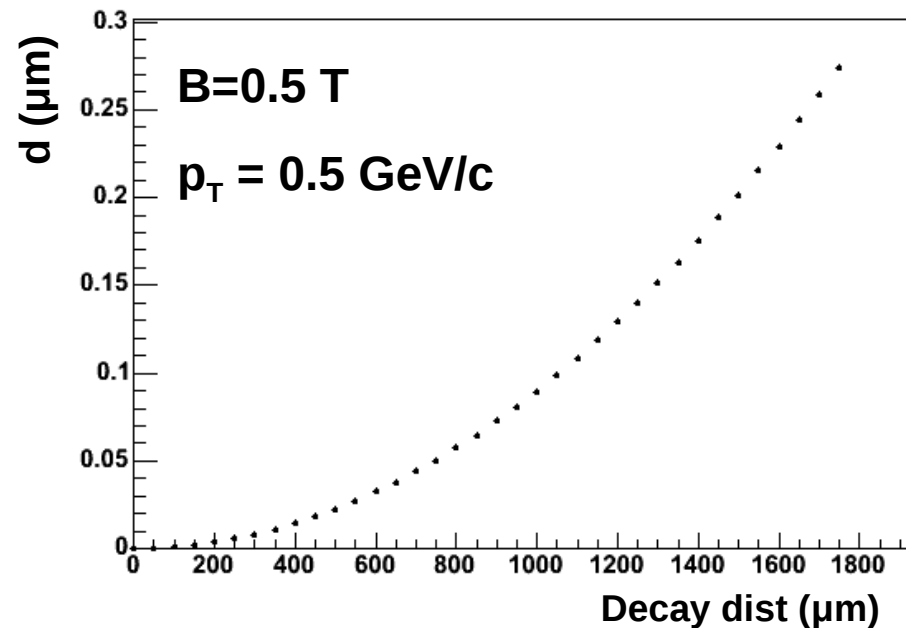
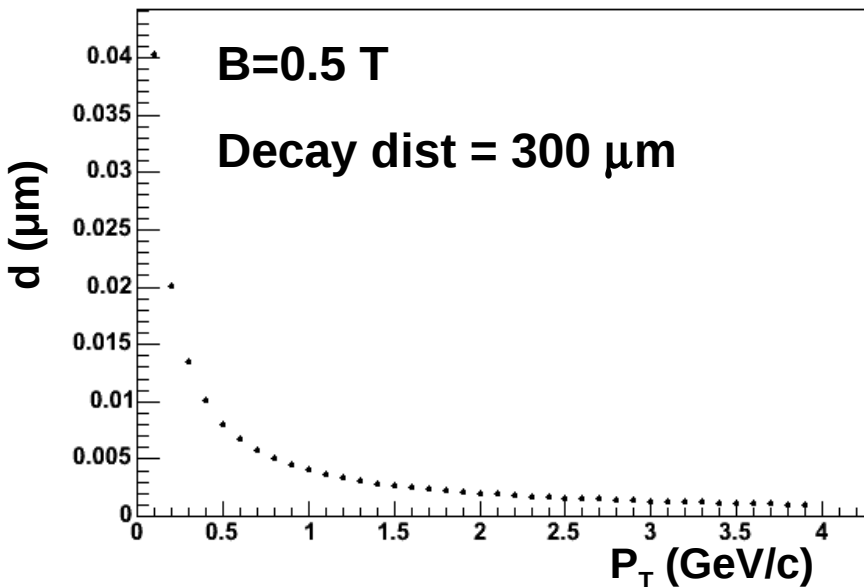
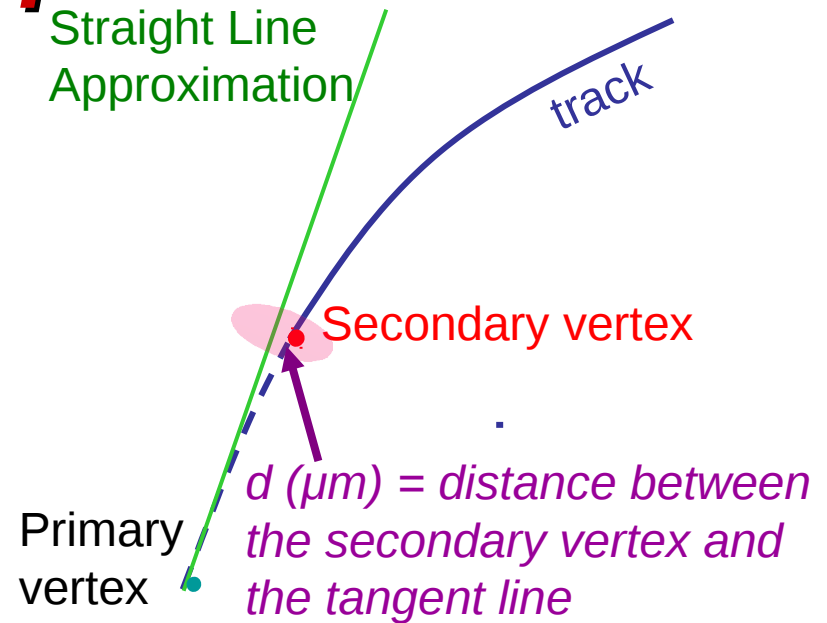
$$\sigma^2 = \sum_{k=1}^3 \left[ (x_k - x_o)^2 + (y_k - y_o)^2 + (z_k - z_o)^2 \right]$$

□ used to select good vertices

# ***Straight Line Approximation***

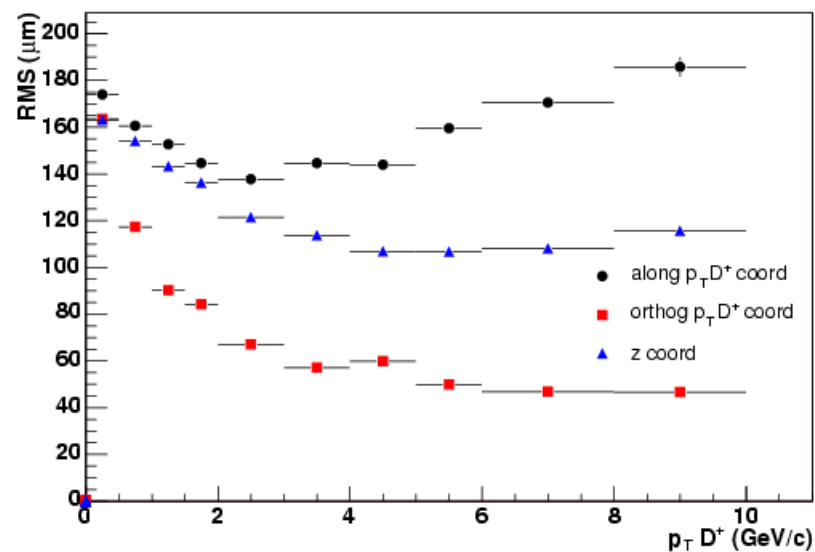
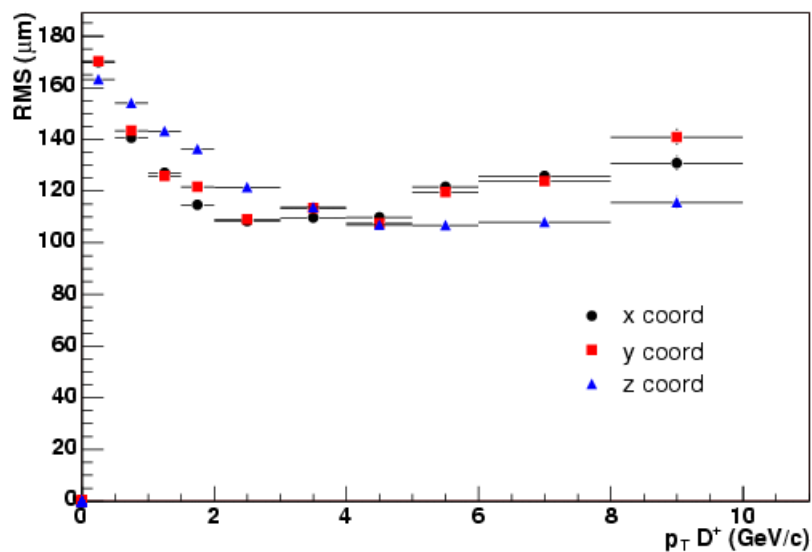
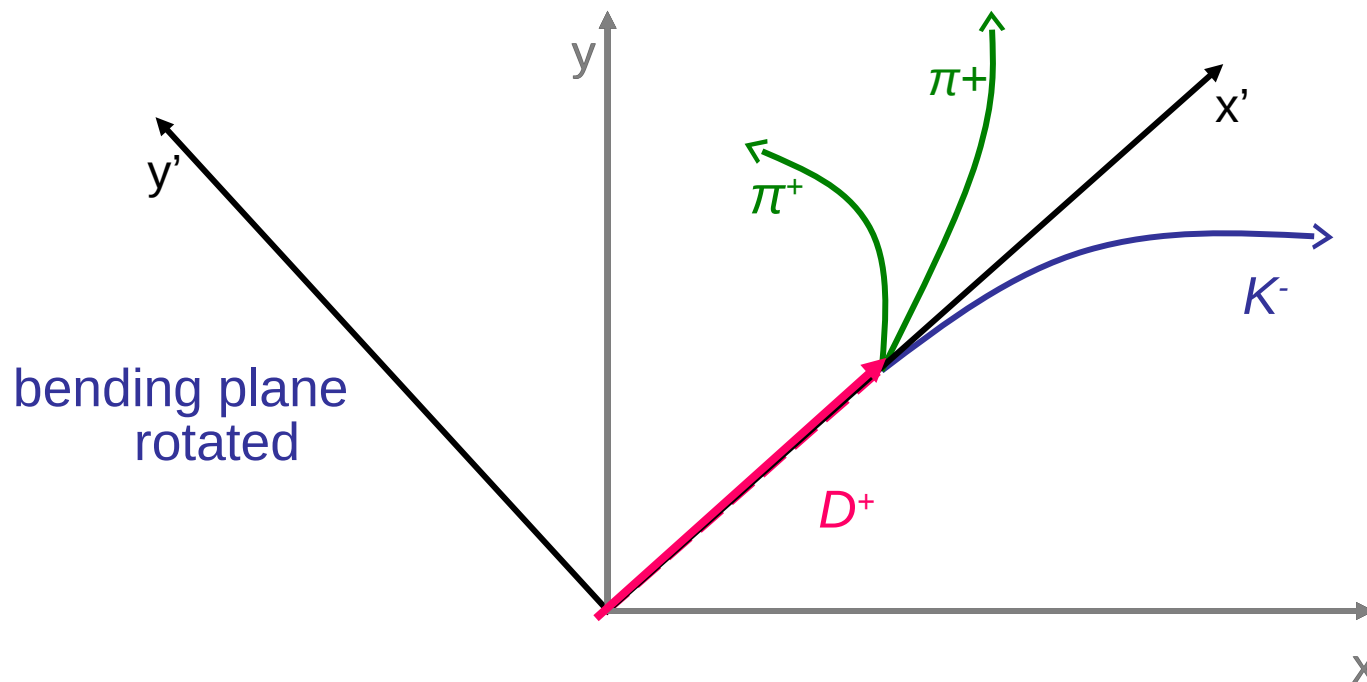
- Geometrical calculation of the “error” introduced by approximating the track (helix) with a straight line close to the primary vertex.

□ Good approximation: error is negligible w.r.t. tracks  $r\phi$   $d_0$  resolution ( $\approx 100 \mu\text{m}$  for 0.5 GeV/c tracks)





# Vertex finder: $D^+ \rightarrow K\pi\pi$

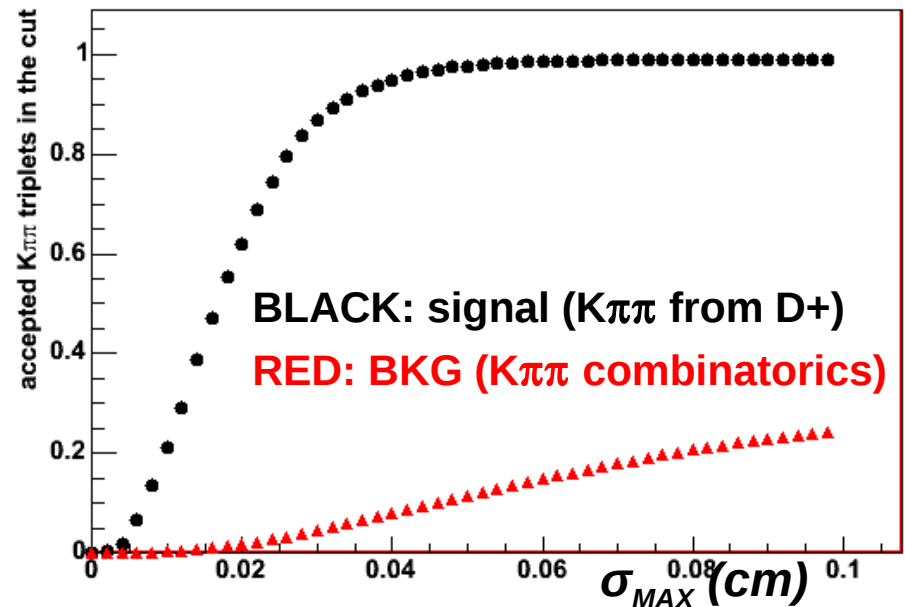
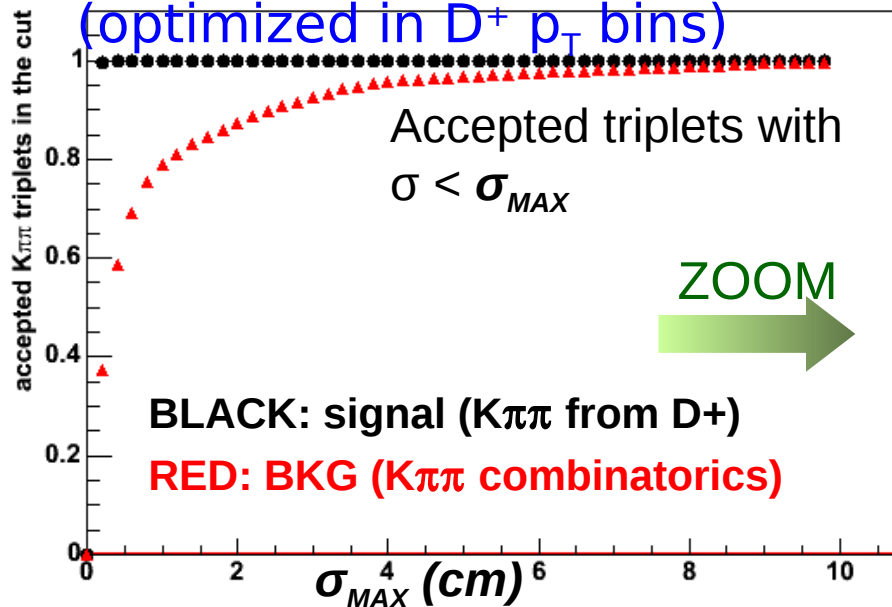
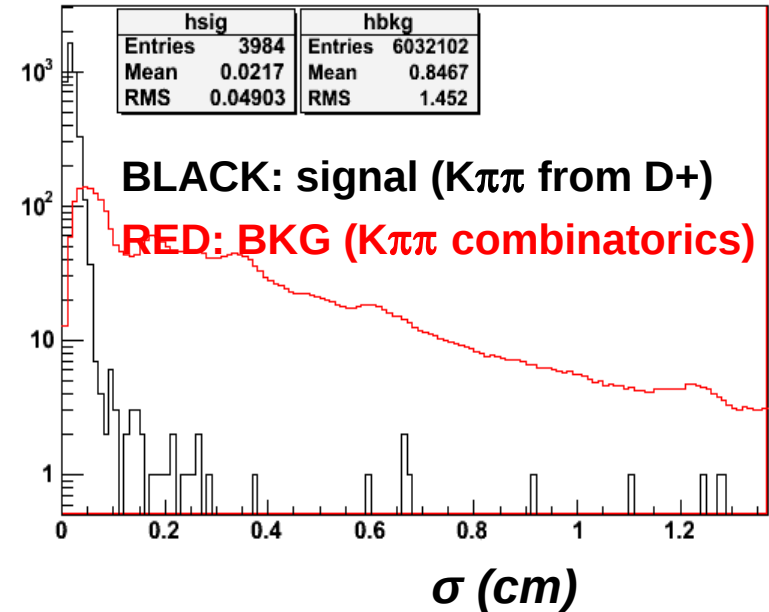


# Vertex selection: $D^+ \rightarrow K\pi\pi$

- Vertex quality selection based on track dispersion  $\sigma$  around the found vertex

- Distribution of  $\sigma$  for signal and background  $K\pi\pi$  triplets
- Fraction of selected signal and background triplets as a function of the cut on track dispersion ( $\sigma_{MAX}$ ).

- Working point:  $\sigma < 200 \mu\text{m}$  (optimized in  $D^+ p_T$  bins)



# ***D<sup>+</sup> final selection steps (I)***

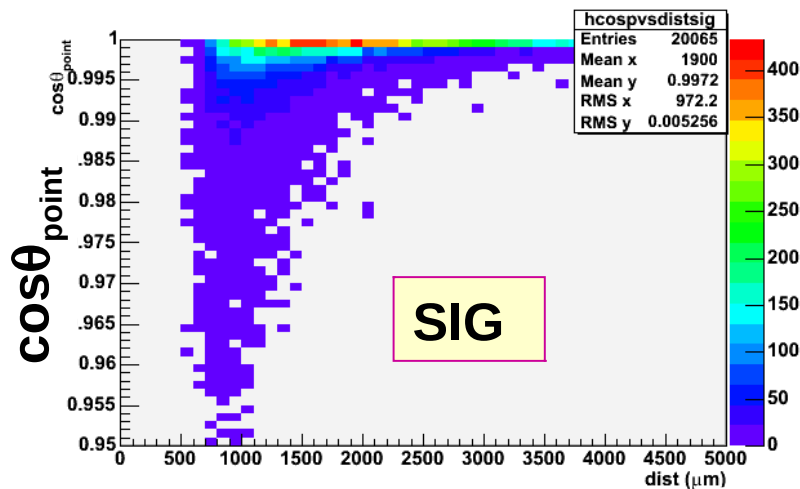
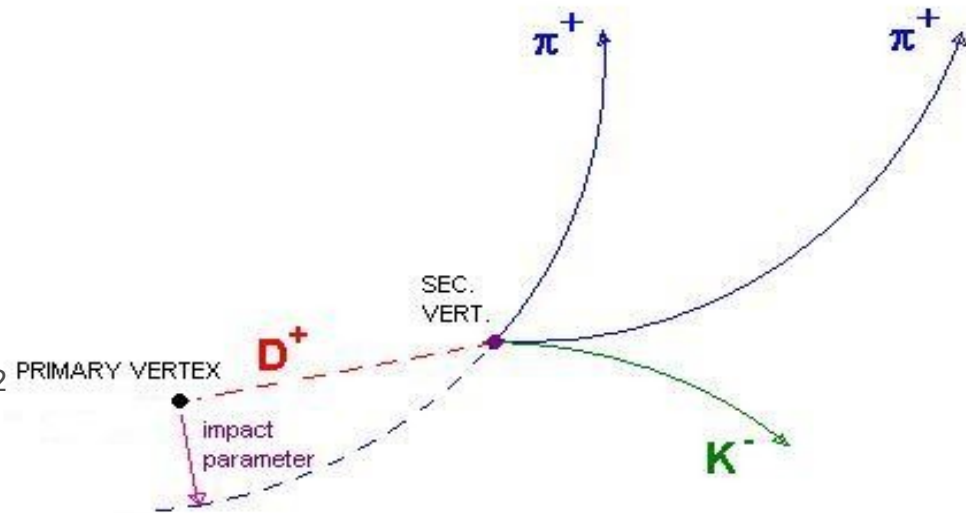
- Four selection variables:

- Distance between primary and secondary vertex ( $d_{PS}$ )

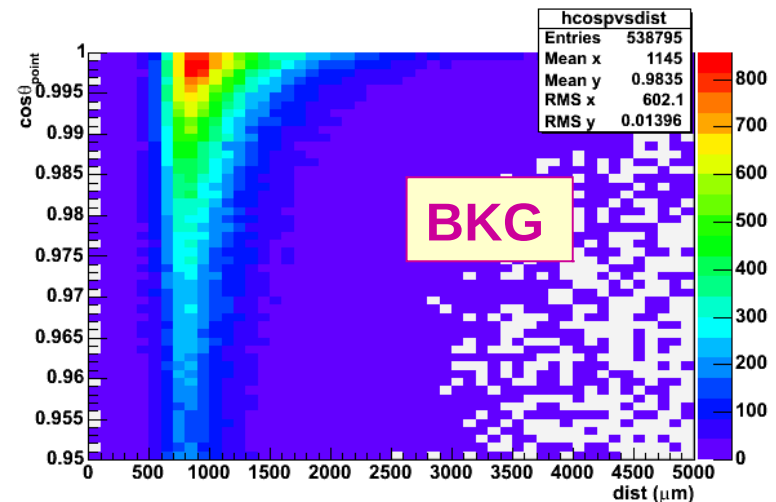
- $\cos\theta_{\text{point}}$

- Sum of squared impact parameters  $s = d_{01}^2 + d_{02}^2 + d_{03}^2$

- Max.  $p_T$  among the 3 tracks  
 $p_M = \text{Max}\{p_{T1}, p_{T2}, p_{T3}\}$



$d_{PS}(\mu\text{m})$



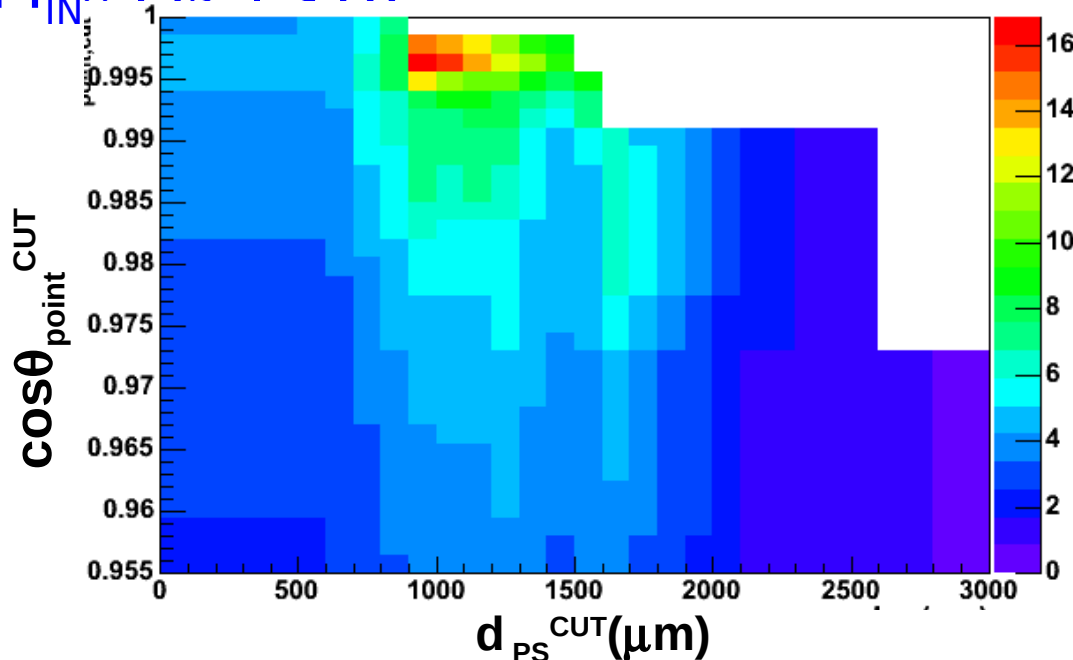
# ***$D^+$ final selection steps (II)***

- Fill matrices  $S^{ijkl}$  and  $B^{ijkl}$

□ each matrix cell contains the number of signal and background triplets passing the set of cuts

$$d_{PS} > c^i, \cos\theta_{point} > c^j, s > c^k, p_M > c^l$$

- Select the set of cuts (i.e. the matrix cell) which maximizes the significance ( $S/\sqrt{S+B}$ ) in the mass range  $|M_{IN} - M_{\pi}| < 1\sigma$



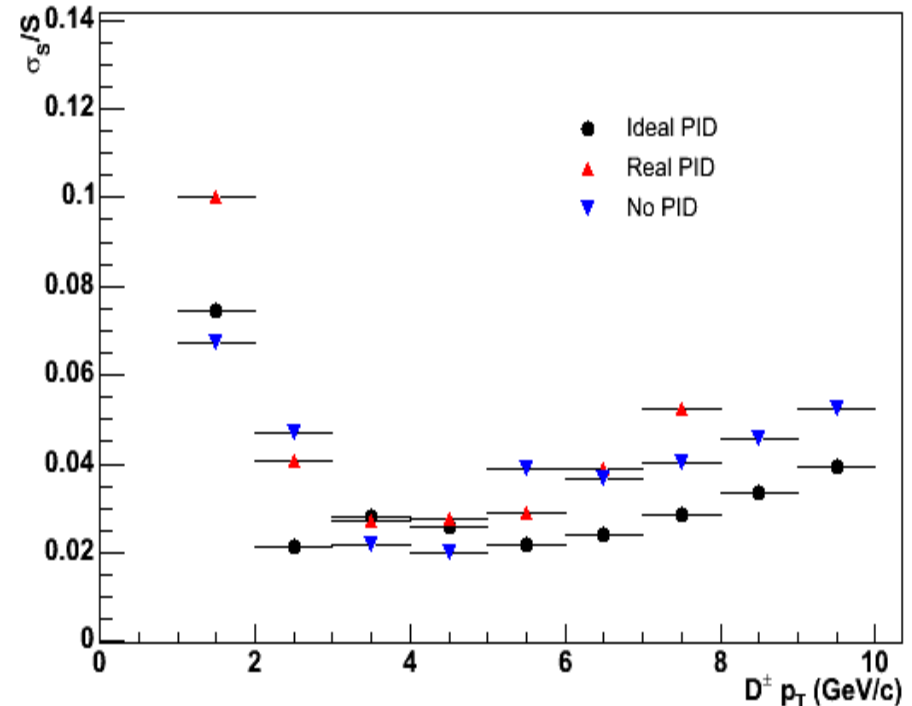
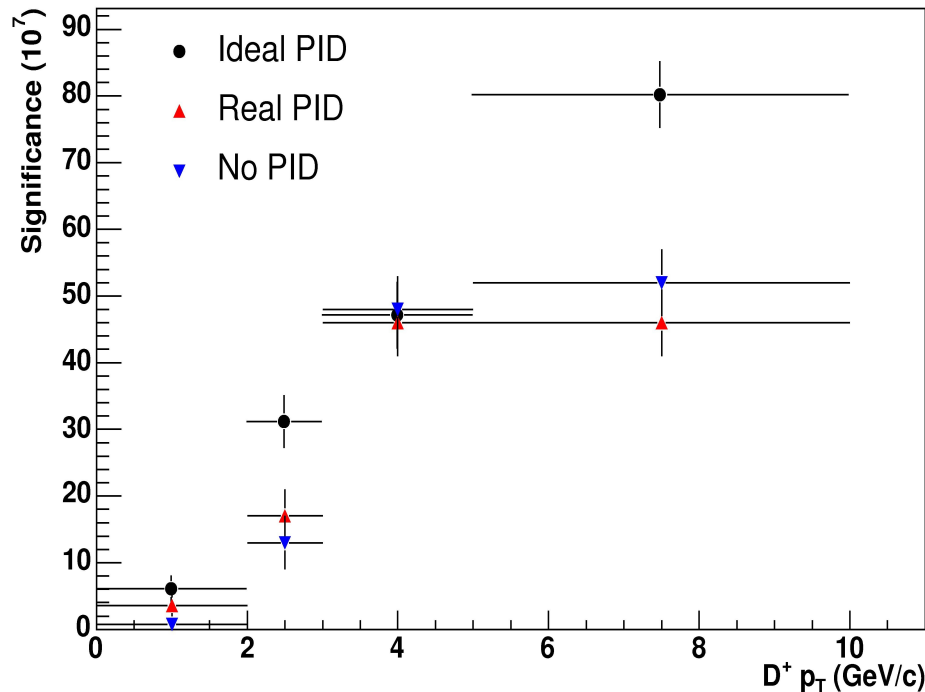
**Significance**  
 $S/\sqrt{S+B}$  for  
 $2 < p_T < 3$   
(normalized to  
 $10^7$  PbPb events)

# Results: PbPb (I)

- Significance and relative statistical error vs.  $D^+$   $p_T$

- $S/\text{ev} \sim 10^{-3}$ ,  $B/\text{ev} \sim 10^{-4}$

- Significance and relative statistical error ( $=1/\sqrt{S}$ ) normalized to  $10^7$  central PbPb events

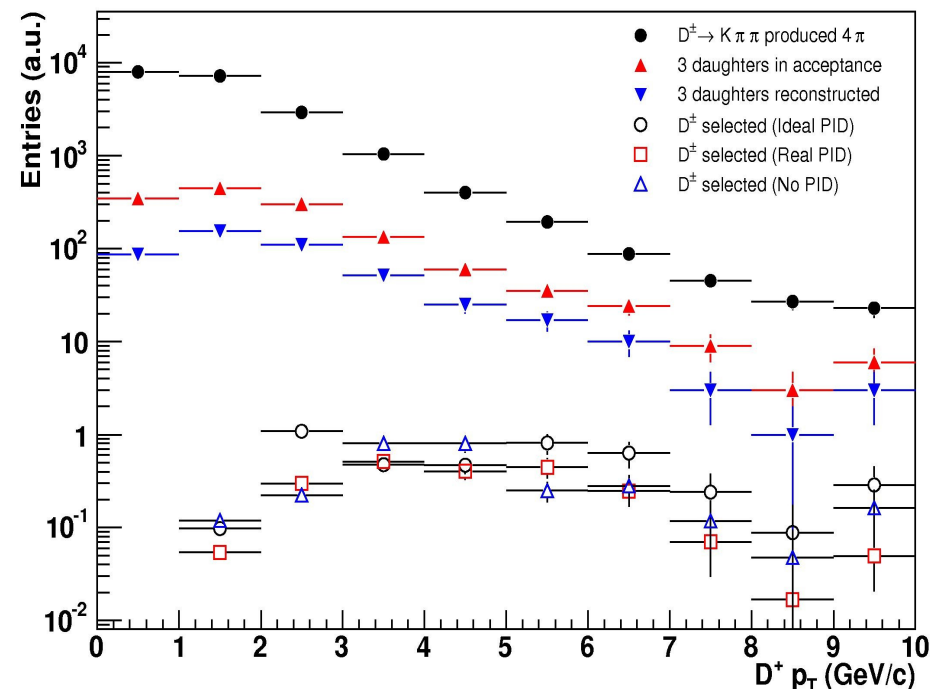
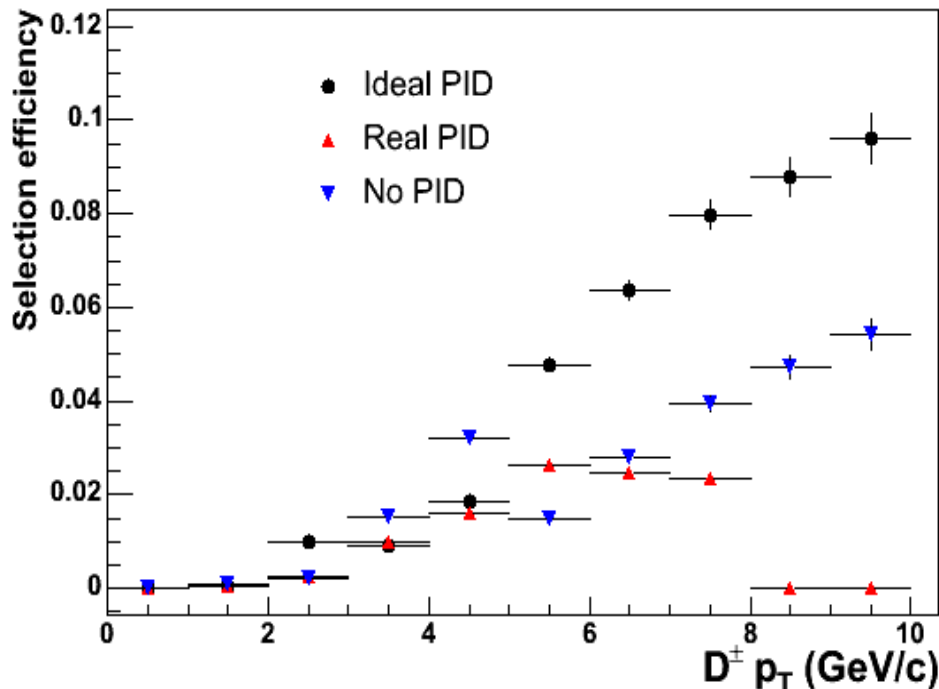


# Results: PbPb (II)

- Fraction of selected signal triplets and  $p_T$  spectra

$$\varepsilon = \frac{\text{selected } D^+}{D^+ \text{ with 3 reconstructed daughters}}$$

- $p_T$  integrated fraction of selected  $D^+ \approx 1.5\%$  (Ideal PID), 0.6% (Real PID), 1% (no PID)

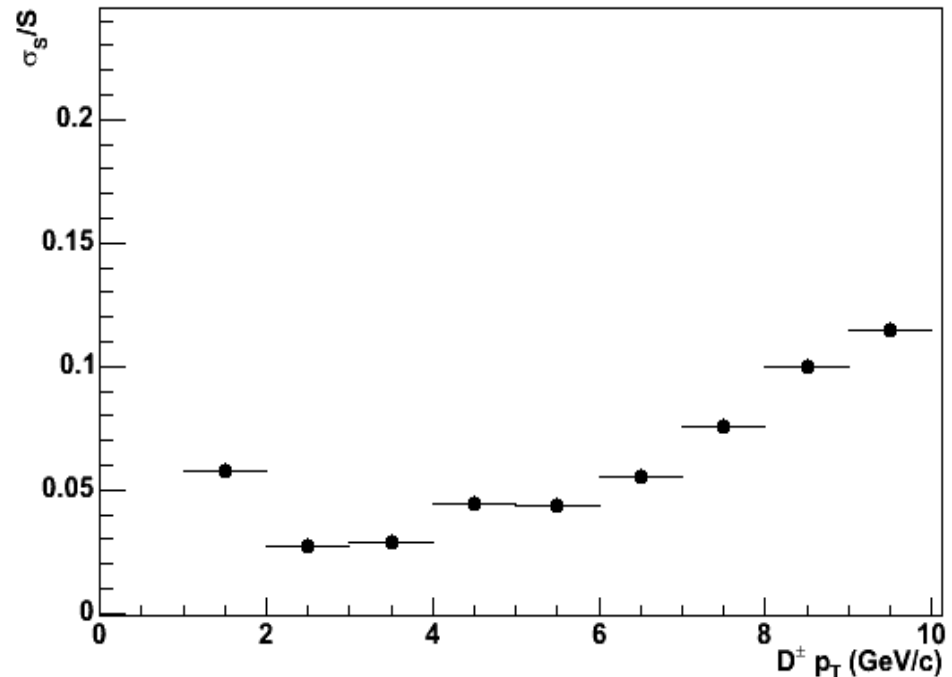
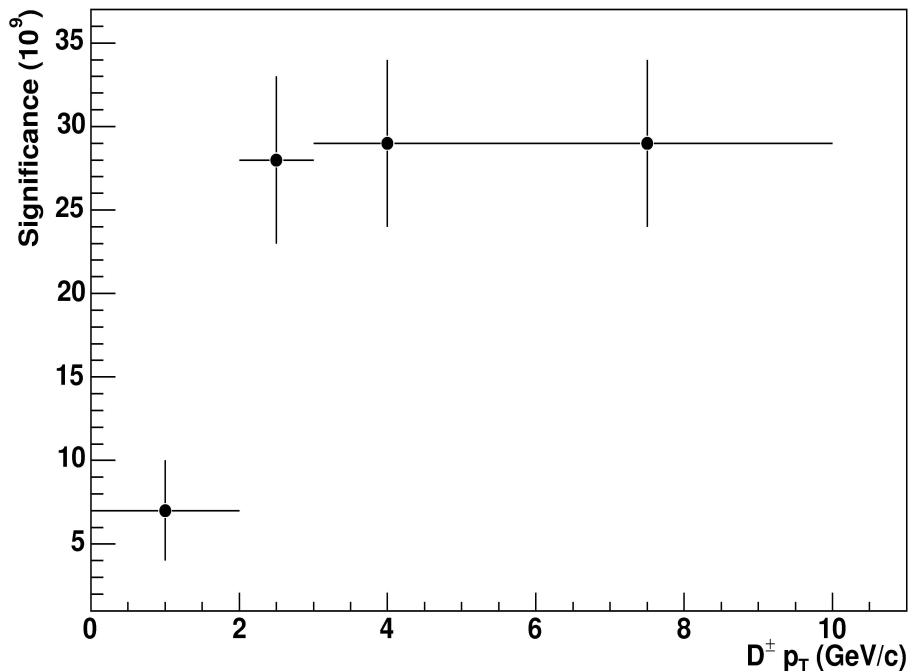


# Results: pp (I)

- Significance and relative statistical error vs.  $D^+$   $p_T$

- $S/\text{ev} \sim 5 \cdot 10^{-6}$ ,  $B/\text{ev} \sim 5 \cdot 10^{-6}$

- Significance and relative statistical error ( $=1/\sqrt{S}$ ) normalized to  $10^9$  pp Minimum Bias events

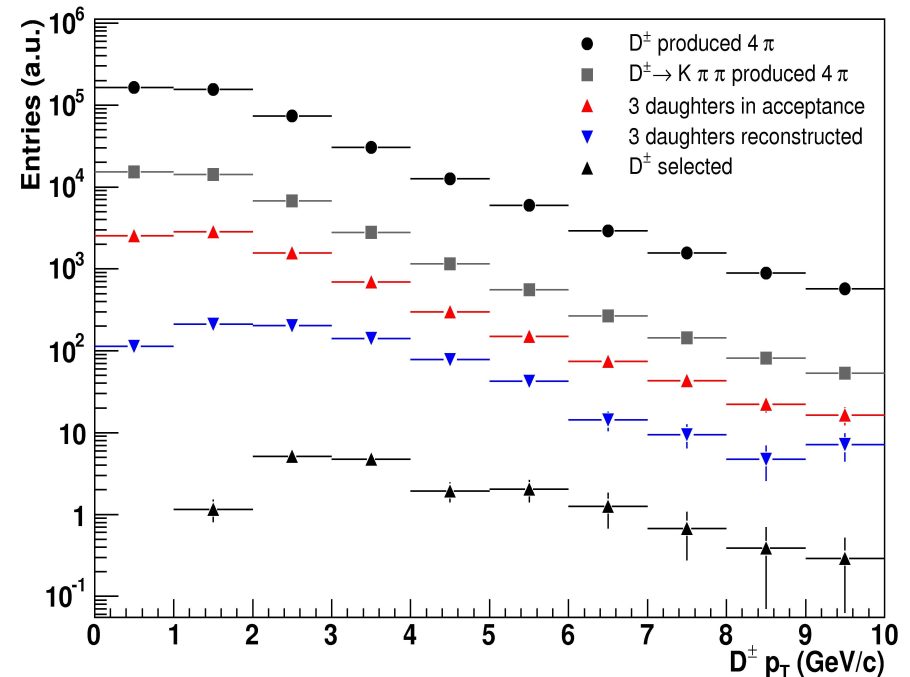
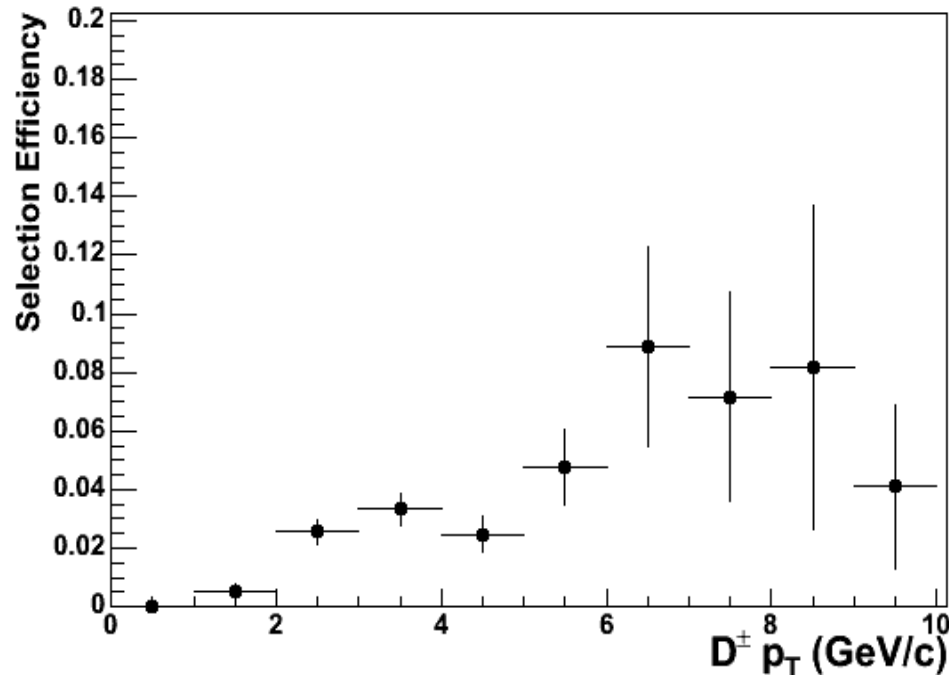


# Results: pp (II)

- Fraction of selected signal triplets and  $p_T$  spectra

$$\varepsilon = \frac{\text{selected } D^+}{D^+ \text{ with 3 reconstructed daughters}}$$

- $p_T$  integrated fraction of selected  $D^+ \approx 4\%$  (only NO PID case studied)





# Systematic uncertainties

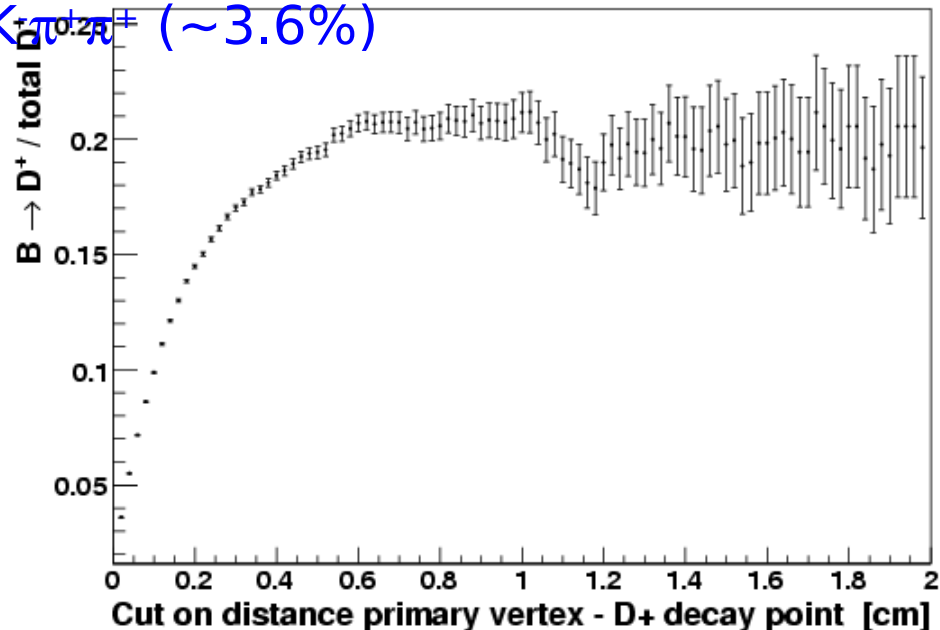
- Acceptance, reconstruction and PID efficiencies ( $\sim 10\%$ )
- Centrality selection ( $\sim 7\%$ )
- Nucleon-nucleon inelastic cross section ( $\sim 5\%$ )
- Parameters of the Woods-Saxon profile and nuclear density ( $\sim 5\%$ )
- Error on branching Ratio  $D^+ \rightarrow K^+ \pi^+ \pi^-$  ( $\sim 3.6\%$ )
- Feed-down from beauty:

$$N_{c \rightarrow D^\pm} = N_{D^\pm} - N_{b \rightarrow B \rightarrow D^\pm}$$

- Contamination (from MNR c.s. for c and b and B.R. for  $B \rightarrow D^\pm$ )

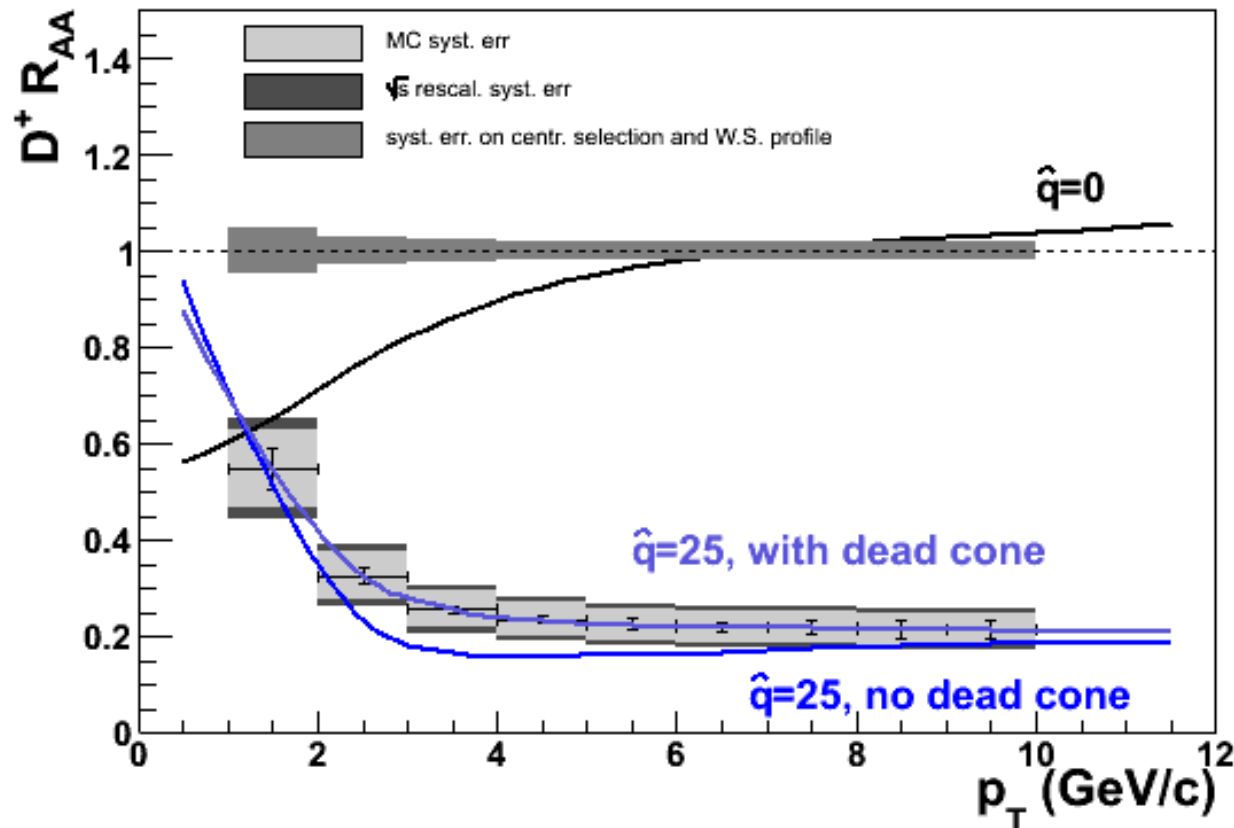
$$K = N_{b \rightarrow B \rightarrow D^\pm} / N_{c \rightarrow D^\pm} = 4\%$$

- $D^+$  from B are more displaced
  - ✓ *The cut on distance between primary to secondary vertex increases the fraction of selected  $D^+$  coming from B decay*



# Perspectives for $D^+ R_{AA}$

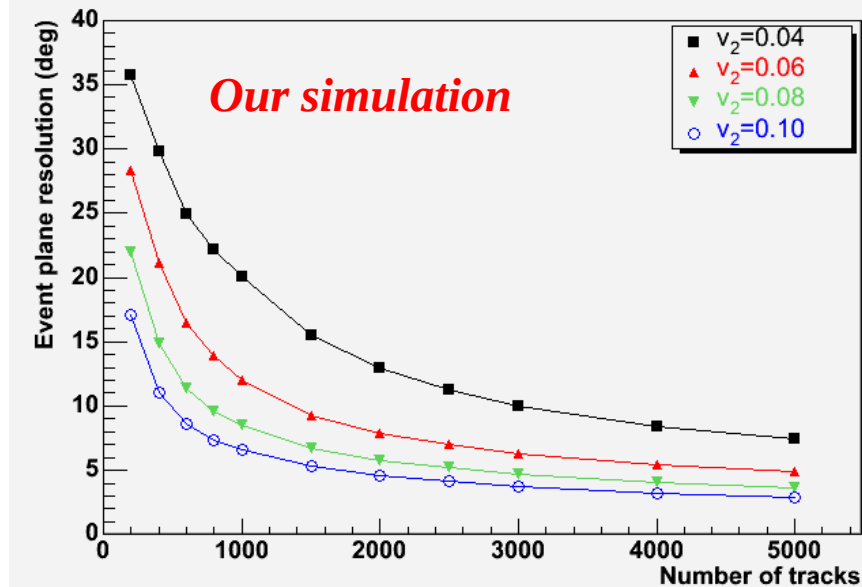
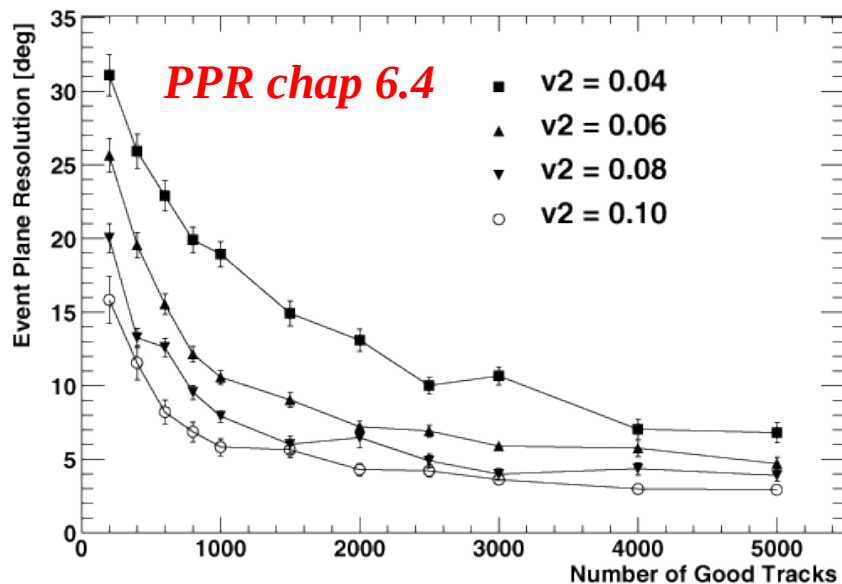
- Statistical error bars from  $10^9$  pp Min. Bias events and  $10^7$  central PbPb events (1 year of data taking)
  - Statistical error smaller than the syst. errors up to 10 GeV/c



# Perspectives for $D^+ v_2$ (I)

- GOAL: evaluate statistical error bars on the measurement of  $v_2(p_T)$  of D mesons
- TOOL: fast simulation (ROOT+3 classes +1 macro)
- Ingredients for event plane resolution

□ Multiplicity of charged particles



# Perspectives for $D^+ v_2$ (II)

- Simulations performed for centrality class  $6 < b \text{ (fm)} < 9$ 
  - To compare with model calculations at  $b=8$  fm (see next slide)
- Multiplicity (□ Armesto, Salgado, Wiedemann hep/ph 0407018)

$$\frac{1}{N_{part}} \frac{dN_{ch}^{AA}}{d\eta} \Big|_{\eta \sim 0} = N_0 \sqrt{s}^\lambda N_{part}^{\frac{1-\delta}{3\delta}}$$

□ From Glauber in  $6 < b < 9$  :  $\langle N_{part} \rangle = 175 \rightarrow N_{ch}(|y| < 1) = 1570$

- $v_2$  of charged hadrons = 0.125
  - From (Low Density Limit) extrapolation of  $v_2/\varepsilon$  vs.  $1/S \, dN/dy$  (see E. Simili)
- $D^+$  azimuthal angle resolution from the PbPb sample of simulated signal
- $D^+$  statistics in  $6 < b < 9$  centrality class:
  - Number of  $D^+$  per event from analysis in central events rescaled with the number of  $N_{cc}$  per event in the 2 centrality classes (=42/118)
  - Number of events in  $6 < b \text{ (fm)} < 9$  (normalized to 2  $10^7$  Min. Bias events)
    - ✓ =18% (from 14% to 32%) of total inelastic cross section

# Perspectives for $D^+$ $v_2$ (III)

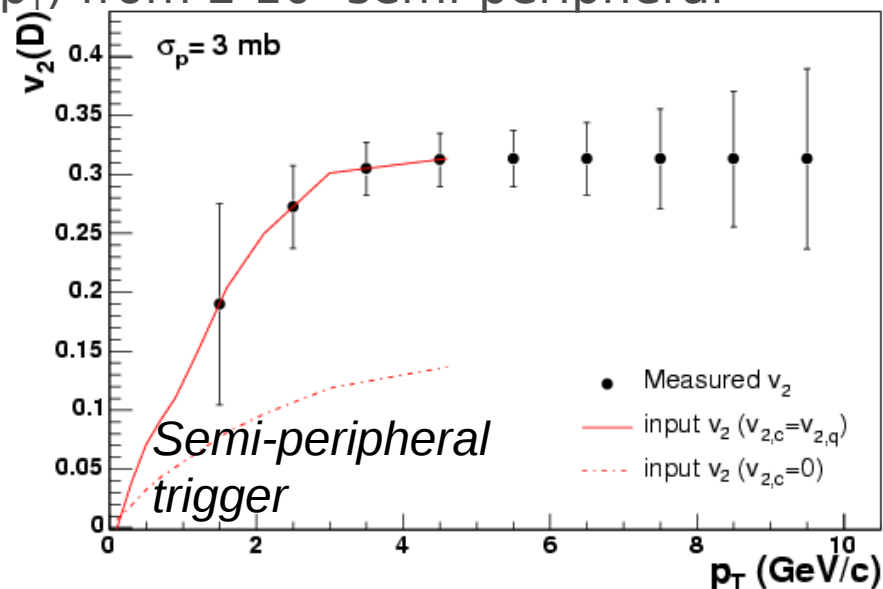
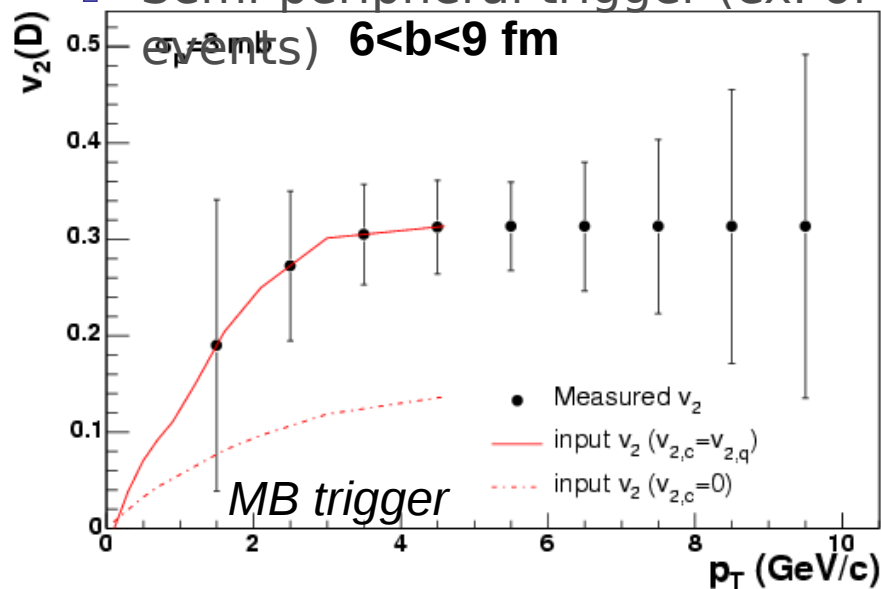
## Model calculations:

- $v_2(c)$  at the LHC for  $b=8\text{fm}$  (Ko, Chen, Zhang Braz. J. phys. To be publ. )
- Hadronization via  $v_2^D(p_\perp) \approx v_2^c(\frac{5p_\perp}{6}) + v_2^q(\frac{p_\perp}{6})$  → similar velocities

## Statistical error bars quite large

- Sum  $D^0 \rightarrow K\pi$  and  $D^\pm \rightarrow K\pi\pi$ 
  - ✓ Number of events roughly  $\times 2$  → error bars on  $v_2$  roughly  $/\sqrt{2}$

- Semi-peripheral trigger (ex. of  $v_2(p_T)$  from  $2 \cdot 10^7$  semi-peripheral



# Conclusions

- Monte Carlo studies on  $D^+ \rightarrow K^- \pi^+ \pi^+$  show that the analysis is feasible with a pretty good significance down to  $p_T \approx 0.5-1$  GeV/c both in PbPb and pp collisions by means of:
  - ▮ Selection strategy based on pre-selection cuts, vertex finding and maximization of the significance based on multi-dimensional matrices
  - ▮ Vertex Finding algorithm for secondary vertices (AliVertexerTracks::VertexForSelectedTracks)
- Analysis tools:
  - ▮ AliAODRecoDecayHF3prong class will be soon prototyped
    - ✓ *Selection strategy and cut variables are defined*
- Perspectives for observables  $R_{AA}$  and  $v_2$ 
  - ▮ Background “subtraction” method(s) for  $v_2$  analysis still to be defined
    - ✓ *Need for large statistics of reconstructed PbPb events with elliptic flow*

***Backup slides***

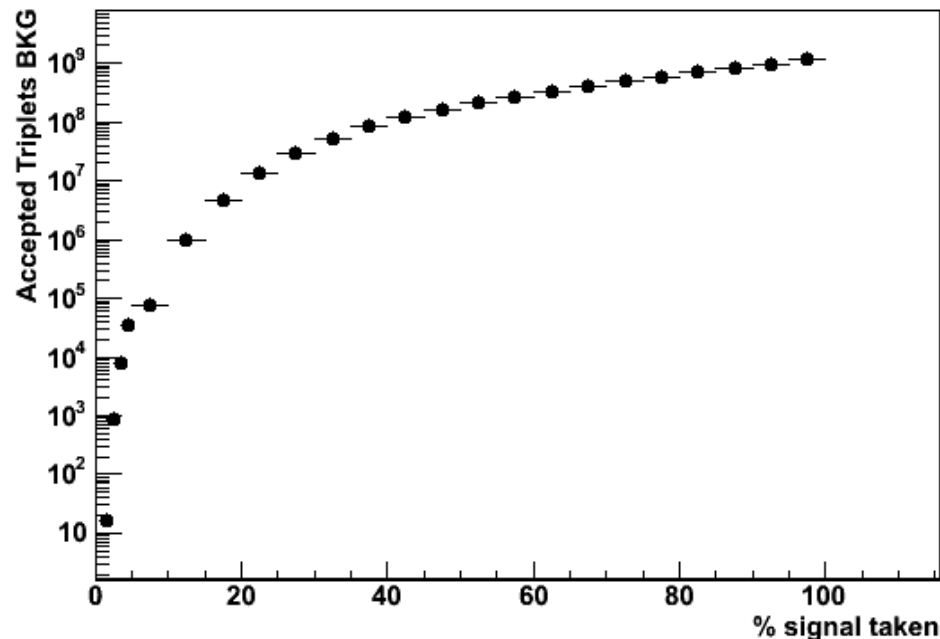
# ***Results scaled to a lower multiplicity scenario for Pb-Pb***

- Results presented so far for Pb-Pb based on  $dN_{ch}/dy=6'000$ 
  - $N_{tracks}=7000$
  - $BKG/ev=N(N-1)(N-2)/3! \sim 6 \times 10^{10}$
- Extrapolations from RHIC results seem to favour a lower multiplicity scenario,  $dN_{ch}/dy=2'000$ 
  - $N_{tracks} \sim 7000/3 \sim 2300$
  - $BKG/ev \sim 2 \times 10^9$
- Let's consider the  $D^+$   $p_T$  interval:  $0 < p_T < 2$  GeV/c:
  - The results in the highest multiplicity scenario ( $dN_{ch}/dy=6'000$ ) are not satisfactory
  - $BKG/ev$  is downscaled by a factor  $\sim 30$ ;
  - $SIG/ev$  not rescaled
  - $S/\sqrt{S+B}$  (normalized to  $10^7$  ev.)  $\sim 10$  in case of Real PID: it is possible the study of the low- $p_T$  spectra



# ***1<sup>st</sup> step: single track cuts***

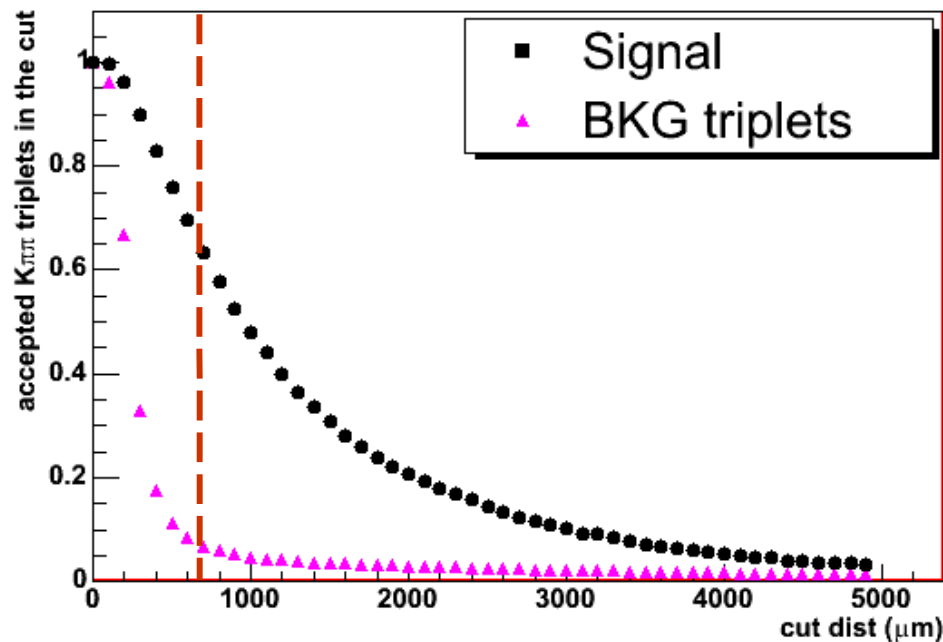
- Cuts on  $p_T$  and  $d_0$  of all tracks
- If PID information is used
  - Reject p, e and  $\mu$
  - Different  $p_T$  cut for  $\pi$  and K



Selection	SIG/event	Selected SIG	BKG/event t	Selected BKG	S/B
No cuts	0.1	100%	10 <sup>9</sup>	100%	10 <sup>-10</sup>
<b><math>P_T \pi &gt; 0.5</math> GeV/c</b> <b><math>P_T K &gt; 0.7</math> GeV/c</b> <b><math>d_0 = 95 \mu\text{m}</math></b>	0.008	8%	10 <sup>6</sup>	0.1%	10 <sup>-8</sup>

# Combining $K\pi\pi$ triplets

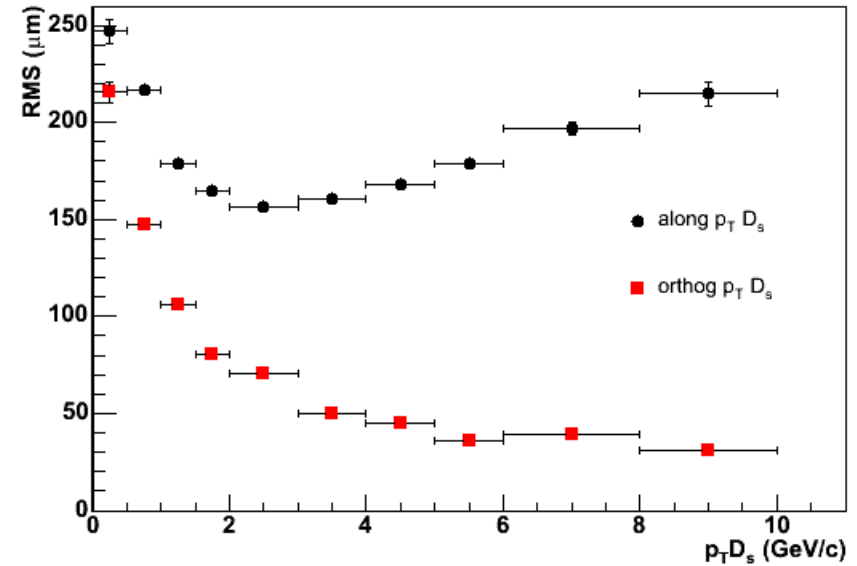
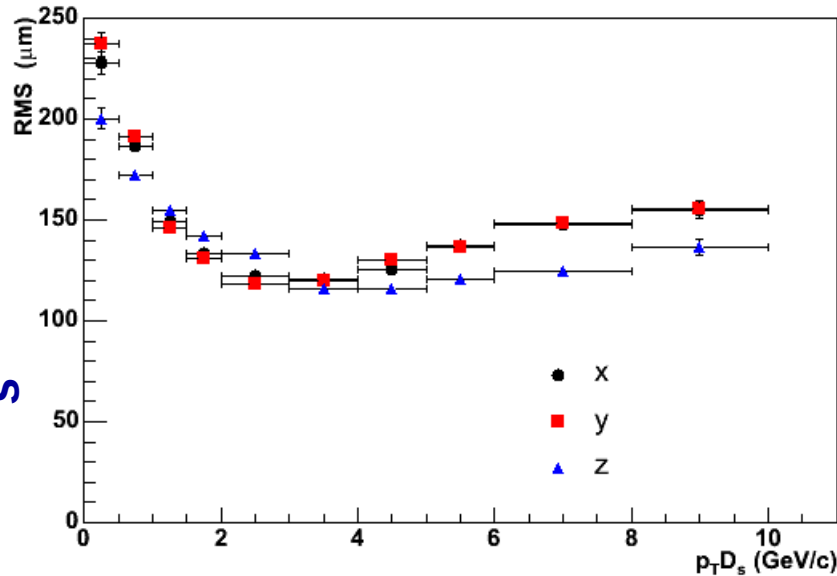
- Build the triplets starting from two selected  $K\pi$  pairs
  - both  $K\pi$  pairs with vertex displaced from the primary vertex



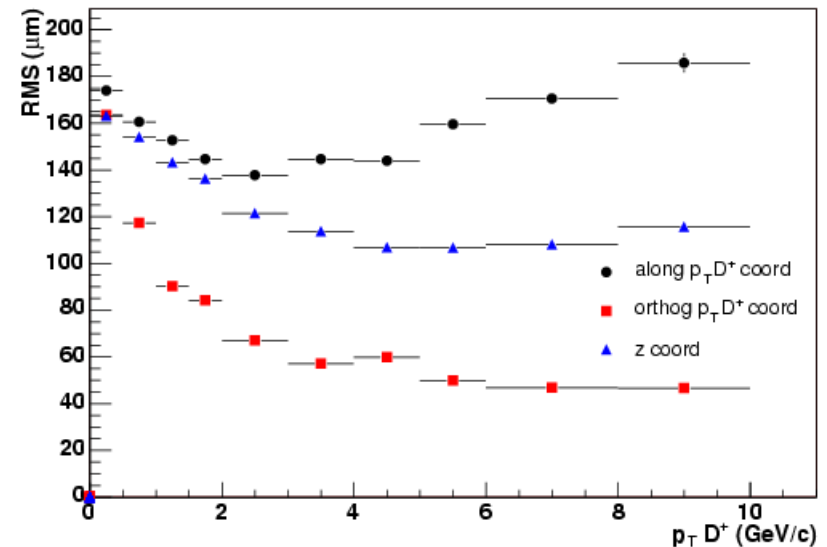
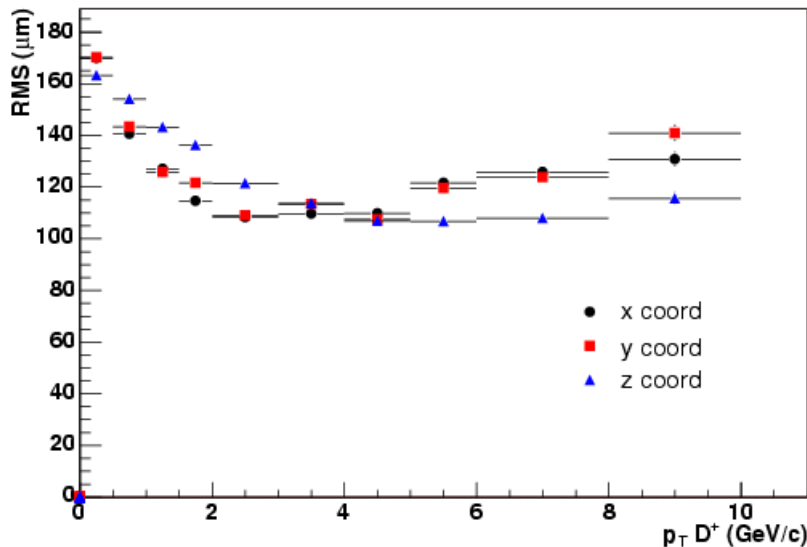
# Vertex finder: $D_s \rightarrow KK\pi$

R. Silvestri, E. Bruna

$D_s \rightarrow KK\pi$

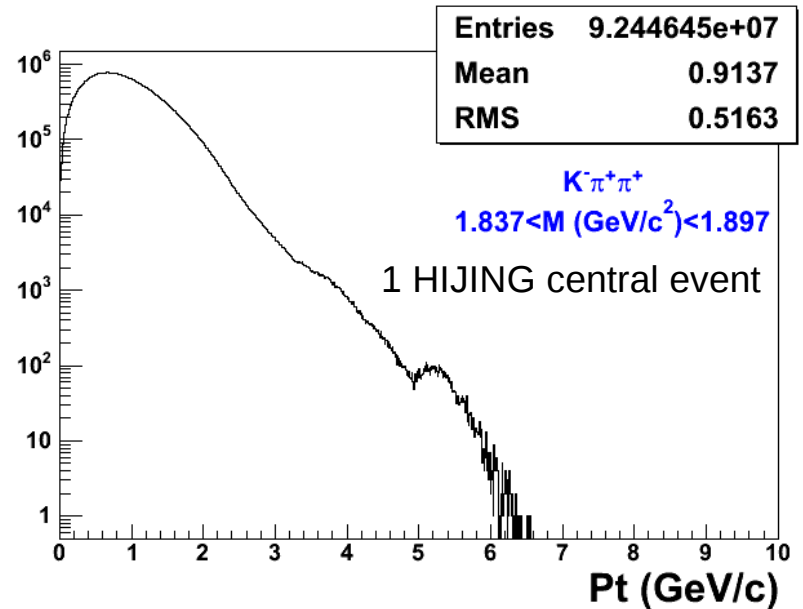
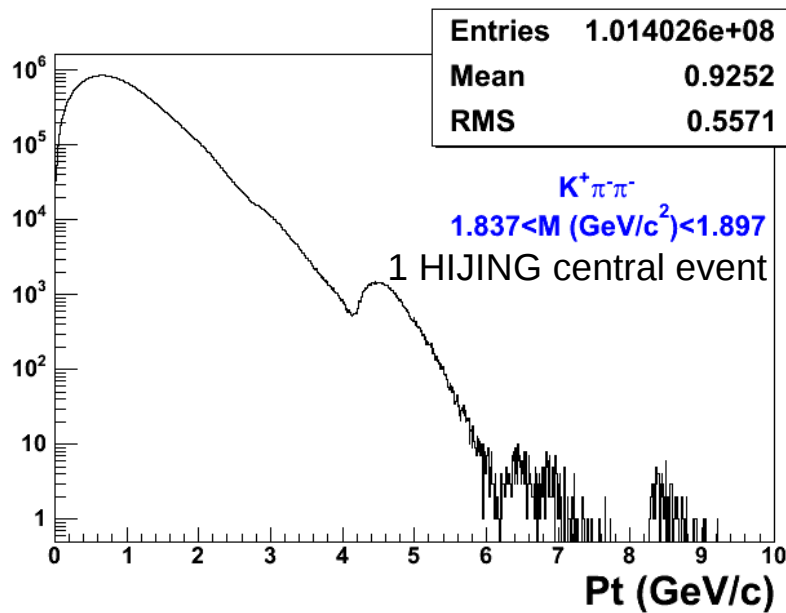


$D^+ \rightarrow K\pi\pi$



- Better resolution for  $D^+$  due to larger average momentum of daughter tracks

# Combinatorial background

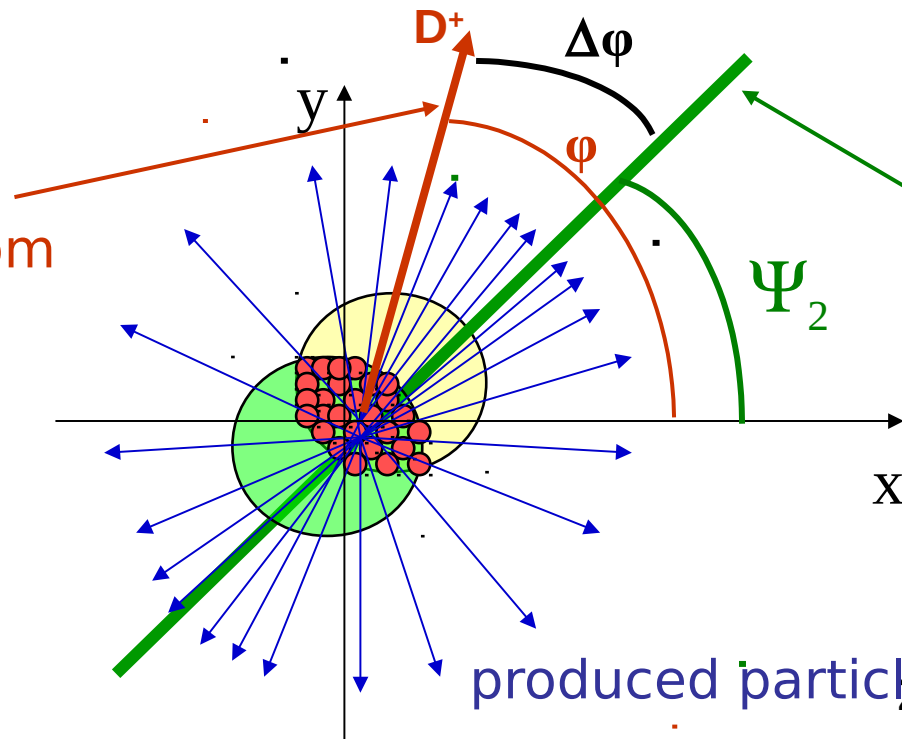


- Huge number ( $\approx 10^{10}$  without PID) of combinatorial  $K\pi\pi$  triplets in a HIJING central event
  - $\approx 10^8$  triplets in mass range  $1.84 < M < 1.90$   $\text{GeV/c}^2$  ( $D^\pm$  peak  $\pm 3\sigma$ )
    - ✓ *Final selection cuts not yet defined*
  - Signal almost free from background only for  $p_T > 6$   $\text{GeV/c}$
  - At lower  $p_T$  need to separate signal from background in  $v_2$  calculation

# ***First ideas for background***

- Sample candidate  $K\pi\pi$  triplets in bins of azimuthal angle relative to the event plane ( $\Delta\phi = \phi - \Psi_2$ )
  - Build invariant mass spectra of  $K\pi\pi$  triplets in  $\Delta\phi$  bins
  - Extract number of  $D^\pm$  in  $\Delta\phi$  bins from an invariant mass analysis
- Quantify the anisotropy from numbers of  $D^\pm$  in the  $\Delta\phi$  bins

D meson  
momentum as  
reconstructed from  
the  $K\pi\pi$  triplet

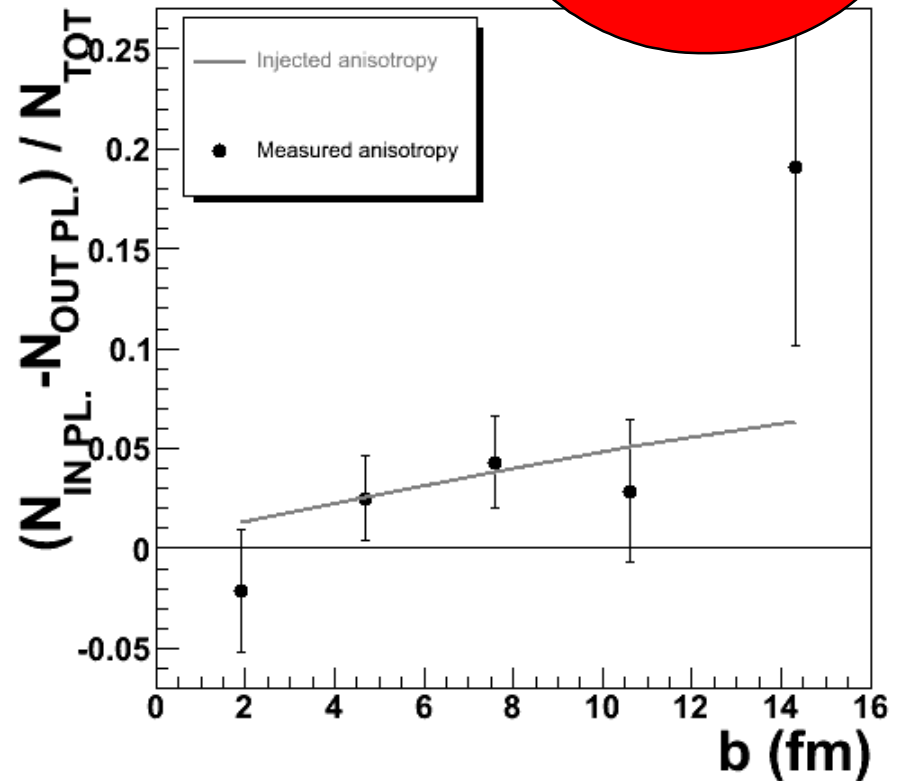
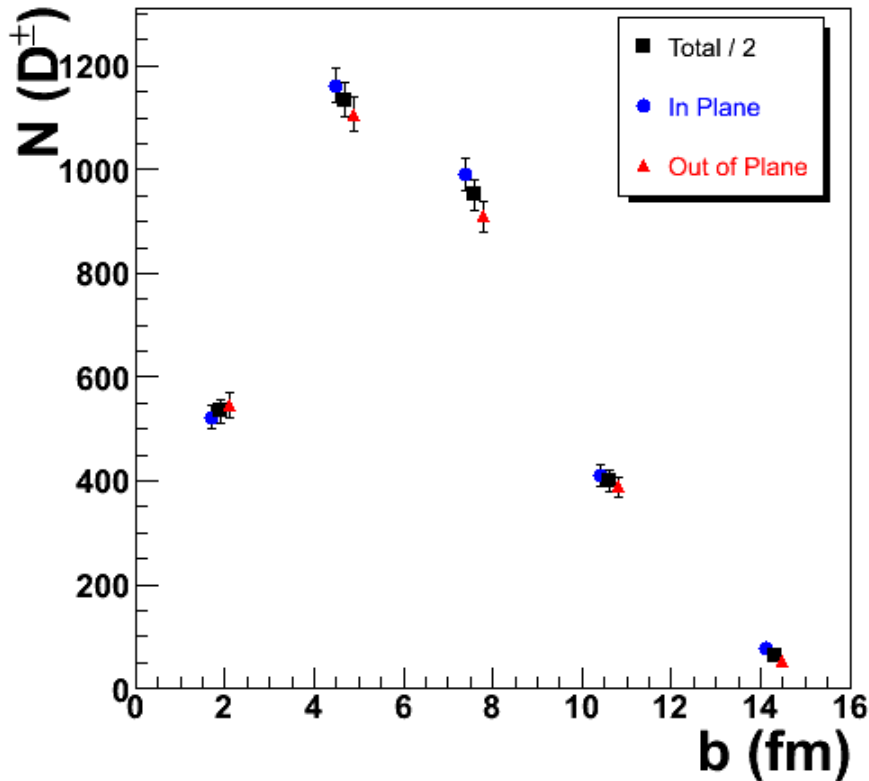
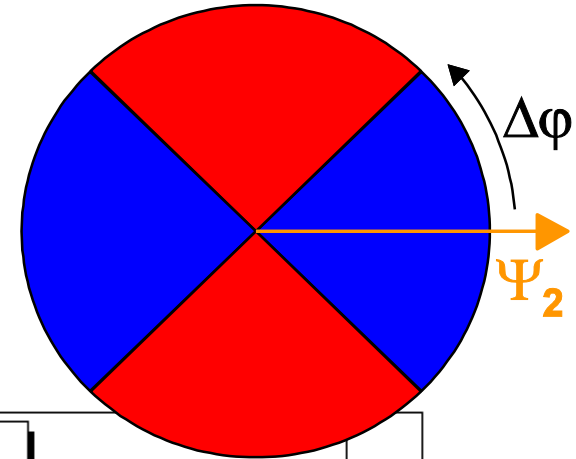


**Event plane**  
(estimator of  
the unknown  
reaction  
plane)

produced particles (mostly pions)

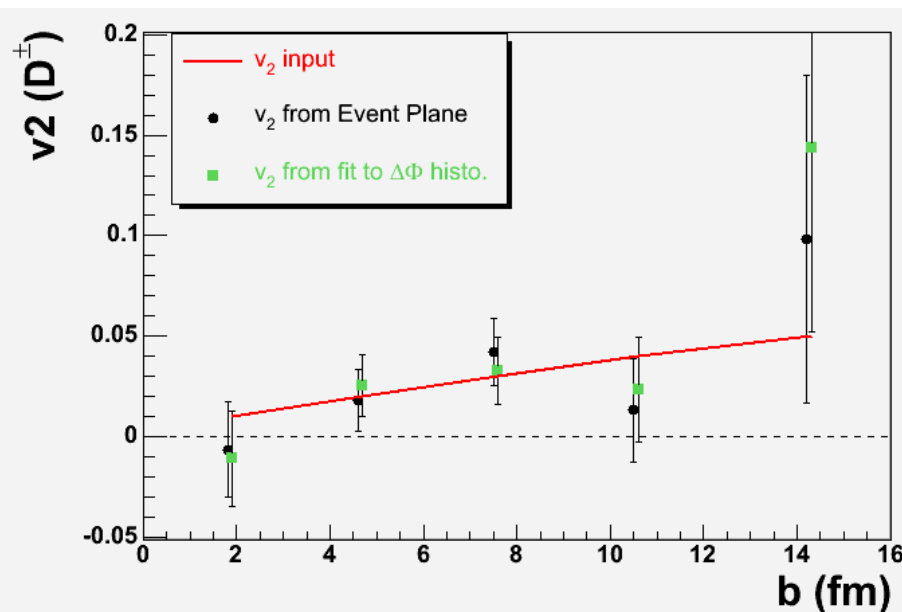
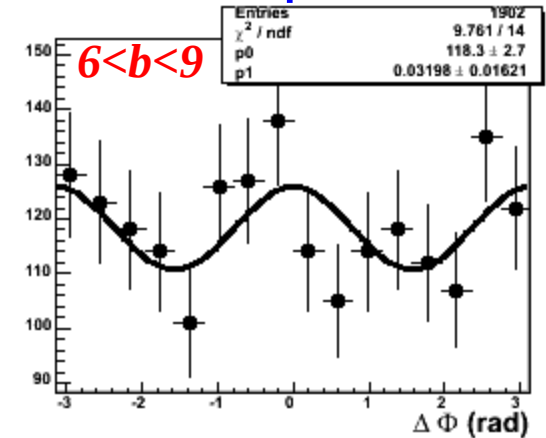
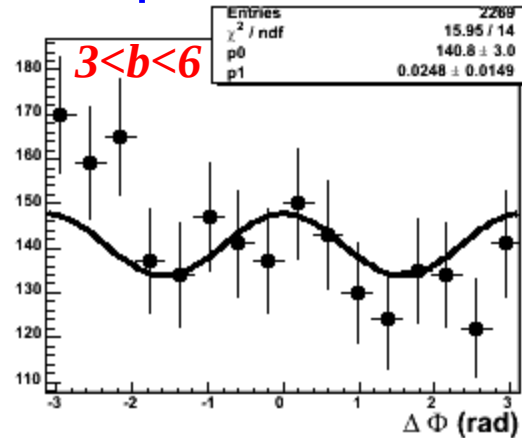
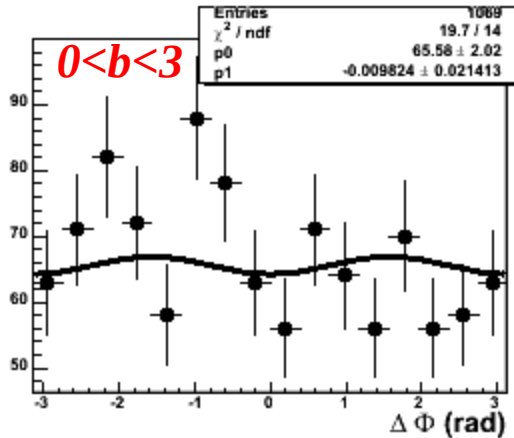
# Analysis in 2 bins of $\Delta\phi$

- Non-zero  $v_2$   $\Rightarrow$  difference between numbers of  $D^\pm$  in-plane and out-of-plane
- Extract number of  $D^\pm$  in  $90^\circ$  “cones”:
  - $\square$  in-plane ( $-45 < \Delta\phi < 45$  U  $135 < \Delta\phi < 225$ )
  - $\square$  out-of-plane ( $45 < \Delta\phi < 135$  U  $225 < \Delta\phi < 315$ )



# Analysis in more bins of $\Delta\phi$

- 16  $\Delta\phi$  bins
- Fit number of  $D^\pm$  vs.  $\Delta\phi$  with  $K[1 + 2v_2\cos(2\Delta\phi)]$



**$v_2$  values and error bars compatible with the ones obtained from  $\langle \cos(2\Delta\phi) \rangle$**

# ***Other ideas for background***

Different analysis methods to provide:

1. Cross checks
2. Evaluation of systematics

- Apply the analysis method devised for  $\Lambda$ s by Borghini and Ollitrault [ PRC 70 (2004) 064905 ]

$$N_{\text{pairs}}(M) = N_b(M) + N_{\Lambda}(M). \quad \longrightarrow \quad \begin{aligned} N_{\text{pairs}}(M) v_{c,n}(M) &= N_b(M) v_{c,n}^{(b)}(M) + N_{\Lambda}(M) v_{c,n}^{\Lambda}, \\ N_{\text{pairs}}(M) v_{s,n}(M) &= N_b(M) v_{s,n}^{(b)}(M) + N_{\Lambda}(M) v_{s,n}^{\Lambda}. \end{aligned}$$

- Used by STAR for  $\Lambda$ s
- To be extended from pairs (2 decay products) to triplets (3 decay products)
- Extract the  $\cos[2(\phi - \Psi_{\text{RP}})]$  distribution of combinatorial  $K\pi\pi$  triplets from:
  - Invariant mass side-bands
  - Different sign combinations (e.g.  $K^+\pi^+\pi^+$  and  $K^-\pi^-\pi^-$ )