NEURAL NETWORK MODELS

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NEURAL NETWORK STRUCTURE

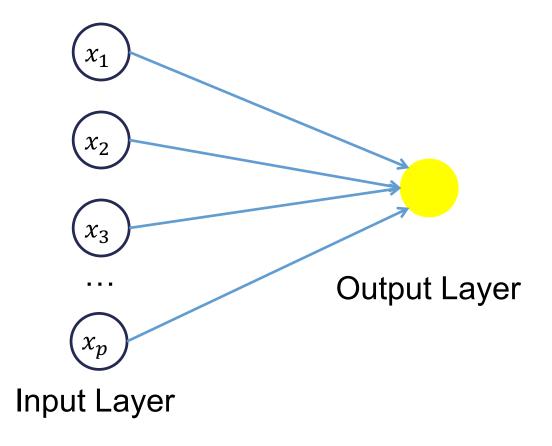
Neural Networks Overview

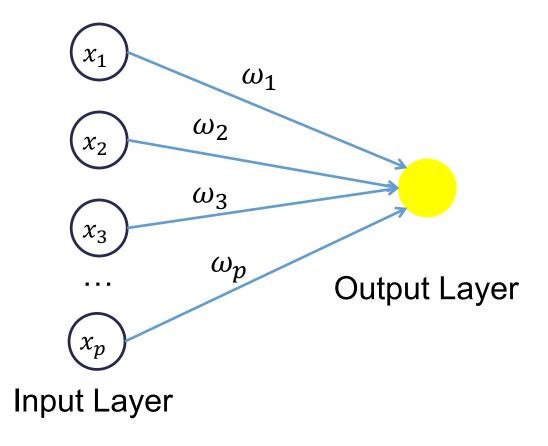
- Neural networks are considered "black-box" models.
 - Complex and hard to decipher relationships between variables and the target.
- Potential to model very complicated patterns in datasets both for continuous and categorical targets.

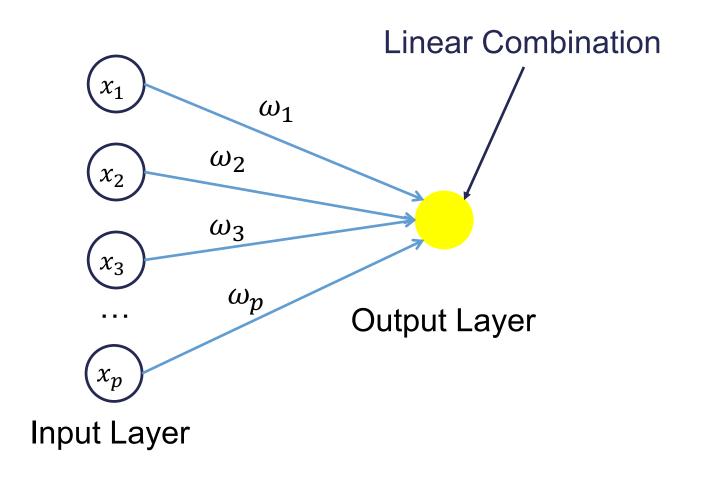
Neural Networks History

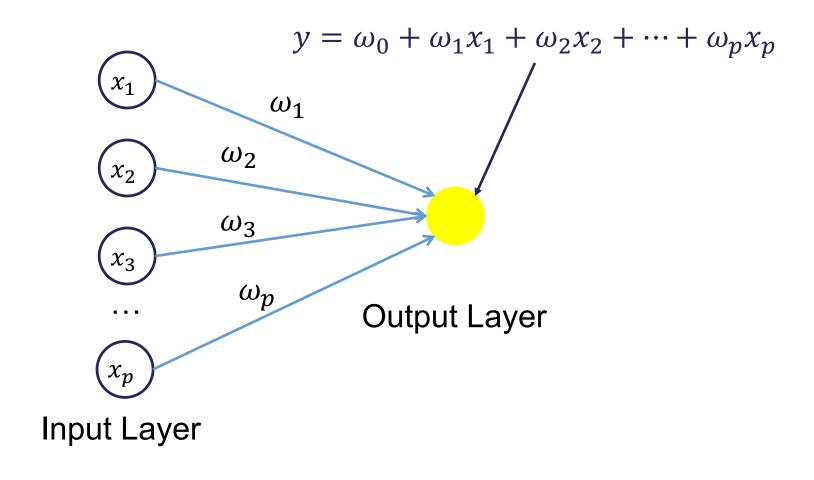
- Concept was well received in 1980's.
- Didn't live up to expectations... ☺
- Support Vector Machines (SVM's) overtook neural networks in the early 2000's as the popular "black-box" model.
- Revitalized with the growth in image and visual recognition problems.
 - Tons of research
 - "Deep Learning" → Recurrent NN, Convolutional NN, Feedforward NN, etc.

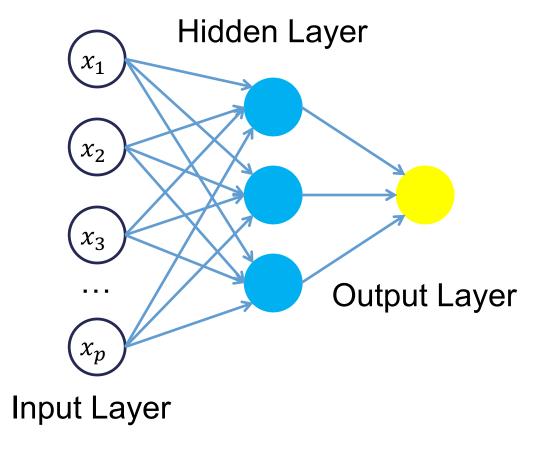
- They are organized in a network of neurons through layers.
- The input variables are considered the neurons on the bottom layer.
- The output variable is considered the neuron on the top layer.
- The layers in between, called hidden layers, transform the input variables through non-linear methods to try and best model the output variable.

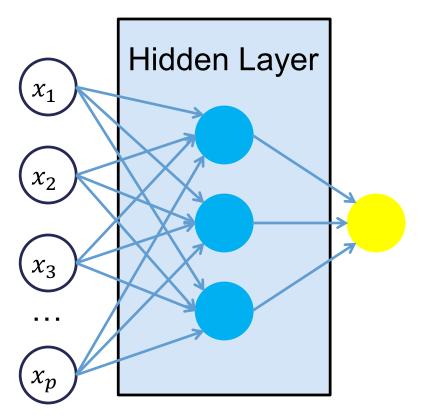




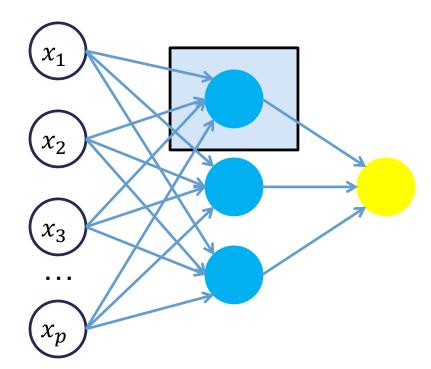


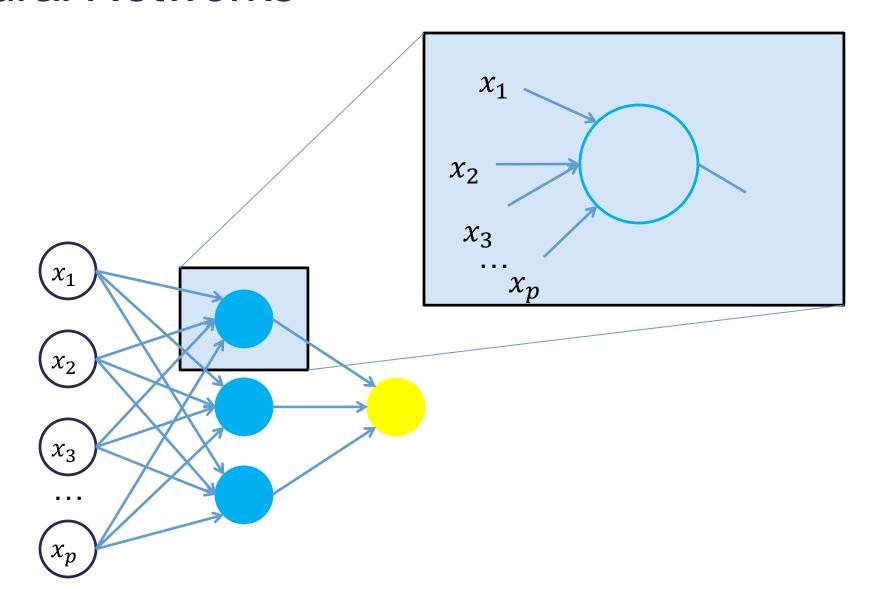


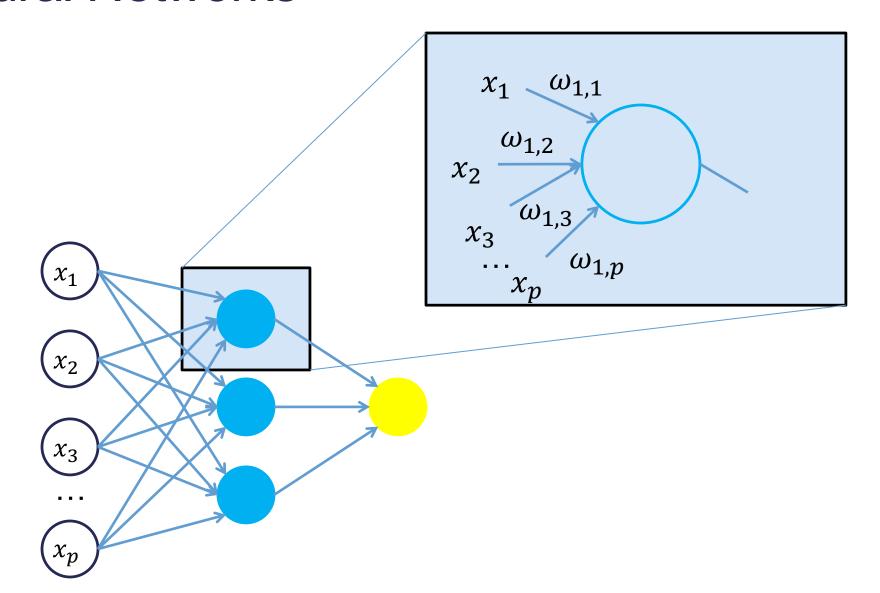


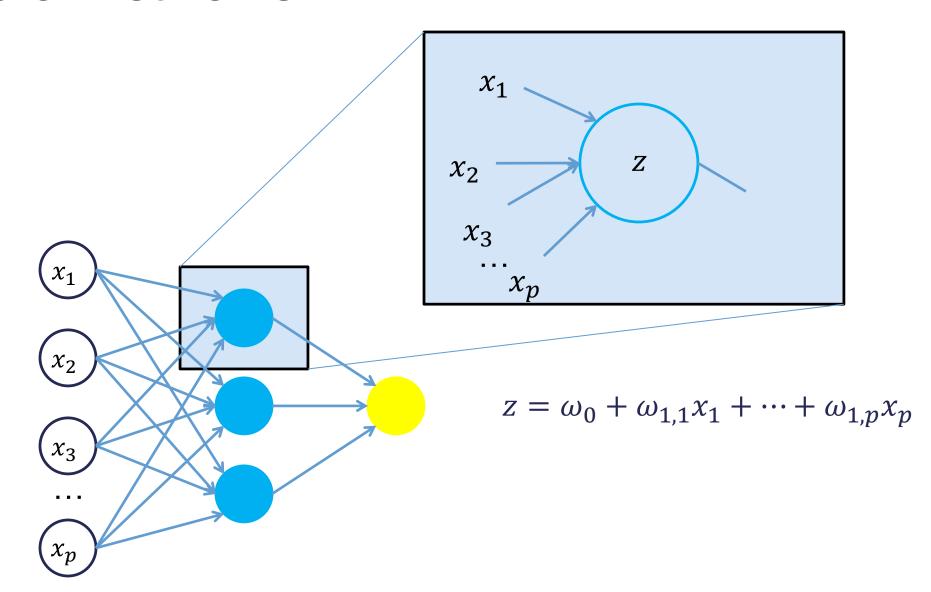


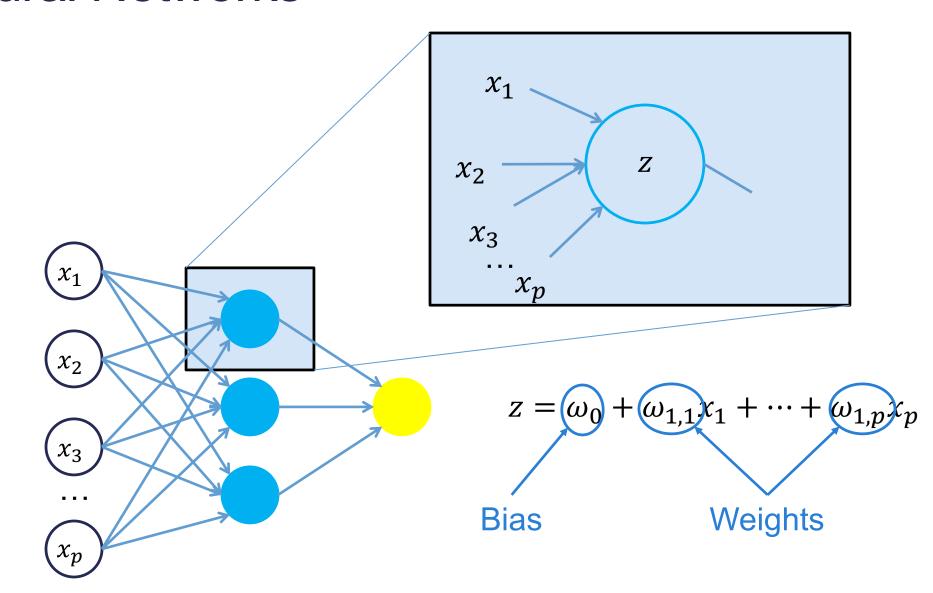
All of the nonlinearities and complication of the variables get added to the model here.

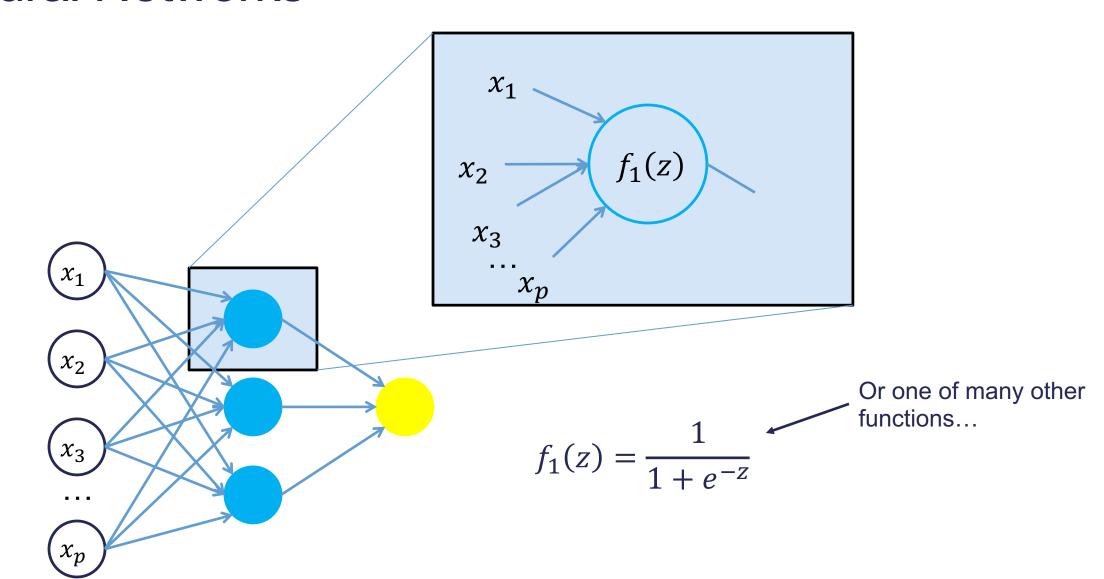


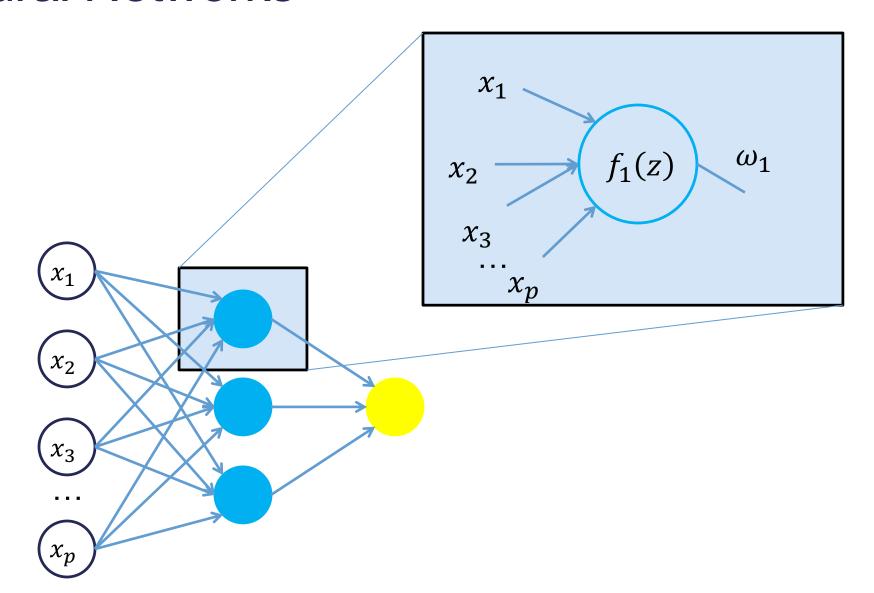


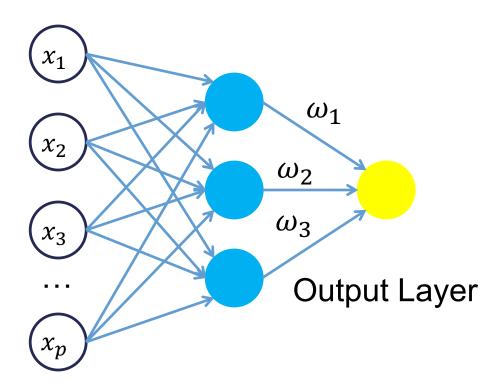


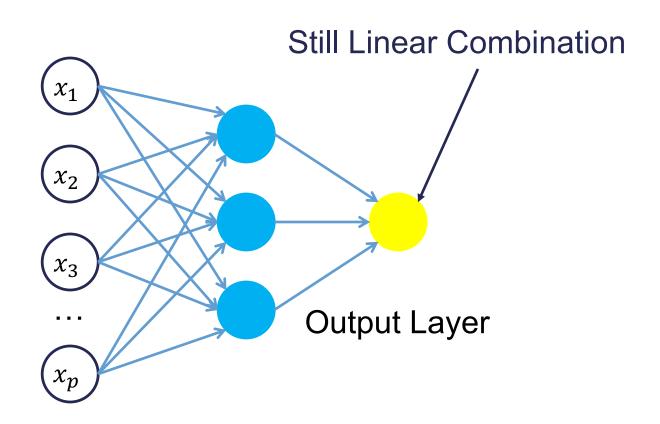


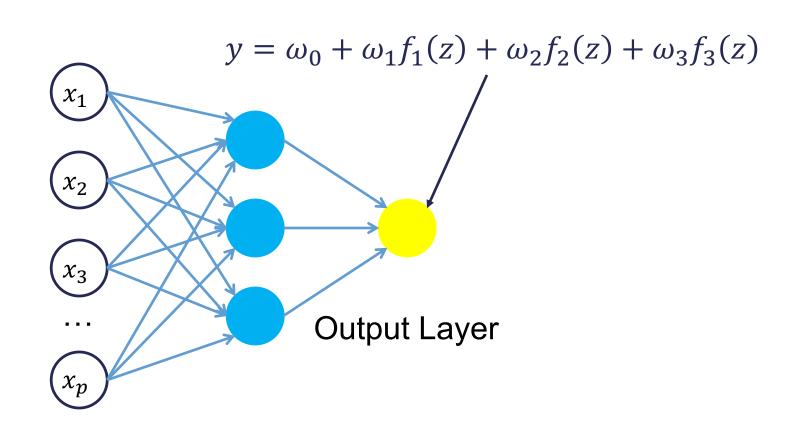












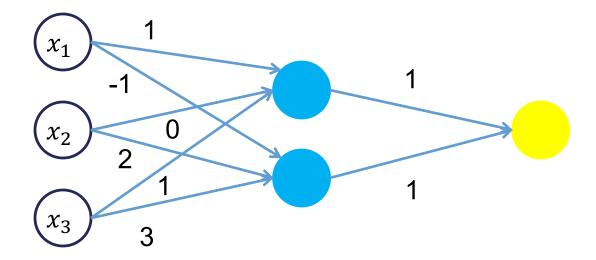


BACKPROPAGATION

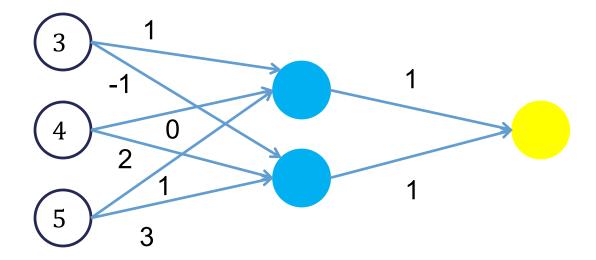
Backpropagation Algorithm

- Forward phase:
 - 1. Start with some initial weights (often random).
 - Calculations passed through network.
 - 3. Predicted value computed.
- Backward phase:
 - 1. Predicted value compared with actual value (error).
 - 2. Work backwards through network to adjust weights to make the prediction better.
- Repeat until some notion of convergence!

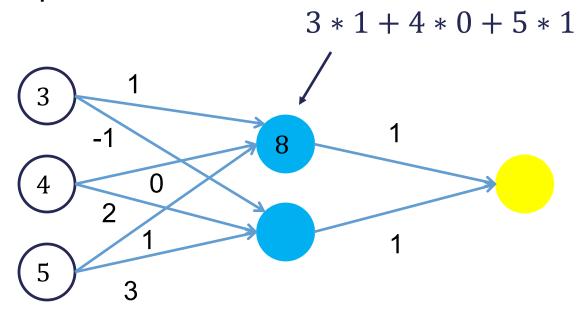
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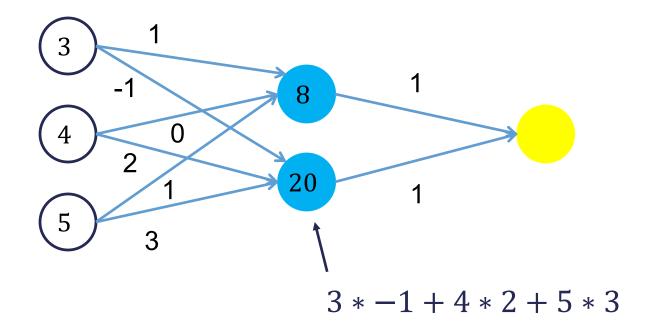
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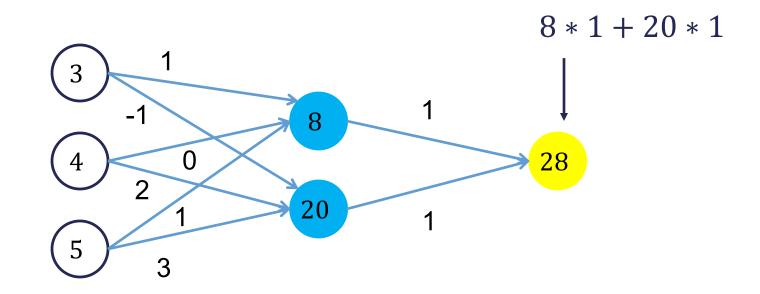
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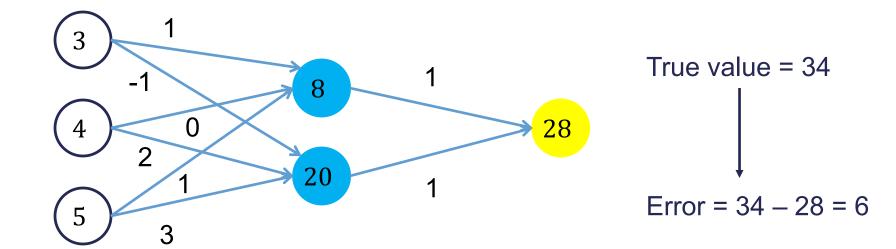


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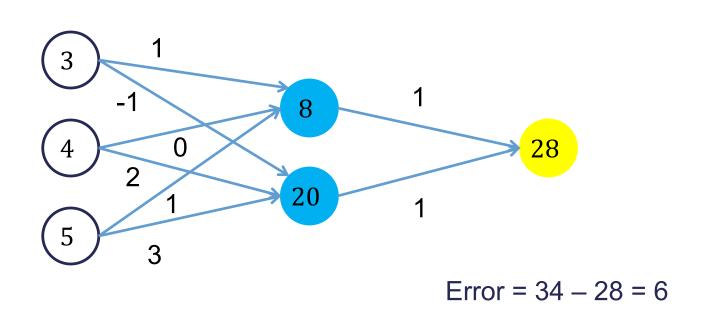
Backward Phase

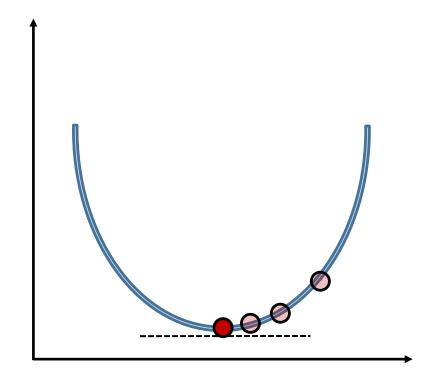
- 1. Predicted value compared with actual value (error).
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Backward Phase

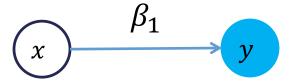
- 1. Predicted value compared with actual value (error).
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Easy Example

- Let's work through a very, very, very, very watered-down example...
- You know that you have $y = \beta_1 x$.
- You know that x = 5 and y = 20, but you don't know division...
- Use backpropagation to solve what β_1 is.



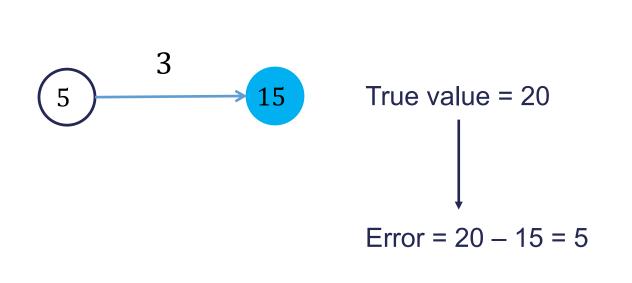
Easy Example – Forward

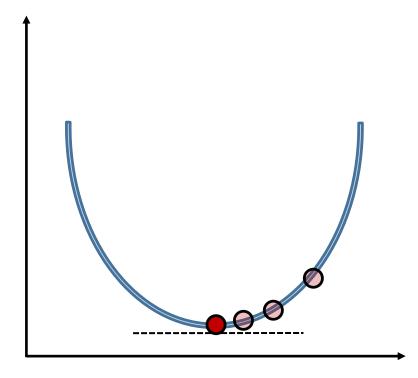
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Easy Example – Backward

- 1. Predicted value compared with actual value (error).
- 2. Work backwards through network to adjust weights to make the prediction better. BUT HOW?!?!?!



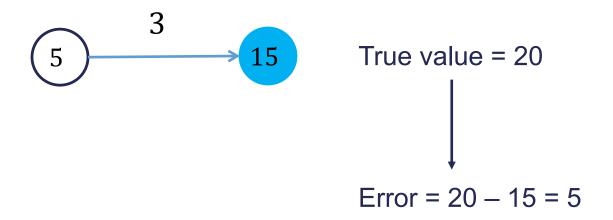


Easy Example – Backward

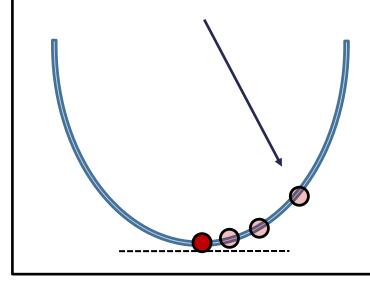
Predicted value compared with actual value (error).

2. Work backwards through network to adjust weights to make the prediction

better. BUT HOW?!?!?!?!



Slope of error curve (SSE) is derivative of SSE which is 2 times sum of error.

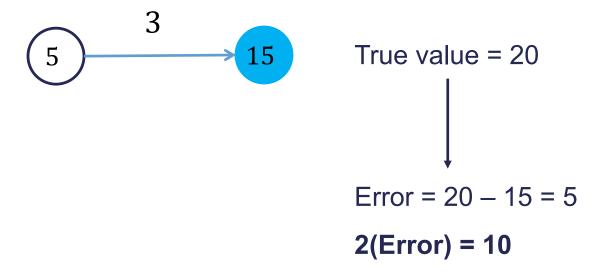


Easy Example – Backward

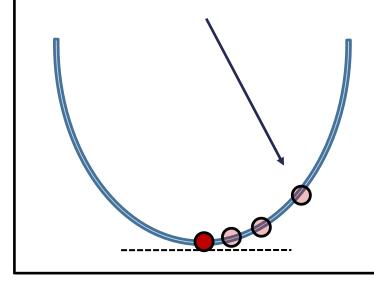
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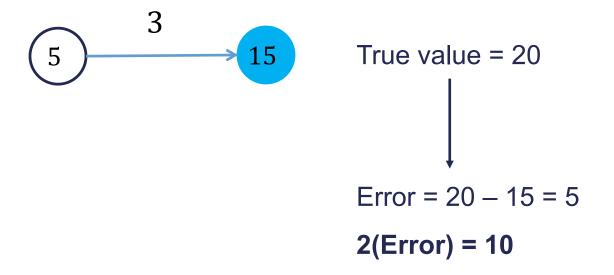
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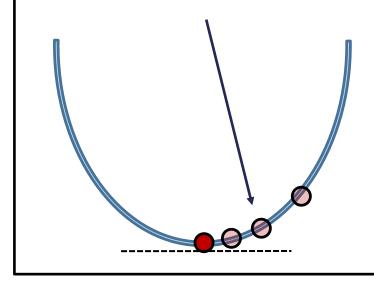
1. Predicted value compared with actual value (error).

2. Work backwards through network to adjust weights to make the prediction

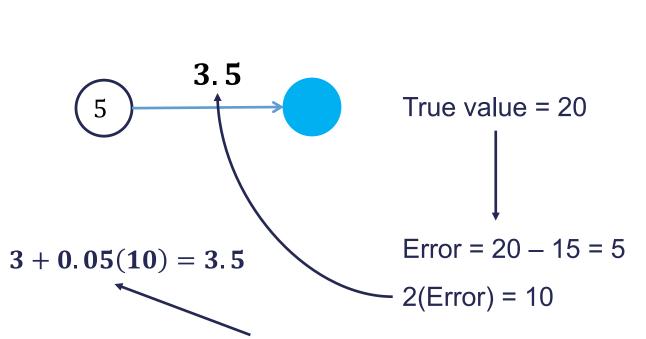
better. BUT HOW?!?!?!?!

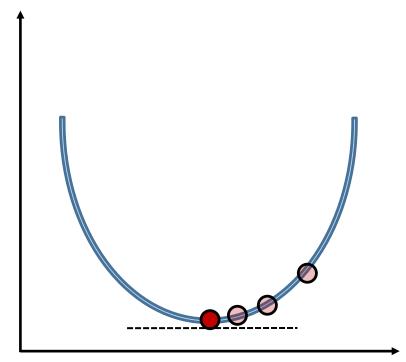


Need to adjust original guess of β_1 (was 3) to new value to get new estimate...



- Predicted value compared with actual value (error).
- 2. Work backwards through network to adjust weights to make the prediction better. BUT HOW?!?!?!?!

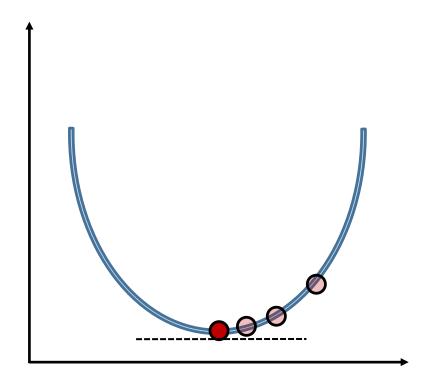




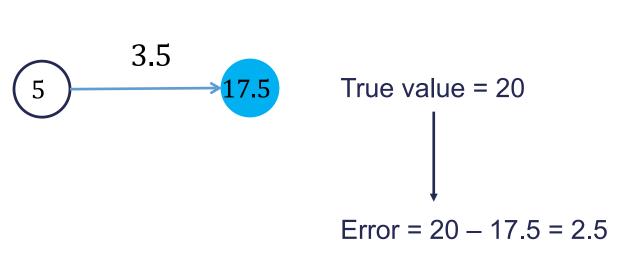
Multiply slope of error curve by **learning rate** and add to original estimate...

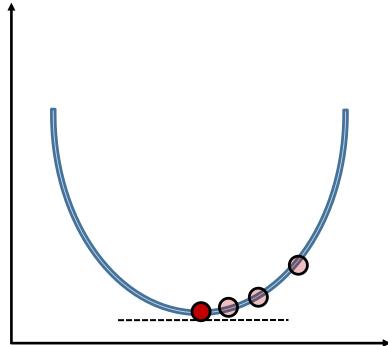
- 1. Predicted value compared with actual value (error).
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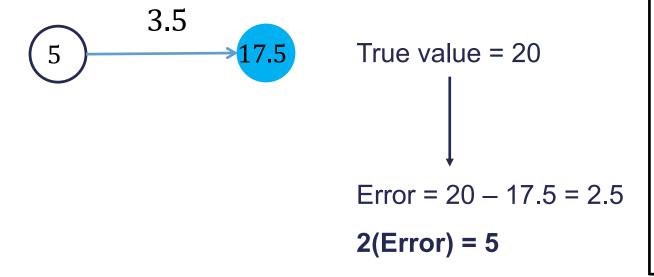




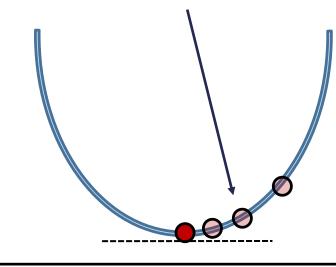
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2. Work backwards through network to adjust weights to make the prediction

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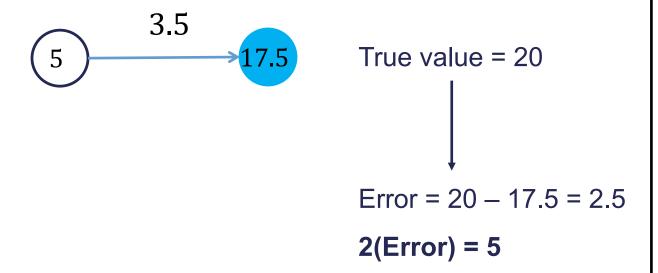
Slope of error curve (SSE) is derivative of SSE which is 2 times sum of error.



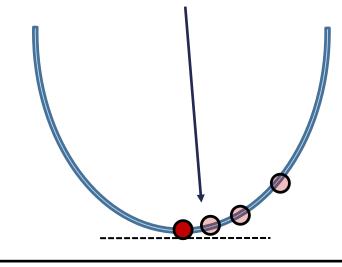
Predicted value compared with actual value (error).

2. Work backwards through network to adjust weights to make the prediction

better. BUT HOW?!?!?!?!



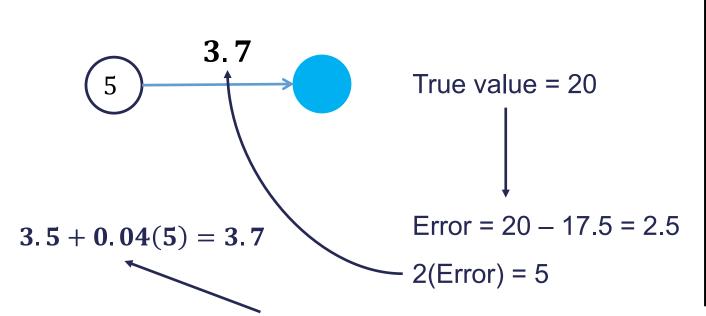
Need to adjust original guess of β_1 (3.5) to new value to get new estimate...



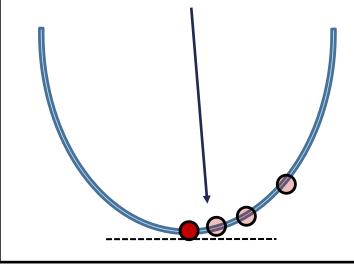
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2. Work backwards through network to adjust weights to make the prediction

better. BUT HOW?!?!?!?!

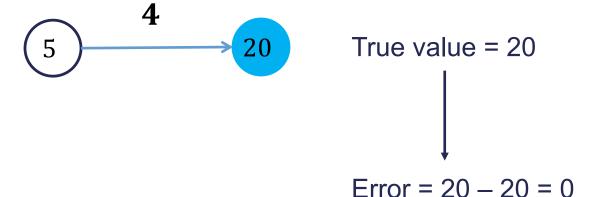


New value of learning rate should be **smaller** (taking smaller step)

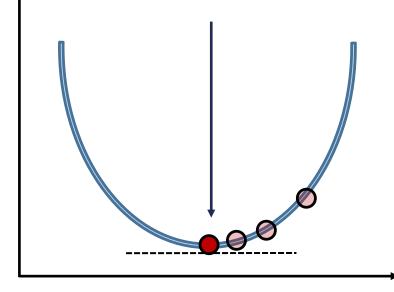


Multiply slope of error curve by **learning rate** and add to original estimate...

- 1. Predicted value compared with actual value (error).
- Work backwards through network to adjust weights to make the prediction better.
- 3. Repeat, repeat, repeat,...



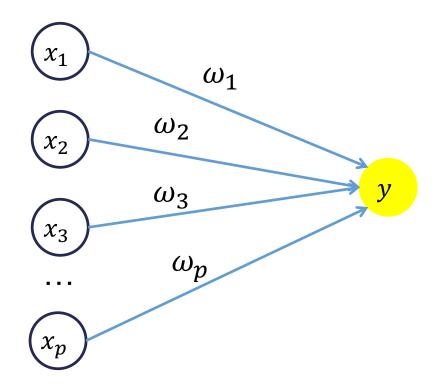
Continue process until you reach some level of "convergence".



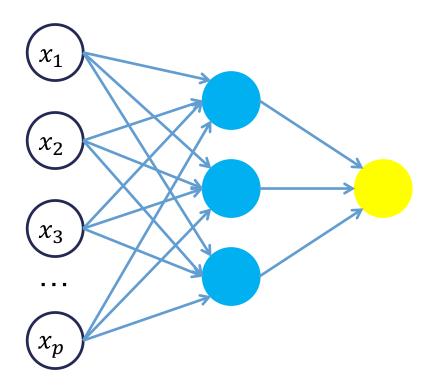
- Multiple values of x and y to optimize across, not just one observation...
 - Aggregate errors across all observations (SSE).



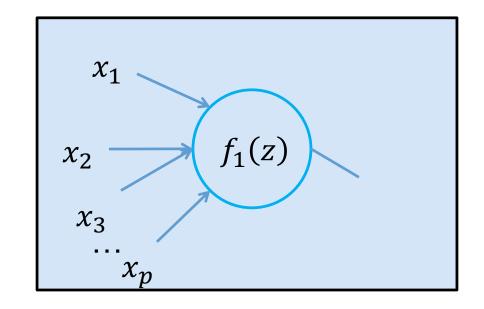
- Multiple variables instead of just one.
 - More than one weight you must now optimize at once.



 Hidden layers add complexity to the model since one change in slope impacts many different nodes instead of one.



 Nonlinearities inside the hidden nodes make the calculus harder since the predictor variables are NOT just related to the slope of the SSE function, but the combined (think calculus chain rule) slope of the error loss function with the nonlinear (logistic function) relationship...



$$f_1(z) = \frac{1}{1 + e^{-z}}$$

Backpropagation Algorithm

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- Backward phase:
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- Repeat until some notion of convergence! MATH IS HARD!!!



FITTING NEURAL NETWORK IN R

Ames Data

```
set.seed(4321)
training <- ames %>% sample_frac(0.7)
testing <- anti_join(ames, training, by = 'id')</pre>
training <- training %>%
  select(Sale Price,
         Bedroom AbvGr,
         Year_Built,
         Mo_Sold,
         Lot Area,
         Street,
         Central_Air,
         First_Flr_SF,
         Second_Flr_SF,
         Full Bath,
         Half Bath,
         Fireplaces,
         Garage Area,
         Gr_Liv_Area,
         TotRms_AbvGrd)
```

Standardization

- Neural networks work best when input data are scaled (but NOT required) to a narrow range around 0.
- For bell-shaped data, statistical z-scores standardization work:

$$z = \frac{x - \bar{x}}{S_{\chi}}$$

• For severely asymmetric data, midrange standardization works better:

$$\frac{x - \operatorname{midrange}(x)}{0.5 \times \operatorname{range}(x)} = \frac{x - \frac{(\max(x) + \min(x))}{2}}{0.5 \times (\max(x) - \min(x))}$$

Standardization

```
training <- training %>%
  mutate(s SalePrice = scale(Sale Price),
         s Bedroom AbvGr = scale(Bedroom AbvGr),
         s Year Built = scale(Year Built),
         s Mo Sold = scale(Mo Sold),
         s Lot Area = scale(Lot Area),
         s First Flr SF = scale(First Flr SF),
         s Second Flr SF = scale(Second Flr SF),
         s Garage Area = scale(Garage Area),
         s Gr Liv Area = scale(Gr Liv Area),
         s TotRms AbvGrd = scale(TotRms AbvGrd))
training$Full Bath <- as.factor(training$Full Bath)</pre>
training$Half Bath <- as.factor(training$Half Bath)</pre>
training$Fireplaces <- as.factor(training$Fireplaces)</pre>
```

Neural Network

```
set.seed(12345)
nn.ames <- nnet(Sale_Price ~</pre>
                  s Bedroom AbvGr +
                  s_Year_Built +
                  s_Mo_Sold +
                  s_Lot_Area +
                  s_First_Flr_SF +
                  s Second Flr SF +
                  s_Garage_Area +
                  s Gr Liv Area +
                  s_TotRms_AbvGrd +
                  Street +
                  Central Air +
                  Full_Bath +
                  Half_Bath +
                  Fireplaces
                  , data = training, size = 5, linout = TRUE)
```

Optimize Number of Hidden Nodes and Decay

```
tune grid <- expand.grid(</pre>
  .size = c(3, 4, 5, 6, 7),
  .decay = c(0, 0.5, 1)
set.seed(12345)
nn.ames.caret <- train(Sale Price ~</pre>
                          s Bedroom AbvGr + s Year Built + s Mo Sold + s Lot Area + s First Flr SF +
                          s_Second_Flr_SF + s_Garage_Area + s_Gr_Liv_Area + s_TotRms_AbvGrd + Street +
                         Central_Air + Full Bath + Half Bath + Fireplaces
                        , data = training,
                        method = "nnet",
                        tuneGrid = tune grid,
                        trControl = trainControl(method = 'cv', number = 10),
                        trace = FALSE, linout = TRUE)
nn.ames.caret$bestTune
##
      size decay
## 12
```

Optimize Number of Hidden Nodes and Decay

```
tune grid <- expand.grid(</pre>
                                             Size = Number of hidden nodes
  .size = c(3, 4, 5, 6, 7),
                                             Decay = Regularization parameter to prevent overfitting
  .decay = c(0, 0.5, 1)
set.seed(12345)
nn.ames.caret <- train(Sale Price ~</pre>
                         s Bedroom AbvGr + s Year Built + s Mo Sold + s Lot Area + s First Flr SF +
                         s Second Flr SF + s Garage Area + s Gr Liv Area + s TotRms AbvGrd + Street +
                         Central_Air + Full Bath + Half Bath + Fireplaces
                       , data = training,
                        method = "nnet",
                        tuneGrid = tune grid,
                        trControl = trainControl(method = 'cv', number = 10),
                        trace = FALSE, linout = TRUE)
nn.ames.caret$bestTune
##
      size decay
## 12
```

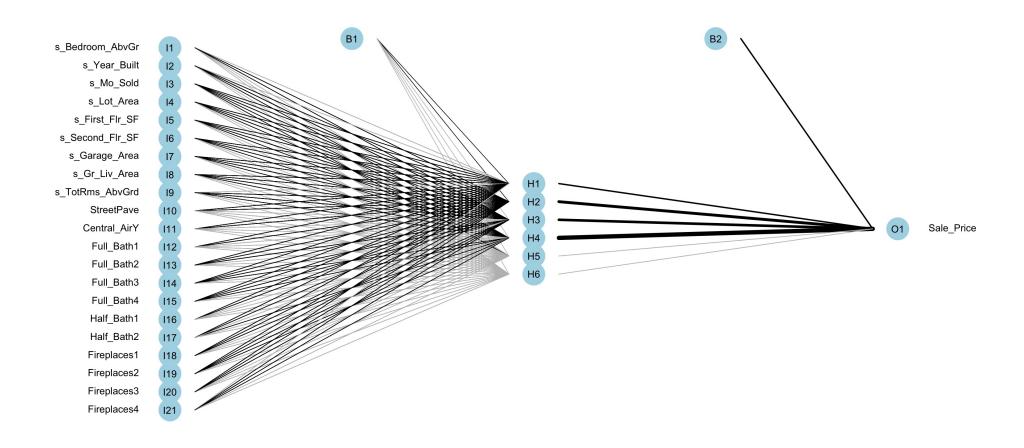
Optimize Number of Hidden Nodes and Decay

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  .decay = c(0, 0.5, 1)
set.seed(12345)
nn.ames.caret <- train(Sale Price ~</pre>
                         s Bedroom AbvGr + s Year Built + s Mo Sold + s Lot Area + s First Flr SF +
                         s Second Flr SF + s Garage Area + s Gr Liv Area + s TotRms AbvGrd + Street +
                         Central Air + Full Bath + Half Bath + Fireplaces
                       , data = training,
                        method = "nnet",
                        tuneGrid = tune grid,
                        trControl = trainControl(method = 'cv', number = 10),
                        trace = FALSE, linout = TRUE)
nn.ames.caret$bestTune
                                              Size = 6 hidden nodes
##
      size decay
                                              Decay = 1 for penalty
## 12
```

Optimized Neural Network

```
set.seed(12345)
nn.ames <- nnet(Sale Price ~</pre>
                  s Bedroom AbvGr +
                  s Year Built +
                  s_Mo_Sold +
                  s Lot Area +
                  s First Flr SF +
                  s Second Flr SF +
                                                                     Size = 6 hidden nodes
                  s Garage Area +
                  s Gr Liv Area +
                                                                     Decay = 1 for penalty
                  s_TotRms_AbvGrd +
                  Street +
                  Central Air +
                  Full Bath +
                  Half Bath +
                  Fireplaces
                , data = training, size = 6, decay = 1, linout = TRUE)
plotnet(nn.ames)
```

Neural Network Plot





VARIABLE SELECTION

Variable Selection

- Neural networks typically do NOT care about variable selection.
- All variables are used by default in a complicated and mixed way.
- IF you want to do variable selection, you can examine the weights for each variable → if all weights are low, then MAYBE delete.
- Hinton diagram is one way to visualize these weights IF there are a small number of variables.

Hinton Diagram

```
nn_weights <- matrix(data = nn.ames$wts[1:126], ncol = 6, nrow = 22)
rownames(nn_weights) <- c("bias", nn.ames$coefnames)
colnames(nn_weights) <- c("h1", "h2", "h3", "h4", "h5", "h6")

ggplot(melt(nn_weights), aes(x=Var1, y=Var2, size=abs(value), color=as.factor(sign(value)))) +
    geom_point(shape = 15) +
    scale_size_area(max_size = 40) +
    labs(x = "", y = "", title = "Hinton Diagram of NN Weights") +
    theme_bw()</pre>
```

Hinton Diagram





SUMMARY

Neural Network Summary

Advantages

- Used for categorical / numerical target variables.
- Capable of modeling complex nonlinear patterns.
- No assumptions about the data distributions.

Disadvantages

- No insights for variable importance.
- Extremely computationally intensive (VERY SLOW TO TRAIN).
- Tuning of parameters.
- Prone to overfitting training data.

