

Assignment - I

Statistics

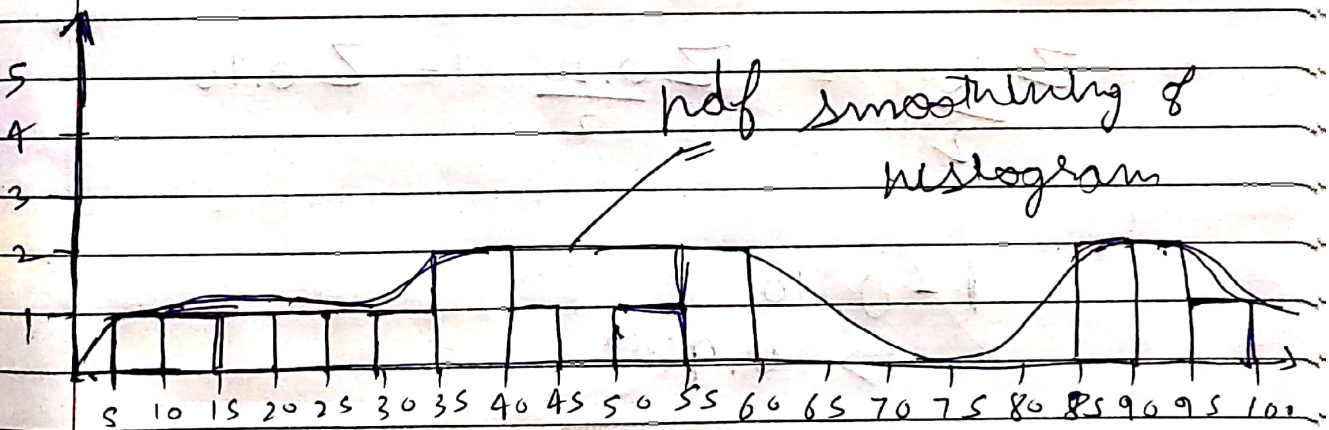
Q1 Plot a histogram

10, 13, 18, 22, 27, 32, 38, 40, 45, 51, 56,
57, 88, 90, 92, 94, 99.

Step ①:- Sort in asc. order

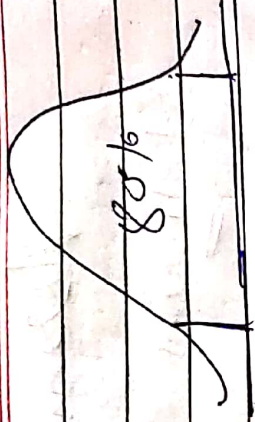
Bins = 5

$$\text{Bin size} = \frac{100}{5} = 20$$



Q2 In a quant test of the CAT exam the population std is known to be 100. A sample of 25 tests taken has a mean of 520. Construct 80% C.I about the mean.

Ans $\sigma = 100$
 $n = 25$
 $\bar{x} = 520$



$$P(Z) = 80\%$$

$$= 0.80$$

$$1 - 0.80 = 0.20$$

$d = \text{significant value}$

C.T. \Rightarrow least extreme \pm Margin of error

$$Z_{\frac{\alpha}{2}} = Z_{\frac{0.20}{2}} = Z_{0.10}$$

$$1 - 0.10 \Rightarrow 0.900$$

from Z table

$$\Rightarrow 1.29$$

Lower formula $= \bar{x} - Z_{\frac{\alpha}{2}} \frac{\sigma}{\sqrt{n}}$

$$\Rightarrow 520 - 1.29 \times \frac{100}{\sqrt{25}}$$

$$= 520 - 1.29 \times 20$$

$$\Rightarrow 494.2$$

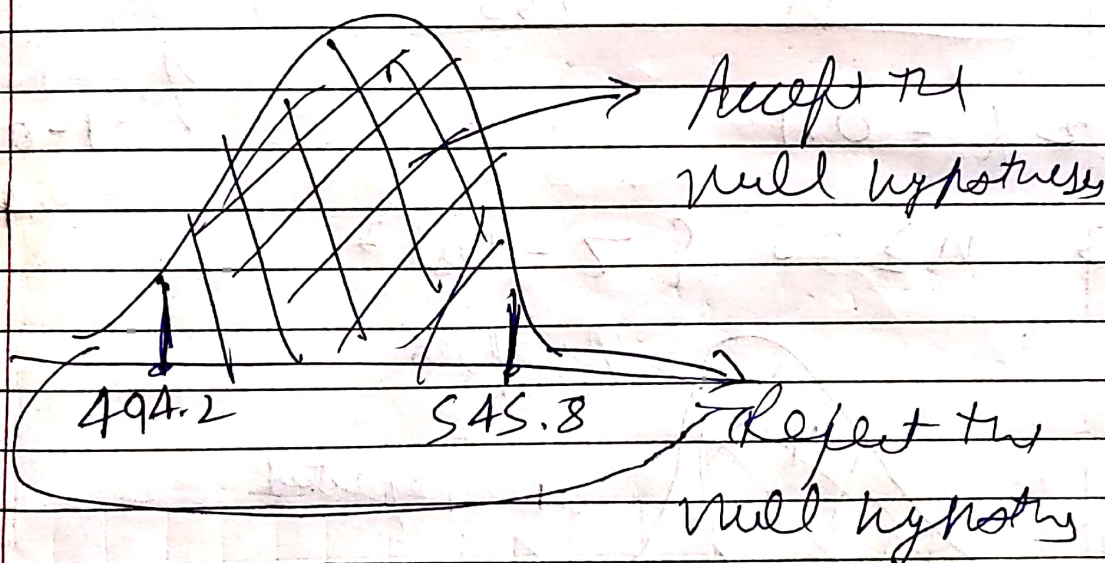
$$\text{Higher fence} = \bar{x} + \frac{Z_{\alpha/2} \sigma}{\sqrt{n}}$$

$$= 520 + 1.29 \times \frac{100}{\sqrt{25}}$$

$$= 520 + 1.29 \times \frac{100 \times 20}{8}$$

$$= 520 + 25.8$$

$$= 545.8$$



Q3 A car believes that the percentage of citizens in city ABCI that owns a vehicle is 60% or less. A sales manager disagrees with this. He conducted a hypothesis testing surveying 250 residents & found that 170 residents responded yes to owning a vehicle.

- (a) State the null & alternate hypotheses
 (b) At a 10% significance level, is there ~~less~~ enough evidence to support the idea that vehicle owner in ABC city is 60% or less.

$$x = 170, n = 250$$

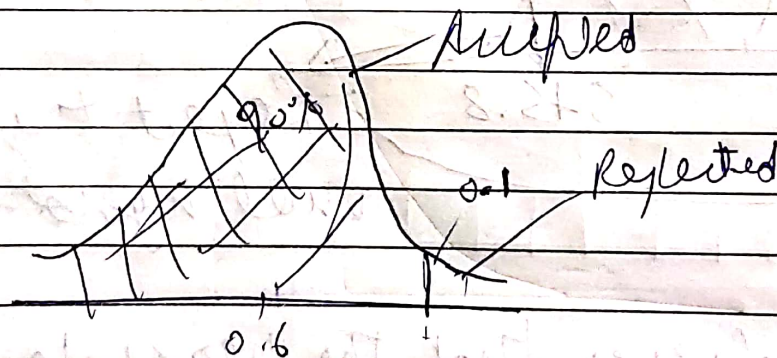
Ans $H_0 = p_0 \leq 60\%$ { Null hypothesis }
 $H_1 = p_0 > 60\%$ { Alternate hypothesis }

$$\hat{p} = \frac{x}{n} = \frac{170}{250} = 0.68$$

Step 2 $\alpha = 0.1$

$$q_0 = 1 - p_0 \\ = 1 - 0.6 \\ = 0.4$$

Step 3 $n \geq 30$ { Z-test }



$$1 - 0.1 \\ = 0.900 \\ = +1.285$$

Step 4 Calculate Z test statistics

$$Z = \frac{\hat{p} - p_0}{\sqrt{p_0 q_0}} = \frac{0.68 - 0.6}{\sqrt{0.6 \times 0.4}}$$

$$= 2.5$$

Step 5:- conclusion

$$Z = 2.5 > 1.28$$

Reject the null hypothesis

(b) No, At 10% significance level, idea is not enough to support.

Q4 What is the value of the 99 percentile?

2, 2, 3, 4, 5, 5, 5, 6, 7, 8, 8, 8, 8, 9, 9, 10, 11, 14, 12

$$\text{Value at 99 percentile} = \frac{\text{percentile}}{100} \times (n+1)$$

$$\Rightarrow \frac{99}{100} \times (20+1)$$

$$= \frac{99}{100} \times 21$$

$$= 20.79 \Rightarrow \text{order}$$

∴

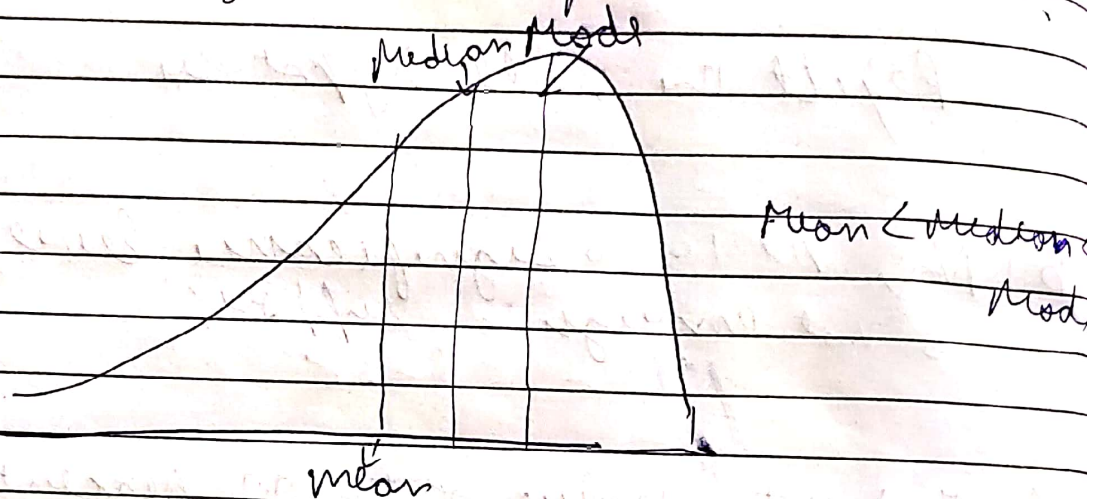
$$\text{Value} = 112$$

Value at 99 percentile is 12

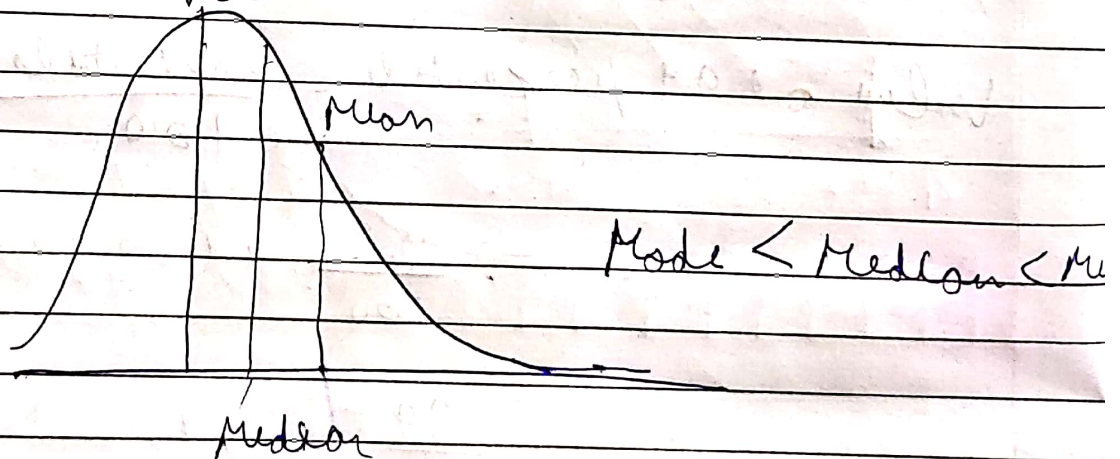
Q5 In left & right skewed data, what is the relationship b/w mean, median & mode?

Draw a graph to represent the same.

Ans



Left Skewed data



Right skewed data