

## Assignment 5: Manual calculations:

### -Mini Batch Gradient Descent:

Step 1: read dataset  $[x, y]$ ,  $\eta = 0.1$ ,  $m = 1$ ,  $c = -1$

epochs = 2, batch-size = 2

x	y
0.2	3.4
0.4	3.8
0.6	4.2
0.8	4.6

Step 2: Splitting data into batches

batch 1	batch 2
0.2   3.4	0.4   3.8
0.8   4.6	0.6   4.2

Step 3: iter = 1

Step 4: batch = 1

Step 5: calculate gradient descents

$$\begin{aligned}\frac{\partial \epsilon}{\partial m} &= -\frac{1}{2} [(3.4 - (-1)(0.2) - (-1)(0.2)) + (4.6 - (-1)(0.8) - (-1)(0.8))] \\ &= -\frac{1}{2} [(3.4 - 0.2 + 1)(0.2) + (4.6 - 0.8 + 1)(0.8)] \\ &= -\frac{1}{2} [(4.2)(0.2) + (4.8)(0.8)] = -\frac{1}{2} [4.68] \\ &= -2.34\end{aligned}$$

$$\frac{\partial \epsilon}{\partial c} = -\frac{1}{2} [4.2 + 4.8] = -9.0/2 = -4.5$$

Step 6:  $\Delta m = -\eta \frac{\partial \epsilon}{\partial m} = 0.234$ ,  $\Delta c = 0.45$

Step 7:  $m \neq m + \Delta m \Rightarrow 1 + 0.234 = 1.234$

$$c = c + \Delta c = -1 + 0.45 = -0.55$$

Step 8: batch = batch + 1 = 1 + 1 = 2

Step 9: if batch  $\geq$  no of batches 2  $\Rightarrow$  false

then go to step 5

$$\begin{aligned}
 \text{step 5: } \frac{\partial \epsilon}{\partial m} &= -\frac{1}{n_b} \sum_{i=1}^{n_b} (y_i - mx_i - c) x_i \\
 &= -\frac{1}{5} [(3.8 - (1.234 \times 0.4) + 0.55)(0.4) + (4.2 - (1.234 \times 0.6) + (0.55 \times 0.6))] \\
 &= -\frac{1}{5} \times [3.8564 \times 0.4 + 4.0096 \times 0.6] \\
 &= -1.97416 \\
 \frac{\partial \epsilon}{\partial c} &= -\frac{1}{5} [3.8564 + 4.0096] = -3.933
 \end{aligned}$$

$$\text{step 6: } \Delta m = -\eta \frac{\partial \epsilon}{\partial m} = 0.197416 \quad \Delta c = -\eta \frac{\partial \epsilon}{\partial c} = 0.3933$$

$$\begin{aligned}
 \text{step 7: } m &= 1.234 + 0.197416 = 1.4314 \\
 c &= -0.55 + 0.3933 = -0.1567
 \end{aligned}$$

$$\text{step 8: } \text{batch} = \text{batch} + 1 = 2 + 1 = 3$$

step 9: if  $\text{batch} > n_b \Rightarrow 3 > 2$  then go to step 10.

$$\text{step 10: } \text{iter} = \text{iter} + 1 = 1 + 1 = 2$$

step 11: if  $\text{iter} > \text{epoch } 2 > 2 \Rightarrow \text{false}$   
go to step 4

$$\text{step 4: } \text{batch} = 1$$

$$\begin{aligned}
 \text{step 5: } \frac{\partial \epsilon}{\partial m} &= -\frac{1}{5} [(3.4 - (1.4314)(0.2) + 0.1567 \times 0.2 + (4.6 - (1.4314)(0.8) + 0.1567 \times 0.8)] \\
 &= -\frac{1}{5} [(3.27042)(0.2) + (3.61158)(0.8)] \\
 &= -1.77167
 \end{aligned}$$

$$\frac{\partial \epsilon}{\partial c} = -\frac{1}{2} [3.27042 + 3.61158] = -3.441$$

$$\text{step 6: } \Delta m = -\eta \frac{\partial \epsilon}{\partial m} = 0.177167$$

$$\Delta c = -\eta \frac{\partial \epsilon}{\partial c} = 0.3441$$

Step 7:  $m = m + \Delta m = 1.4314 + 0.177167 = 1.60856$

$C = C + \Delta C = -0.1567 + 0.3441 = 0.1874$

Step 8:  $batch = batch + 1 = 1 + 1 = 2$

Step 9: if  $batch > n_b = 272 \Rightarrow \text{false}$   
go to step 5

Step 5:  $\frac{\partial \epsilon}{\partial m} = -\frac{1}{3} [(3.8 - (1.6085)(0.4) - 0.1874)(0.4) + (4.2 - (1.6085)(0.6) - 0.1874)(0.6)]$   
 $= -\frac{1}{3} [1.187668 + 1.828478] = -1.50807$

$\frac{\partial \epsilon}{\partial C} = -\frac{1}{3} [6.01663] = -3.00831$

Step 6:  $\Delta m = 0.150807, \Delta C = 0.300831$

Step 7:  $m = 1.60856 + 0.150807 = 1.759367$

$C = 0.1874 + 0.300831 = 0.488231$

Step 8:  $batch = 2 + 1 = 3$

Step 9: if  $batch > n_b = 372$  go to step 10

Step 10:  $iter = iter + 1 = 2 + 1 = 3$

Step 11: if  $iter > epoch \Rightarrow 372 = \text{goto step 12}$

Step 12:  $\text{print}(m, C) \Rightarrow 1.759367, 0.488231$

Step 13: Mean square error

$= \frac{(3.4 - 0.84004) + (3.8 - 1.19185) + (4.2 - 1.54) + (4.6 - 1.89548)}{4}$

$mse = 2.63224$