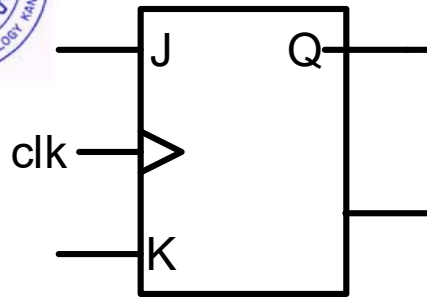




ESc201, Lecture 37: FF Converters & Counting ADC

Characteristic table of FFs

JK Flip-flop



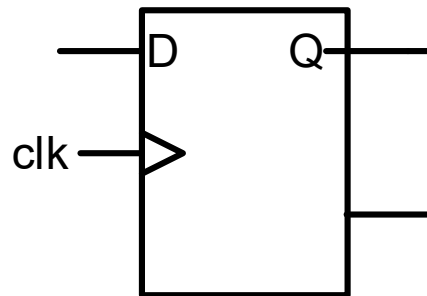
Truth table:

J_n	K_n	Q_{n+1}
0	0	Q_n
0	1	0
1	0	1
1	1	\bar{Q}_n

Characteristic equation:

$$Q_{n+1} = J\bar{Q}_n + \bar{K}Q_n$$

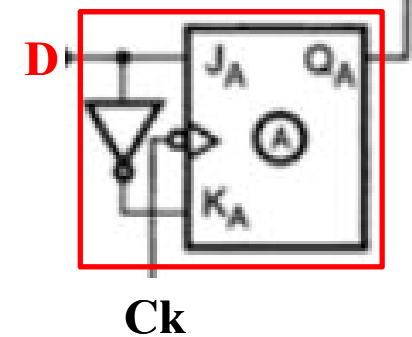
D Flip-flop



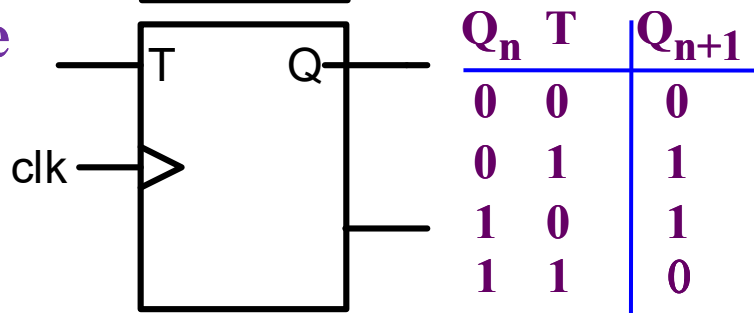
D_n	Q_{n+1}
0	0
1	1

$$Q_{n+1} = D$$

Conversion

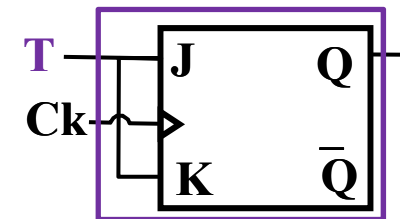


Toggle or T Flip-flop

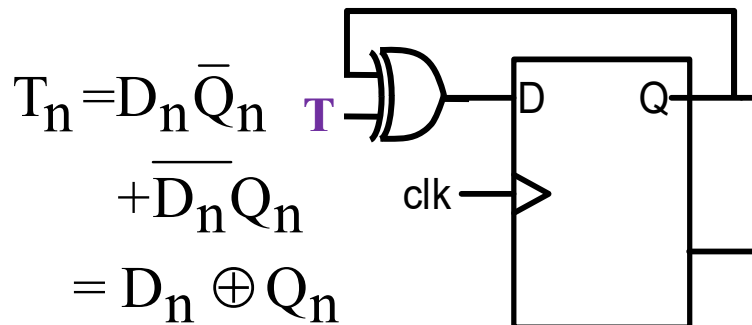


Q_n	T	Q_{n+1}
0	0	0
0	1	1
1	0	1
1	1	0

$$Q_{n+1} = T \oplus Q_n$$

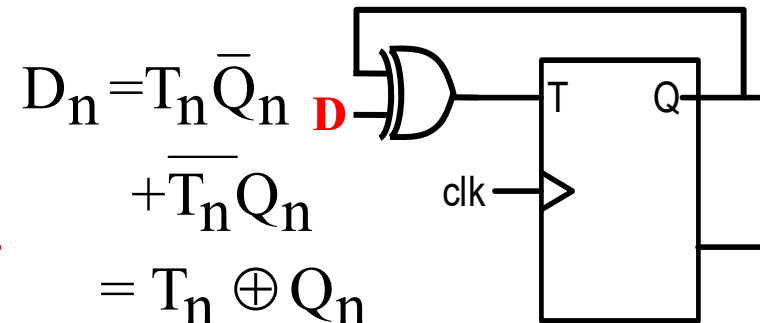


D Flip-flop to T Flip-flop



$$\begin{aligned} T_n &= D_n \bar{Q}_n + \bar{D}_n Q_n \\ &= D_n \oplus Q_n \end{aligned}$$

T Flip-flop to D Flip-flop

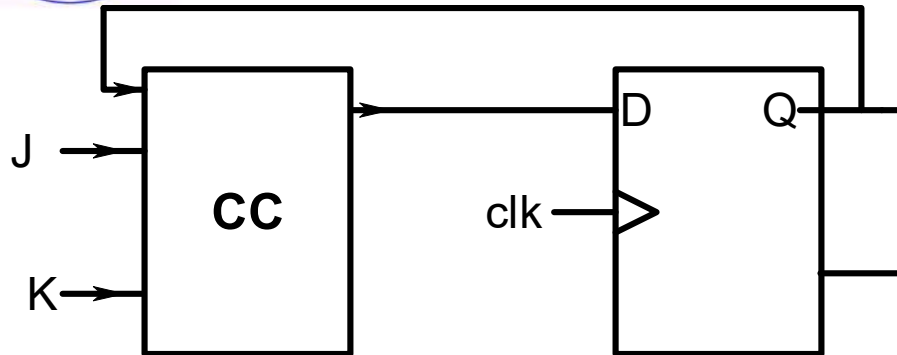


$$\begin{aligned} D_n &= T_n \bar{Q}_n + \bar{T}_n Q_n \\ &= T_n \oplus Q_n \end{aligned}$$



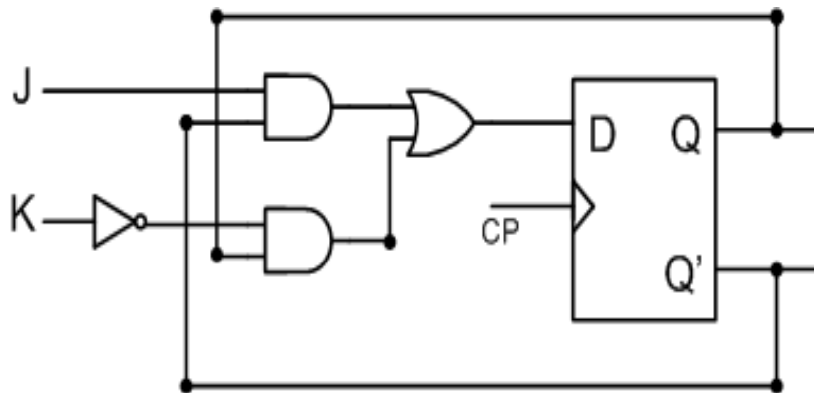
ESc201, Lecture 37: Digital counters and counting-ADC

Convert a D FF to JK FF



J	K	Q	Q(t+1)	D
0	x	0	0	0
1	x	0	1	1
x	1	1	0	0
x	0	1	1	1

JK \ Q	00	01	11	10
0			1	1
1	1			1



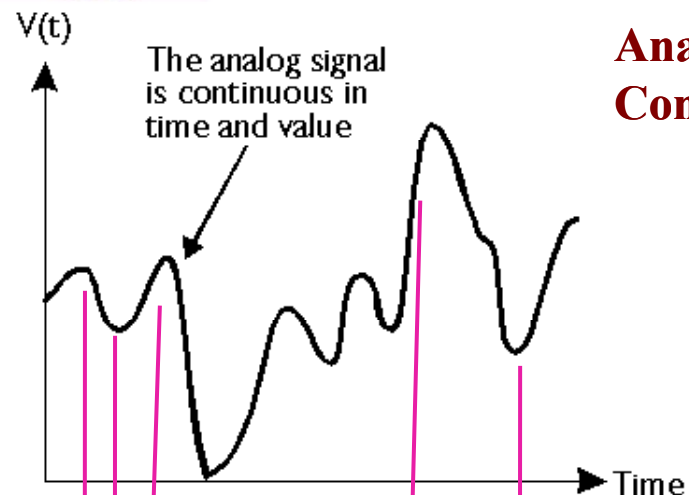
$$D = \bar{Q}.J + Q.\bar{K}$$

Q	J	K	D	Q _{n+1}
0	0	0	0	0
0	0	1	0	0
0	1	0	1	1
0	1	1	1	1
1	0	0	1	1
1	0	1	0	0
1	1	0	1	1
1	1	1	0	0



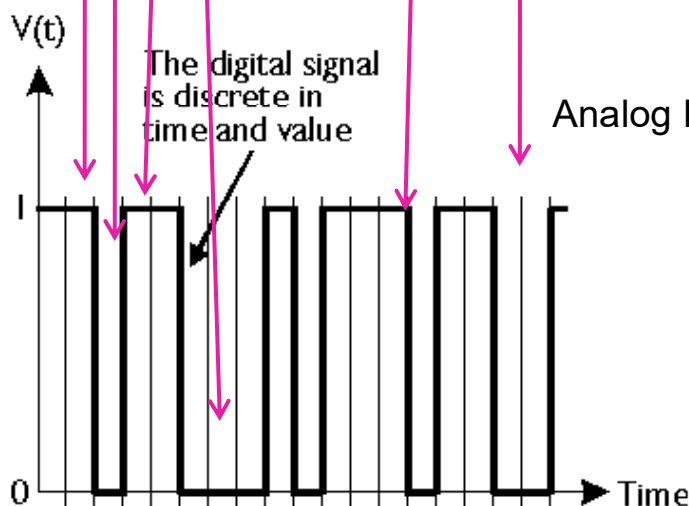
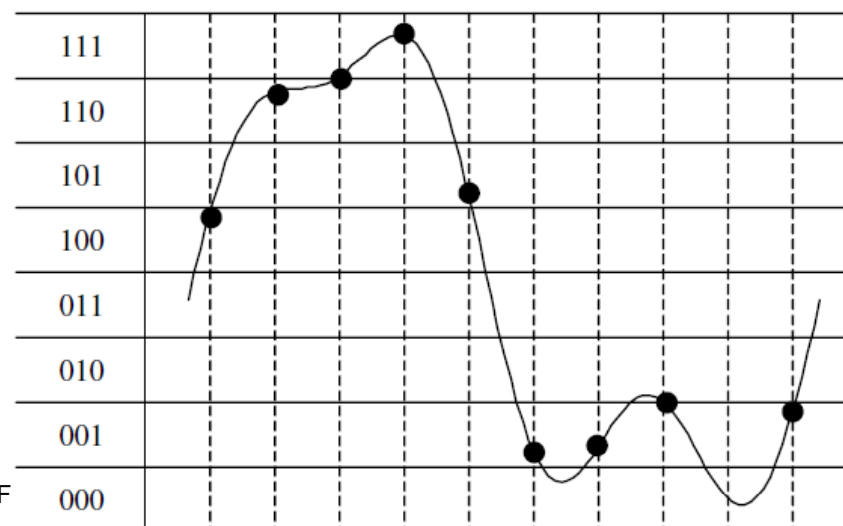
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Sampling and **Quantization**-How to represent real-valued (X&Y) signals as bits?
Quantization and Encoding

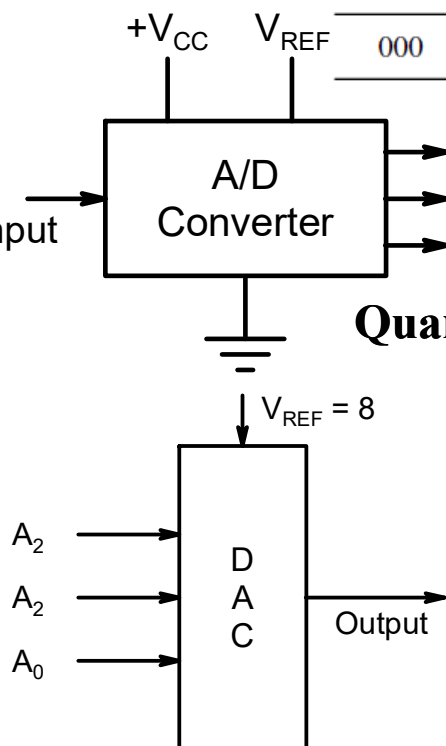


Analog to Digital Converter (ADC)

Resolution = 3 bits;
1 LSB =
 $V_{REF}/2^N = 1V$



$$V_0 = \frac{V_{REF}}{2^3} \times (A_2 2^2 + A_1 2^1 + A_0 2^0)$$



Quantization error

So 101 gives
5 x 1 = 5V

- $0V < V_{in} < 1V \rightarrow 000$
- $1V < V_{in} < 2V \rightarrow 001$
- $2V < V_{in} < 3V \rightarrow 010$
- $3V < V_{in} < 4V \rightarrow 011$
- $4V < V_{in} < 5V \rightarrow 100$
- $5V < V_{in} < 6V \rightarrow 101$
- $6V < V_{in} < 7V \rightarrow 110$
- $7V < V_{in} < 8V \rightarrow 111$



ESc201, Lecture 37: Digital counters and counting-ADC

Error can be as large as 1V or 1LSB

$0V < V_{in} < 1V \rightarrow 000$

$1V < V_{in} < 2V \rightarrow 001$

$2V < V_{in} < 3V \rightarrow 010$

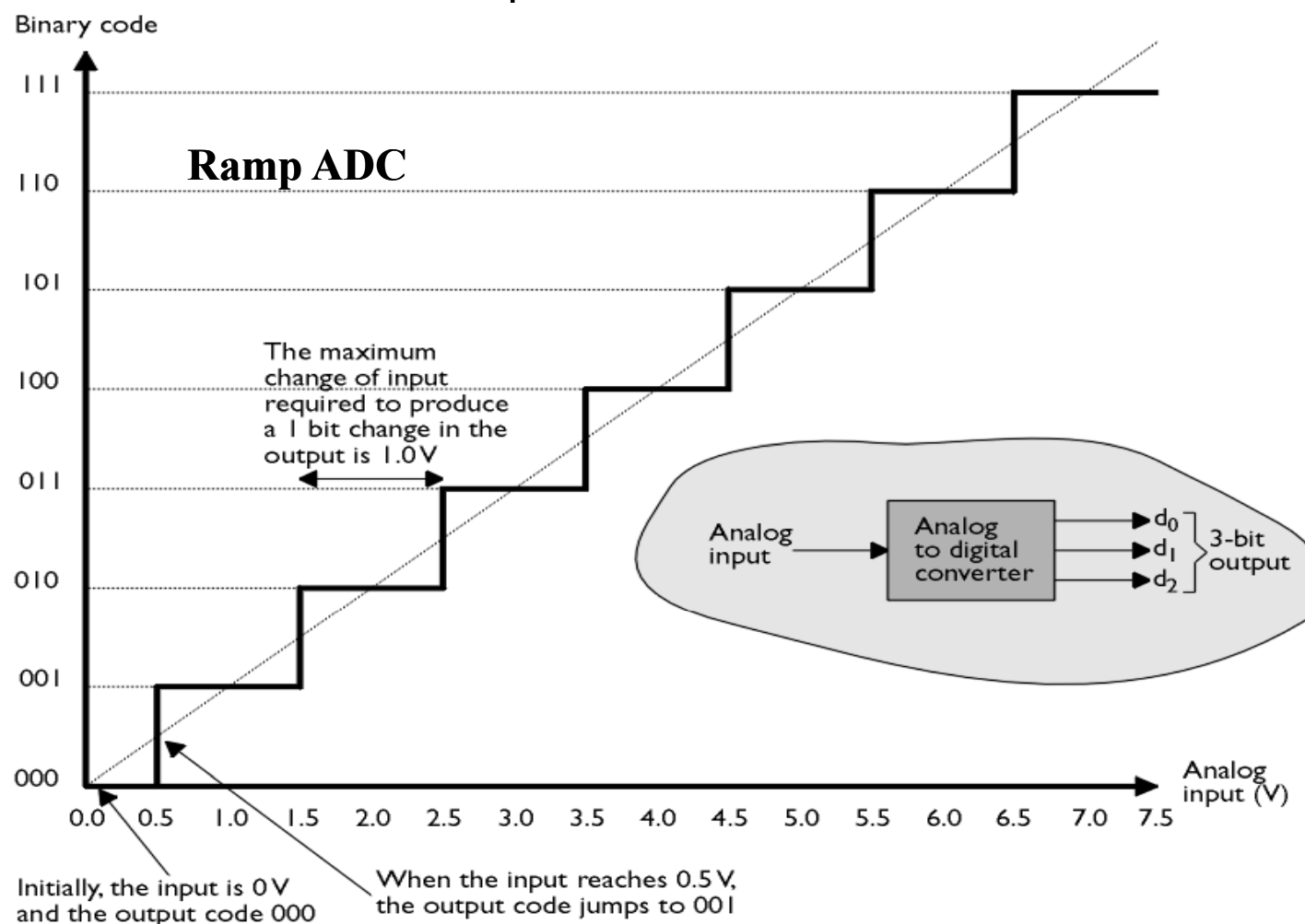
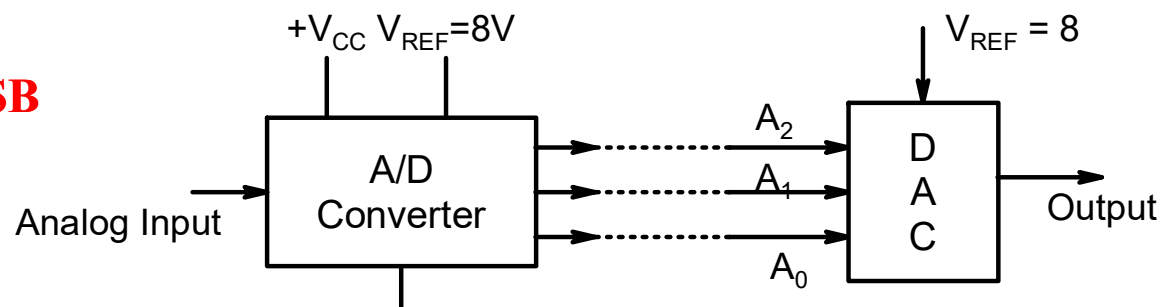
$3V < V_{in} < 4V \rightarrow 011$

$4V < V_{in} < 5V \rightarrow 100$

$5V < V_{in} < 6V \rightarrow 101$

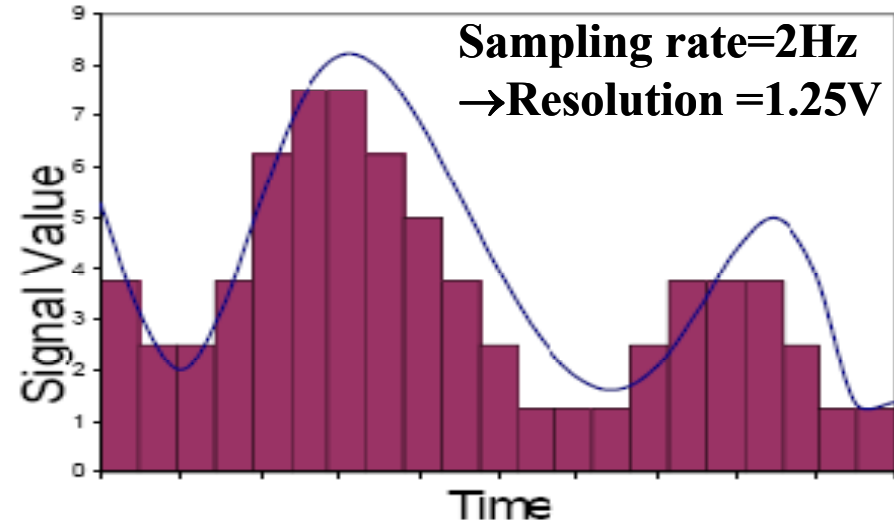
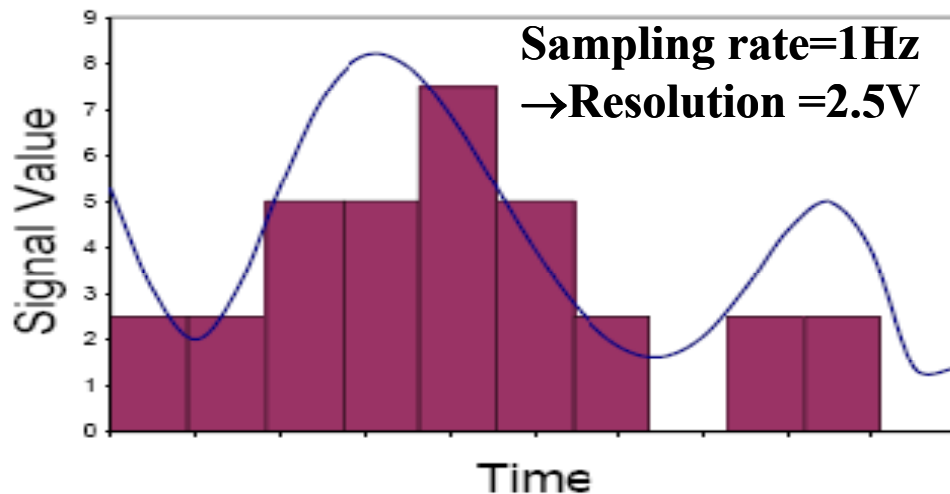
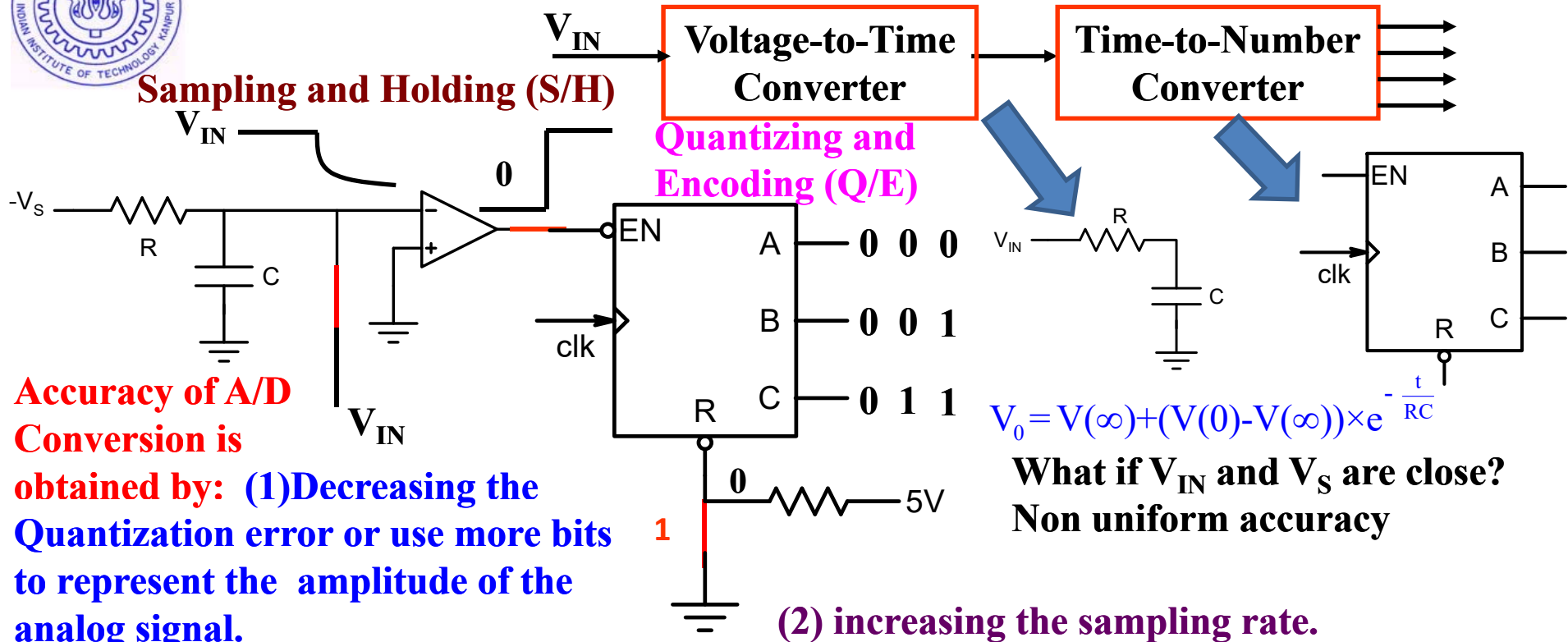
$6V < V_{in} < 7V \rightarrow 110$

$7V < V_{in} < 8V \rightarrow 111$





ESc201, Lecture 36: Digital counters and counting-ADC



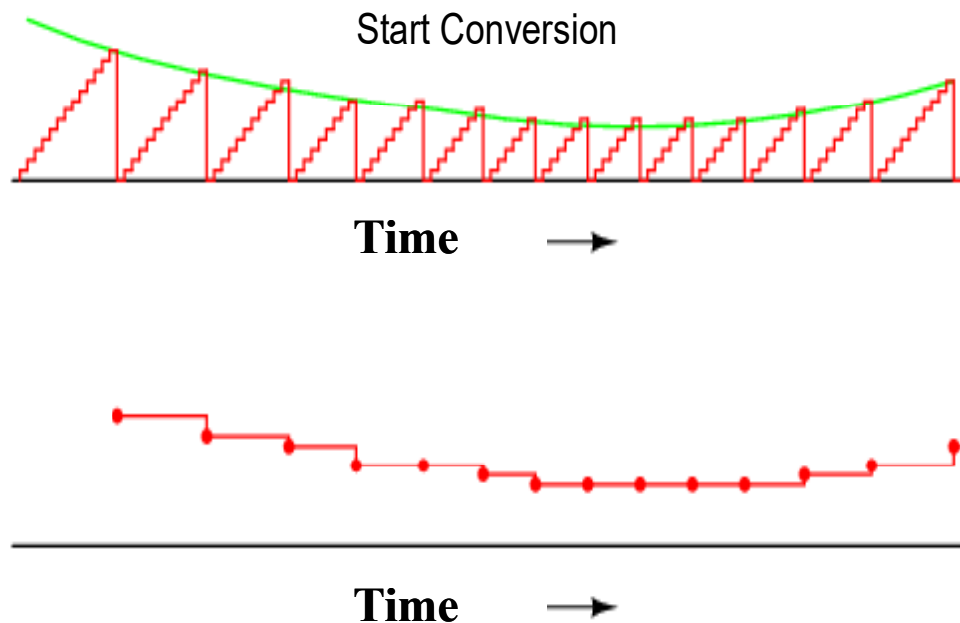
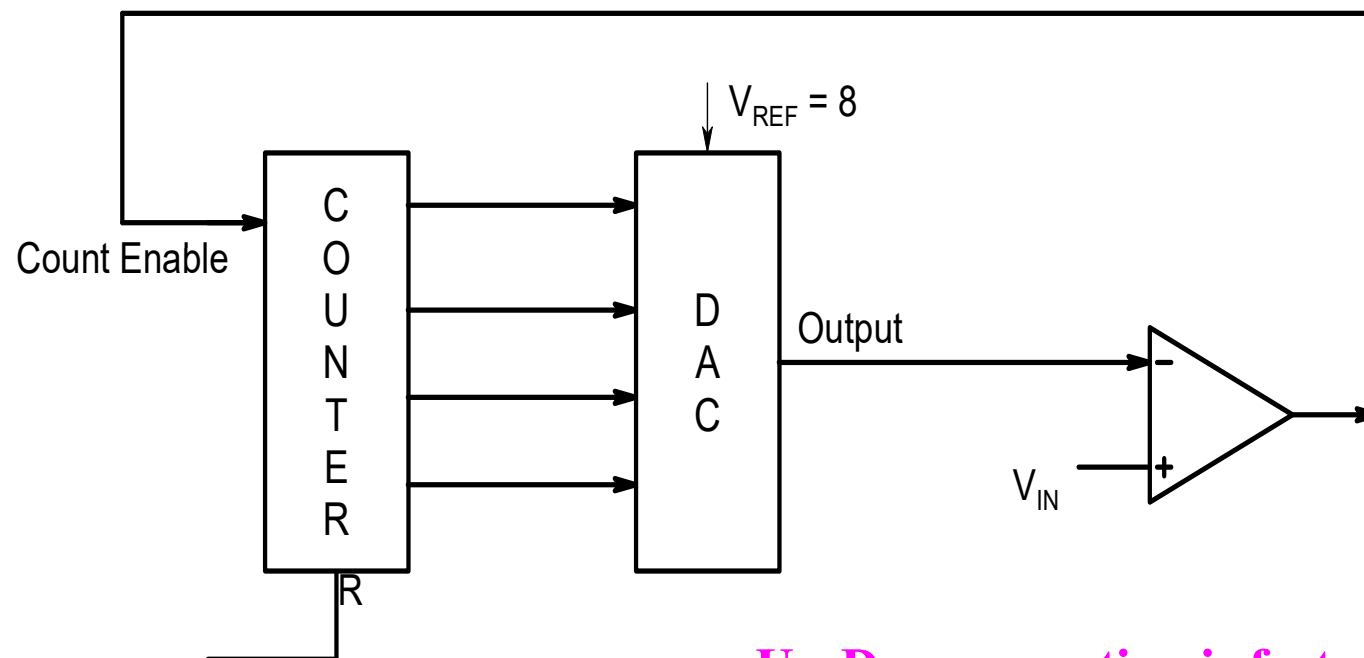


ESc201, Lecture 37: Digital counters and counting-ADC

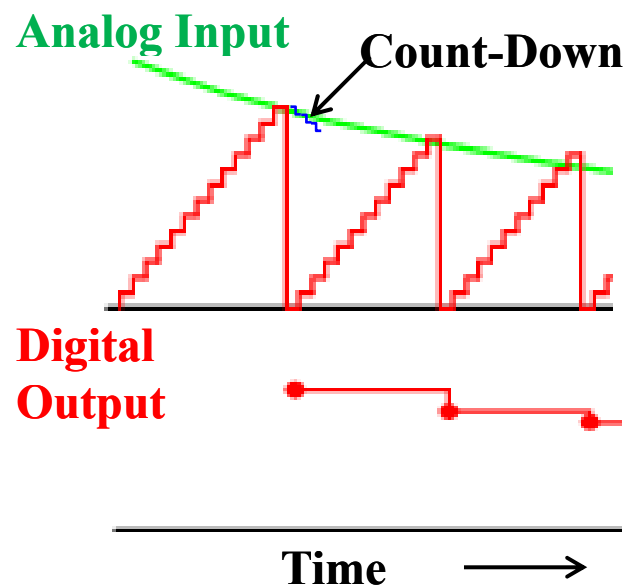
**Digital word
corresponding
to 1.2V is 0010**

**Worst case
conversion
time is 8 clock
periods**

Analog Input



Up-Down counting is faster





ESc201, Lecture 37: Digital counters and Dual Slope ADC

Integrates an unknown input voltage (V_{IN}) for a fixed time (T_{INT}), and then "de-integrates" (T_{DEINT}) using a reference voltage (V_{REF}) for a variable time.

Fundamental components :

- 1) Integrator
- 2) Electronic Switches
- 3) Counter
- 4) Clock
- 5) Control Logic
- 6) Comparator

At $t < 0$, S_1 is set to ground, S_2 is closed, and counter=0.

1) At $t=0$ a conversion begins and S_2 is open, and S_1 is set so the input to the integrator is V_{IN} .

2) S_1 is held for T_{INT} which is a constant predetermined time interval.

3) When S_1 is set the counter begins to count clock pulses, the

counter resets to zero after T_{INT} .

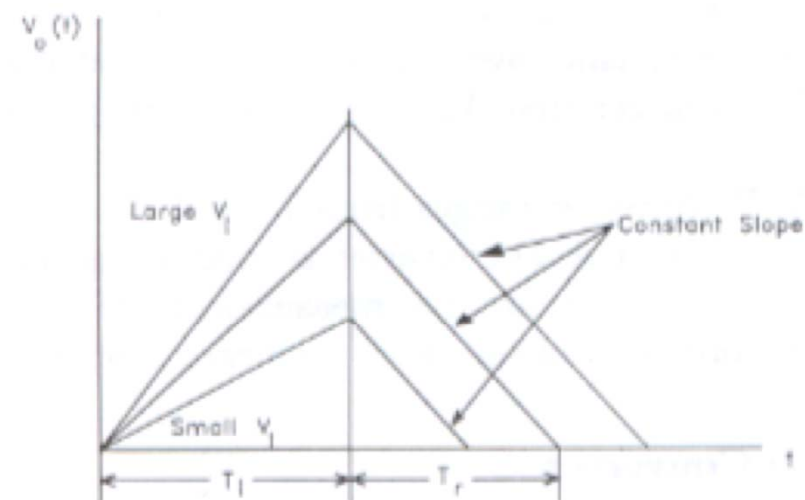
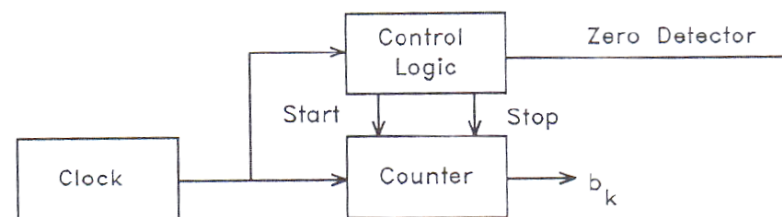
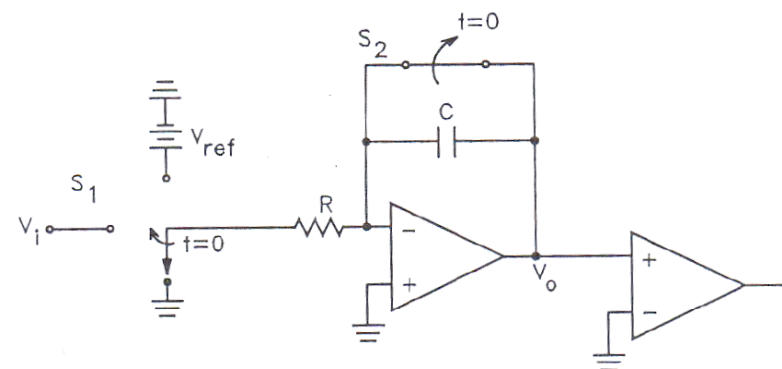
4) V_{out} of integrator at $t=T_{INT}$ is $(V_{IN}T_{INT}/RC) \propto V_{IN}$

5) At $t=T_{INT}$ S_1 is set so $-V_{REF}$ is the input to the integrator which has the voltage $V_{IN}T_{INT}/RC$ stored in it.

6) The integrator voltage then drops linearly with a slope $-V_{REF}/RC$.

7) A comparator is used to determine when the output voltage of the integrator crosses zero

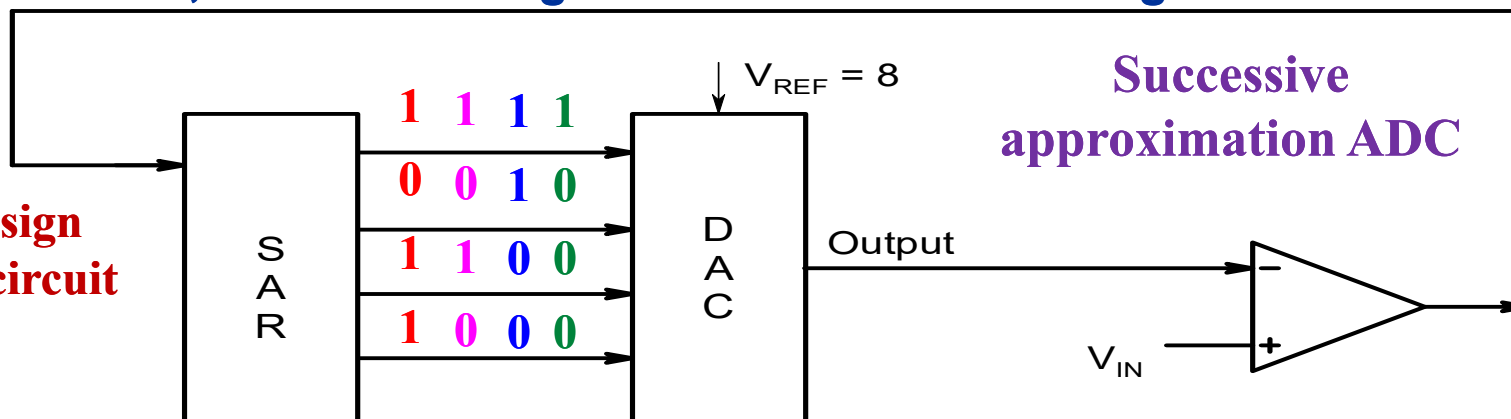
8) When it is zero the digitized output value is the state of the counter





ESc201, Lecture 36: Digital counters and counting-ADC

To do: Design the logic circuit for SAR



Type	Speed (relative)
Dual Slope	Slow
Flash	Very Fast
Successive Approximation	Medium – Fast
Type	Cost (relative)
Dual Slope	Med
Flash	High
Successive Approximation	Low

