

Assignment 2: Manual calculations:-

Step 1: $f(x, y) = x^2 + y^2 + 10$

calculating derivatives

$$\frac{\partial f}{\partial x} = 2x$$

$$\frac{\partial f}{\partial y} = 2y$$

Step 2: Initialising parameters

$$x = 1$$

$$y = -1$$

$$\eta = 0.1$$

$$\text{iters} = 1$$

$$\text{epochs} = 2$$

Step 3: $\frac{\partial f}{\partial x} \bigg|_{x=1} = 2(1) = 2$

$$\frac{\partial f}{\partial y} \bigg|_{y=-1} = 2(-1) = -2$$

Step 4: $\Delta x = -\eta \frac{\partial f}{\partial x} = -(0.1) \times 2 = -0.2$

$$\Delta y = -\eta \frac{\partial f}{\partial y} = (0.1) \times (-2) = -0.2$$

Step 5: $x = x + \Delta x$

$$= 1 + (-0.2) = 0.8$$

$$y = y + \Delta y$$

$$= -1 + (-0.2) = -1.2$$

Step 6: $\text{iters} = \text{iters} + 1 = 1 + 1$

2 epochs go to step 3

step 3: $\frac{\partial f}{\partial x} \big|_{x=0.8} = 2(0.8) = 1.6$

$\frac{\partial f}{\partial y} \big|_{y=-0.8} = 2(-0.8) = -1.6$

step 4: $x = x + \Delta x = 0.8 - 0.16 = 0.64$

$y = y + \Delta y = -0.8 + 0.16 = -0.64$

step 6: $iters = iters + 1 = 2 + 1 = 3 \text{ epochs}$
goto step 7

$f(x, y) = (0.16)^2 + (-0.16)^2 + 10 = 10.0512$

Global point: $(0.64, -0.64)$

Global value: 10.0512