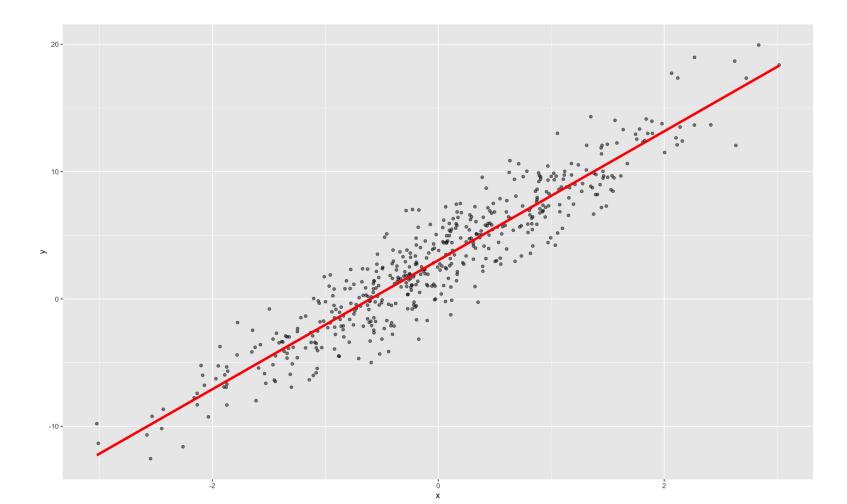
MODEL AGNOSTIC INTERPRETABILITY

Dr. Aric LaBarr
Institute for Advanced Analytics

"INTERPRETABILITY"

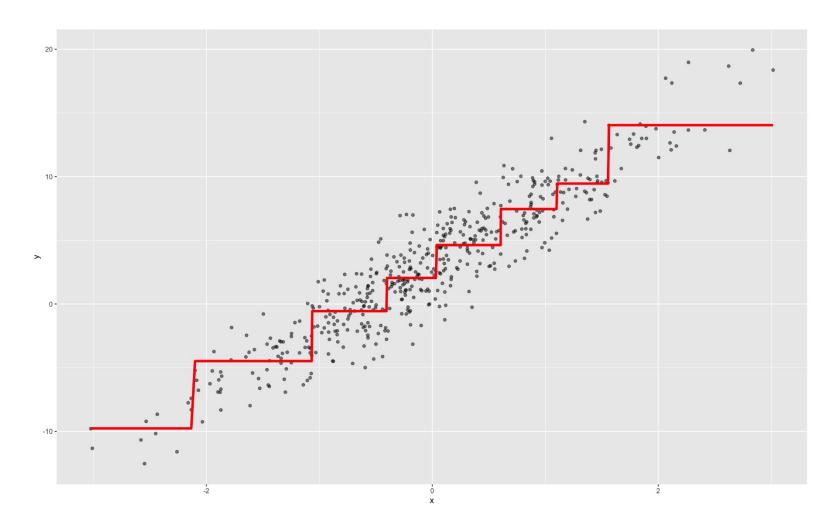
Generalized Linear Models

• If x increases by 1 unit, then on average y increases by β units...



Decision Trees

• If x is between A and B, then y is ... If x is between C and D then y is ...



"Interpretable"

- Most machine learning models are **not** interpretable in the classical sense –
 as one predictor variable increase, the target variable always does...BLAH.
- This is because the relationships are not linear.
- The relationships are more complicated than a linear relationship, so the interpretations are as well.

Still Want Interpretability

- People (especially clients) want to interpret and understand model behavior.
- Questions drive this need for interpretability:
 - Why was someone's loan rejected?
 - Why is this symptom occurring in this patient?
 - Why is the stock price expected to decrease?
- Interpretations can be model and context dependent:
 - Model variable importance in regression has different implication than variable importance in tree-based models.
 - Context the effects of a change in a single variable on a target variable.

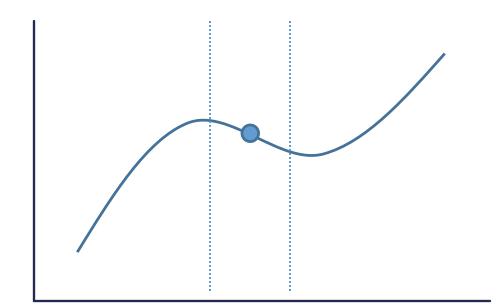
Importance of Interpretability

- Fairness/Transparency:
 - Understanding model decisions improves client/customer trust.
 - Interpretations reveal model behavior on different (potentially marginalized) groups of people.
- Model Robustness and Integrity:
 - Reveal odd model behavior or overfitting problems (does this conclusion make intuitive sense?).
- Adverse Action Requirements:
 - Equal Credit Opportunity Act (ECOA)
 - Fair Credit Reporting Act (FCRA)
 - More on the horizon...

Types of Model Interpretability

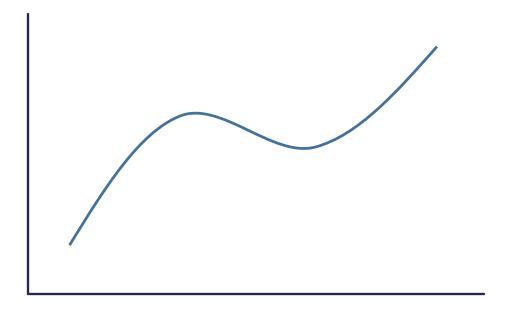
Local

- Example:
 - When x = 10, y decreases as x increases...



Global

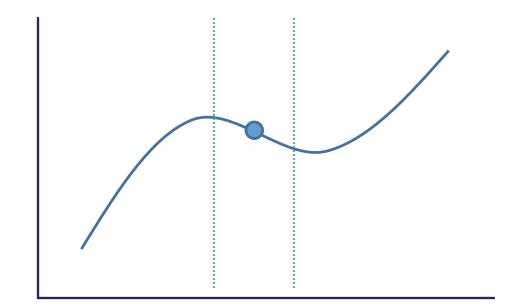
- Example:
 - As x increases, y tends to increase...



Model Agnostic Interpretability

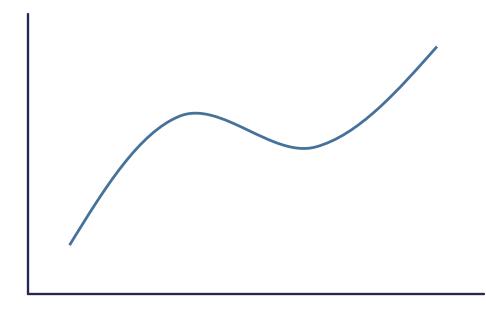
Local

- ICE
- LIME
- Shapley Values



Global

- Permutation Importance
- Partial Dependence
- ALE



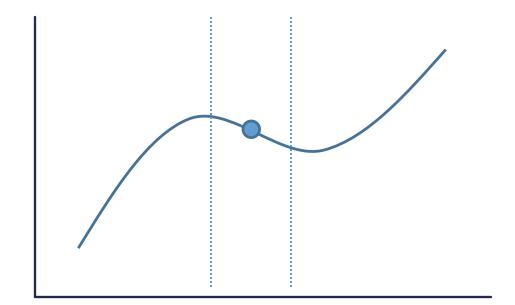


PERMUTATION IMPORTANCE

Model Agnostic Interpretability

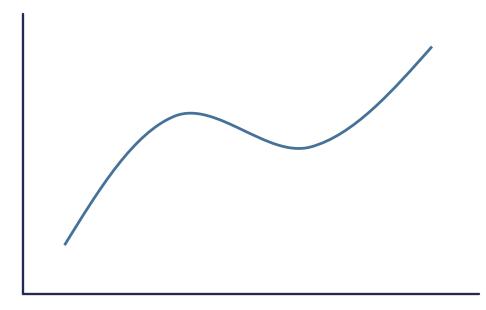
Local

- ICE
- LIME
- Shapley Values



Global

- Permutation Importance
- Partial Dependence
- ALE



Permutation Importance

- General Idea:
 - "Let me show you how much worse the predictions of our model get if we input randomly shuffled data values for each variable."

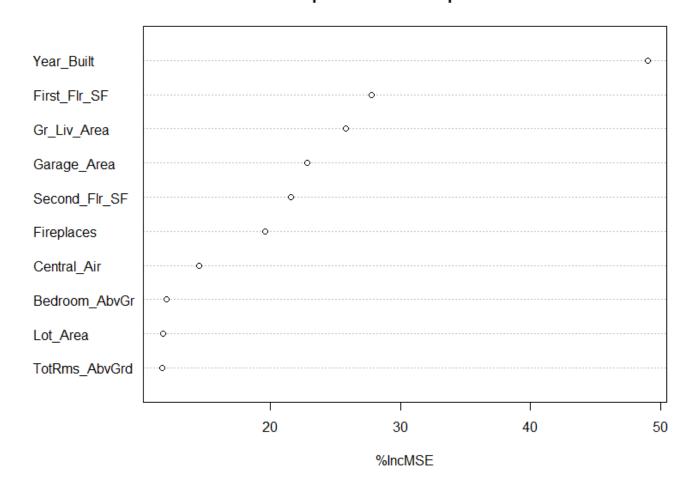
Permutation Importance

- If a variable is important, the model should get worse when that variable is removed.
- To make a direct comparison, rather than remove a variable from the model, we will remove the signal from the variable.
- By randomly shuffling (permuting) the values in that variable, we will break the true relationship between the variable and the target.
- Ex: How much worse does the model get when we take the average impact of 5 random permutations?

Permutation Importance (Random Forest)

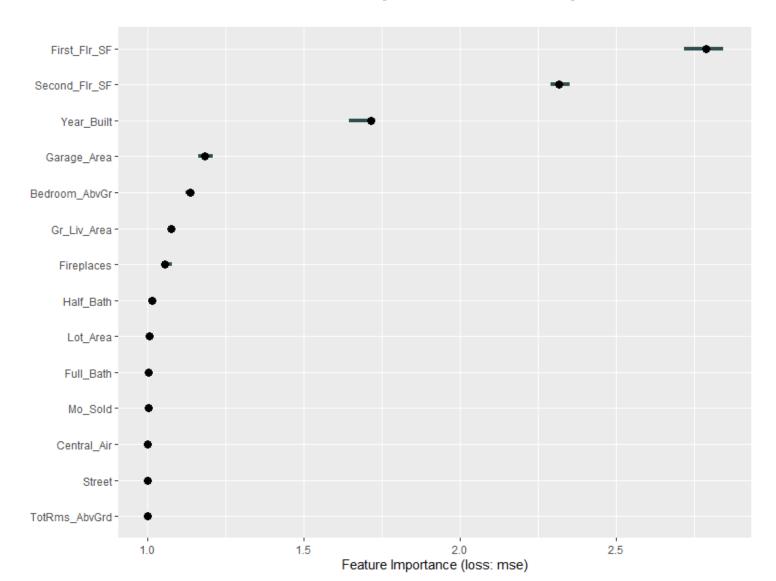
 These were already given to us by default for random forests!

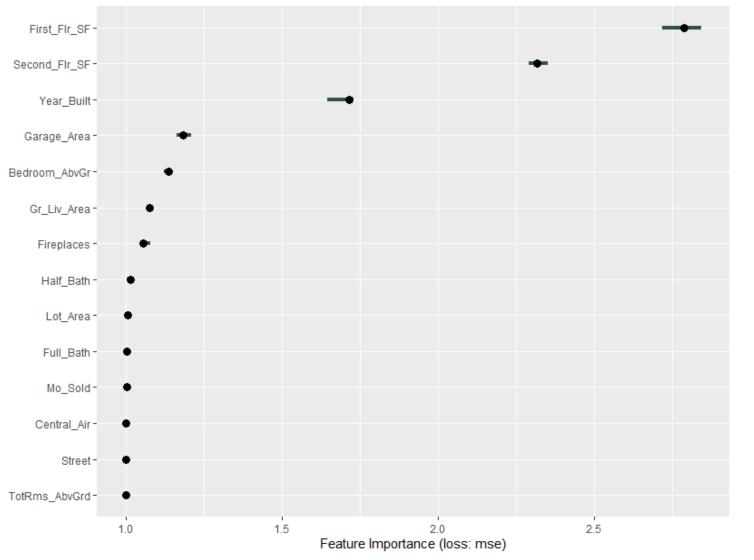
Top 10 - Variable Importance



Build a linear regression just for example other model







```
## Coefficients:
                           Pr(>|t|)
##
                 Estimate
               -1.513e+06
                            < 2e-16 ***
## (Intercept)
## Bedroom AbvGr -1.251e+04
                           2.39e-16 ***
## Year Built 7.700e+02
                            < 2e-16 ***
## Mo_Sold -5.963e+02
                            0.06467 .
## Lot Area
                3.471e-01
                            0.00297 **
## StreetPave
                2.173e+04
                            0.15425
## Central AirY 6.043e+03
                            0.11900
                           2.26e-06 ***
## First Flr SF
                9.762e+01
## Second_Flr_SF 7.404e+01
                            0.00033 ***
## Full Bath
               -3.270e+03
                            0.18077
## Half Bath -6.372e+03
                            0.01139 *
                           2.61e-11 ***
## Fireplaces 1.056e+04
                            < 2e-16 ***
## Garage_Area
                5.816e+01
## Gr Liv Area
                1.601e+01
                             .43115
## TotRms AbvGrd -5.310e+02
                            0.62539
```

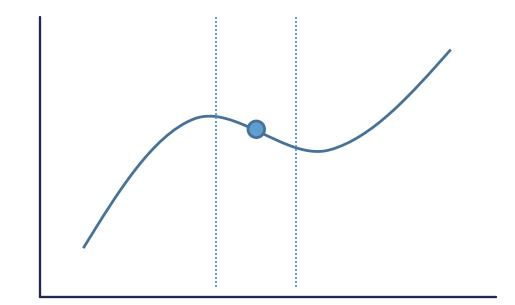


INDIVIDUAL CONDITIONAL EXPECTATION (ICE)

Model Agnostic Interpretability

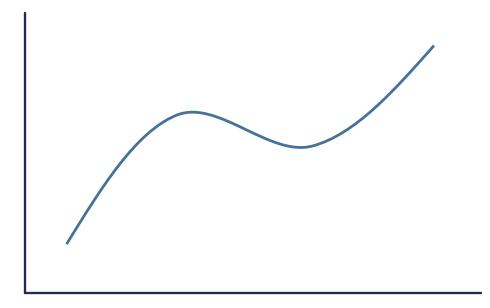
Local

- ICE
- LIME
- Shapley Values



Global

- Permutation Importance
- Partial Dependence
- ALE



Individual Conditional Expectation

- General Idea:
 - "Let me show you how the predictions for each observation change if we vary the feature of interest."

Individual Conditional Expectation

- Local method

 visualizes the dependence of an individual prediction on a given predictor variable.
- Fix all other variables for a single observation while changing the variable of interest.
- Plot the resulting predictions vs. the variable of interest.

Choose a variable of interest and a single observation.

Year Built	Central Air	Garage Area	Greater Living Area	 Sale Price	Predicted Sale Price
2001	Y	725	1947	 274,000	248,756.99
1922	Υ	100	816	 75,200	92,225.59
2005	Y	784	2358	 329,900	331,746.07
1926	Υ	506	1285	 145,400	122,841.74

Choose a variable of interest and a single observation.

Year Built	Central Air	Garage Area	Greater Living Area		Sale Price	Predicted Sale Price
2001	Y	725	1947		274,000	248,756.99
1922	Y	100	816		75,200	92,225.59
2005	Y	784	2358	•••	329,900	331,746.07
1926	Υ	506	1285	•••	145,400	122,841.74

Replicate single observation, holding all other variables constant.

Year Built	Central Air	Garage Area	Greater Living Area	 Sale Price	Predicted Sale Price
2001	Y		1947	 274,000	
2001	Y		1947	 274,000	
2001	Y		1947	 274,000	
2001	Υ		1947	 274,000	

• Fill in values for variable of interest across the entire range of the variable.

Year Built	Central Air	Garage Area	Greater Living Area		Sale Price	Predicted Sale Price
2001	Y	0	1947		274,000	
2001	Y	1	1947		274,000	
2001	Y	2	1947	•••	274,000	
2001	Y	1488	1947	•••	274,000	

Use the model to predict each of these simulated observations.

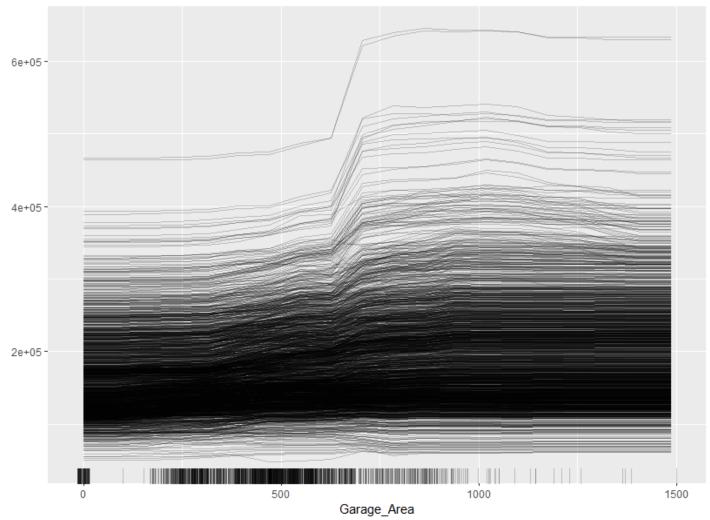
Year Built	Central Air	Garage Area	Greater Living Area		Sale Price	Predicted Sale Price
2001	Y	0	1947		274,000	213,198.60
2001	Y	1	1947		274,000	213,198.60
2001	Υ	2	1947		274,000	213,198.60
				•••		
2001	Y	1488	1947		274,000	268,953.00

REPEAT FOR ALL OBSERVATIONS (or large sample)!

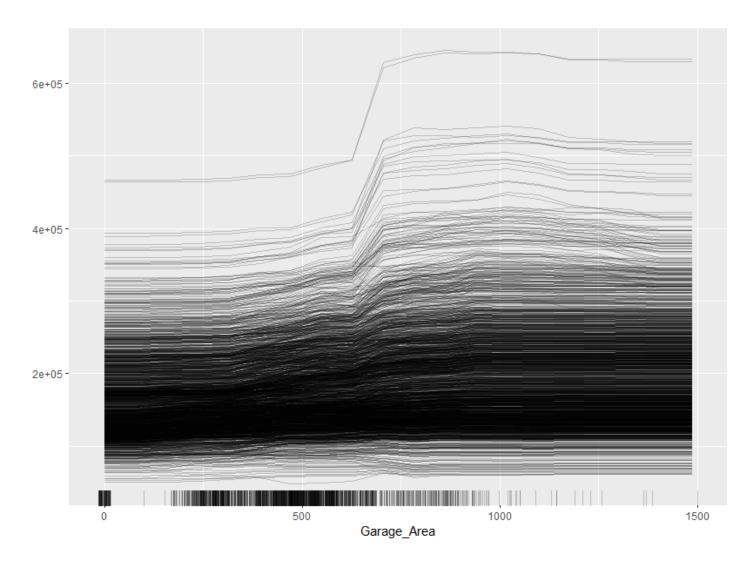
Year Built	Central Air	Garage Area	Greater Living Area	 Sale Price	Predicted Sale Price
2001	Y	725	1947	 274,000	248,756.99
1922	Υ	100	816	 75,200	92,225.59
2005	Y	784	2358	 329,900	331,746.07
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ICE Plot

 One line for every observation in the dataset.



ICE Plot



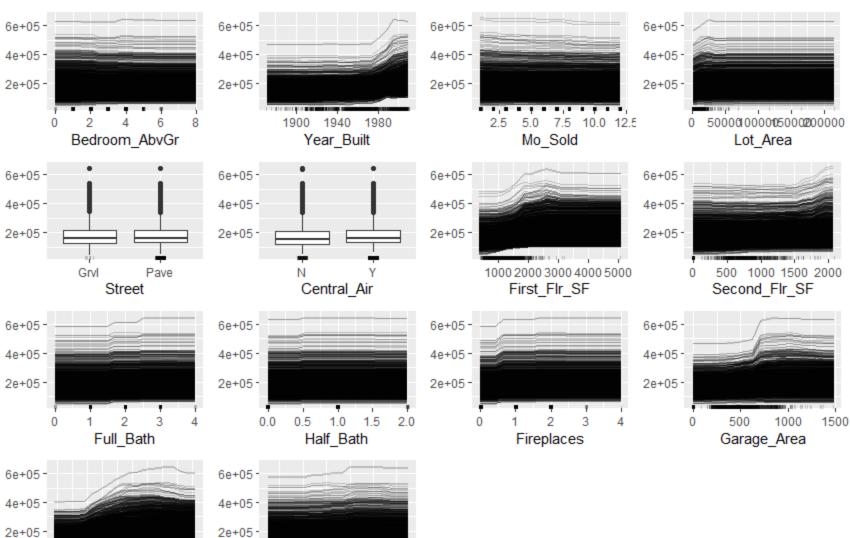
ICE Plot

ice_plot\$plot()



1000 2000 3000 4000 5000

Gr_Liv_Area

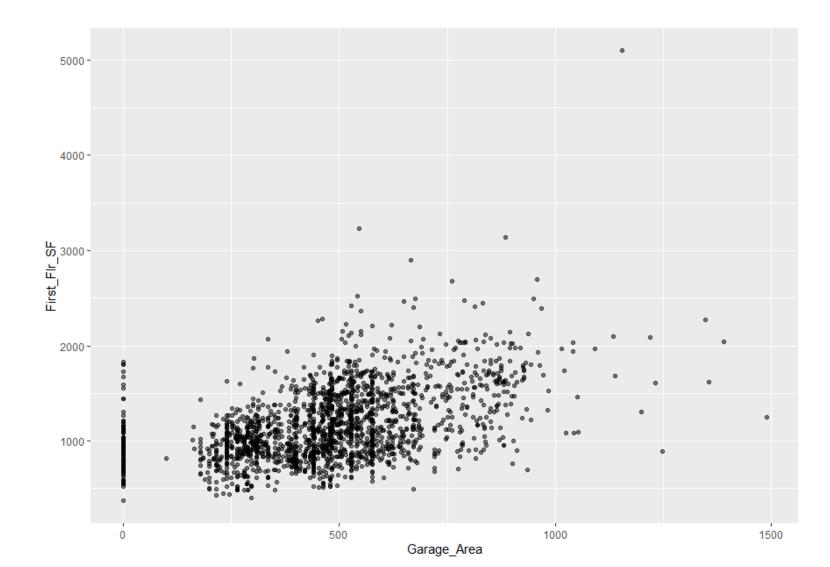


12

TotRms_AbvGrd

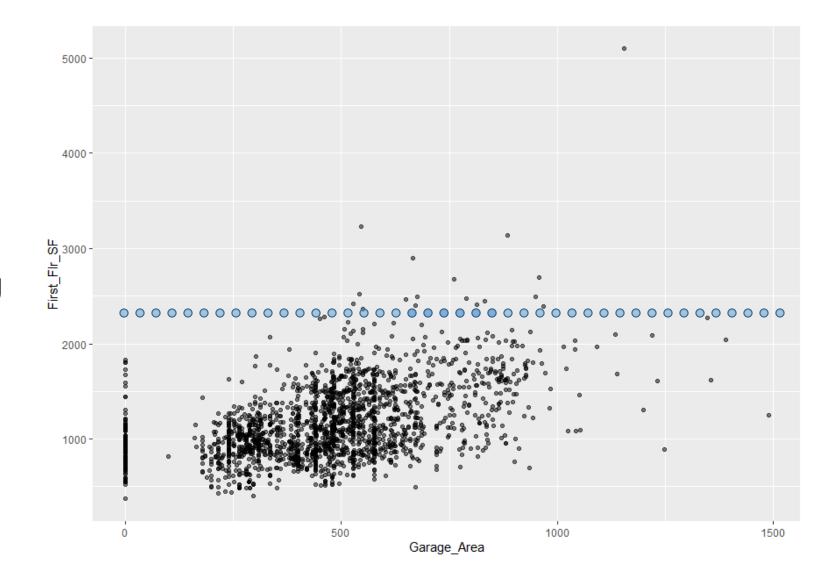
Multicollinearity Problems

 If variable of interest is correlated with other inputs, some of the simulated data may be invalid.



Multicollinearity Problems

- If variable of interest is correlated with other inputs, some of the simulated data may be invalid.
- Keep all other variables constant while replicating across all values of garage area.



Summary

Advantages

- Intuitive
 one line represents
 predictions for one observation if
 we change the variable of interest.
- Capable of showing changing relationships (different impact of variable across different observations).

Disadvantages

- Computationally expensive.
- Hard to visualize with many observations.
- Multicollinearity problems.
- One variable at a time.

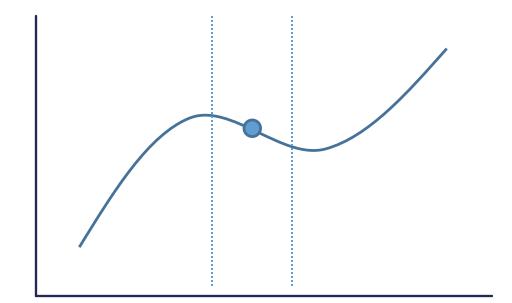


PARTIAL DEPENDENCE

Model Agnostic Interpretability

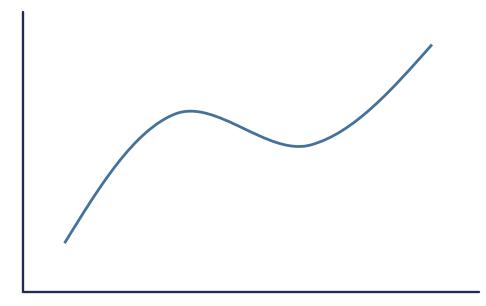
Local

- ICE
- LIME
- Shapley Values



Global

- Permutation Importance
- Partial Dependence
- ALE



Partial Dependence

- General Idea:
 - "Let me show you what the model predicts on average when each observation has the value k for that feature. We'll ignore whether the value k makes sense for all data instances."

Partial Dependence Plots (PDP)

- Attempts to show marginal effect of inputs on the target variable.
- Marginal effects are essentially averaged effects over all possible values of a single variable.
- Think average of all the lines in the ICE plot!

Choose a variable of interest.

Year Built	Central Air	Garage Area	Greater Living Area	 Sale Price	Predicted Sale Price
2001	Υ	725	1947	 274,000	248,756.99
1922	Υ	100	816	 75,200	92,225.59
2005	Y	784	2358	 329,900	331,746.07
1926	Υ	506	1285	 145,400	122,841.74

 Replicate your dataset, holding all variables constant except the variable of interest.

Year Buil	It Central Air	Garage Area	Greater Living Area	 Sale Price	Predicted Sale Price
2001	Υ		1947	 274,000	
1922	Υ		816	 75,200	
2005	Υ		2358	 329,900	
1926	Υ		1285	 145,400	

Year Built	Central Air	Garage Area	Greater Living Area	 Sale Price	Predicted Sale Price
2001	Y		1947	 274,000	
1922	Υ		816	 75,200	
2005	Υ		2358	 329,900	
1926	Υ		1285	 145,400	

Year Built	Central Air	Garage Area	Greater Living Area	 Sale Price	Predicted Sale Price
2001	Υ		1947	 274,000	
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2005	Υ		2358	 329,900	
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Year Built	Central Air	Garage Area	Greater Living Area	 Sale Price	Predicted Sale Price
2001	Υ		1947	 274,000	
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1926	Υ	0	1285	 145,400	

Year Built	Central Air	Garage Area	Greater Living Area	 Sale Price	Predicted Sale Price
2001	Y	1487	1947	 274,000	
1922	Υ	1487	816	 75,200	
2005	Υ	1487	2358	 329,900	
1926	Υ	1487	1285	 145,400	

Year Built	Central Air	Garage Area	Greater Living Area	 Sale Price	Predicted Sale Price
2001	Υ	1	1947	 274,000	
1922	Υ	1	816	 75,200	
2005	Υ	1	2358	 329,900	
1926	Υ	1	1285	 145,400	

Year Built	Central Air	Garage Area	Greater Living Area	 Sale Price	Predicted Sale Price
2001	Y	1488	1947	 274,000	
1922	Υ	1488	816	 75,200	
2005	Υ	1488	2358	 329,900	
1926	Υ	1488	1285	 145,400	



Use model to generate predictions for all this simulated data.

Year Built	Central Air	Garage Area	Greater Living Area	 Sale Price	Predicted Sale Price
2001	Y	0	1947	 274,000	213,198.63
1922	Υ	0	816	 75,200	83,683.52
2005	Y	0	2358	 329,900	271,165.62
1926	Y	0	1285	 145,400	113,025.91

Year Built	Central Air	Garage Area	Greater Living Area	 Sale Price	Predicted Sale Price
2001	Y	1487	1947	 274,000	268,952.96
1922	Υ	1487	816	 75,200	97,340.47
2005	Y	1487	2358	 329,900	329,710.53
1926	Υ	1487	1285	 145,400	133,129.74

Year Built	Central Air	Garage Area	Greater Living Area	 Sale Price	Predicted Sale Price
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Year Built	Central Air	Garage Area	Greater Living Area	 Sale Price	Predicted Sale Price
2001	Y	1488	1947	 274,000	268,952.96
1922	Υ	1488	816	 75,200	97,340.47
2005	Y	1488	2358	 329,900	329,710.53
1926	Y	1488	1285	 145,400	133,129.74



- Use model to generate predictions for all this simulated data.
- Take average of each prediction column corresponding to variable value.

 x_0

 \bar{x}_{1487}

Year Built	Central Air	Garage Area	Greater Living Area	 Sale Price	Predicted Sale Price
2001	Y	0	1947	 274,000	213,198.63
1922	Υ	0	816	 75,200	83,683.52
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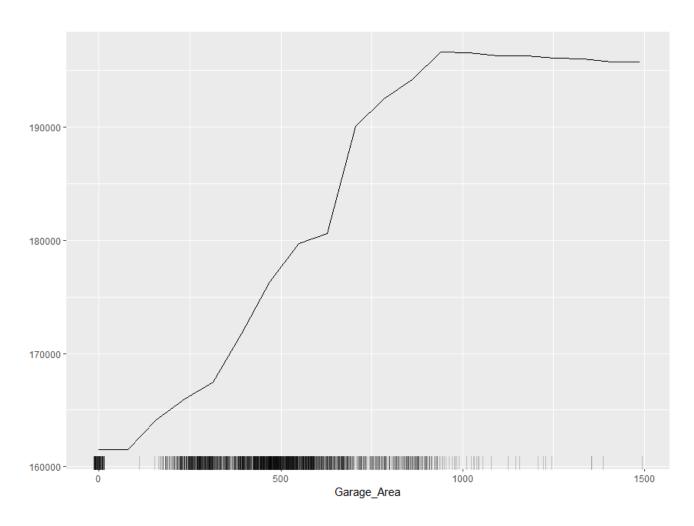
Year Built	Central Air	Garage Area	Greater Living Area	 Sale Price	Predicted Sale Price
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2005	Υ	1488	2358	 329,900	329,710.53
1926	Υ	1488	1285	 145,400	133,129.74

 \bar{x}_1

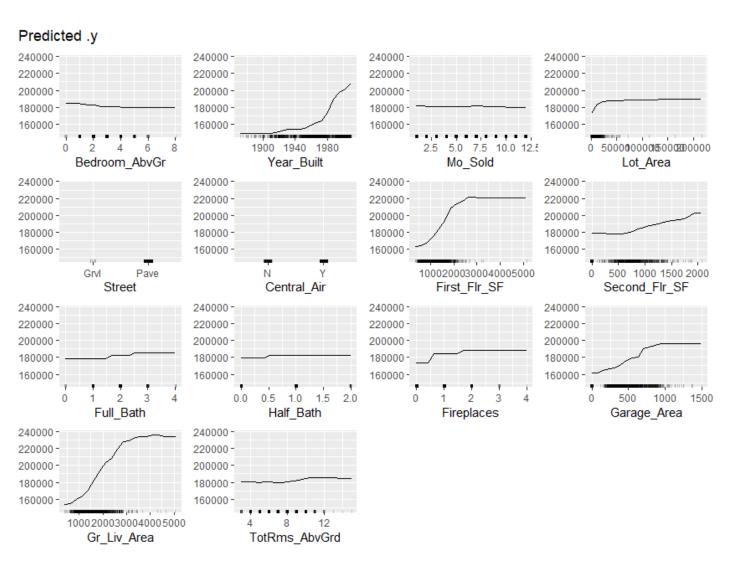
 \bar{x}_{1488}



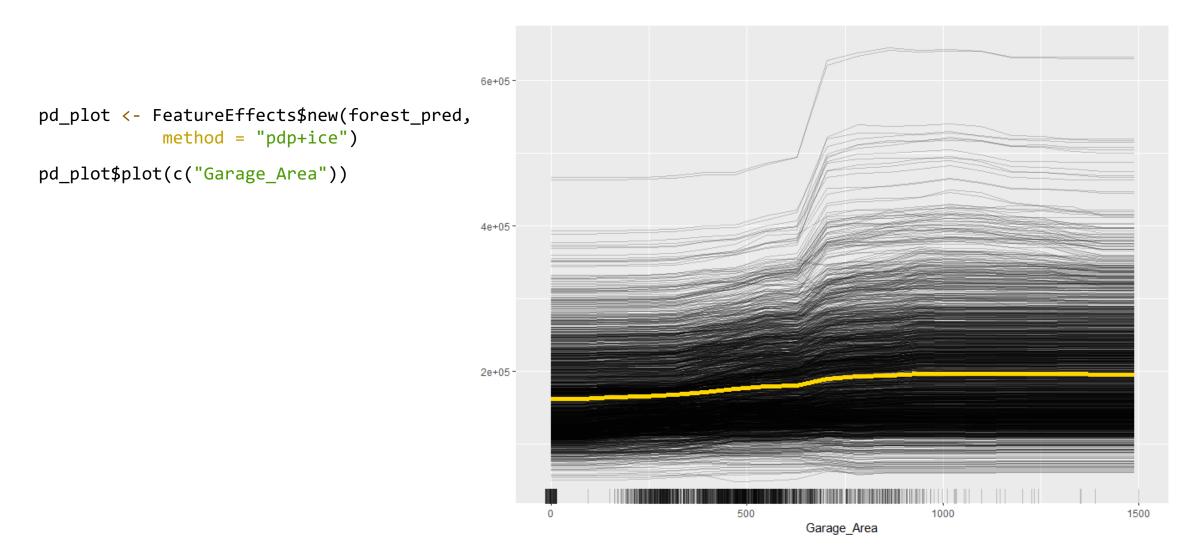
Partial Dependence Plot



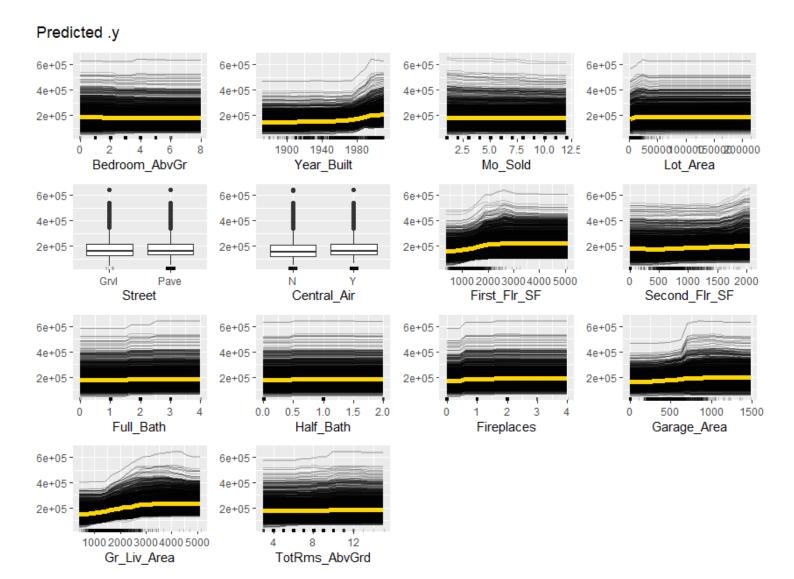
Partial Dependence Plot



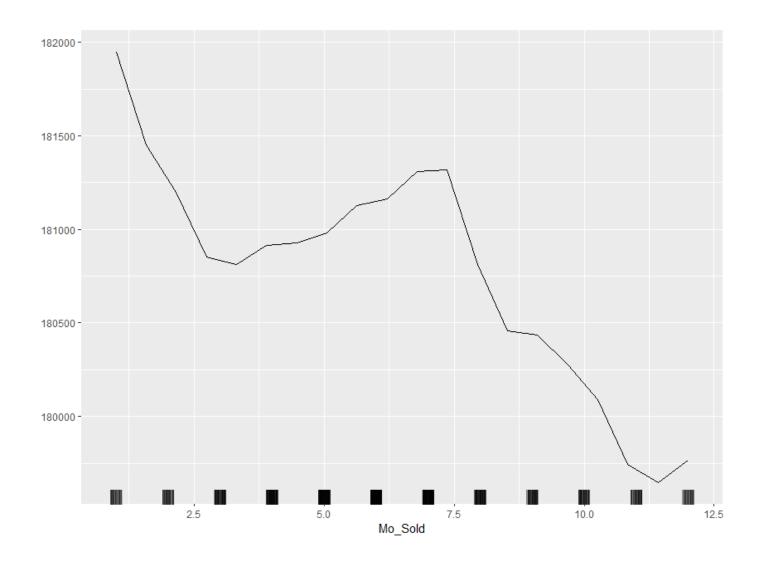
Partial Dependence Plot with ICE



Partial Dependence Plot Interpretation



Watch-out for Scale!



Watch-out for Scale!



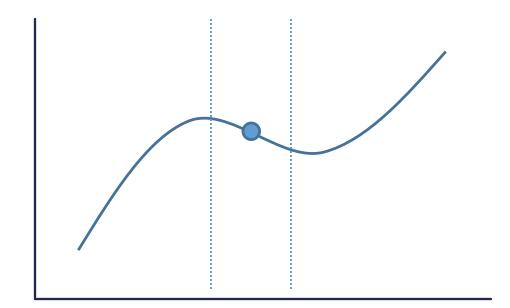


ACCUMULATED LOCAL EFFECTS (ALE)

Model Agnostic Interpretability

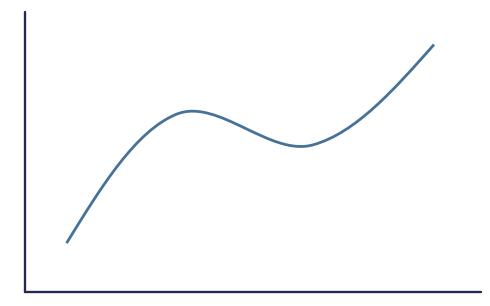
Local

- ICE
- LIME
- Shapley Values



Global

- Permutation Importance
- Partial Dependence
- ALE

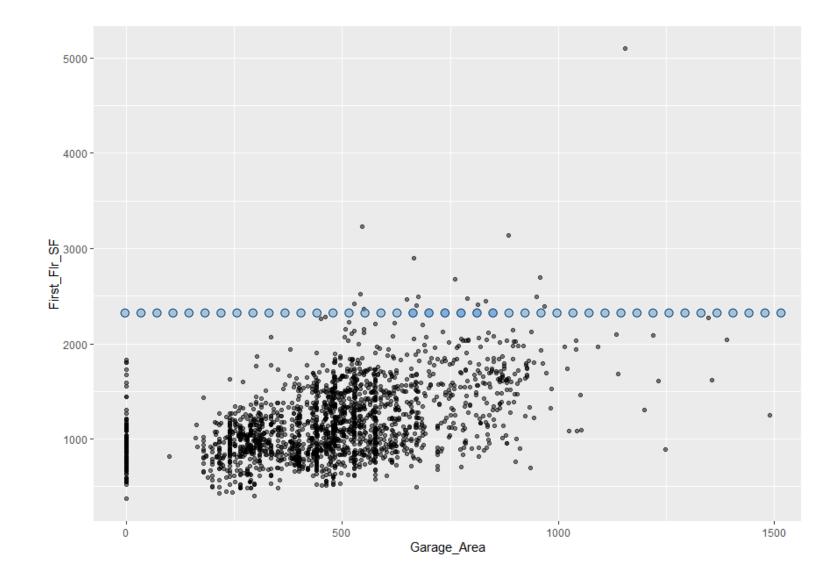


Accumulated Local Effects

- General Idea:
 - "Let me show you how the model predictions change when I change the variable the interest to values within a small interval around their current values."

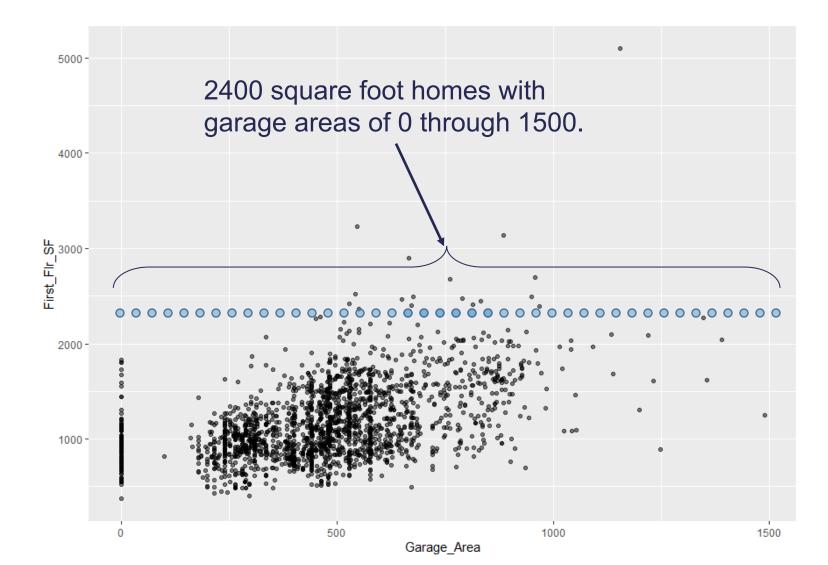
Partial Dependence Plot Problem

- Multicollinearity still a problem in the predictor variables.
- Conclusions are now based on simulated data with possibly some impossible data values.



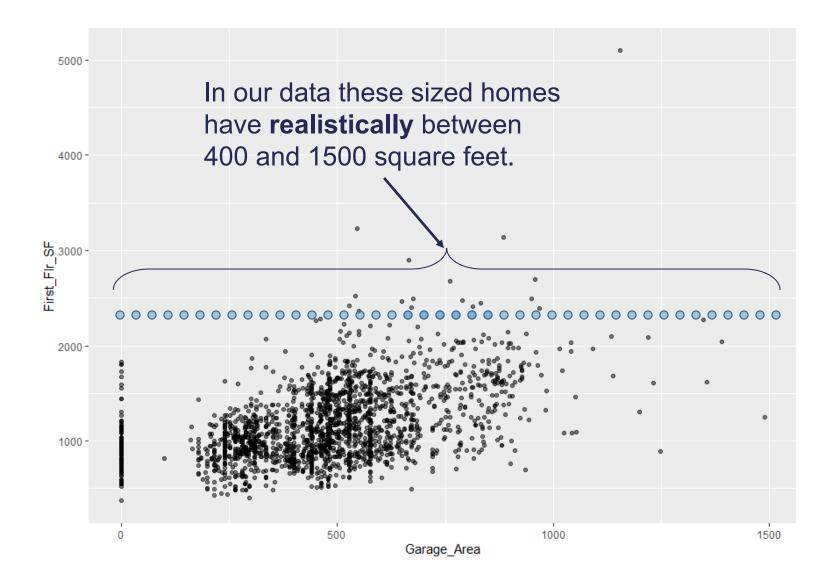
Partial Dependence Plot Problem

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Partial Dependence Plot Problem

- Multicollinearity still a problem in the predictor variables.
- Conclusions are now based on simulated data with possibly some impossible data values.

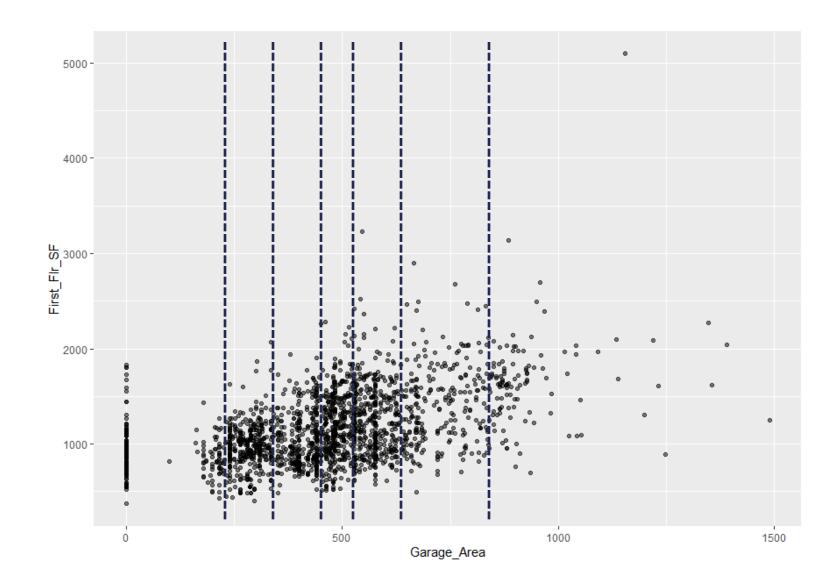


 The accumulated local effects (ALE) approach uses only reasonably contrived data to get a clearer picture of the relationship between a variable of interest and the target.

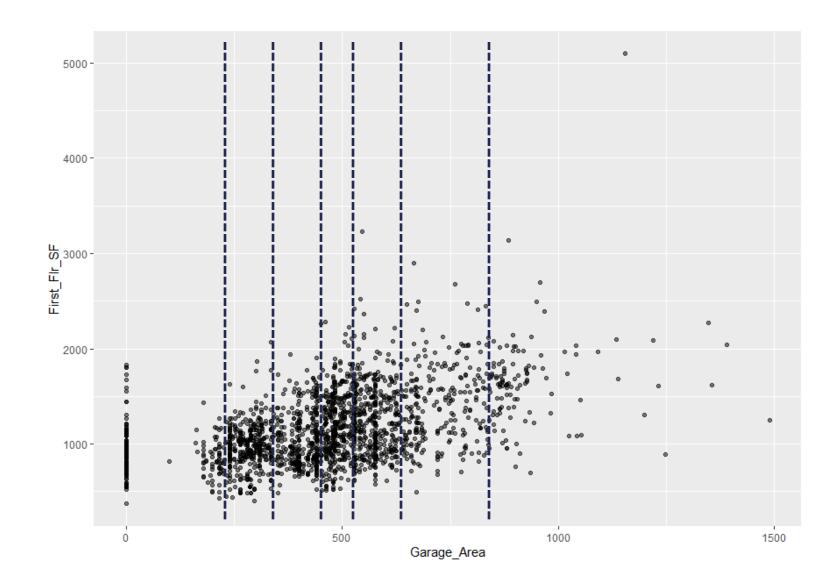
Previously used all possible values in range of the data...

Year Built	Central Air	Garage Area	Greater Living Area	 Sale Price	Predicted Sale Price
2001	Y	0	1947	 274,000	
2001	Y	1	1947	 274,000	
2001	Υ	2	1947	 274,000	
2001	Y	1488	1947	 274,000	

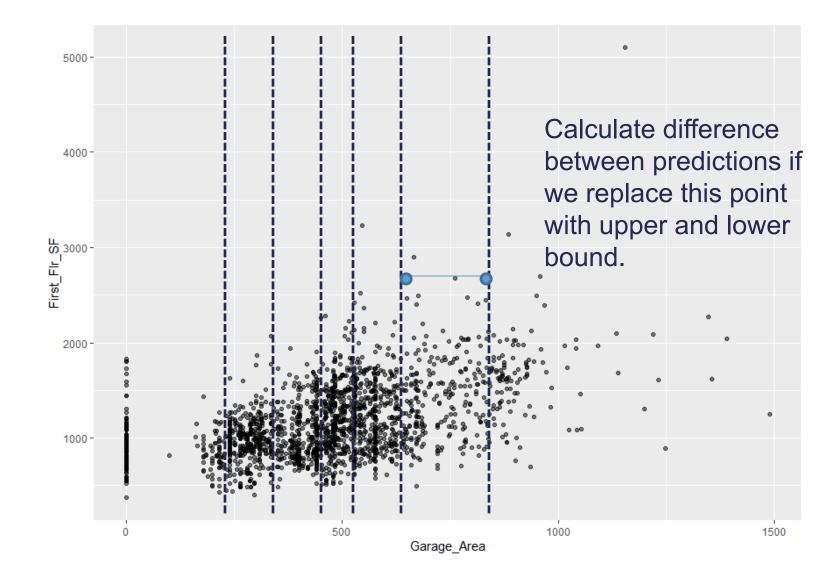
- ALE uses quantiles of your data (by default) to define reasonable range.
- Uses quantiles to get approximately same number of observations in each group.



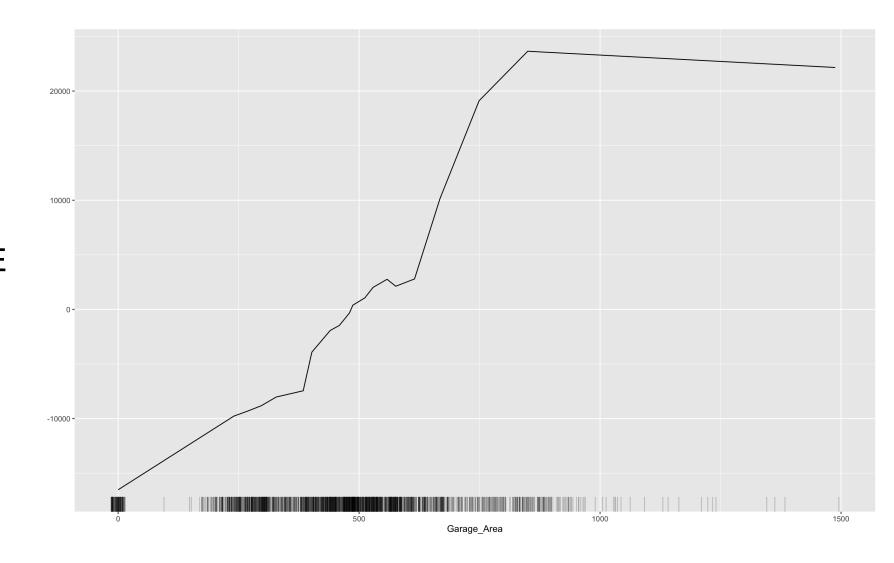
 For observations in each interval, determine how much their prediction would change if we replace the feature of interest with the upper and lower bounds of the interval (keeping all other variables constant).



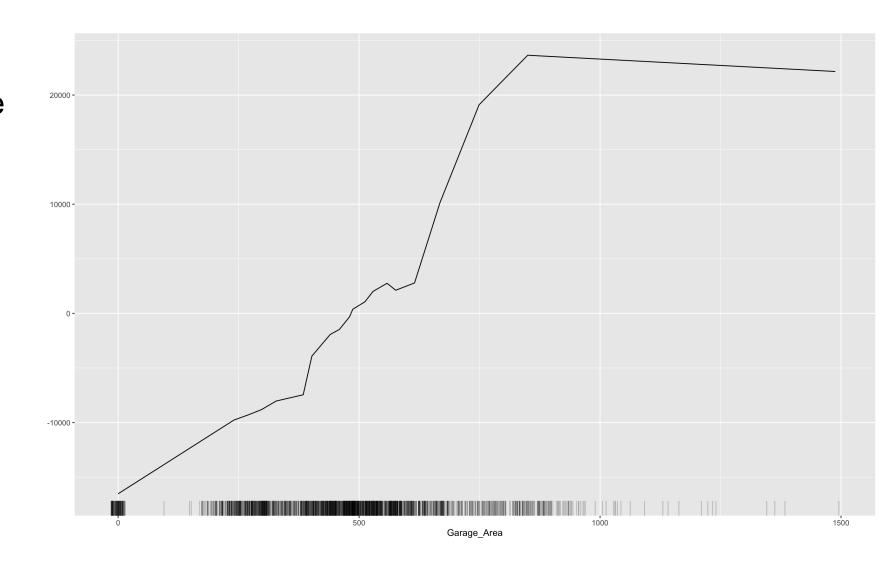
• For observations in each interval, determine the difference in prediction if the variable of interest is set at the upper vs. lower bound of this interval (keeping all other variables constant).



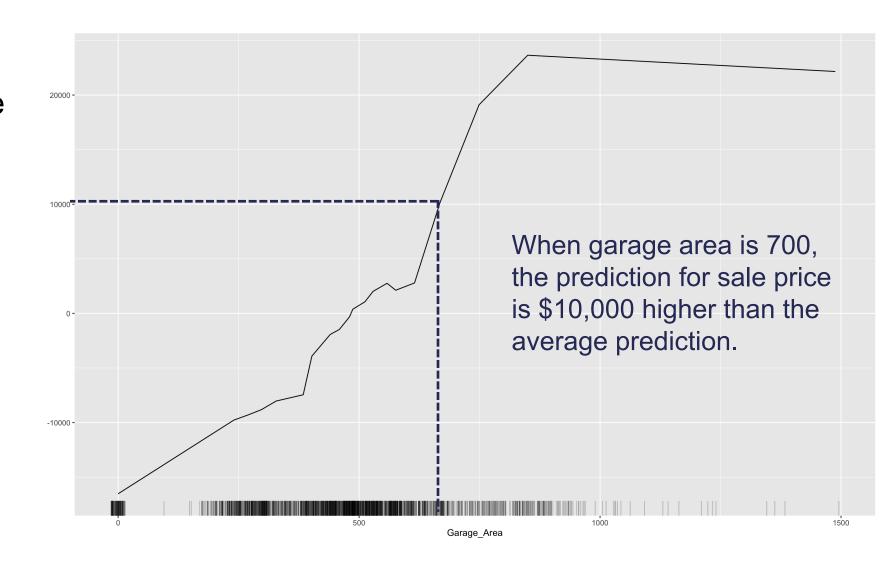
- Do this for all observations in the interval.
- Accumulate these changes and center them to form the ALE curve.



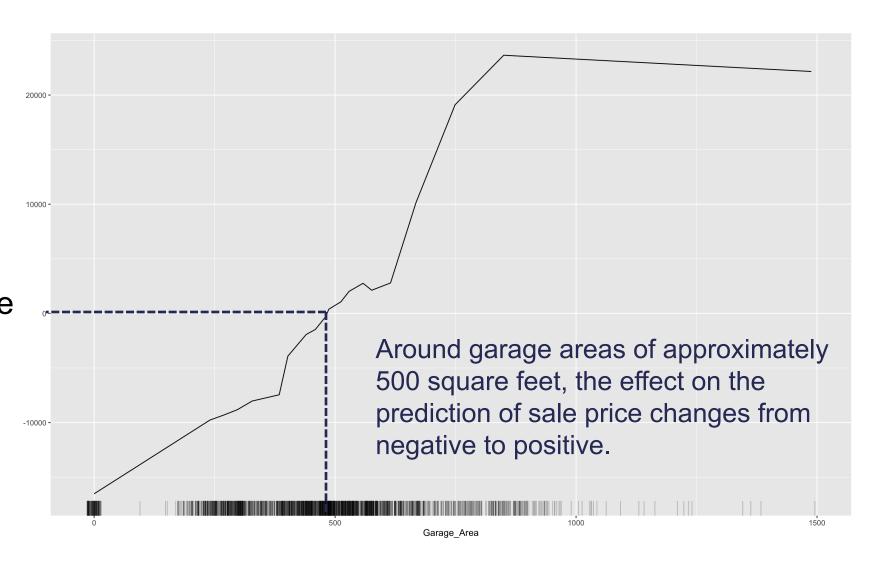
 ALE curve describes the main effect of the input variable compared to the data's average prediction.

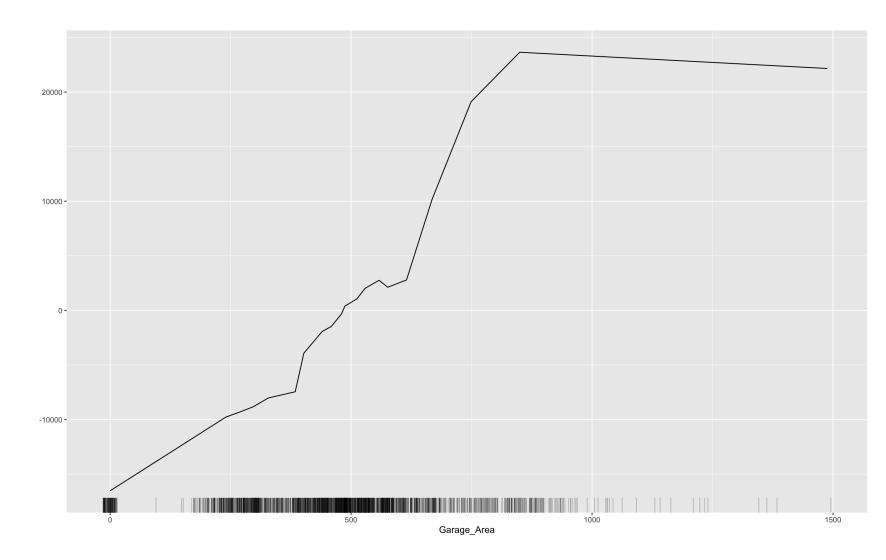


 ALE curve describes the main effect of the input variable compared to the data's average prediction.



- ALE curve describes the main effect of the input variable compared to the data's average prediction.
- Changes from negative to positive (or vice versa) are also important.





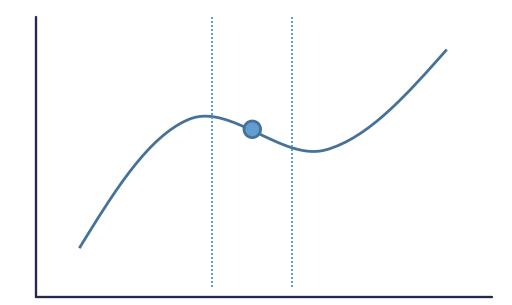


LOCAL INTERPRETABLE MODEL-AGNOSTIC EXPLANATIONS (LIME)

Model Agnostic Interpretability

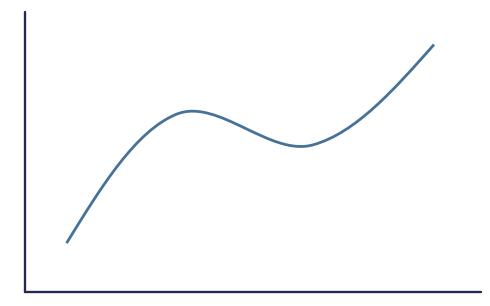
Local

- ICE
- LIME
- Shapley Values



Global

- Permutation Importance
- Partial Dependence
- ALE

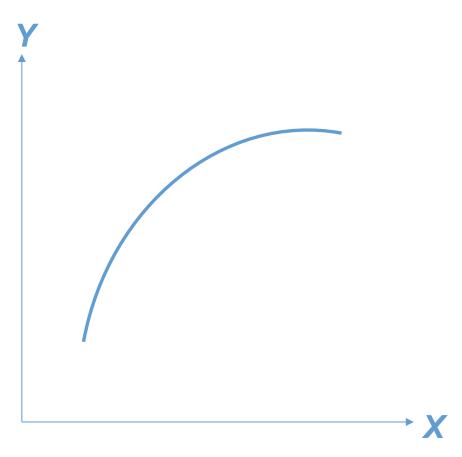


Local Interpretable Model-Agnostic Explanations

- General Idea:
 - "Let me show you a linear model that could explain the exact orientation of the predictive model at a specific point."

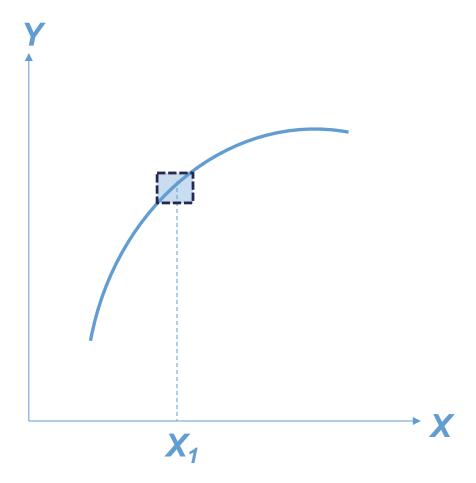
LIME Intuition

 Imagine that you had a nonlinear relationship between a target and a predictor variable.



LIME Intuition

- Imagine that you had a nonlinear relationship between a target and a predictor variable.
- Zoom in REALLY close to a specific point of interest...



LIME Intuition

- Imagine that you had a nonlinear relationship between a target and a predictor variable.
- Zoom in REALLY close to a specific point of interest...
- Looks (approximately) like a straight line!
- We can model straight lines with linear regression → we can understand the predictive model at that exact point.



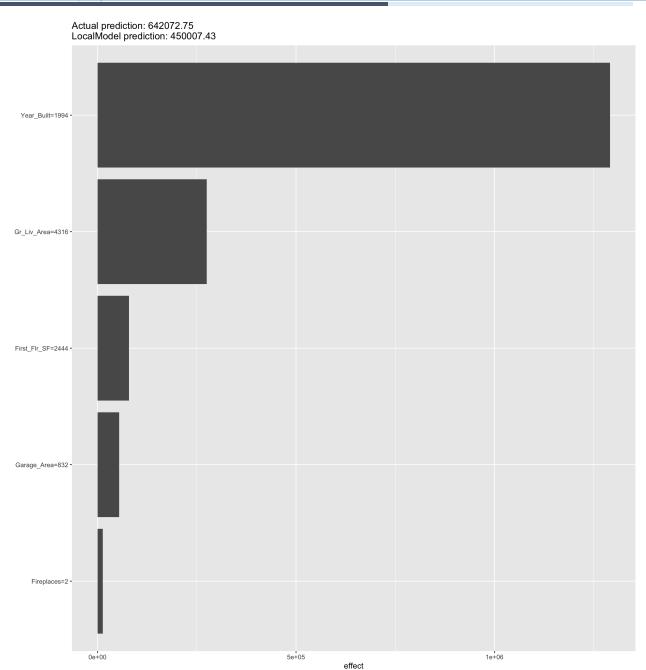
LIME Process

- We can model straight lines with linear regression → we can understand the predictive model at that exact point.
- But how...?
- Here are the basic steps to what LIME is doing:
 - Randomly generate values (Normally distributed) for each variable in the model.
 - Weight more heavily the fake observations that are near the real observation of interest.
 - Build a weighted linear regression model based on fake observations and observation of interest.
 - 4. "Interpret" coefficients of variables from linear regression model.

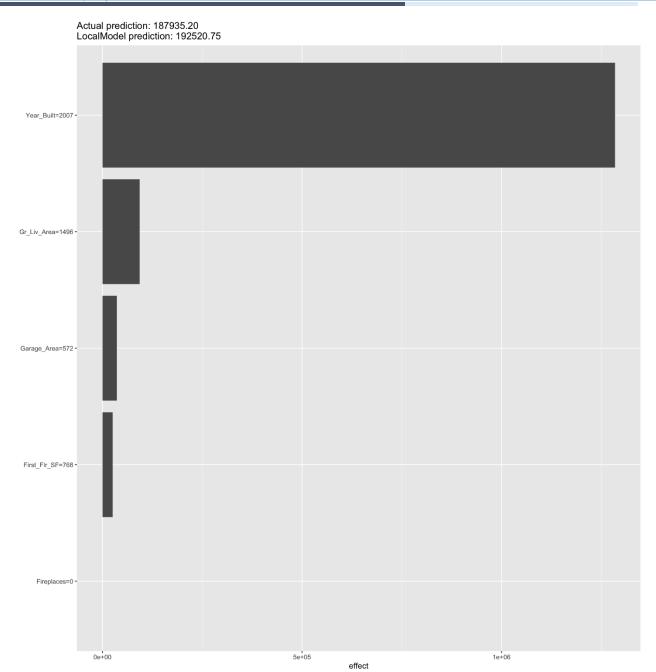
LIME Details

- LIME not actually limited to linear regression... could use any interpretable model (decision tree for example).
- Choices → how much explanation do you want your model to have (aka, number of variables to use in explainable model)?
- LIME commonly used for small local models (not a lot of variables).
- The definition of "near the points of interest" is a very big and unsolved problem in the world of LIME.

LIME



LIME



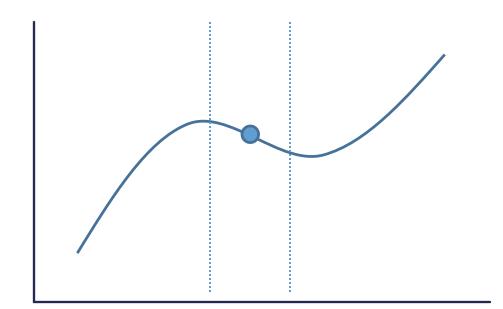


SHAPLEY VALUES

Model Agnostic Interpretability

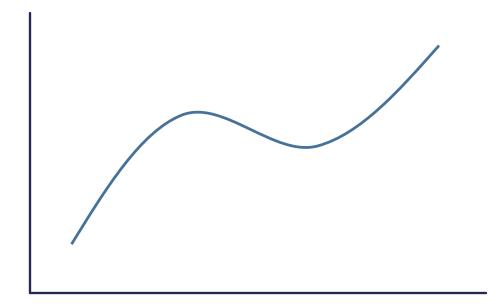
Local

- ICE
- LIME
- Shapley Values



Global

- Permutation Importance
- Partial Dependence
- ALE

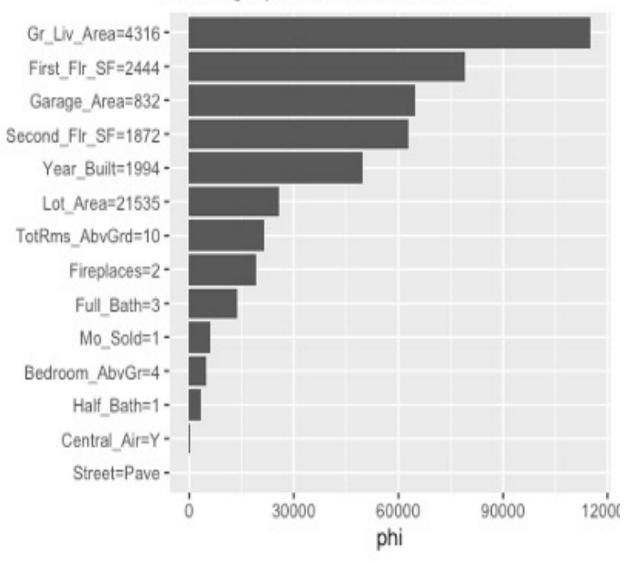


Shapley Values

- General Idea:
 - "The value of the *j*th feature contributed ... to the prediction of this particular instance compared to the average prediction for the dataset."

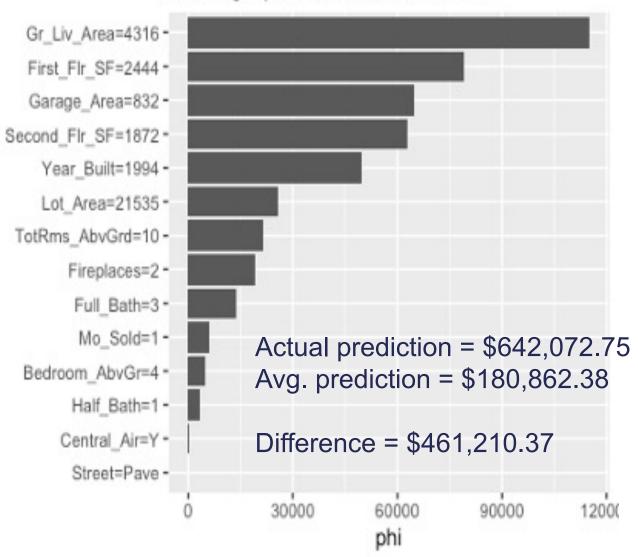
Actual prediction: 642072.75 Average prediction: 180862.38

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 - In other words... how do I get from the average prediction to the actual prediction and WHY!



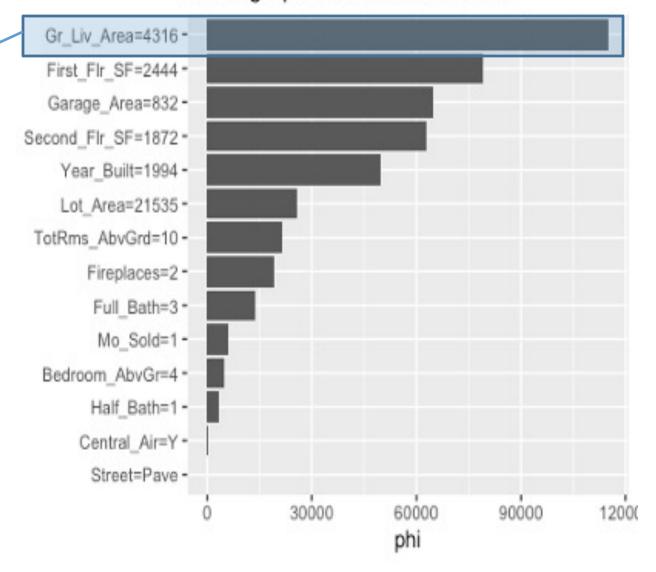
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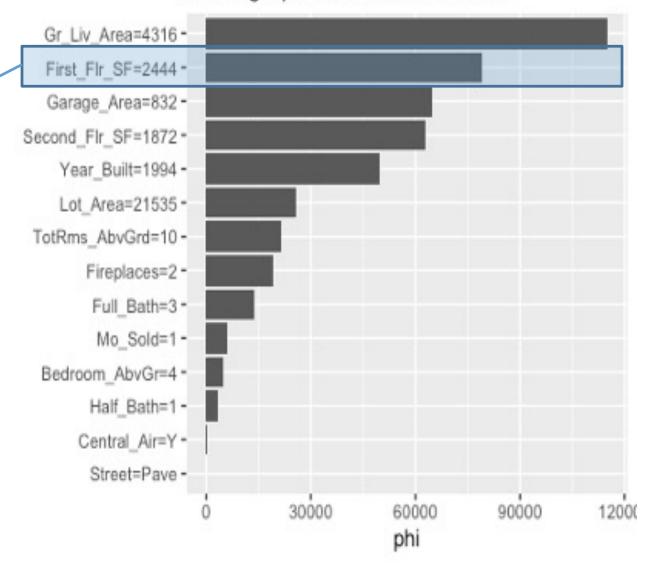
Actual prediction: 642072.75 Average prediction: 180862.38

• Difference = \$461.210.37 = \$114,137.72 +

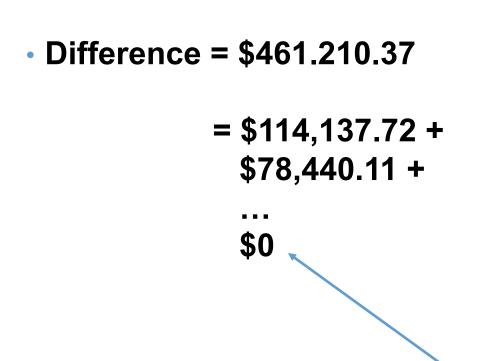


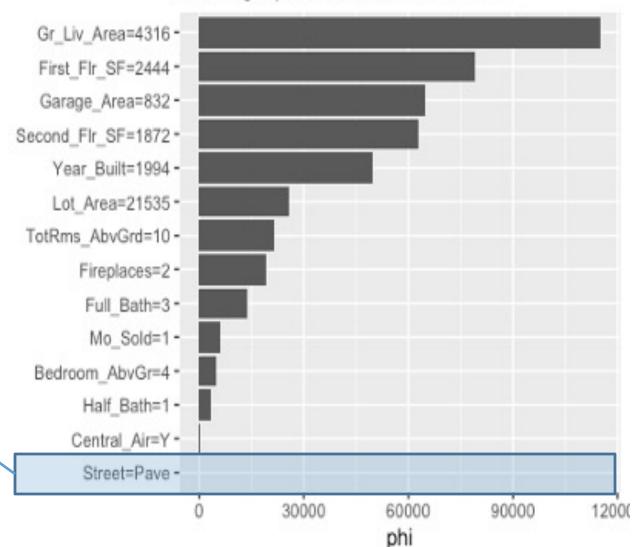
Actual prediction: 642072.75 Average prediction: 180862.38

Difference = \$461.210.37
= \$114,137.72 + \$78,440.11 +



Actual prediction: 642072.75 Average prediction: 180862.38

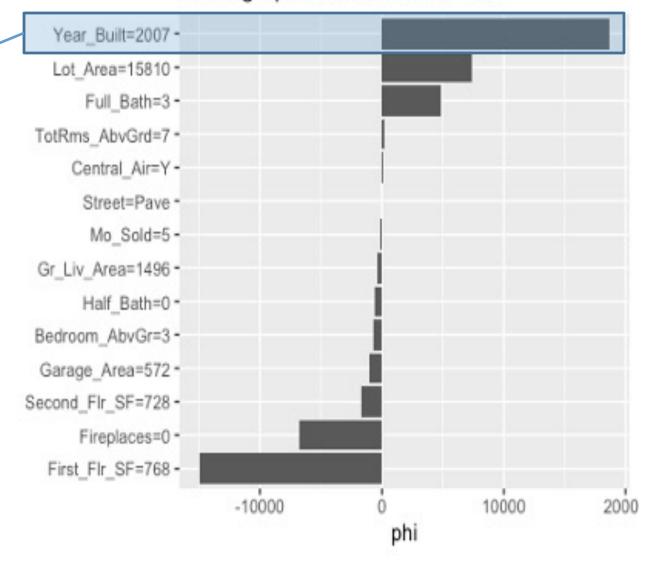




Shapley Values (obs. 1000)

Actual prediction: 187935.20 Average prediction: 180862.38

• Difference = \$7,072.82 = \$21,206.09 + \$6,081.23 + ... -\$14,590.45



- Neat idea, but how does it work? Game theory!
- Shapley (1953) assigned a payout value for players depending on their contribution to the total payout across the coalition (think team).
 - In other words, you are a team of players (say basketball)...
 - You win some money at a local tournament...
 - Do you split it evenly? Maybe...
 - Or you split it based on contribution! Star player gets most, next best player gets second highest, and so on...
- That is the idea of a Shapley value in game theory!

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- That is the idea of a Shapley value in game theory!
- The Shapley value in machine learning is the average marginal contribution of a feature (teammate) across all possible coalitions of variables (collections of teammates).

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Advantages

- **Efficiency** variable contributions must sum to the difference of prediction for point of interest compared to the average.
- **Symmetry** contributions of two variables (j and k) should be the same if they contribute equally to all possible combinations of variables (coalitions).
- Dummy a variable that does not change the predicted value, for any combination of variables, should have a Shapley value of 0.
- Additivity for a forest of trees, the Shapley value of the forest for a given observation should be the average of the Shapley values for each tree at that given point.

Disadvantages

- Some people look at distributions of all Shapley values across a variable to measure "overall impact" of a variable.
- BE VERY CAREFUL OF THIS!
- Shapley values were never designed for this as they are created for local interpretations, not global ones.
- Only thing you might be able to do is to see if all Shapley values are positive or negative.

```
Actual prediction: 642072.75
Average prediction: 180862.38
```

