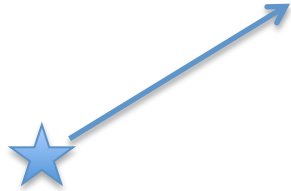


Subset Selection: Using R!

Statistical Data Mining
Rachael Hageman Blair

Specialized Packages (selected)



Supervised Learning	
Task	Select Packages
Linear Models	glm
Discriminant Analysis	stats
Shrinkage	lars
Subset Selection	leaps
Principal Components	stats
Partial Least Squares	pls
Classification and Regression Trees	tree, rpart
Bootstrap	boot
Random Forest	randomForest

Unsupervised Learning	
Task	Select Packages
Association Rules	arules
Clustering	cluster, pam
Recommender Systems	recommenderlab
Hierarchical Random Graphs	igraph
Graphical Models	Rhugin, Rgraphviz, gRim, gRain
Graphical Lasso	glasso
Self Organizing Maps	kohonen

Outline

- Motivation
- Basics on Subset Selection
- A “Simple Example”: - prostate cancer
perform exhaustive subset selection:
R-tasks: load data, subset data, perform subset selection, examine results, plot results, write a for-loop.
- Basics on Model Selection
- A “Simple Example” continued – prostate cancer
R-tasks: format model matrix, predict response, write a function, call a function, write a double for-loop.

Motivation

In a regression setting consider the linear model:

$$Y = \beta_0 + \beta_1 X_1 + \cdots + \beta_p X_p + \varepsilon$$

Used to describe the relationship between a response $Y \in \Re^N$ and a set of variables: $\{X_1, X_2, \dots, X_p\}$.

✓ Great Interpretability (despite simplicity)

This may not be desirable..... Why?

Motivation

- **Predictive Accuracy:**
a smaller set of predictors may
yield a more accurate model.
Especially when $p > N$

Motivation



OCCAM'S RAZOR

"WHEN FACED WITH TWO POSSIBLE EXPLANATIONS, THE SIMPLER OF THE TWO IS THE ONE MOST LIKELY TO BE TRUE."

- **Predictive Accuracy:**
a smaller set of predictors may yield a more accurate model.
Especially when $p > N$
- **Model Interpretation:**
by removing irrelevant or redundant predictors, we can obtain a model that is easier to interpret.

(Feature selection)

Three basic approaches

1. **Subset Selection:** Selection of a “best subset” of variables, identified by fitting several nested models and assessing performance.
2. **Shrinkage:** (aka Penalized Regression) Fit a model over all of the variables, and shrink the regression coefficients (for some penalties we can shrink to 0).
3. **Dimension Reduction:** Project the data into lower-dimensional subspace. Use the dimensions of this subspace as the new set of predictors.

Subset Selection: Exhaustive

Exhaustive Subset Selection(best subset selection).

- Exactly what it sound like (exhausting, especially for large p).

Algorithm 6.1 *Best subset selection*

1. Let \mathcal{M}_0 denote the *null model*, which contains no predictors. This model simply predicts the sample mean for each observation.
 2. For $k = 1, 2, \dots, p$:
 - (a) Fit all $\binom{p}{k}$ models that contain exactly k predictors.
 - (b) Pick the best among these $\binom{p}{k}$ models, and call it \mathcal{M}_k . Here *best* is defined as having the smallest RSS, or equivalently largest R^2 .
 3. Select a single best model from among $\mathcal{M}_0, \dots, \mathcal{M}_p$ using cross-validated prediction error, C_p (AIC), BIC, or adjusted R^2 .
-

Subset Selection

Best subset selection - Leaps and Bounds algorithm:

- Find the best subset of size $k \in \{0, 1, 2, \dots, p\}$, which minimizes the RSS.
- Computationally intensive, works well for $p \leq 30$.
- Choice of k is somewhat subjective.

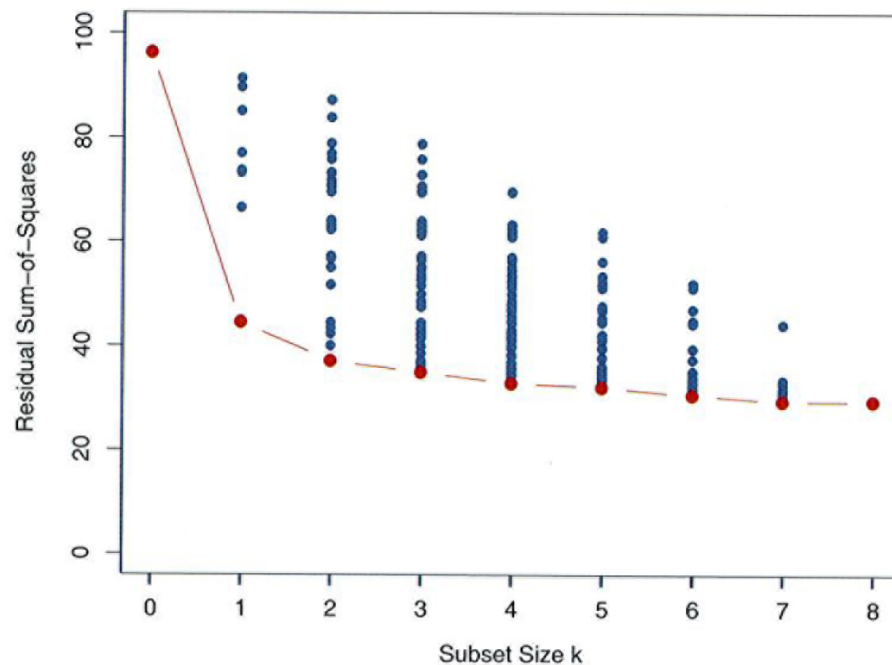


FIGURE 3.5. All possible subset models for the prostate cancer example. At each subset size is shown the residual sum-of-squares for each model of that size.

Model Selection Issue

206 6. Linear Model Selection and Regularization

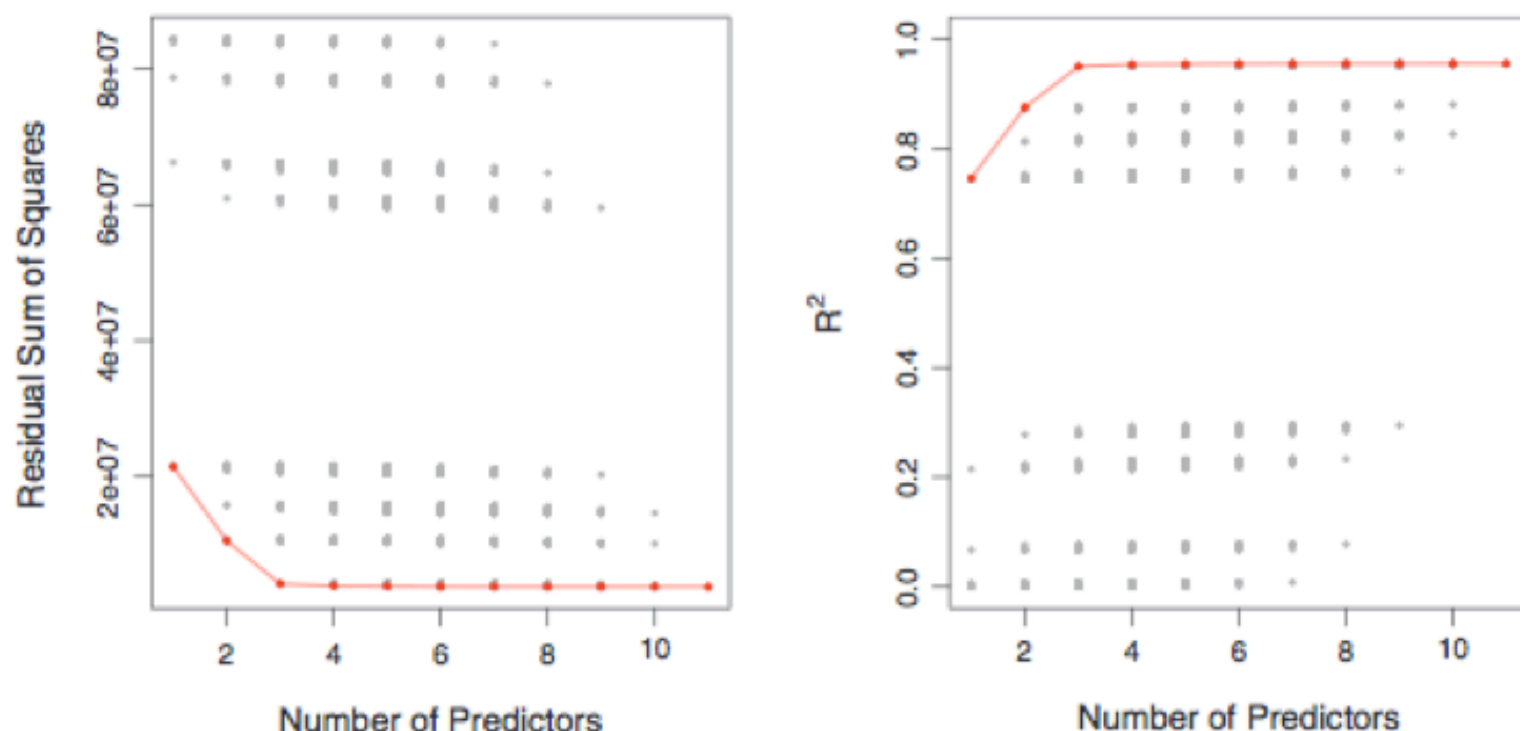


FIGURE 6.1. For each possible model containing a subset of the ten predictors in the **Credit** data set, the RSS and R^2 are displayed. The red frontier tracks the best model for a given number of predictors, according to RSS and R^2 . Though

Subset Selection

Forward Stepwise Selection:

- A greedy algorithm which produces a nested sequence of models.
- Starts with the intercept, and progressively adds to the model to find the best fit for k predictors.
- Searches for the next step in the path in a “smart way”.
- Still need to specify k .
- May not be optimal.... Conditional!

Subset Selection

Forward Stepwise Selection:

- A greedy algorithm which produces a nested sequence of models.
- Starts with the intercept, and progressively adds to the model to find the best fit for k predictors.
- Searches for the next step in the path in a “smart way”.
- Still need to specify k .
- May not be optimal.... Conditional!

# Variables	Best subset	Forward stepwise
One	rating	rating
Two	rating, income	rating, income
Three	rating, income, student	rating, income, student
Four	cards, income student, limit	rating, income, student, limit

TABLE 6.1. *The first four selected models for best subset selection and forward stepwise selection on the **Credit** data set. The first three models are identical but the fourth models differ.*

Subset Selection: Forward Stepwise

Algorithm 6.2 *Forward stepwise selection*

1. Let \mathcal{M}_0 denote the *null* model, which contains no predictors.
 2. For $k = 0, \dots, p - 1$:
 - (a) Consider all $p - k$ models that augment the predictors in \mathcal{M}_k with one additional predictor.
 - (b) Choose the *best* among these $p - k$ models, and call it \mathcal{M}_{k+1} . Here *best* is defined as having smallest RSS or highest R^2 .
 3. Select a single best model from among $\mathcal{M}_0, \dots, \mathcal{M}_p$ using cross-validated prediction error, C_p (AIC), BIC, or adjusted R^2 .
-

Subset Selection : Forwards Stepwise

Backwards Stepwise Selection:

- Starts with the full model, and sequentially deletes the predictor with the least impact.
- Searches for the next step in the path in a “smart way”.

Subset Selection: Backwards Stepwise

Algorithm 6.3 *Backward stepwise selection*

1. Let \mathcal{M}_p denote the *full* model, which contains all p predictors.
 2. For $k = p, p - 1, \dots, 1$:
 - (a) Consider all k models that contain all but one of the predictors in \mathcal{M}_k , for a total of $k - 1$ predictors.
 - (b) Choose the *best* among these k models, and call it \mathcal{M}_{k-1} . Here *best* is defined as having smallest RSS or highest R^2 .
 3. Select a single best model from among $\mathcal{M}_0, \dots, \mathcal{M}_p$ using cross-validated prediction error, C_p (AIC), BIC, or adjusted R^2 .
-

Subset Selection: Backwards Stepwise

Backwards Stepwise Selection:

- Starts with the full model, and sequentially deletes the predictor with the least impact.
- Searches for the next step in the path in a “smart way”.

Subset Selection: Forwards Stagewise

Forwards Stagewise:

- Better for higher dimensional problems, $N < p$.
- Relates to the LASSO path.
- Works on correlation with residual in a sequential way.
- Often dismissed as being “slow fitting”.

Incremental Forward stagewise regression aka
BOOSTING for linear models.

Subset Selection: Forwards Stagewise

ALGORITHM 1. Incremental Forward Stagewise Regression: FS_ϵ

1. Start with $\mathbf{r} = \mathbf{y} - \bar{\mathbf{y}}$, $\beta_1, \beta_2, \dots, \beta_p = 0$.
 2. Find the predictor \mathbf{x}_j most correlated with \mathbf{r} .
 3. Update $\beta_j \leftarrow \beta_j + \delta_j$, where $\delta_j = \epsilon \cdot \text{sign}[\text{corr}(\mathbf{r}, \mathbf{x}_j)]$;
 4. Update $\mathbf{r} \leftarrow \mathbf{r} - \delta_j \mathbf{x}_j$, and repeat steps 2 and 3 until no predictor has any correlation with \mathbf{r} .
-



Track for stopping

Subset Selection

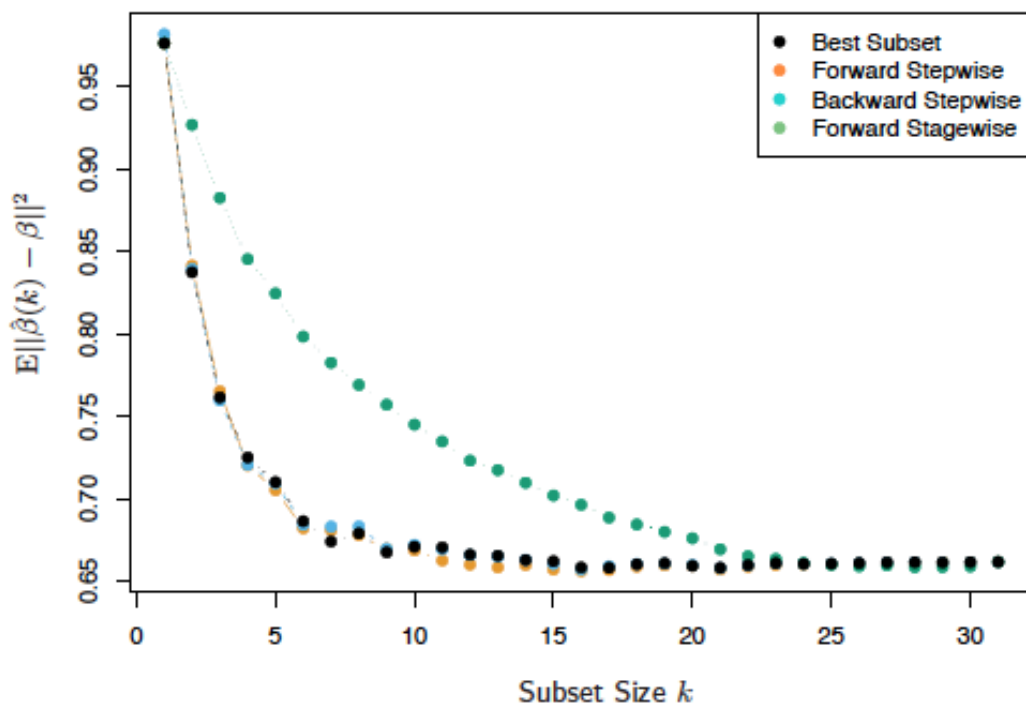


FIGURE 3.6. Comparison of four subset-selection techniques on a simulated linear regression problem $Y = X^T \beta + \varepsilon$. There are $N = 300$ observations on $p = 31$ standard Gaussian variables, with pairwise correlations all equal to 0.85. For 10 of the variables, the coefficients are drawn at random from a $N(0, 0.4)$ distribution; the rest are zero. The noise $\varepsilon \sim N(0, 6.25)$, resulting in a signal-to-noise ratio of 0.64. Results are averaged over 50 simulations. Shown is the mean-squared error of the estimated coefficient $\hat{\beta}(k)$ at each step from the true β .

Simple Example

Prostate Cancer

Input Variable:

Log cancer volume (lcavol)

Log prostate weight (lweight)

Log amt of benign (lbph)

Seminal invasion (svi)

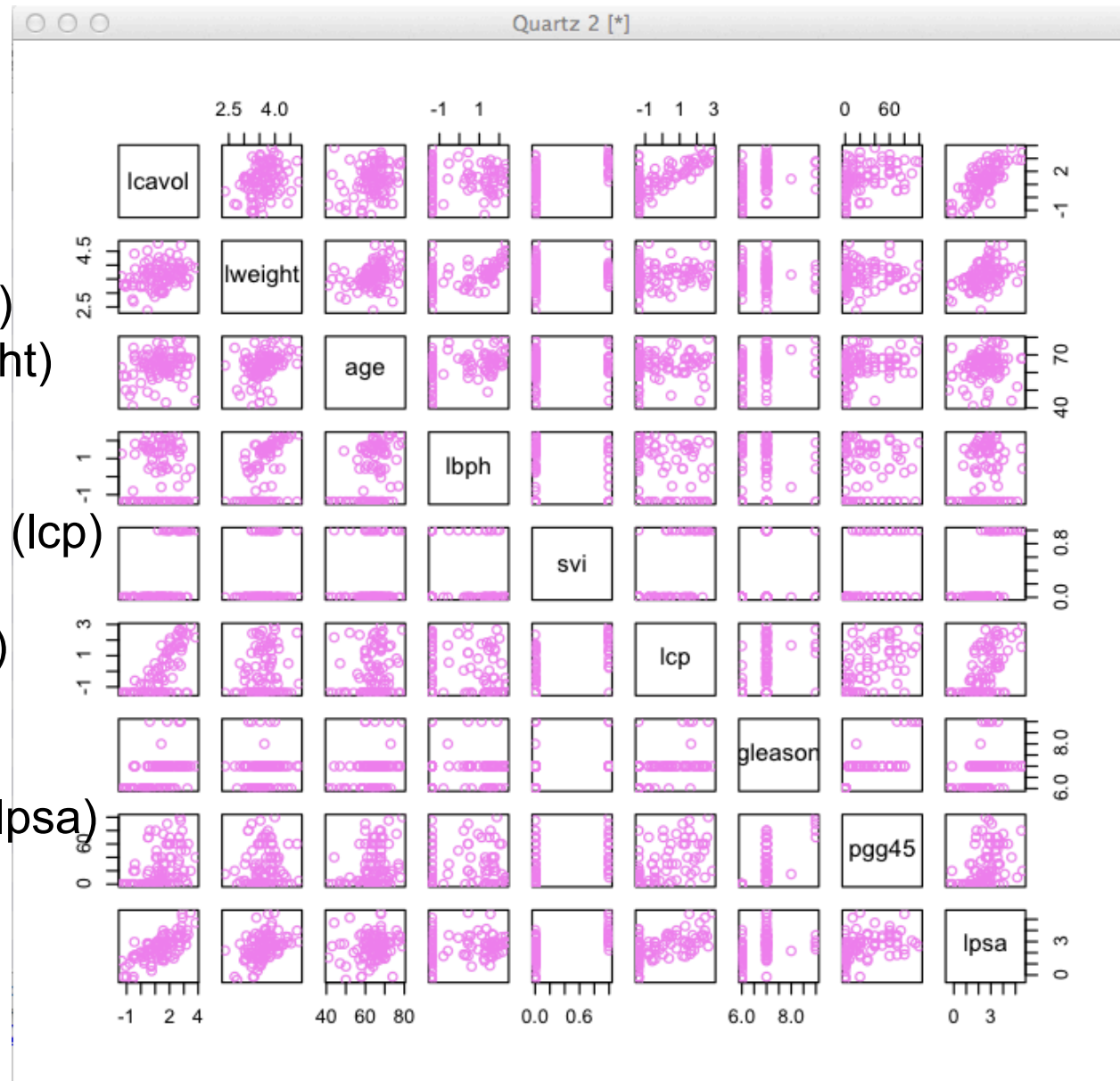
Log of capular penetration (lcp)

Gleason score (gleason)

Gleason score 4/5 (pgg45)

Output Variable:

Prostate-specific antigen (lpsa)



Simple Example

```
> # Load the data
> data(prostate)
> dim(prostate)
[1] 97 10
> ?prostate
> head(prostate)
```

	lcavol	lweight	age	lbph	svi	lcp	gleason	pgg45	lpsa	train
1	-0.5798185	2.769459	50	-1.386294	0	-1.386294	6	0	-0.4307829	TRUE
2	-0.9942523	3.319626	58	-1.386294	0	-1.386294	6	0	-0.1625189	TRUE
3	-0.5108256	2.691243	74	-1.386294	0	-1.386294	7	20	-0.1625189	TRUE
4	-1.2039728	3.282789	58	-1.386294	0	-1.386294	6	0	-0.1625189	TRUE
5	0.7514161	3.432373	62	-1.386294	0	-1.386294	6	0	0.3715636	TRUE
6	-1.0498221	3.228826	50	-1.386294	0	-1.386294	6	0	0.7654678	TRUE

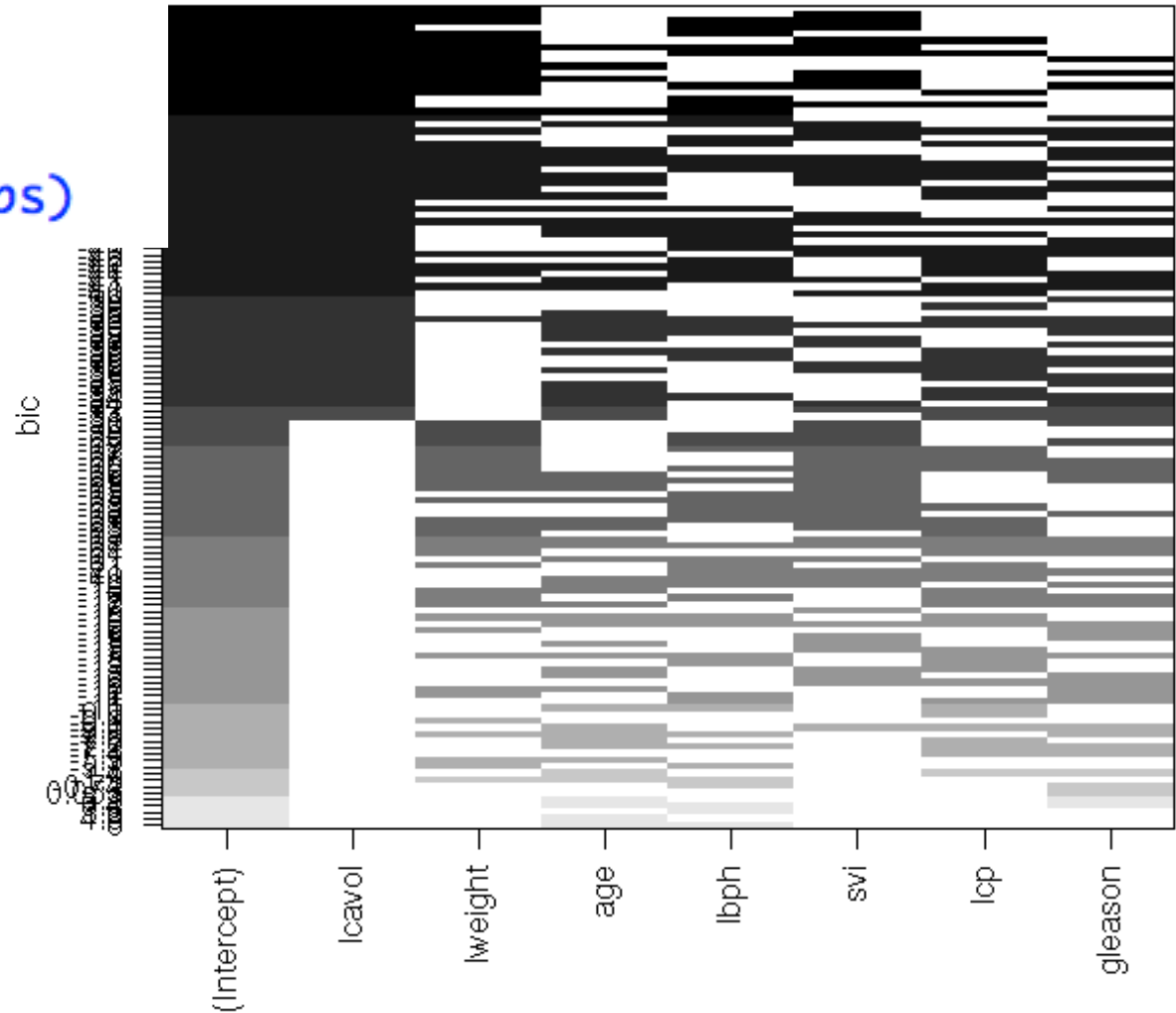
```
>
> # Let's eliminate the 8th column pgg45 - as it is related to gleason variable
> prostate <- prostate[, -c(8,10)]
>
> # Divide the data into test and training
> set.seed(1)
> indi = sample(1:length(prostate[,1]), 2/3*length(prostate[,1]))
> train = prostate[indi, ]
> test = prostate[-indi, ]
```

Simple Example

[illegible]

Simple Example

```
>
> ?plot.regsubsets
>
> x11()
> plot(prostate.leaps)
```



Simple Example

```
> # Lets examine the objects, and create a plot of our own
> prostate.models.rss <- prostate.leaps.sum$rss
>
> # Use tapply to collect the min rss for the best model of size k.
> ?tapply
> prostate.models.best.rss <- tapply(prostate.models.rss, prostate.models.size, min )
> prostate.models.best.rss
      1      2      3      4      5      6      7
39.42975 32.37867 28.37854 26.82124 24.17263 23.65731 23.37737
>
> # Lets include results for the "intercept only" model
> prostate.dummy <- lm( lpsa ~ 1, data=train )
> prostate.models.best.rss <- c(sum(resid(prostate.dummy)^2),
+ prostate.models.best.rss)
>
> # Making a plot:
> x11()
> plot(0:7, prostate.models.best.rss, ylim=c(0, 100), type="b", xlab="subset size", ylab="Residual Sum
Square", col="red2" )
> points( prostate.models.size, prostate.models.rss, pch=17, col="brown",cex=0.7 )
.
```


Simple Example

```
> # Lets examine the objects, and create a plot of our own
```

```
> prostate.models.rss <- prostate.leaps.sum$rss
```

```
>
```

```
> # Use tapply to collect the min rss for the bes
```

```
> ?tapply
```

```
> prostate.models.best.rss <- tapply(prostate.mod
```

```
> prostate.models.best.rss
```

```
      1      2      3      4      5  
39.42975 32.37867 28.37854 26.82124 24.17263 23.6
```

```
>
```

```
> # Lets include results for the "intercept only"
```

```
> prostate.dummy <- lm( lpsa ~ 1, data=train )
```

```
> prostate.models.best.rss <- c(sum(resid(prostat
```

```
+ prostate.models.best.rss)
```

```
>
```

```
> # Making a plot:
```

```
> x11()
```

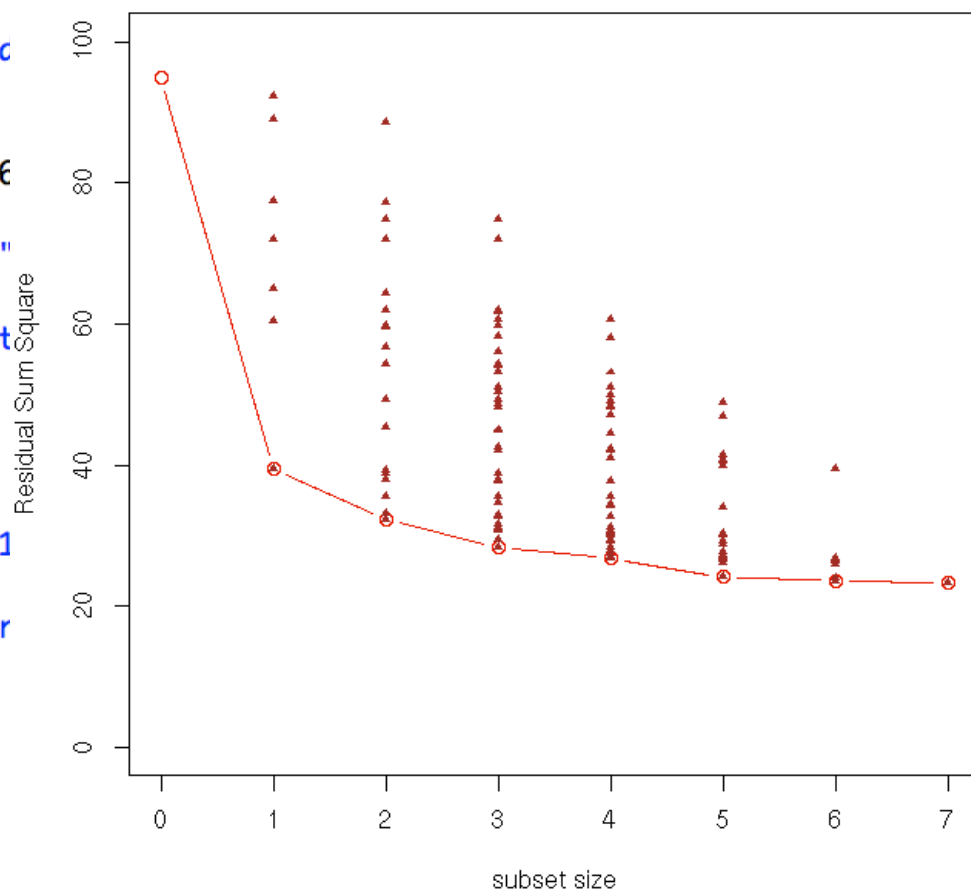
```
> plot(0:7, prostate.models.best.rss, ylim=c(0, 1
```

```
 Square", col="red2" )
```

```
> points( prostate.models.size, prostate.models.r
```

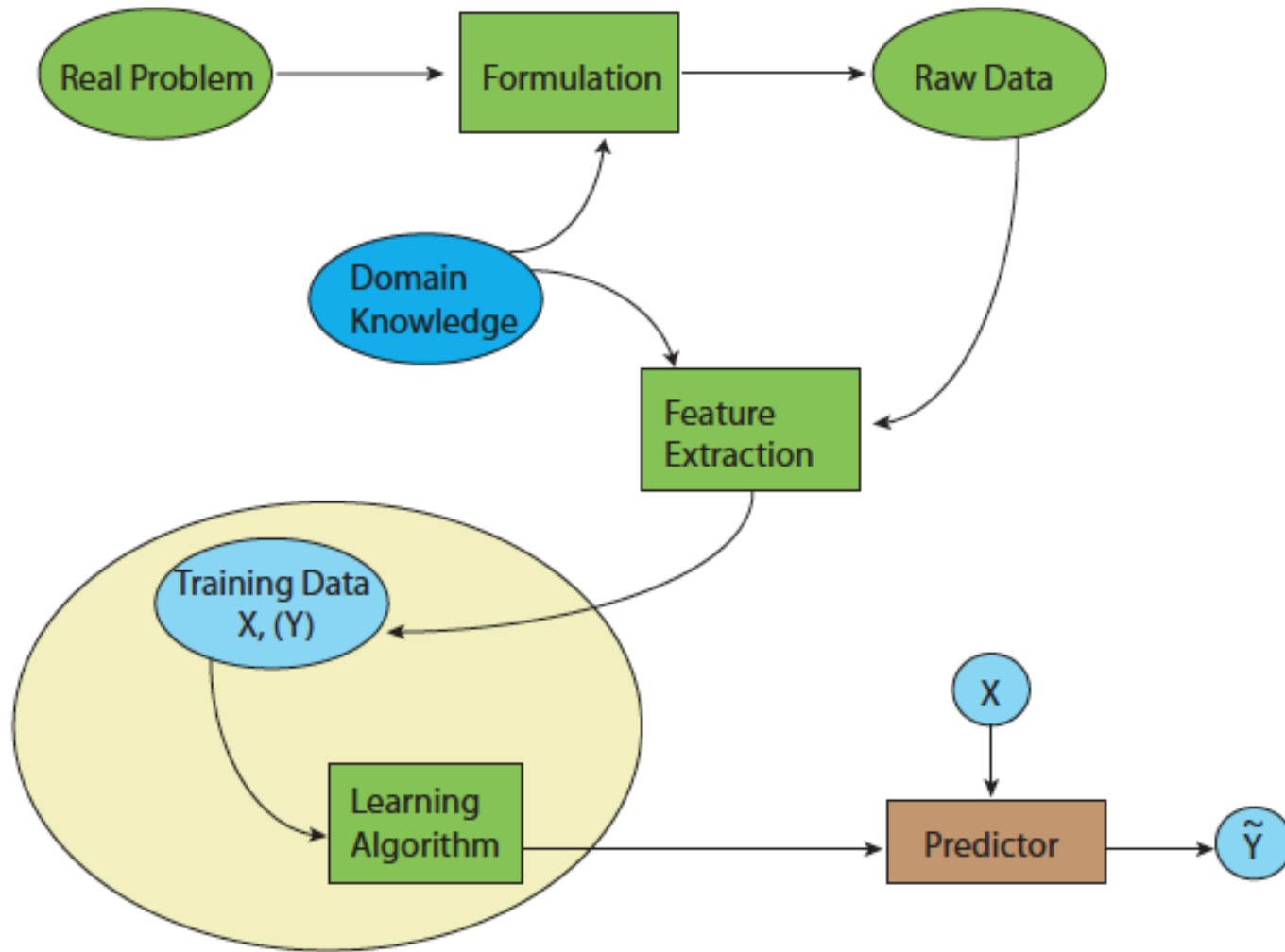
```
.
```

R Graphics: Device 2 (ACTIVE)

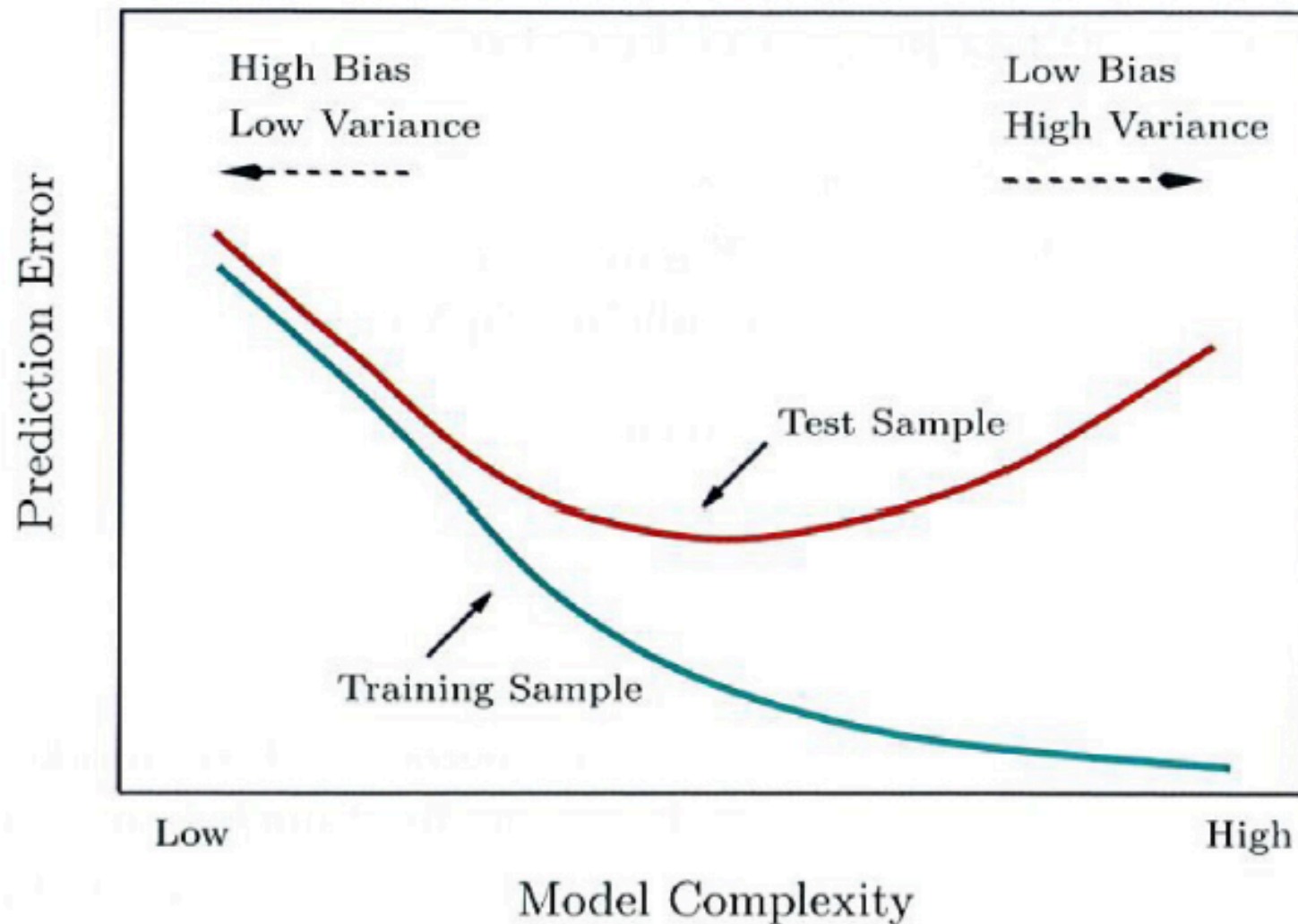


Subset

Birds Eye View: Prediction



Model Selection and Bias-Variance tradeoff



Model Selection

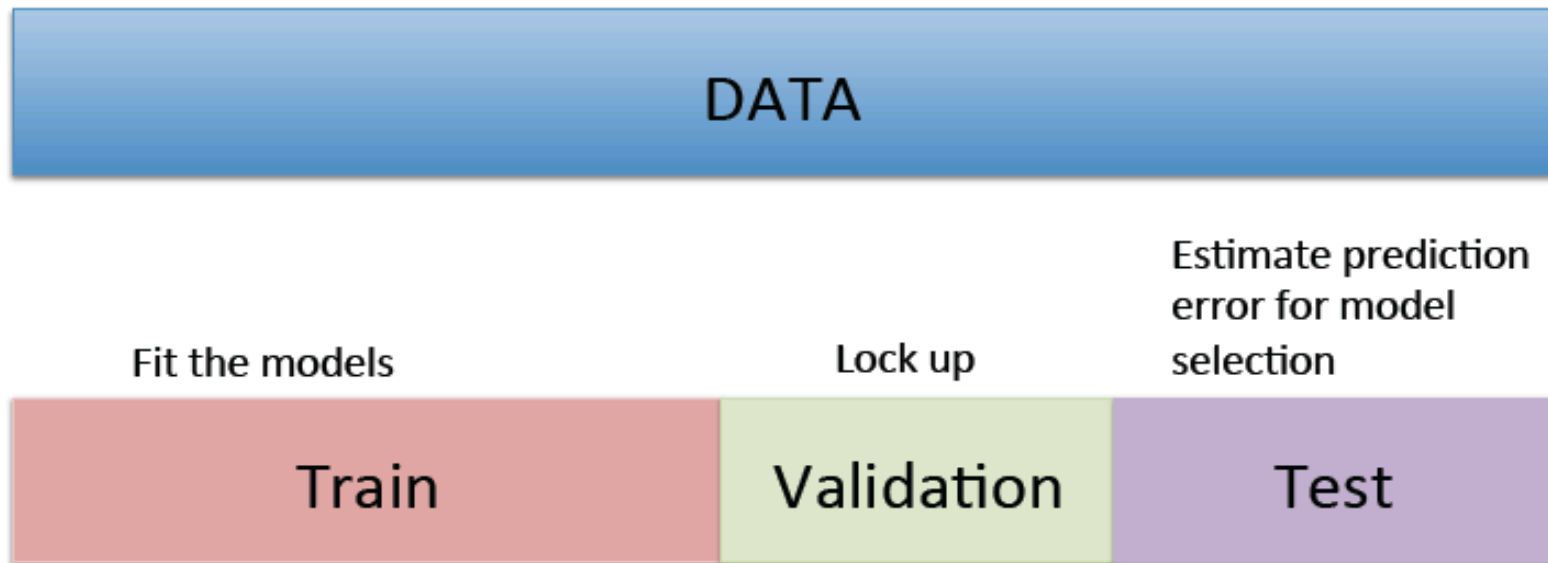
Some Approaches:

- Hold-out method
- AIC, BIC, MDL, etc.
- K-fold cross validation
- Bootstrap

Model Selection

Ideal situation:

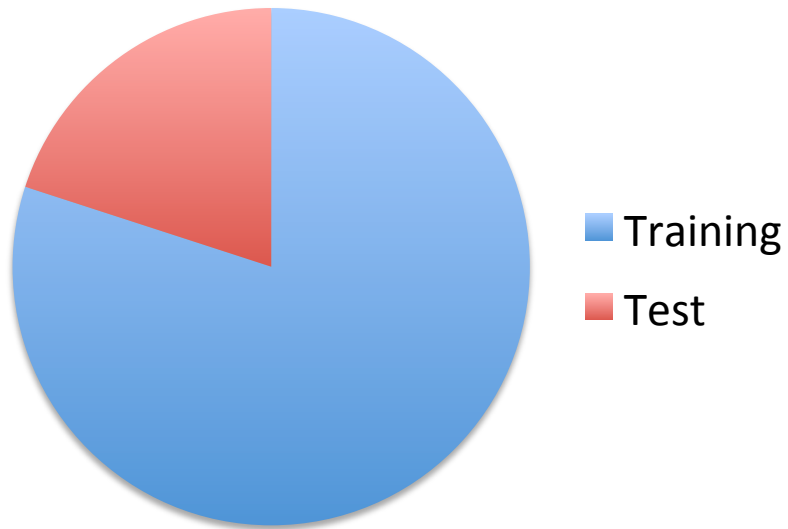
LOTS OF DATA!



Model Selection

A reality (hold-out method)

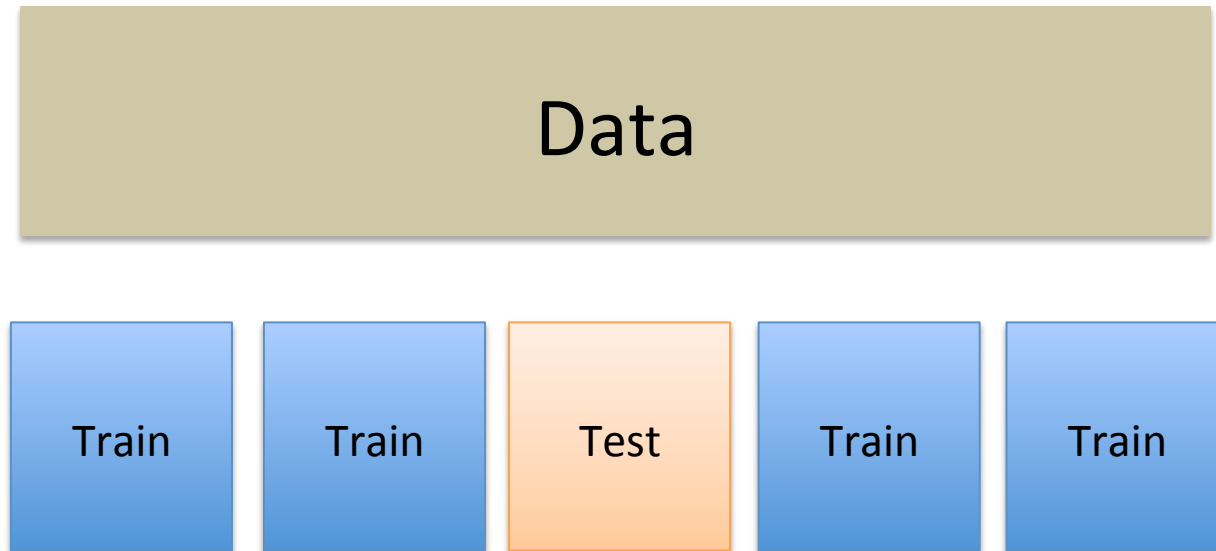
Data Poor



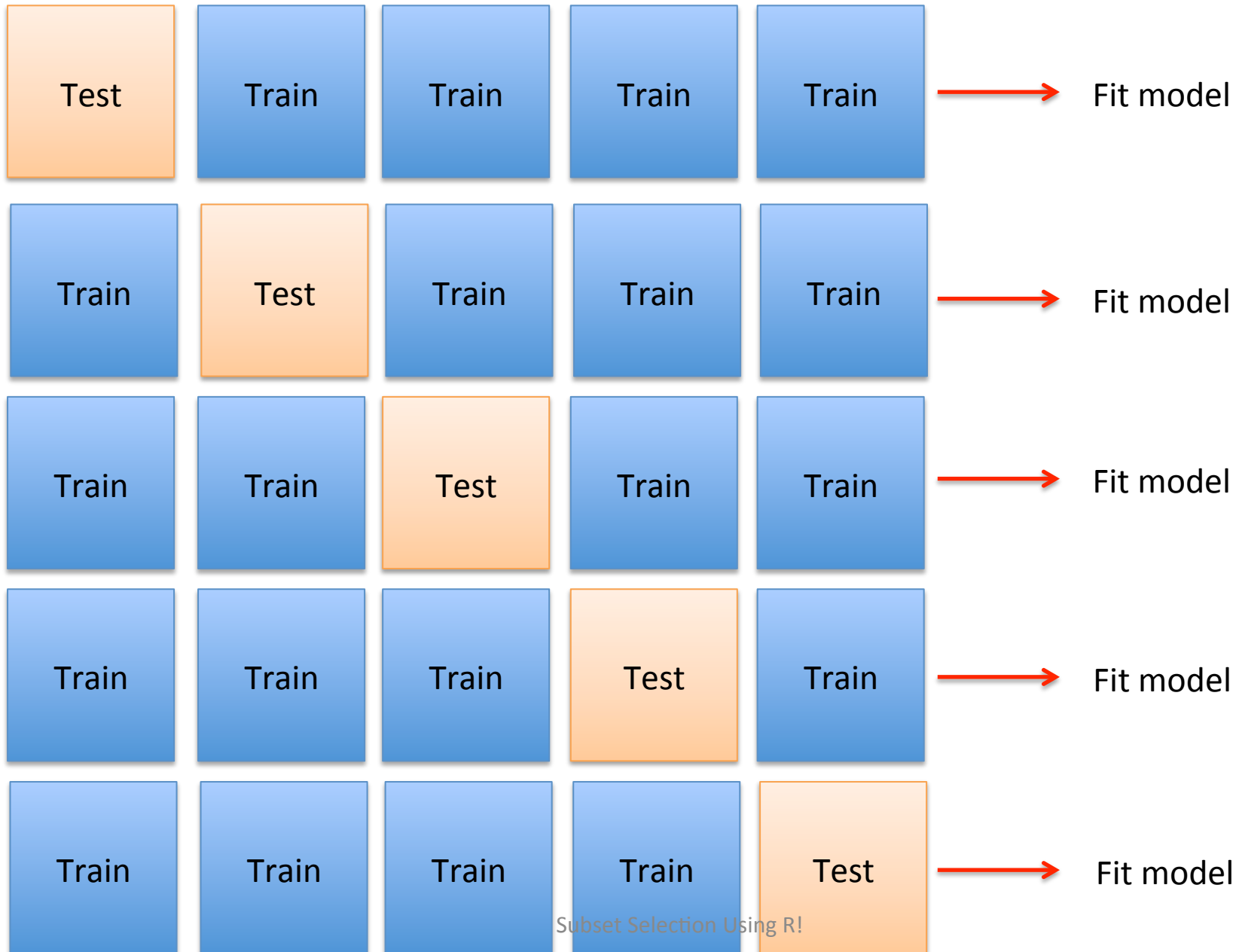
*If we get an unfortunate “split”
this can be misleading.*

Model Selection

K-fold cross-validation: For the k^{th} part (third below) we fit the model to the other $K-1$ parts of the data, and calculate the prediction error of the fitted model when predicting the k^{th} part of the data.



Data



Back to our “Simple Example”

Prostate Cancer

Input Variable:

Log cancer volume (lcavol)

Log prostate weight (lweight)

Log amt of benign (lbph)

Seminal invasion (svi)

Log of capular penetration (lcp)

Gleason score (gleason)

Gleason score 4/5 (pgg45)

Output Variable:

Prostate-specific antigen (lpsa)

Let's consider:

- Test/training
- Mallow's Cp/ Adjusted R^2
- K-fold cross validation

Back to our “Simple Example”

```
> prostate.leaps <- regsubsets(lpsa ~ ., nvmax = 7, method = "backward", data=train)
> sum.prost <- summary(prostate.leaps)
> sum.prost$outmat
```

```
      lcavol lweight age lbph svi lcp gleason
1 ( 1 ) "*"      " "   " " " " " " " " " "
2 ( 1 ) "*"      "*"   " " " " " " " " " "
3 ( 1 ) "*"      "*"   " " " " "*" " " " " "
4 ( 1 ) "*"      "*"   " " "*" "*" " " " " "
5 ( 1 ) "*"      "*"   "*" "*" "*" " " " " "
6 ( 1 ) "*"      "*"   "*" "*" "*" " " " "*"
7 ( 1 ) "*"      "*"   "*" "*" "*" "*" "*" "
```

We want to evaluate
our test set on each of
these models!

But we have to get our
data ready!

```
>
> # Look at the names of the coefficients, they have to match our data
> coef(prostate.leaps, id = 7)
(Intercept)      lcavol      lweight      age      lbph      svi      lcp      gleason
-0.50771021  0.58575658  0.78349493 -0.03328929  0.17569954  0.82243647 -0.07756983  0.18008332
```

```
>
> # Get a Matrix ready for multiplication
```

```
> head(test) # our test data
```

```
      lcavol lweight age      lbph svi      lcp gleason      lpsa
3  -0.5108256 2.691243 74 -1.386294  0 -1.3862944      7 -0.1625189
8   0.6931472 3.539509 58  1.536867  0 -1.3862944      6  0.8544153
9  -0.7765288 3.539509 47 -1.386294  0 -1.3862944      6  1.0473190
14  1.4770487 2.998229 67 -1.386294  0 -1.3862944      7  1.3480731
15  1.2059708 3.442019 57 -1.386294  0 -0.4307829      7  1.3987169
22  2.0592388 3.501043 60  1.474763  0  1.3480732      7  1.6582281
```

Back to our “Simple Example”

```
> # we need to "tack on" a column of ones
> new_test <- cbind(rep(1, length(test[,1])), test)
> colnames(new_test) <- c("(Intercept)", colnames(test)) #the var. name has to match
> head(new_test)
```

	(Intercept)	lcavol	lweight	age	lbph	svi	lcp	gleason	lpsa
3	1	-0.5108256	2.691243	74	-1.386294	0	-1.3862944	7	-0.1625189
8	1	0.6931472	3.539509	58	1.536867	0	-1.3862944	6	0.8544153
9	1	-0.7765288	3.539509	47	-1.386294	0	-1.3862944	6	1.0473190
14	1	1.4770487	2.998229	67	-1.386294	0	-1.3862944	7	1.3480731
15	1	1.2059708	3.442019	57	-1.386294	0	-0.4307829	7	1.3987169
22	1	2.0592388	3.501043	60	1.474763	0	1.3480732	7	1.6582281

```
>
> # lets do the same thing for the training data.
> new_train <- cbind(rep(1, length(train[,1])), train)
> colnames(new_train) <- c("(Intercept)", colnames(train))
> head(new_train)
```

	(Intercept)	lcavol	lweight	age	lbph	svi	lcp	gleason	lpsa
26	1	1.4469190	3.124565	68	0.3001046	0	-1.3862944	6	1.766442
36	1	1.3083328	4.119850	64	2.1713368	0	-1.3862944	7	2.085672
55	1	3.1535904	3.516013	59	-1.3862944	0	-1.3862944	7	2.704711
86	1	3.3028493	3.518980	64	-1.3862944	1	2.3272777	7	3.630985
19	1	-0.5621189	3.267666	41	-1.3862944	0	-1.3862944	6	1.558145
83	1	2.6130067	3.888754	77	-0.5276327	1	0.5596158	7	3.565298

```
>
```

```

> # Look at the coefficients
> coef(prostate.leaps, id = 7)
(Intercept)      lcavol      lweight      age      lbph      svi
-0.86571905  0.55633762  0.61915631 -0.01867975  0.14429952  0.80304060
      lcp      gleason
-0.13148317  0.19808495
>
> # Get a Matrix ready for multiplication
> new_test <- cbind(rep(1, length(test[,1])), test)
> colnames(new_test) <- c("(Intercept)", colnames(test))
> new_test[1:3,]
(Intercept)      lcavol      lweight      age      lbph      svi      lcp      gleason      lpsa
1           1 -0.5798185  2.769459   50 -1.386294    0 -1.386294         6 -0.4307829
2           1 -0.9942523  3.319626   58 -1.386294    0 -1.386294         6 -0.1625189
3           1 -0.5108256  2.691243   74 -1.386294    0 -1.386294         7 -0.1625189
>
> new_train <- cbind(rep(1, length(train[,1])), train)
> colnames(new_train) <- c("(Intercept)", colnames(train))
> new_train[1:3,]
(Intercept)      lcavol      lweight      age      lbph      svi      lcp      gleason      lpsa
1           1 -0.5798185  2.769459   50 -1.386294    0 -1.386294         6 -0.4307829
2           1 -0.9942523  3.319626   58 -1.386294    0 -1.386294         6 -0.1625189
3           1 -0.5108256  2.691243   74 -1.386294    0 -1.386294         7 -0.1625189
>

```

Back to our “Simple Example”

Let's make predictions using the best models of size “k”.

track the training and testing error

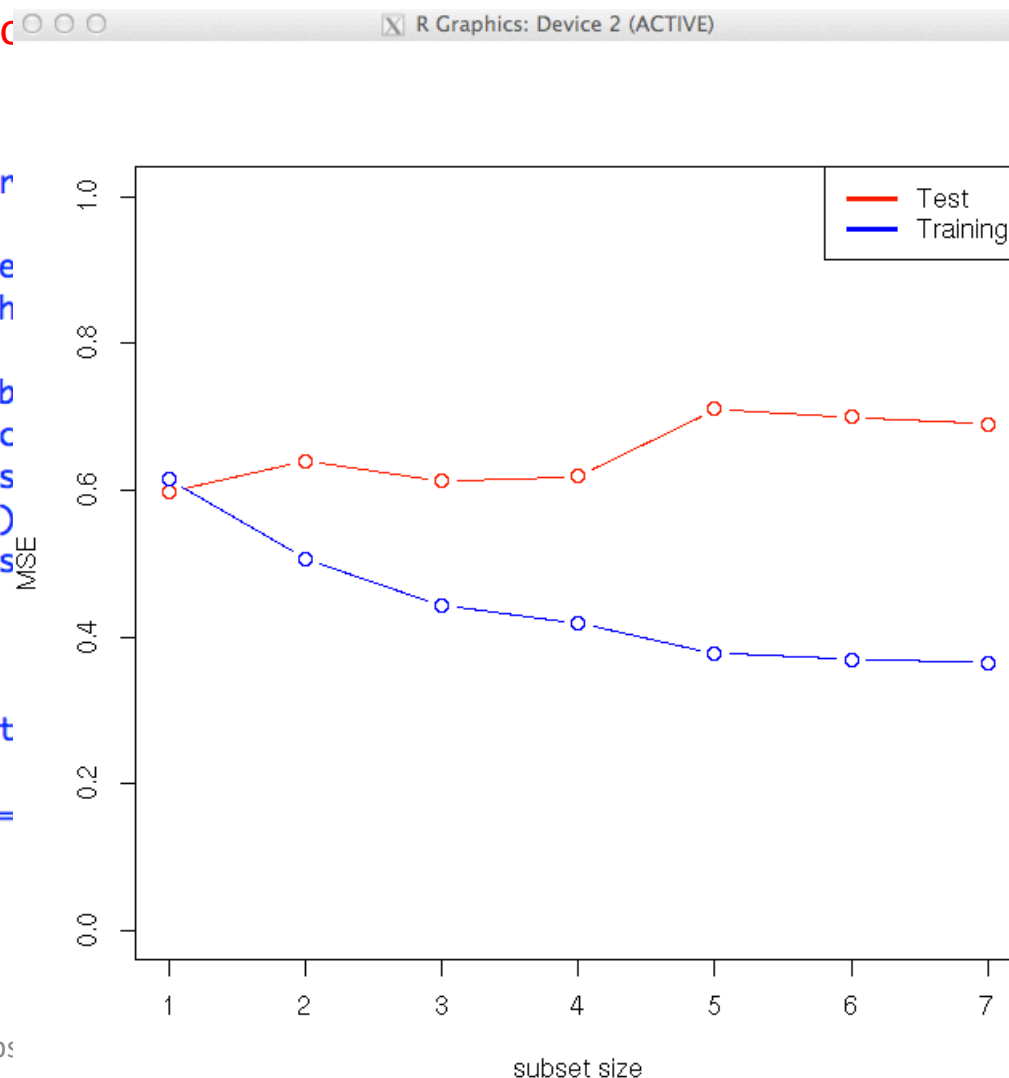
```
> # lets loop through and predict the test error, and training error for models
> # of size 1... 7.
> test.errors = rep(NA, 7) #for collecting the test error
> train.errors = rep(NA, 7) #for collecting the train error
> for(i in 1:7){
+   coefi = coef(prostate.leaps, id=i) # grab the coefficients
+   pred_test = as.matrix(new_test[ , names(coefi)])%%coefi # y_hat (data matrix * coefficients)
+   pred_train = as.matrix(new_train[ , names(coefi)])%%coefi # y_hat (data matrix * coefficients)
+   test.errors[i] = (1/length(new_test$lpsa))*sum((new_test$lpsa-pred_test)^2) # store the error
+   train.errors[i] = (1/length(new_train$lpsa))*sum((new_train$lpsa-pred_train)^2) # store the error
+ }
>
> x11()
> plot(test.errors, ylim=c(0, 1), col="red", type = "b", xlab="subset size", ylab="MSE" )
> lines(train.errors, col = "blue", type="b")
> legend("topright", c("Test","Training"),lty=c(1,1), lwd=c(2.5,2.5),col=c("red", "blue"))
```

Back to our “Simple Example”

Let's make predictions using the best models of size “k”.

track the training and testing error

```
> # lets loop through and predict the test err
> # of size 1... 7.
> test.errors = rep(NA, 7) #for collecting the
> train.errors = rep(NA, 7) #for collecting th
> for(i in 1:7){
+   coefi = coef(prostate.leaps, id=i) # grab
+   pred_test = as.matrix(new_test[, names(c
+   pred_train = as.matrix(new_train[, names
+   test.errors[i] = (1/length(new_test$lpsa)
+   train.errors[i] = (1/length(new_train$lps
+ }
>
> x11()
> plot(test.errors, ylim=c(0, 1), col="red", t
> lines(train.errors, col = "blue", type="b")
> legend("topright", c("Test","Training"),lty=
```



Back to our “Simple Example”

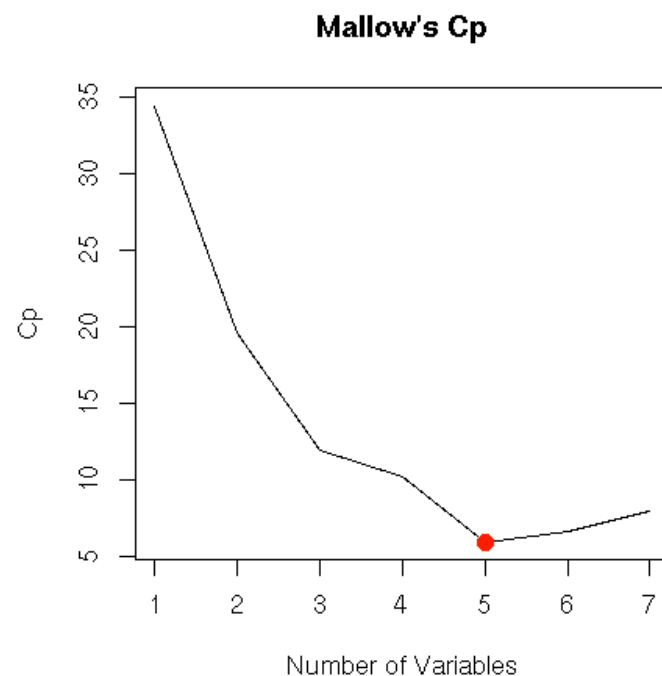
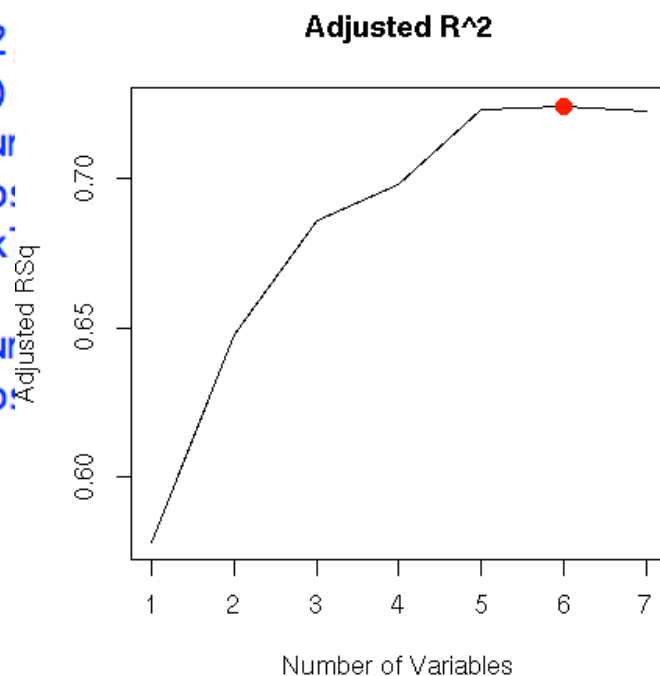
```
> x11()
> par(mfrow=c(1,2))
> plot(sum.prost$adjr2, xlab="Number of Variables", ylab="Adjusted RSq", type="l",
main = "Adjusted R^2")
> temp <- which.max(sum.prost$adjr2)
> points(temp, sum.prost$adjr2[temp], col="red", cex=2, pch=20)
> plot(sum.prost$cp, xlab="Number of Variables", ylab="Cp", type='l', main = "Mallow's
Cp")
> temp <- which.min(sum.prost$cp)
> points(temp, sum.prost$cp[temp], col="red", cex=2, pch=20)
>
```

Back to our “Simple Example”

```
> x11()
> par(mfrow=c(1,2))
> plot(sum.prost$adjr2,
main = "Adjusted R^2")
> temp <- which.max(sum.prost$adjr2)
> points(temp, sum.prost$adjr2)
> plot(sum.prost$cp, x11(),
main = "Mallow's Cp")
> temp <- which.min(sum.prost$cp)
> points(temp, sum.prost$cp)
>
```



R Graphics: Device 2 (ACTIVE)



Back to our “Simple Example”

Write a simple function to do the prediction

```
> data(prostate) # let's start fresh
> head(prostate)
      lcavol  lweight age      lbph svi      lcp gleason pgg45      lpsa train
1 -0.5798185 2.769459  50 -1.386294  0 -1.386294      6      0 -0.4307829 TRUE
2 -0.9942523 3.319626  58 -1.386294  0 -1.386294      6      0 -0.1625189 TRUE
3 -0.5108256 2.691243  74 -1.386294  0 -1.386294      7     20 -0.1625189 TRUE
4 -1.2039728 3.282789  58 -1.386294  0 -1.386294      6      0 -0.1625189 TRUE
5  0.7514161 3.432373  62 -1.386294  0 -1.386294      6      0  0.3715636 TRUE
6 -1.0498221 3.228826  50 -1.386294  0 -1.386294      6      0  0.7654678 TRUE
> dats <- prostate[, -c(8,10)]
>
> # Write a simple function.
> # Input: regsubsets object, new data, and id (k)
> # Output: a prediction
> predict.regsubsets = function(object, newdata, id, ...){
+   temp_X <- cbind(rep(1, length(newdata[,1])), newdata)
+   colnames(temp_X) <- c("(Intercept)", colnames(newdata))
+
+   coefi = coef(object, id=i)
+   my_pred = as.matrix(temp_X[,names(coefi)])%*%coefi
+
+   return(my_pred)
+ }
```

Back to our “Simple Example”

Let's call that simple function in a cross-validation routine.

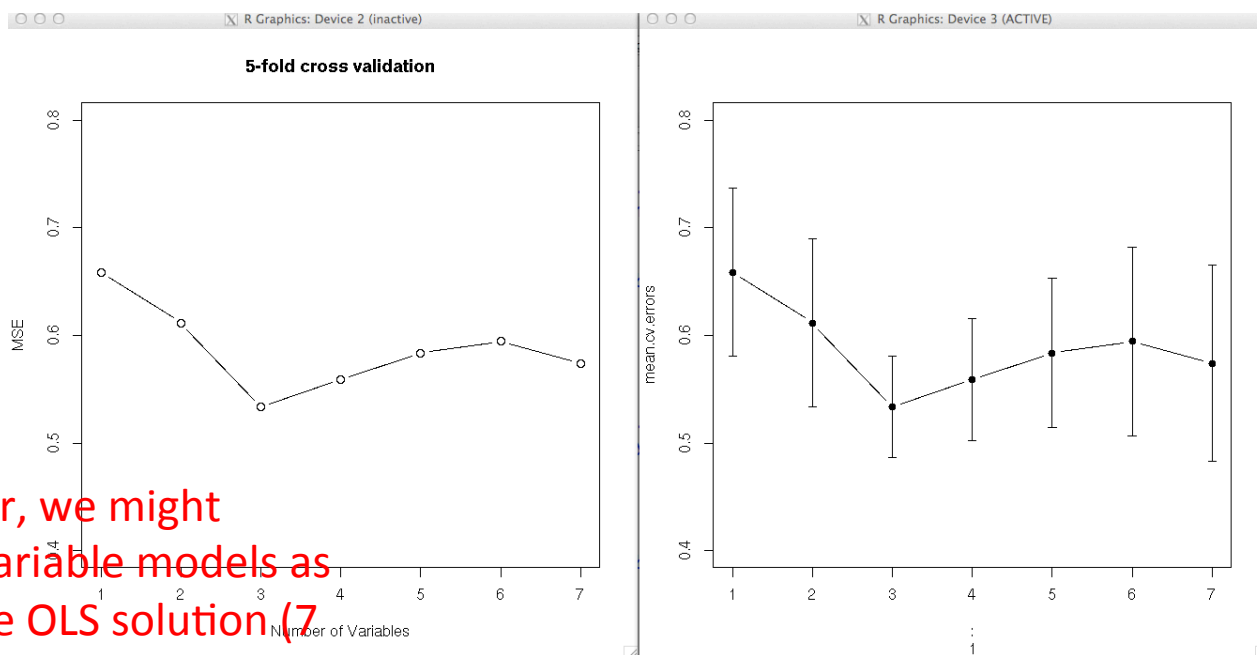
```
> # K-fold cross validation
> k=5
> set.seed(1)
> folds = sample(1:k,nrow(dats), replace=TRUE)
> cv.errors=matrix(NA, k, 7, dimnames=list(NULL, paste(1:7)))
> cv.errors # a matrix for storing the error (number of folds x number of variables)
      1  2  3  4  5  6  7
[1,] NA NA NA NA NA NA NA
[2,] NA NA NA NA NA NA NA
[3,] NA NA NA NA NA NA NA
[4,] NA NA NA NA NA NA NA
[5,] NA NA NA NA NA NA NA
> for(j in 1:k){
+   best.fit=regsubsets(lpsa ~ ., data = dats[folds!=j,], nvmax = 7)
+   for(i in 1:7){
+     pred=predict(best.fit, newdata = dats[folds==j,], id=i)
+     cv.errors[j,i]=mean((dats$lpsa[folds==j]-pred)^2)
+   }
+ }
> mean.cv.errors = apply(cv.errors, 2, mean)
> se.cv.errors = apply(cv.errors, 2, sd)/sqrt(k)
>
```

K-fold cross
validation

A natural
double for-
loop

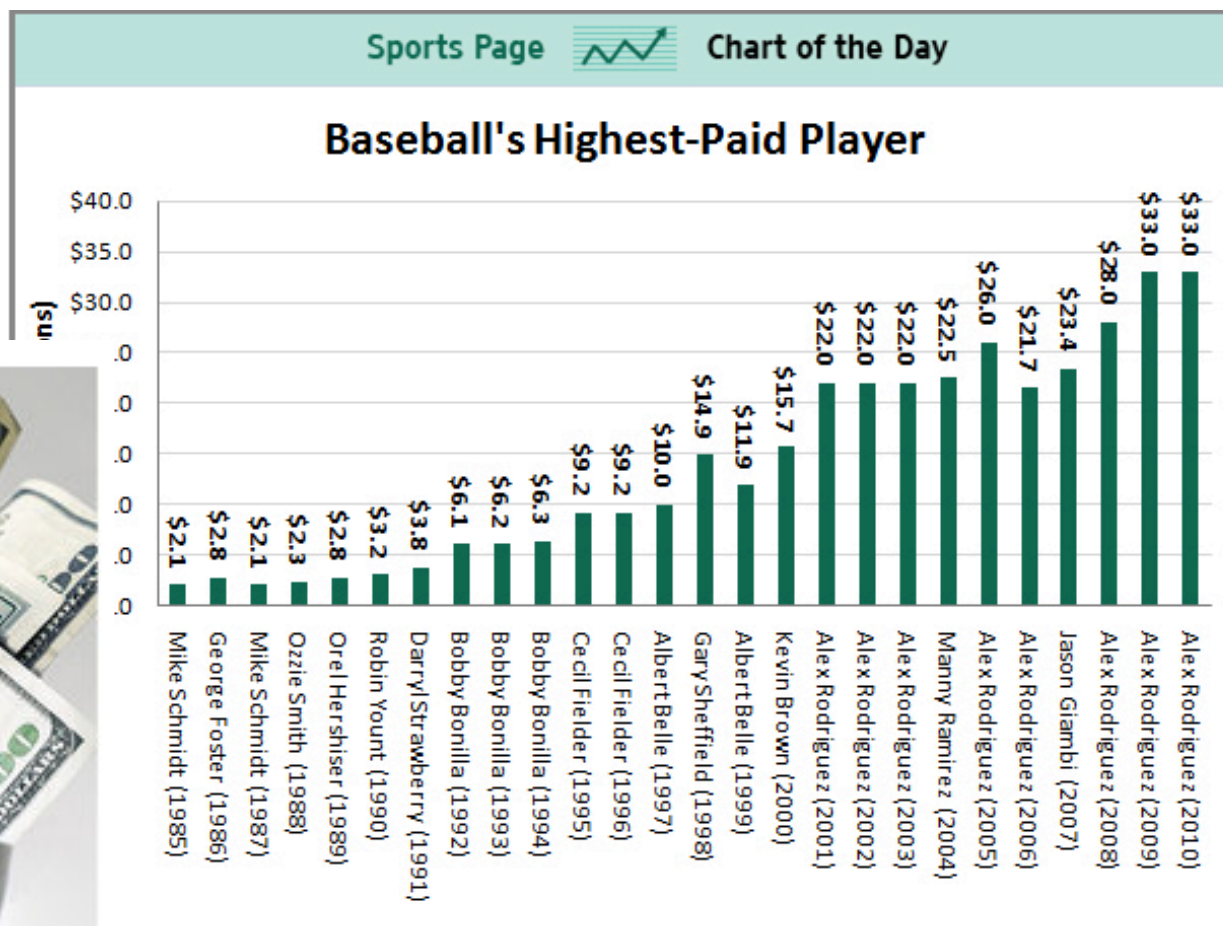
Back to our “Simple Example”

```
> x11()
> plot(1:7, mean.cv.errors, xlab="Number of Variables", ylab="MSE", main = "5-fold cross validation",
type = "b", ylim = c(.4,.8))
>
>
> library(Hmisc)
> x11()
> errbar(1:7, mean.cv.errors, mean.cv.errors + se.cv.errors, mean.cv.errors - se.cv.errors, main = "5-
fold cross validation", type = "b", ylim = c(.4,.8))
>
```



Taken together, we might consider 3-5 variable models as opposed to the OLS solution (7 variables).

On your own



On your own

```
> library(ISLR)
> data(Hitters)
> ?Hitters
```

Hitters {ISLR}

Baseball Data

Description

Major League Baseball Data from the 1986 and 1987 seasons.

Usage

Hitters

Format

A data frame with 322 observations of major league players on the following 20 variables.

AtBat

Number of times at bat in 1986

Hits

Number of hits in 1986

HmRun

Number of home runs in 1986

Runs

Number of runs in 1986

RBI

Number of runs batted in in 1986

Walks

Number of walks in 1986