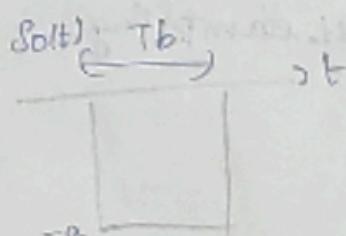
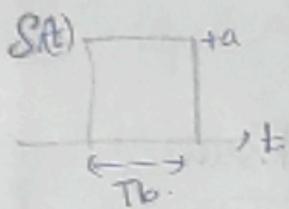


12/08/12

## Digital Communication:

- We try to map 0,1 into well defined waveforms.
- Binary Communication System:-

$$\text{Map } \{0,1\} \text{ go } \{S_0(t), S_1(t)\}$$



where  $T_b$  = Bit Duration

$$R_b = \frac{1}{T_b} = \text{Bit Rate} \quad (\text{bit/sec})$$

- It is not necessary rectangular waveform but it's the convention.
- Receiver has to take decision on the received system.
- The receiver must know the  $S_0(t)$ ,  $S_1(t)$ .
- The distortion may appear, the receiver must have idea of it.

Digital modulation = Signal Mapping [Signalling]

- Usually  $m(t)$  can be of any shape in AM waves, so receiver has to decode from an infinite set. Since message signal is continuous signal.
- But here, finite symbol set [symbol waveform] (so only receiver chooses from  $S_0(t)$  or  $S_1(t)$ )

M-ary Modulation  $M=4$

Symbol = Waveform

$$00 \rightarrow S_1(t) \quad 01 \rightarrow S_2(t) \quad 10 \rightarrow S_3(t) \quad 11 \rightarrow S_4(t)$$

{  $S_1(t)$ ,  $S_2(t)$ ,  $S_3(t)$ ,  $S_4(t)$  }

Any non-binary modulation  $\rightarrow$  P-ary modulation

Data is represented in binary format.

Message m(t) is encoded using Binary set {0, 1}

(waveform encoding)

Waveform encoding:

2. Quantization      3. Sampling

Last seen

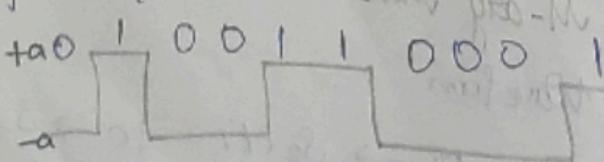
$$\text{Bit Rate} = \frac{\text{Sampling frequency}}{\text{per sample}} \times \text{No. of samples per bit}$$
$$= 3F_s$$

Continuous signal  $\rightarrow$  Sampling  $\rightarrow$  Quantization  $\rightarrow$  Digital signal

So we go ahead with Digital signal.

Map {0, 1} to {S<sub>0</sub>(t), S<sub>1</sub>(t)}

$\Rightarrow$  Transmitted signal



$\Rightarrow$  signal distorted?  
by channel

[Bandwidth limitation]

- In case of ideal channels there is uniform attenuation of  $25\%$  is given to every freq. so only amplitude changes, the signal shape remains same

$\Rightarrow$  signal distorted?

by channel + noise

This noise is usually white noise

$\Rightarrow$  signal detected

by receiver

Analog vs Digital

• Repeater in Analog Modulation AM

\* As the signal is transmitted, Received signal loses

As power, as power  $\frac{Pc^2}{2}$  signal is maintained.

$\Rightarrow$  As Received signal is weak

$\Rightarrow$  Change in shape of signal

$\Rightarrow$  Addition of noise (white noise) for end result

- In order to overcome these issues, Radio uses modulation and amplification.

Amplification of signal leads to unintentional amplification of the [in band noise]

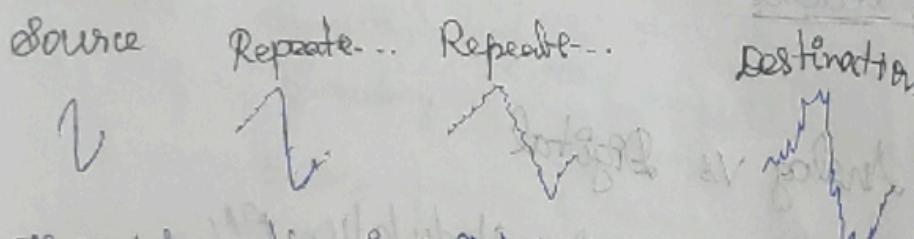
This is because the noise is white noise so it has all frequency.

Let My required freq be 200M-200.5TH Hz

then white noise has 200M-200.5TH Hz also  
So, the ~~base~~ noise gets amplified

This is called in band noise.

Analog Long-Distance communication



This deterioration is reflected due to long distance transmission

- But as distance is large, the received signal is very weak, noise is too loud, so decision can be wrong.
- So Reduce distances,  
This can be done by Regenerative Repeaters

Source → Regenerator ... Regenerator → Destination

- Decision on received symbol
  - Regeneration of signal at the repeater
- ⇒ Performance dependent of the signal over distance, i.e.  
regenerative repeaters.

Advantages of Digi Com:-

- Regenerative Repeaters
- Flexibility of implementation
- Privacy & Security through encryption
- Error detection & correction
- Multiplexing of heterogeneous signals.

Disadvantages:-

- Higher Bandwidth requirement
- Complex synchronization techniques

⇒ Bandwidth, & Bitrate  
& Kind of Modulation.

13/08/2020

- 0, 1 are abstract, so they need a physical form.  
So their waveform should match spectra of existing  
How does it transmit bits over wires/hornets?

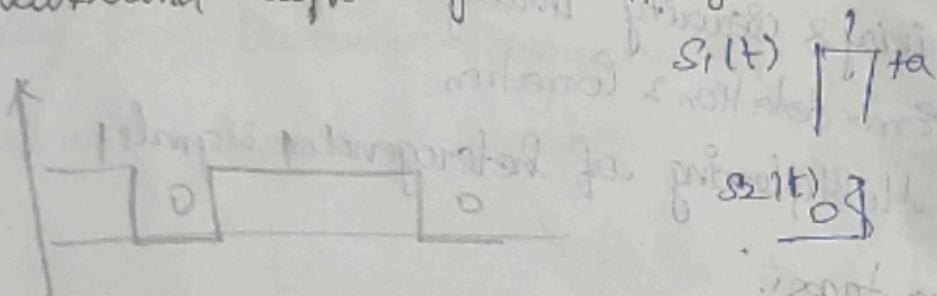
Maps the bits to waveform → Signalling

→ Baseband signalling [Lectures]

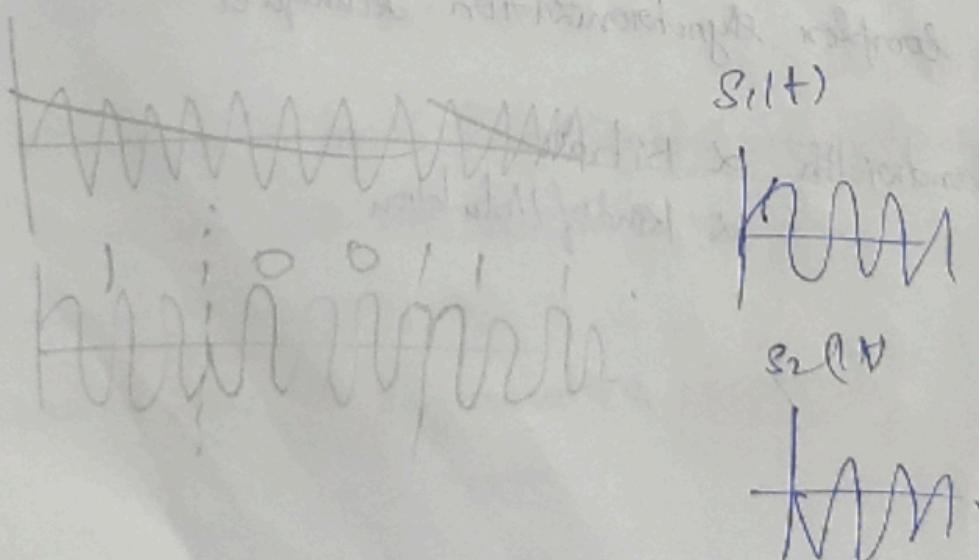
→ Bandpass

Both require Mapping

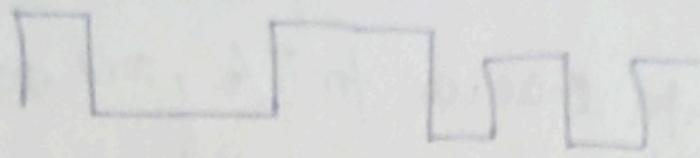
Baseband signalling (Mapping)



Bandpass signalling (Mapping)!



## Baseband vs. Passband



~~MWMMWMWMW~~

Baseband

$$1 \rightarrow S_1(t)$$

$$0 \rightarrow S_2(t)$$

$$\overline{S}_1(t)_{DV}^{+A}$$

$$\underline{S}_2(t)$$

$$S_1(t) = \text{Infinite poss. but mostly } 0$$

$$S_2(t) = 0.$$

Tower transfu.

Passband

$$1 \rightarrow S_1(t)$$

$$0 \rightarrow S_2(t)$$

$$\overline{S}_1(t)_{DV}^{+AV}$$

$$\overline{S}_2(t)_{DV}^{+P}$$

By Fourier transform

Sinc function

Fcc) have much much  
less more than bandwidth.  
Carrier freq is going to be high

filn codes (Baseband Signalling)

Unipolar non return to zero.

1 1 1 0 0 1 0 1 1 0 0 0

+a	+a	+a	0	0	+a	0	+a	+a	0	0	0
----	----	----	---	---	----	---	----	----	---	---	---

$\Rightarrow$  It will be +a for the whole duration. + On off NRZ

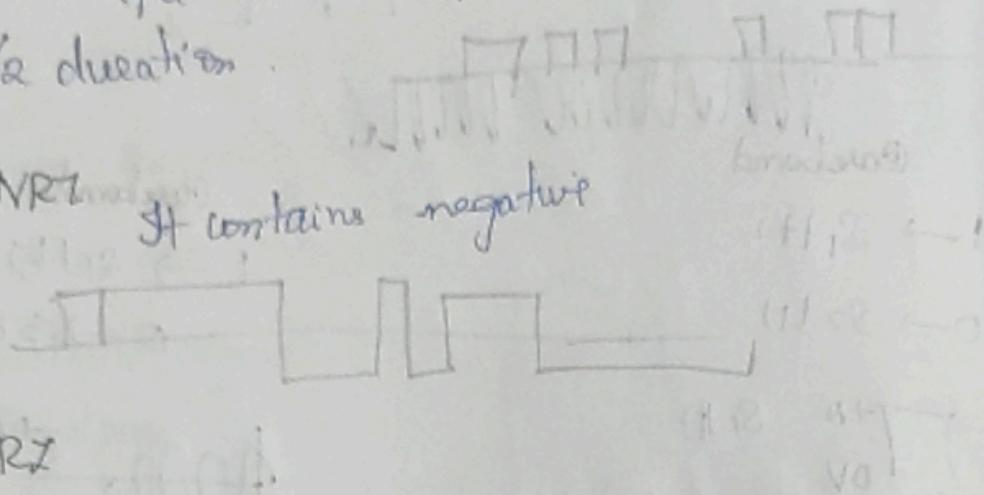
Unipolar RZ.

It increases for  $T/2$ , and decreases for  $T/2$  duration.

Polar NRZ

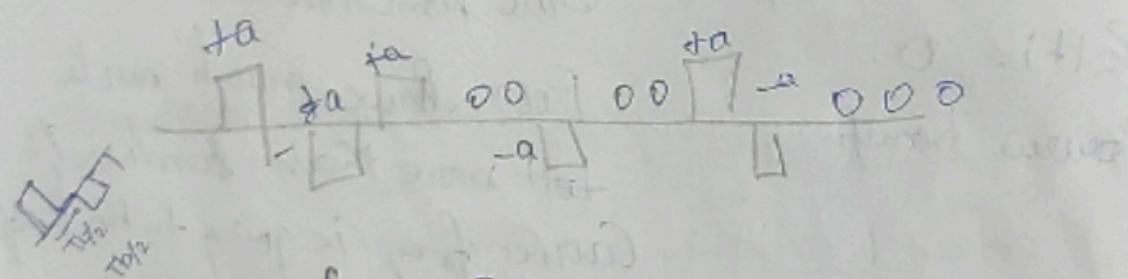
It contains negative

Polar RZ



Bipolar IAM/RZ

Alternate Mark Inversion (RZ)

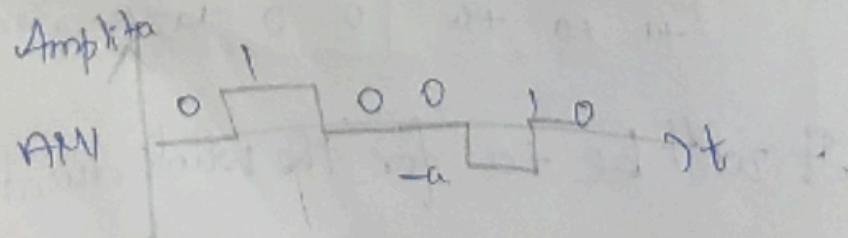


0  $\Rightarrow$  always 0

1  $\Rightarrow$  is preceding ta then -a, ta, -a.

B. Forbidden component =  $+a, +a, -a, -a$

Bipolar NRZ AMI



8p(t) Edge code

Manchester:-

100110

1  $\Rightarrow$  positive, then negative

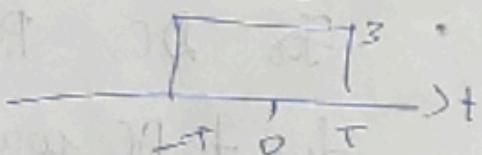
0  $\Rightarrow$  negative to positive

Desirable Properties of Linecode

- Low Transmission Bandwidth
- Favourable Power Spectral Density
- High power Efficiency
- Error detection & correction capability
- Adequate Timing Content
- Homecoming

$\Rightarrow$  Deterministic Signal:

$$\text{ex: } x(t) = e^{-2t}$$



$\Rightarrow$  Random Process:

ex: Statistical Laws of Speech Signals

Frequency Domain Characterization

$$x(t) \quad x(f) = \int_{-\infty}^{\infty} x(t) e^{-j2\pi ft} dt.$$

Random Process  $X(t)$

Autocorrelation Function  $R_x(t)$

and Power Spectral Density  $S_x(f)$

from a Fourier Transform pair

$$S_x(f) = \int_{-\infty}^{\infty} R_x(t) e^{-j2\pi f t} dt$$

$S_x(f)$  = Watts per Hertz

square of the magnitude of fourier  
transform

Power Spectral Density:

How A power of signal is distributed over various frequencies.

Favorable Power Spectral Density:

- Low transmission bandwidth
- For DC, PSD = 0 due to AC coupling of transformers used in repeaters. Significant power in low-freq component causes d.c. wander in pulse sync stream when ac
- AC coupling is required because dc paths provide by cable pairs between repeaters after which are used to transmit power required for repeaters

Power Efficiency:

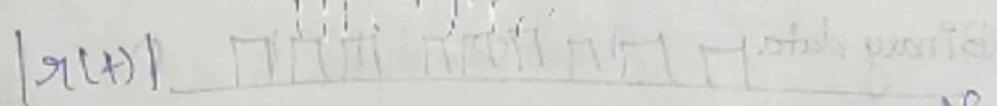
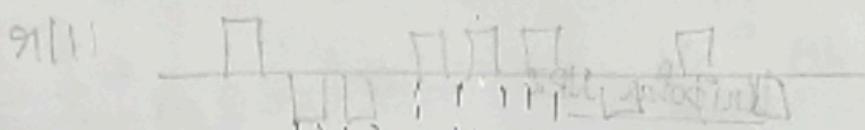
- For a particular data-rate or bit-rate

Adequate Timing Content:-

The line code should have extractable clock information from signal

Timing Signal:-

- We want to be able to easily extract the timing information from the signal.
- Consider the polar RL 2H).



Extract the clock. Extracted must exactly be synchronised with the transmitted clock

→ We get that by taking absolute value of signal

Manchester codes contain transitions in every bit

is very good for clock extraction.

- NRZ codes can be more problematic. Long strings of 1's or 0's can cause a loss of synchronization.



Transparency:

- As a linecode in which the bit pattern does not affect accuracy of timing.

(Ex:) NRZ is not transparent to long string of 0's.

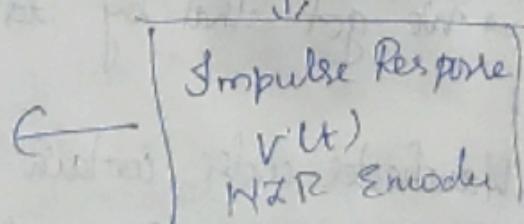
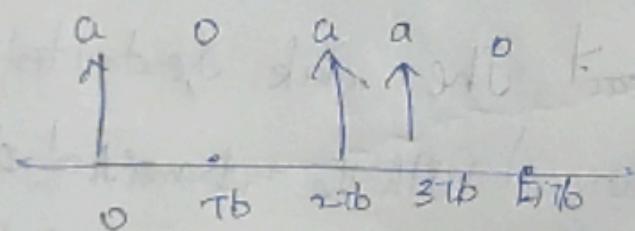
Ques 1.

### Unipolar NRZ

Binary data

1 0 1 1 0

$A_k =$



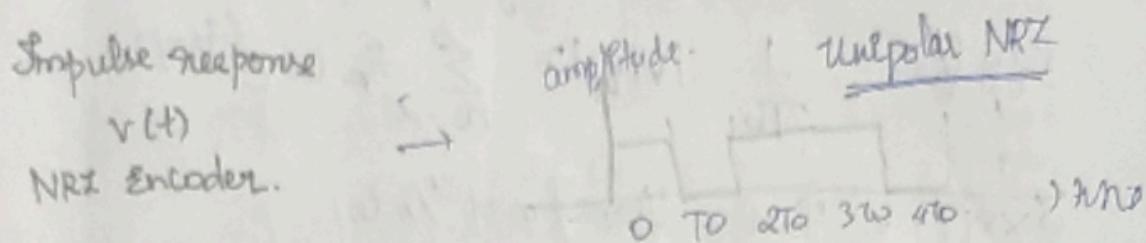
Then it is mathematically represented as

$$a_8(t) + 0_8(t-Tb) + a_8(t-2Tb) + \\ a_8(t-3Tb) + 0_8(t-4Tb)$$

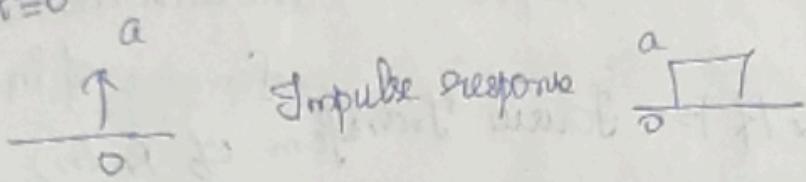
Since amplitude keeps changing let's the  $A_k$

where  $A_k = 0/1$

then Input data  $x(t) = \sum_{k=-\infty}^{\infty} A_k v(t-kT_b)$



The impulse response of the is response of a system applied at  $t=0$



$\delta(t)$   $\quad$  Impulse Response  $v(t)$

Input  $\sum_{k=-\infty}^{\infty} A_k \delta(t-kT_b) \longrightarrow \sum_{k=-\infty}^{\infty} A_k v(t-kT_b)$

This is just a simple convolution,

$$= \sum A(kT_b) * v(t-kT_b)$$

It's a convolution random process with deterministic wave for  
 $A_k * v(t)$

Power spectral Density

$$g(f) = S_{gg}(f) = |V(f)|^2 S_{xx}(f)$$

$\Rightarrow$  Power spectral density of input,

$$S_{xx}(f)$$

PSD of output  $S_{yy}(f) = |H(f)|^2 S_{xx}(f)$

$V(t) =$  Frequency Response of Filter,  
The input is a random binary sequence

$$S_{gg}(f) = \frac{1}{T_b} |V(f)|^2 \sum_{n=-\infty}^{\infty} R_A(n) e^{(j2\pi f T_b)}$$

$S_{xx}(f)$  = Fourier Transform of  $R_A(n)$

$R_A(n)$  = discrete time signal = Fourier transform of the autocorrelation

$S_{xx}(f)$  = Fourier transform of input (of  $R_A(n)$ )

$$|V(f)|^2 = T_b^2 \operatorname{sinc}^2(\pi f T_b)$$

Fourier of  $V(t)$  = sine function

$\Rightarrow$  Now find Autocorrelation function

Autocorrelation Sequence  $R_A(n)$

0 a 0 0 a 0 a a a 0 a 0 0

$$R_A(n) = E(P_k A_{k+n})$$

$$R_A(0) = E(P_k^2) = \sum_{k=1}^2 (P_k)^2$$

$$= P(A_k=0)0^2 + P(A_k=a)a^2$$

$$= \frac{1}{2} \times 0 + \frac{1}{2} a^2 = \frac{a^2}{2}$$

Autocorrelation means each possibility has the same probability. In the seq

0 a 0 0 a 0  $\alpha$  a a a 0 a 0 0

$$p(0) = p(1) = \frac{1}{2}$$

$$R_{XX}(0) = E[X(t)X(t+0)]$$

$$\Rightarrow E(X^3) = \int x^3 f_x(x) dx.$$

$$\text{Why } E(P_k^3) = \sum_{k=1}^2 (P_k P_{k+1}^2)$$

$$= P(A_k=0) 0^2 + P(A_k=a) a^2$$

$$= \frac{1}{2} 0^2 + \frac{1}{2} a^2 = \frac{a^2}{2}$$

$$\text{Why } R_{PA}(1) = E(P_k P_{k+1})$$

We also know  $R_{PA}(1) = R_{PA}(-1)$  since it's symmetric.

So  $E(P_k P_{k+1})$  Possible combination

4 combination,  $\sum P(P_k P_{k+1})$ ,  $P_k P_{k+1}$

Then this is the joint probability of  $A_k, A_{k+1}$

$$P(A_k A_{k+1}) = \frac{1}{4} \quad \text{because } P(A_k) * P(A_{k+1})$$

$$= \frac{1}{2} * \frac{1}{2}$$

$$= \frac{1}{4}$$

$$R_{PA}(1) = \sum P_k P_{k+1} P(A_k A_{k+1})$$

$$= a \cdot 0 \cdot \frac{1}{4} = 0$$

for 00

$$= 0 \cdot a \cdot \frac{1}{4} = 0$$

0a

$$= 0 \cdot 0 \cdot \frac{1}{4} = 0$$

00

$$= a \cdot a \cdot \frac{1}{4} = a^2 / 4$$

aa

Summing all this =  $R_{AA} = \frac{a^2}{2}$   
 $R_{A(1)} = \frac{a^2}{4}$

then  $R_{A(-1)} = \frac{a^2}{4}$

$R_A(2)$

Autocorrelation  $A_k, A_{k+2},$

1st + 3rd bit > 3rd bit probability 0 or 1  
 $\Rightarrow 0.5$

so simple results are obtained  
 $\Rightarrow R_A(n) = \frac{a^2}{4}$

Thus  $R_{AA}(n) = \frac{a^2}{4}$  for  $n \neq 0.$

$$R_A(0) = \frac{a^2}{2}$$

$$\Rightarrow |V(f)|^2 = Tb^2 \sin^2(\pi f Tb)$$

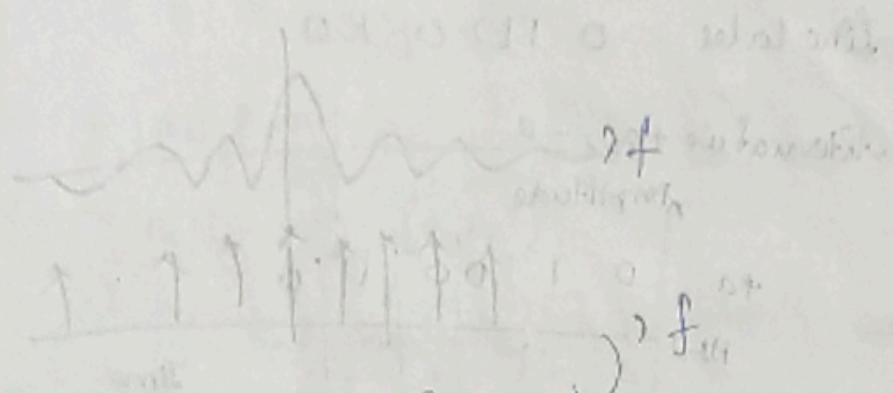
$$S_{GG}(f) = \frac{1}{Tb} |V(f)|^2 = \sum_{n=-\infty}^{\infty} R_A(n) e^{-j2\pi nf Tb}$$

$$S_{GG}(f) = \frac{1}{Tb} Tb^2 \sin^2(\pi f Tb) \left[ \frac{a^2}{4} + \sum_{n=1}^{\infty} e^{-j2\pi nf Tb} \right]$$

$$= \frac{a^2}{4} Tb \sin^2(\pi f Tb) \left\{ 1 + \sum_{n=1}^{\infty} e^{-j2\pi nf Tb} \right\}$$

$$= \frac{a^2}{4} Tb \sin^2(\pi f Tb) \left\{ 1 - (-1)^{\lfloor f \rfloor} \right\}$$

Consider two functions of freq.  $f(t)$



When 0 in sinc, value in the positive step  
value in step, 0 in step

Except at  $f(0)$ , = value 1 or 0

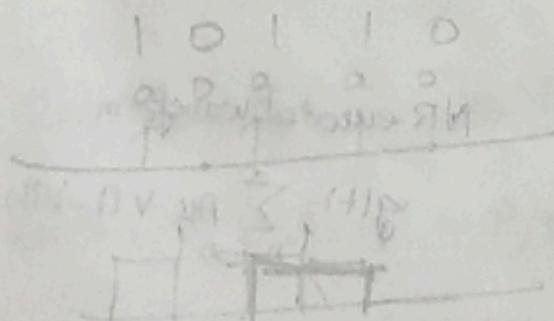
PSD of ~~the~~ unipolar NRZ waveform:

Bandwidth =  $\frac{2f}{T_b}$  DC Component.

$$PSD = \frac{\alpha^2}{4} T_b \operatorname{sinc}^2(f T_b) + \frac{\alpha^2}{4} S(f)$$

10/08/2020

Unipolar no-return-zero



Input data:

$$\sum_{k=-\infty}^{\infty} A_k \delta(k - k T_b) v_k$$

NET encoded  $g(t)$

$$= \sum_{k=-\infty}^{\infty} A_k v_{k T_b} \delta(k T_b)$$

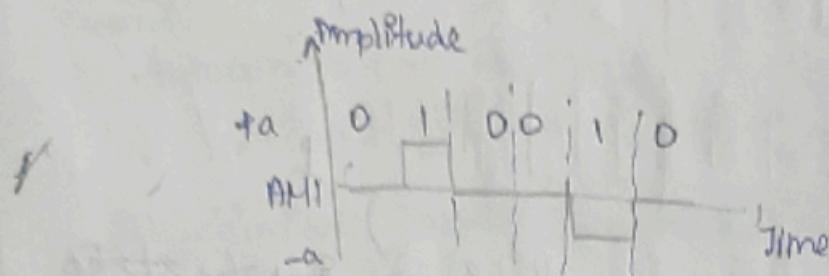
$$\Rightarrow \int g(t) dt = (f) g(t)$$

11/01/20

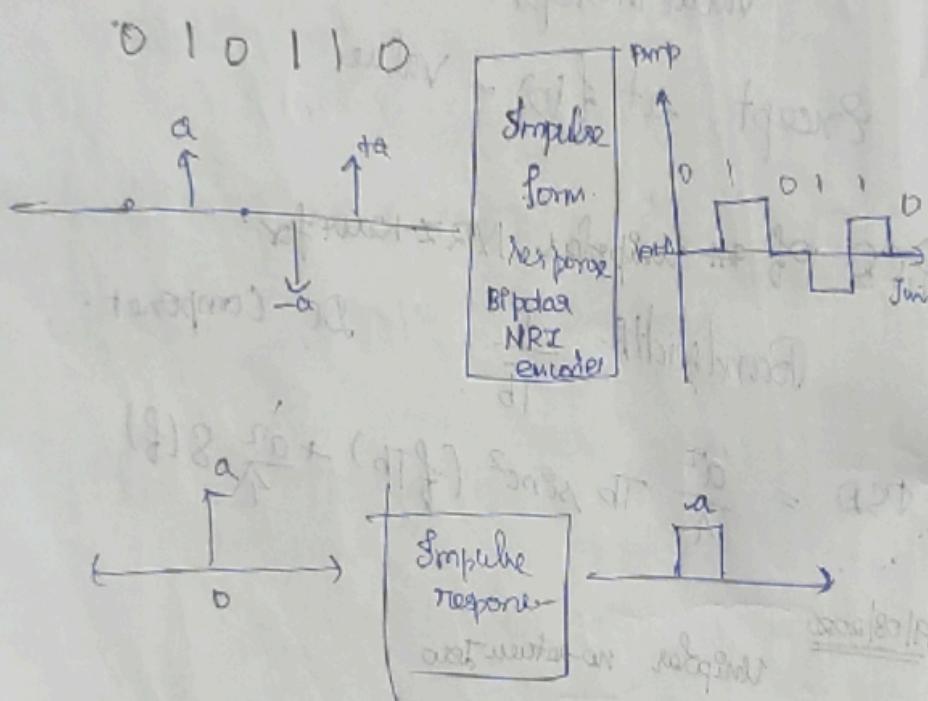
Bipolar Non return to zero

Line code 0 1 0 0 1 0

Alternative to  $+a, -a$



Data



Input data

$$x(t) = \sum_{k=-\infty}^{\infty} A_k \delta(t-kT_b)$$

NR encoded waveform

$$g(t) = \sum_{n=-\infty}^{\infty} A_k V(t-kT_b)$$

Power Spectral Density:

$$S_{gg}(f) = \frac{1}{T_b} |V(f)|^2 \sum_{n=-\infty}^{\infty} R_n e^{-j2\pi f T_b}$$

Autocorrelation equations:

$$0 \quad 0 \mid e^{-\frac{t}{T}} \quad \dots \quad \text{etc}$$

$$R_A(n) = E[A_k A_{k+n}] = (1-p) \cdot \frac{p}{2} + p \cdot \frac{1}{2} =$$

$$R_A(0) = \sum [A_k^2] = \sum_{k=1}^2 [P_k A_k^2]$$

$$= \frac{1}{2} D + \frac{1}{4} a^2 + \frac{1}{4} - a^2$$

$$\Rightarrow -\frac{a^2}{2} \Rightarrow a^2/2$$

III hz

$$R_A(1) = \sum [A_k A_{k+1}] \quad R_A(1) = R_B(-1)$$

Possible combinations:-

$$DD \rightarrow 0 \quad a-a$$

$$DA \rightarrow 0-a \quad -aa$$

$$DD \rightarrow a-a \quad (-a-a)$$

$p(A_k A_{k+1})$

$$R_A(1) = \sum p(A_{k+1}) P(A_k, A_{k+1})$$

$$\begin{aligned} \Rightarrow D \cdot D \cdot \frac{1}{4} &= 0 & a-a \\ DA \cdot \frac{1}{8} &= 0 & a-a \times \frac{1}{16} = -a^2/16 \\ D \cdot -a \cdot \frac{1}{8} &= 0 & -a \cdot a \times \frac{1}{16} = -a^2/16 \\ DA \cdot \frac{1}{8} &= 0 & -a \cdot -a \times \frac{1}{16} = a^2/16 \\ -a \cdot -a \cdot \frac{1}{8} &= 0 & \end{aligned}$$

$$R_A(1) = -a^2/4 \quad R_A(-1) = a^2/4$$

$$R_A(2) = E[A_k A_{k+2}] = -a^2/4$$

$$|V(f)|_2 = Tb^2 \sin^2 C(\pi f T b)$$

$$S_{gg}(f) = \frac{1}{Tb} |V(f)|_2^2 \sum_{k=-\infty}^{\infty} R_A(k) e^{j2\pi f k T b}$$

$$= \frac{1}{Tb} Tb^2 \sin^2(\pi f Tb) \left[ \frac{a^2}{2} + \frac{-a^2}{48} \sum_{n=0}^{\infty} e^{-j2\pi fn Tb} \right]$$

$$\cancel{\frac{a^2}{2}} Tb \sin^2(\pi f Tb) - \cancel{\frac{a^2}{84}} \cancel{8(f)} \quad [ ]$$

So, probability  $\Rightarrow \frac{1}{4} : \frac{1}{2} = \frac{1}{8}$ , because it's a

conditional probability  $= P(A|E) \cdot \frac{P(A^{k+1})}{P_k}$

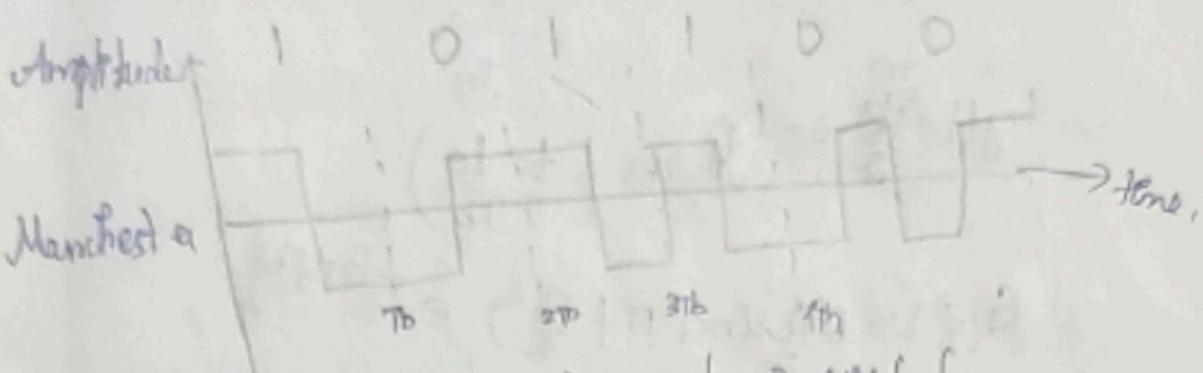
$$\frac{1}{4} \cdot \frac{1}{2}$$

$$f_A(n) = 0$$

$$\log(f) =$$

20/08/2020

## Manchester Coding:-

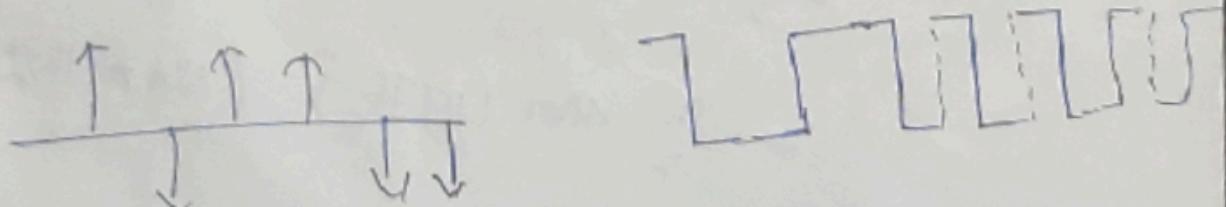
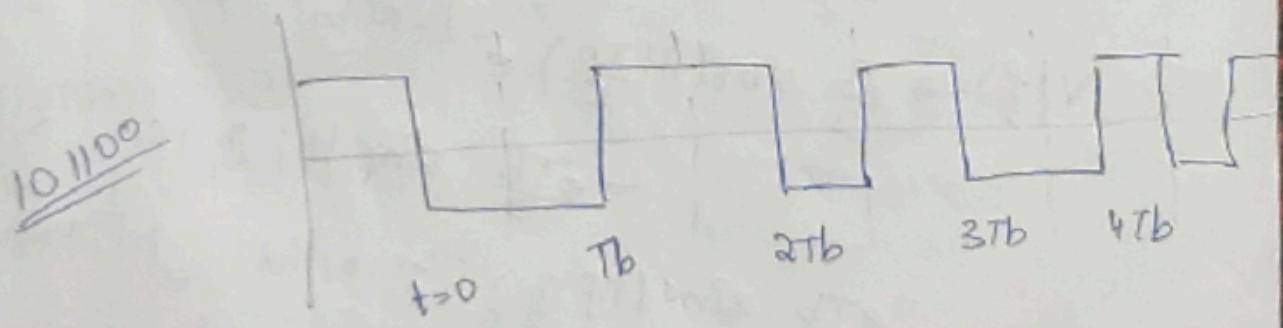
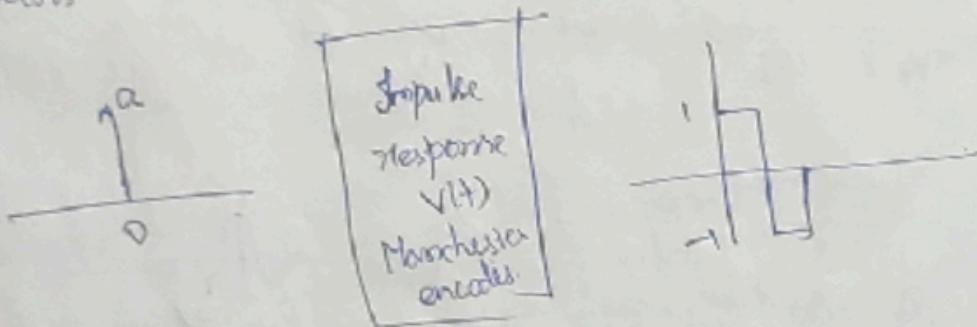


As transitions occurs, this coding is useful.

to determine by sampling,  $+ + \rightarrow 1$  But it is important  
 $- + \rightarrow 0$  to know starting point

But if there is a delay, then tapping signal is hard.

But in Manchester coding,  $+ -$  samples that enables to detect errors.



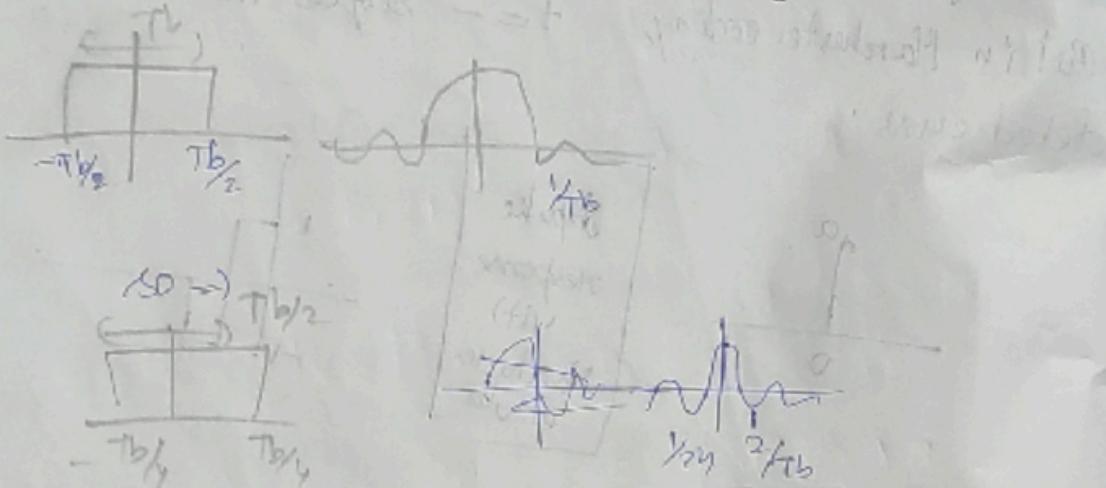
$$V(f) = ?$$

$$g(t - \frac{T_b}{2}) = A \cos\left(\frac{t - \frac{T_b}{2}}{T_b}\right)$$

$$G(f) = P T_b \operatorname{sinc}(\pi f T_b) e^{-j 2 \pi f T_b}$$

Let  $\square \Rightarrow P(t) \Rightarrow \square \Rightarrow P(t + \frac{T_b}{4}) - P(t - \frac{T_b}{4})$

$$V(t) = P\left[t + \frac{T_b}{4}\right] - P\left[t - \frac{T_b}{4}\right]$$



$$\Rightarrow V(f) = \frac{P T_b}{2} \operatorname{sinc}(\pi f T_b) e^{-j 2 \pi f T_b} - \frac{P T_b}{2} \operatorname{sinc}(\pi f T_b) e^{j 2 \pi f T_b}$$

$$= \frac{P T_b}{2} \operatorname{sinc}(\pi f T_b) \frac{e^{-j 2 \pi f T_b} - e^{j 2 \pi f T_b}}{2j}$$

$$= \frac{P}{2} \operatorname{sinc}(\pi f T_b) ((\sin \pi f T_b))^2$$

$$= T_b$$

$$R_A(0) = ?$$

$$R_A(n) = \mathbb{E}[A_k A_{k+n}]$$

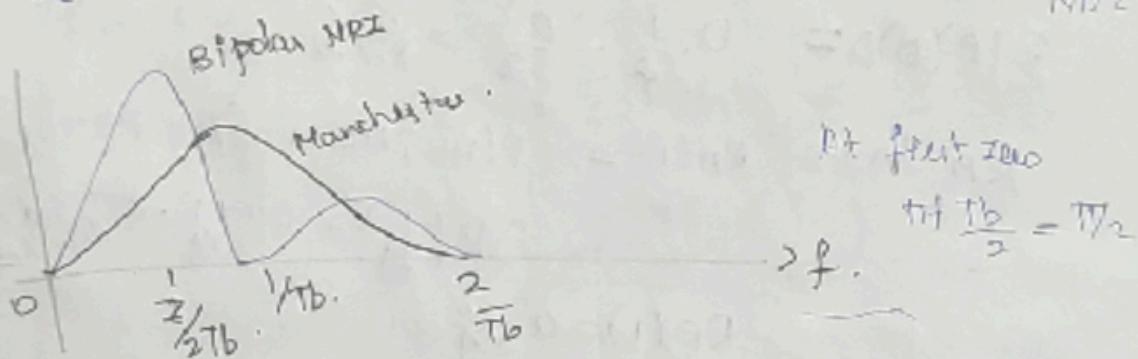
$$R_A(n) = \sum_{k=1}^2 P_k A_k^2 = P_1 A_1^2 + P_2 A_2^2$$

$$R_A(0) = \frac{1}{2} \cdot a^2 + \frac{1}{2} \cdot \frac{1}{2} \cdot a^2 = a^2$$

$$R_A(0) = a^2$$

$$R_A(n) = 0$$

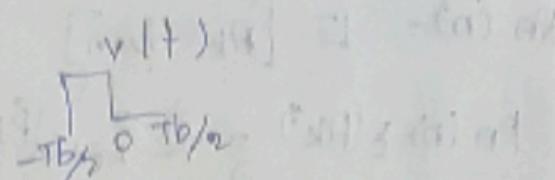
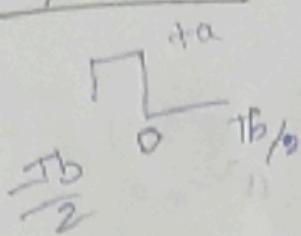
$$S_{qq}(f) = a^2 T_b \sin^2 f(T_b) \sin^2(\pi f T_b) \text{ in Bipolar NDZ}$$



Manchester

$$S_{xx}(f) = T_b a^2 \sin^2 \left( \pi f \frac{T_b}{2} \right) \sin^2 \left( \pi f \frac{T_b}{2} \right)$$

Unipolar RZ



$$V(f) = \frac{Tb}{2} \operatorname{sinc}\left(\frac{fTb}{2}\right) e^{j\beta_2 \pi f \frac{Tb}{4}}$$

$$|V(f)|^2 = \frac{Tb^2}{4} \operatorname{sinc}^2\left(f \frac{Tb}{2}\right)$$

$$R_A(n) = 0.1 \cdot \frac{a^2}{2} = a^2/2$$

$$R_A(n) = R_A(1) = P(A_k, B_{k+1}) (A_k, B_{k+1})$$

$$= 0.01 \left(\frac{1}{4}\right) + 0.01 \left(\frac{1}{4}\right) + 0.01 \left(\frac{1}{4}\right) \cdot 0.01$$

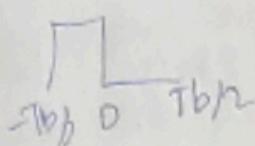
$$\boxed{R_A(1) = a^2/4}$$

$$S_{\text{NR}}(f) = \frac{1}{Tb} |V(f)|^2 \cdot R_A(n) e^{-j\beta_2 \pi n f T_b}$$

$$= \frac{1}{Tb} \left( \frac{Tb^2}{4} \operatorname{sinc}^2\left(f \frac{Tb}{2}\right) \cdot \left[ \frac{a^2}{2} + \frac{a^2}{4} \right] \right)$$

$$= Tb \operatorname{sinc}^2 \underline{a^2}$$

Polar RZ



$$\boxed{V \rightarrow I_b \sin(f \frac{Tb}{2})}$$

$$V(t) \xrightarrow{\text{F}} V(f) = \left( e^{-j2\pi f \frac{Tb}{4}} \right) \frac{I_b}{2} \sin(f \frac{Tb}{2})$$

$$V(f)^2 = \frac{Tb^2}{4} \sin^2 f \frac{Tb}{2}.$$

$$R_A(0) = a^2 \quad n \neq 0$$

$$R_A(n) = 0 \quad -j2\pi f \frac{Tb}{2}$$

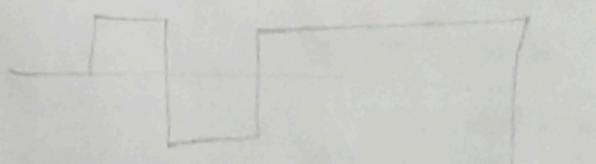
$$S_{gg}(f) = \frac{1}{Tb} |V(f)|^2 = \sum R_A(k) e^{-j2\pi f k \frac{Tb}{2}}$$

$$= \frac{1}{Tb} \frac{Tb^2}{4} \sin^2 \left( f \frac{Tb}{2} \right) \cdot a^2$$

$$\boxed{S_{yy} = \frac{a^2 T_b}{4} \sin^2 \left( f \frac{Tb}{2} \right)}$$

Polar NRZ

0	Tb	2Tb	3Tb	4Tb
1	0	1	1	0
$\uparrow a$	$\downarrow -a$	$\uparrow +a$	$\uparrow -a$	$\downarrow -a$



$$V(f) = T_b \sin(f(T_b))$$

$$R_n(0) = \frac{1}{2} a^2 + \frac{1}{2} a^2 = a^2.$$

$R_n(k)$   $\rightarrow$   $P_k P_{k+1} P_{k+2} \dots P_{k+n}$  Product

+a	+a	$a^2$	$\frac{1}{4}$	$\frac{a^2}{4}$
+a	-a	$-a^2$	$\frac{1}{4}$	$\frac{-a^2}{4}$
-a	+a	$-a^2$	$\frac{1}{4}$	$\frac{-a^2}{4}$
-a	-a	$a^2$	$\frac{1}{4}$	$\frac{a^2}{4}$

$$R_n(1)=0 \Rightarrow R_n(n)=0$$

$$S_{yy}(f) = \frac{1}{Tb} |\nabla f|^2 \sum_{n=0}^{\infty} R_n(n) e^{-jnfb}$$

$$= \frac{1}{Tb} Tb \sin^2(fTb) a^2$$

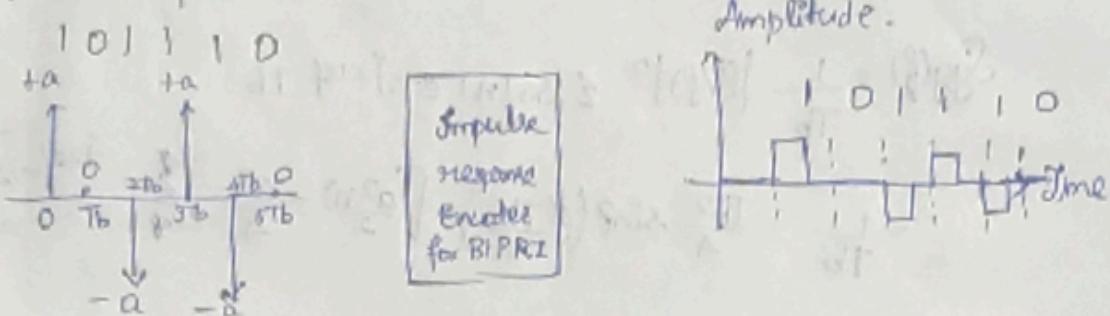
$$\boxed{S_{yy}(f) = a^2 Tb \sin^2(fTb)}$$

22/08/2020

S. Sri Jayarao  
2018504575

Power Spectral Density of BIPolar Return to Zero

bipolar BIPolar Linecode



$$\xrightarrow{\text{Impulse Response}} \Rightarrow V(f) = \frac{Tb}{\pi} \operatorname{sinc}\left(f \frac{Tb}{2}\right)$$

Autocorrelation sequence  $R_A(n)$ 

$$R_A(n) = E(p_k p_{k+n})$$

$$R_A(0) = E(p_k p_k) = E(p_k^2) = \sum_n (p_k p_k^2) = a^2/2$$

$$\boxed{R_A(0) = \frac{a^2}{2}}$$

$$R_A(1) = E(p_k p_{k+1})$$

$A_k$	$A_{k+1}$	$\Pr[A_k, A_{k+1}]$	$P_{A_k, A_{k+1}} \cdot P(A_k, A_{k+1})$
0	0	0	$\frac{1}{2} \cdot \frac{1}{2} = \frac{1}{4}$
0	+a	0	$\frac{1}{8}$
0	-a	0	$\frac{1}{8}$
+a	0	0	0
+a	+a	$a^2$	0
+a	-a	$-a^2$	$-a^2/8$
-a	0	0	0
-a	+a	$-a^2$	$-a^2/8$
-a	-a	$+a^2$	0

$$R_{\text{pt}}(l) = \sum P_{lk} P_{k+1} P(lk, lk+1) = -\alpha^2/4$$

$$R_{\text{pt}}(-l) = R_{\text{pt}}(l)$$

$$R_{\text{pt}}(0) = 0 \quad \text{Since for polar } R_{\text{pt}}(0) = 0$$

$$S_{\text{gg}}(f) = \frac{1}{T_b} |(V_f)|^2 + R_{\text{pt}}(0) e^{-j2\pi f T_b}$$

$$= \frac{1}{T_b} \left[ \frac{T_b^2}{4} \sin^2 \left( f \frac{T_b}{2} \right) \left[ \frac{\alpha^2(1)}{2} - \frac{\alpha^2}{4} \right] + \frac{1}{4} e^{-j2\pi f T_b} \right]$$

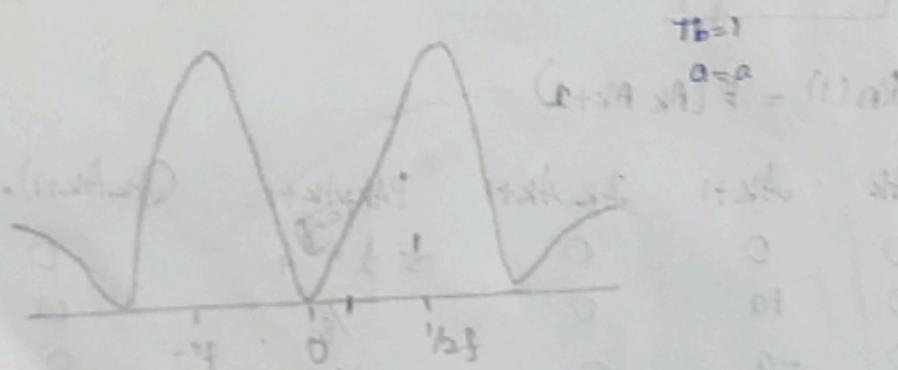
$$= \frac{T_b}{4} \sin^2 \left( f \frac{T_b}{2} \right) \left[ \frac{\alpha^2}{2} - \frac{\alpha^2}{4} \times 2 \cos(2\pi f T_b) \right]$$

$$\boxed{S_{\text{gg}}(f) = \frac{\alpha^2}{4} T_b \sin^2 \left( f \frac{T_b}{2} \right) \sin^2 \left( f f T_b \right)}$$

$\Rightarrow$  Here there is no DC components.

$\Rightarrow$  There is no Clark component to extract at the end of receiver. Therefore not suitable for Clark extraction.

$\Rightarrow$  Bipolar RL has higher bandwidth than other polar RLs



$\Rightarrow$  Since no constants DC component = 0

$\Rightarrow$  Bandwidth of the waveform =  $1/T_b$  compared to

$\Rightarrow$  Manchester, this is less

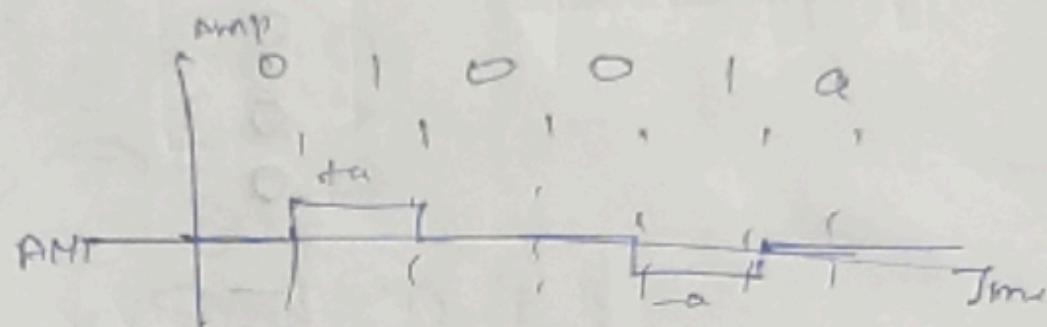
→ This isn't useful / suitable for clock extraction

Power requirements:

$$\text{Power} = \frac{1}{2\pi} \int |x(t)|^2$$

26/09/2020

Bipolar [PAM] NRZ:



$$\text{NRZ} \Rightarrow \left| \frac{Tb}{2} \right| \quad \left. \right\} \uparrow \text{B.W.}$$

$$\text{RZ} \Rightarrow \frac{Tb}{2}$$



EE7181/2020

We assume only one path between Transmitter & Receiver. Single path effect only.

Impulse response  $h(t)$  Frequency response  $H(f)$

Transmitter  $\xrightarrow{\text{Channel}}$  Receiver

• AWGN [Additive White Gaussian Noise] Channel

- {  
⇒ Noise is white has all freq.  
⇒ Noise is Gaussian  
⇒ Added at front end of receiver.

• channel Attenuation

• Bandwidth limitation

### Channel Limitations -

• Attenuation.  $\Rightarrow$  only power change shape remains same.

Bandwidth limitation:- shape may change

(1) Signal distortion:

Received Pulse shape is different [Broader than] the transmitted that of pulse

This is called Intersymbol Interference.

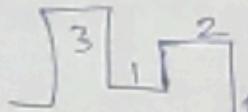
Solution:- Channel Equalization

Wireless communication:-

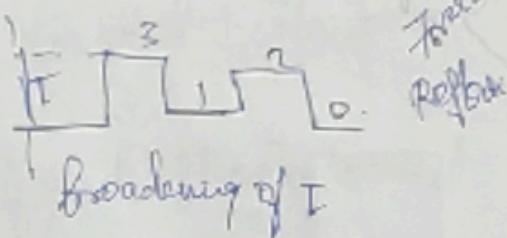
⇒ The broadening will be due to Multipath effect.

ISI due to Multipath effect in Wireless Channel:-

Signal received  
at shorter path



Signal received  
over longer path

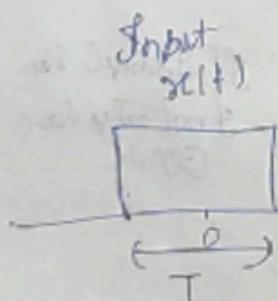


Received signal  
Superposition of  
two

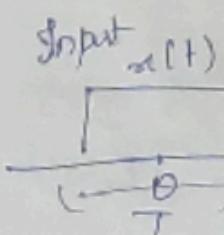
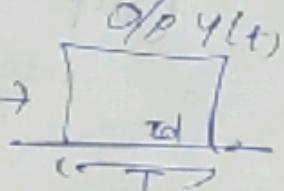


### Channel Width Bandwidth Limitation

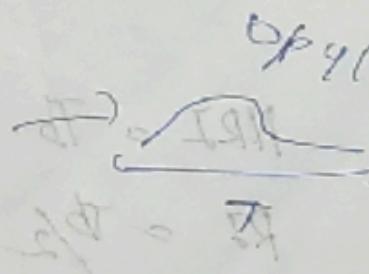
Pulse Broadening



→ Ideal channel  
Distortionless



→ Low Pass channel  
Eliminate high  
frequency



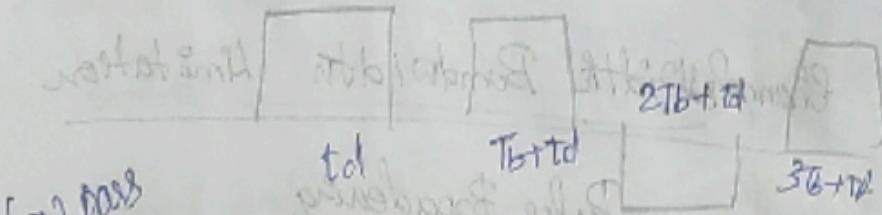
The broadening is because the dispersion is  
 dispersion in time domain  $\rightarrow$  Expansion/Broadening in freq domain

Due to distortion.

Inter. symbol Interference.

Input

Output by ideal



Low pass

Output

But also the other signals interfere.

If 3 sample per symbol  
not only have 3 pulse

$$NRZ = Tb$$

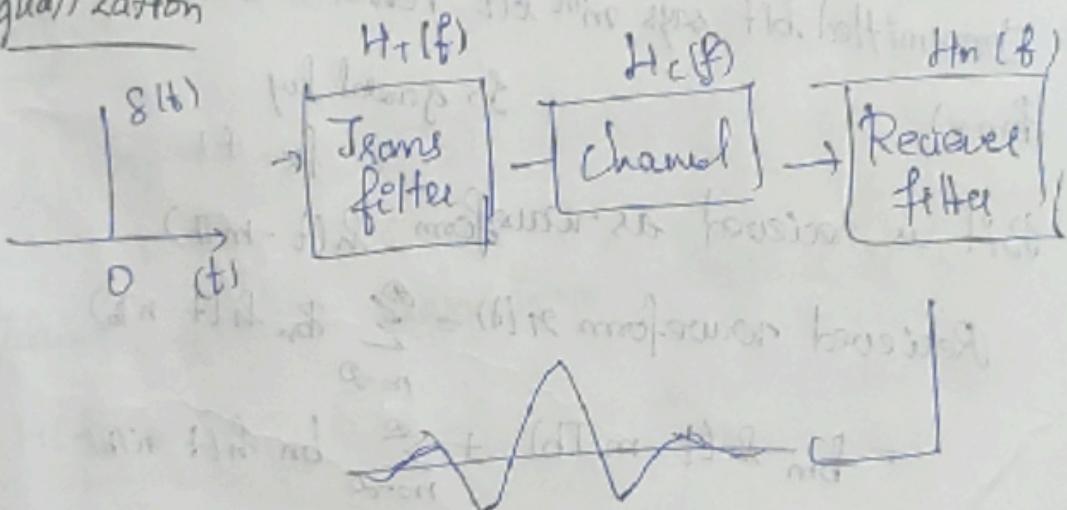
$$RJ = \frac{Tb}{2}$$

Wired channel always have a loss restriction  
 Wireless will have filters which will broaden  
 the pulse.  
 So No matter what, broadening is inevitable.  
 Bit rate  $\rightarrow$  Problem.

Solution: Channel Estimation & Channel Equalization

↓  
 Obtaining  $h(f)$  of a channel.

Equalization



Composite System Transfer Function =  $H(f)$

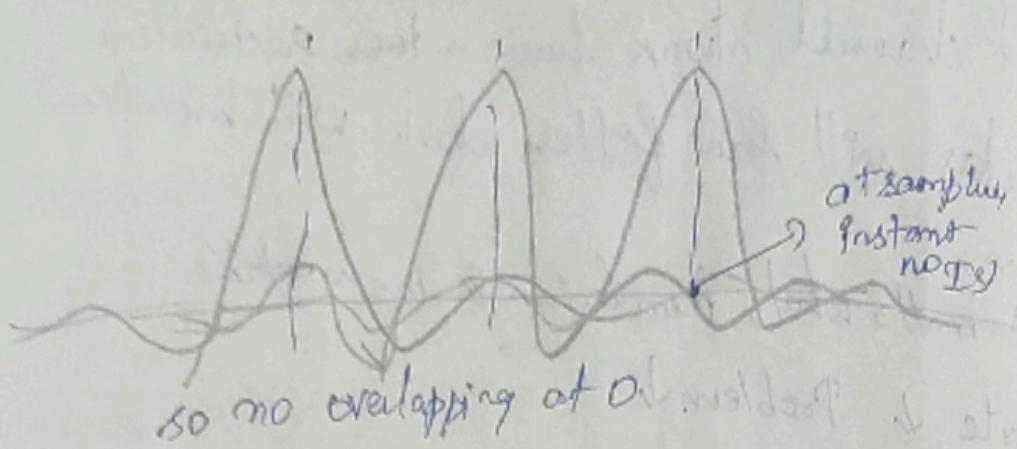
$$H(f) = H_T(f) \cdot H_C(f) \cdot H_R(f)$$

$$H(f) \xrightarrow{FT} H(\omega)$$

time domain

frequency domain

freq



Equalization Receiver filter  
 Compensating the effect of low-pass filter and channel but gives rectangular pulse

Derivation :-

Transmitted bit says,  $m$ th bit is encoded as  $b_m$

$b_m = 1$  or  $-1$  In general say  $b_k = \pm 1$

Bit is received as waveform  $h(t - mT_b)$

$$\text{Received waveform } r(t) = \sum_{n=-\infty}^{\infty} b_n h(t - nT_b)$$

$$= b_m h(t - mT_b) + \sum_{\substack{n=-\infty \\ n \neq m}}^{\infty} b_n h(t - nT_b)$$

This shows that other bits are also present.

To take decision for  $m$ th bit, sampling it at  $t = mT_b$

$$r(mT_b) = b_m h(mT_b - mT_b) + \sum_{\substack{n=-\infty \\ n \neq m}}^{\infty} b_n h(mT_b - nT_b)$$

Due to  $m$ th bit from other bit

$$r(mT_b) = b_m h(0) + \sum_{k=0}^{\infty} b_k h(kT_b)$$

To avoid ISI,

$$g_1(mTb) = b_m \delta(0)$$

equivalently

$$\begin{cases} h(kTb) = 0 & k \neq 0 \\ h(kTb) \neq 0 & k = 0 \end{cases}$$

This is possible only for impulse

consider  $h_{\text{discrete}}(t) = \text{discrete time version of } h(t)$

$$h_{\text{discrete}}(t) = h(t) \sum_{k=-\infty}^{\infty} \delta(t - kTb) = \sum_{k=-\infty}^{\infty} h(kTb) \delta(t - kTb)$$

For zero ISI :-

$$\sum_{k=-\infty}^{\infty} h(kTb) \delta(t - kTb) = h(0) \delta(t)$$

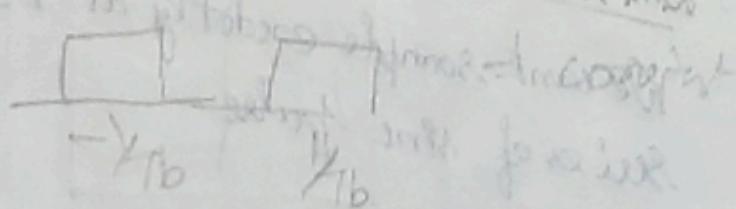
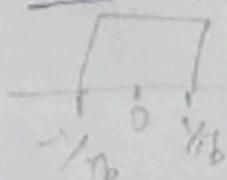
$$h(t) \sum_{k=0}^{\infty} \delta(t - kTb) = h(0) \delta(t)$$

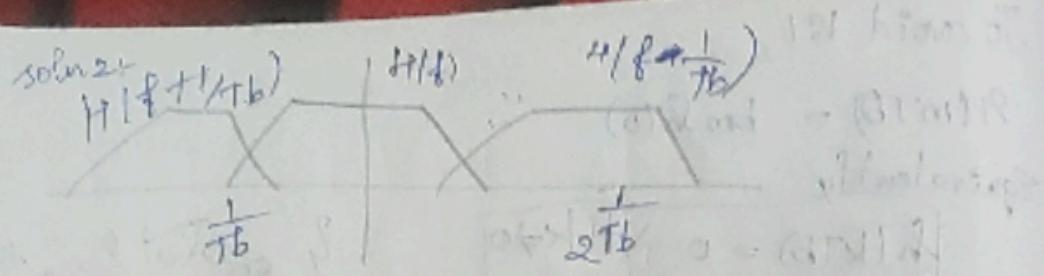
Taking Fourier transform on both sides.

$$H(f) * \sum_{k=0}^{\infty} \delta(f - \frac{k}{Tb}) = h(0) = \text{constant}$$

$$\sum_{k=-\infty}^{\infty} H\left(f - \frac{k}{Tb}\right) = \text{constant}$$

Solve for  $H(f)$





But theoretically rectangular pulse is the best one because of lower bandwidth.

Symbol Rate  $f_s = \frac{1}{T_b} = 2W - \text{Ideal channel}$

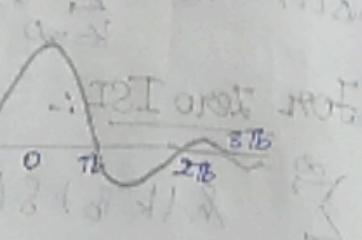
$\Downarrow$  H3 (ideal)  $\Rightarrow$  (SNR)  $\Rightarrow$  (Hd - H3)

symbol = 2

Binary system  $\Rightarrow$  Bi-phase

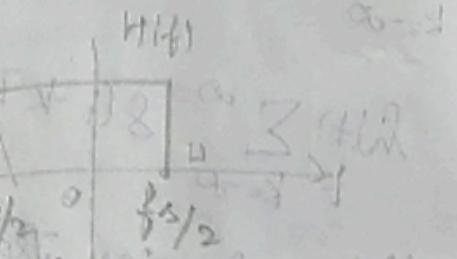
Symbol = 4  $(H3(0)12 \dots 30 \dots 27b \dots 0 \dots 27b \dots 30 \dots H3(1)12 \dots)$

Mary



Absolute Bandwidth  $H8(0)12 \dots$

$$W = \frac{f_s}{2} \quad \begin{cases} \text{Minimum} \\ \text{bandwidth} \end{cases}$$



Symbol Rate  $R_b = \frac{1}{T_b}$

$$BW = \frac{R_b}{2} = W$$

$$\text{Absolute Bandwidth} = \frac{f_s}{2}$$

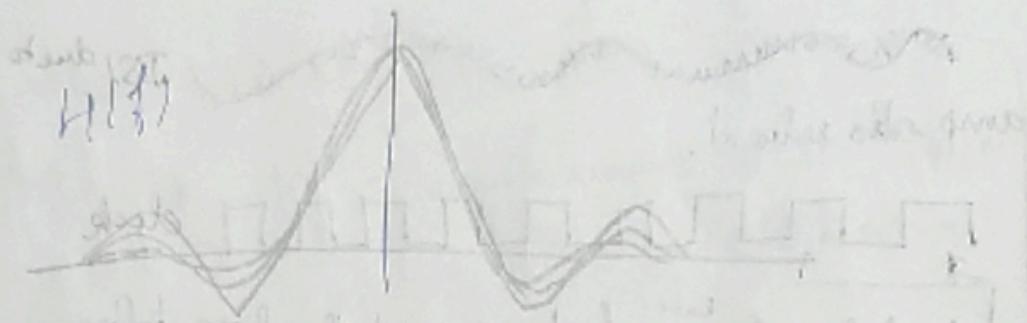
Symbol =  $f_s$

Nyquist signalling rate  $f_s$

Limitation :-

- We can't sample exactly at  $T_b = 0$  in the series of sine pulse.

I have to compromise so that we can have some tolerance  
We can use raised cosine pulses



$$h(t) = \frac{\sin \frac{\pi t}{T}}{\frac{\pi t}{T}} \cos \frac{\pi a t}{T} \cos \frac{\pi (1-a)t}{T}$$

$a=0$  ideal solution -  $h(t)$  is sine function

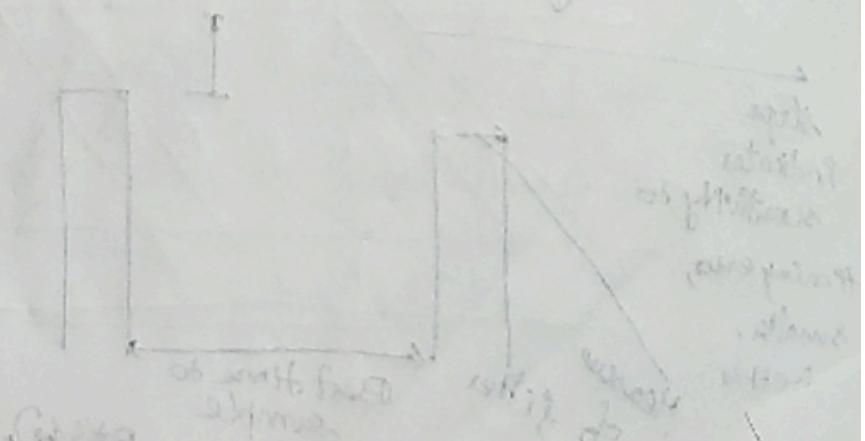
$$W = \frac{1}{2} T b$$

02/09/2020 ..

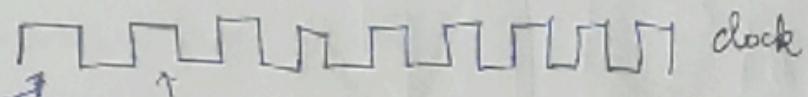
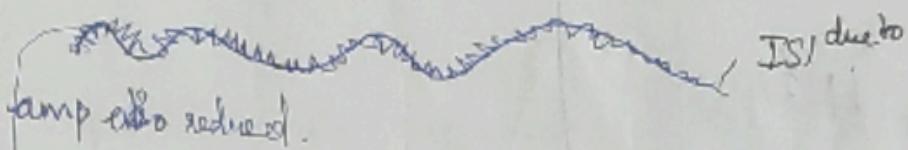
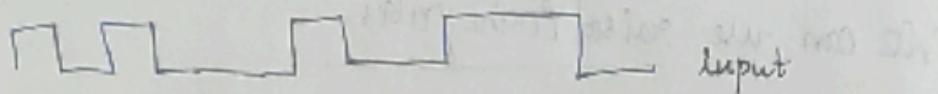
Performance of Bitrate

Probability of error  $\Rightarrow$

BER with  
error free  
cases



Eye pattern:

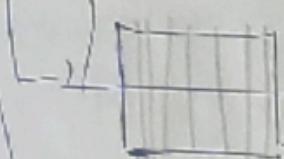


No clock pulse has constant period, they have tolerance

If we trigger the CRO at this point, the first part of wave is traced, second point trigger, second part traced.

If any change takes place before  $\frac{1}{24}$ s, we can notice it.

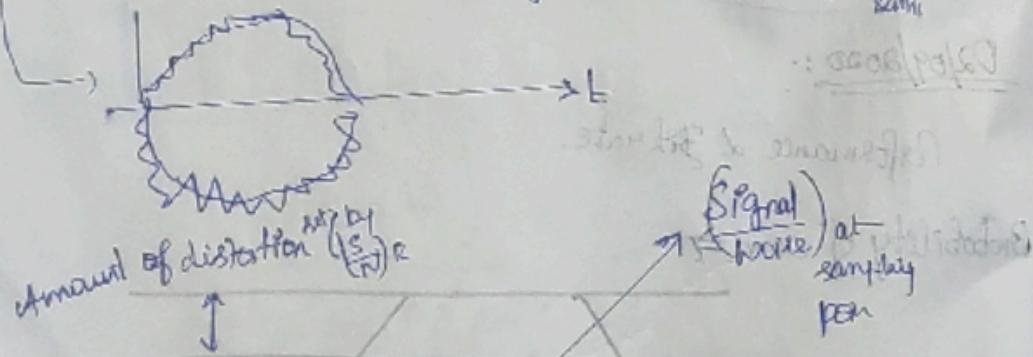
$\Rightarrow 10\text{Mbps}$



With ISI output

sampling here at all points give

some



Slope indicates sensitivity to timing error, smaller, better

Measure of jitter

Best time to sample next open part -  $P(S,W)_R$

Time variation of zero crossing

Sampling is done at falling edge whenever possible.

- for the pattern, we can predict the nature. This is qualitative

To extract values, take BER

$$BFR = \frac{Pe}{Re} \approx 10^{-6}$$

which measures for  $10^6$  Btu only  
one  $\text{ft}^2$  is wrong

(9) H 09/16

## Power Generation

$$\int_{-P}^P S_{qq}(x) f(x) dx = \text{Power}$$

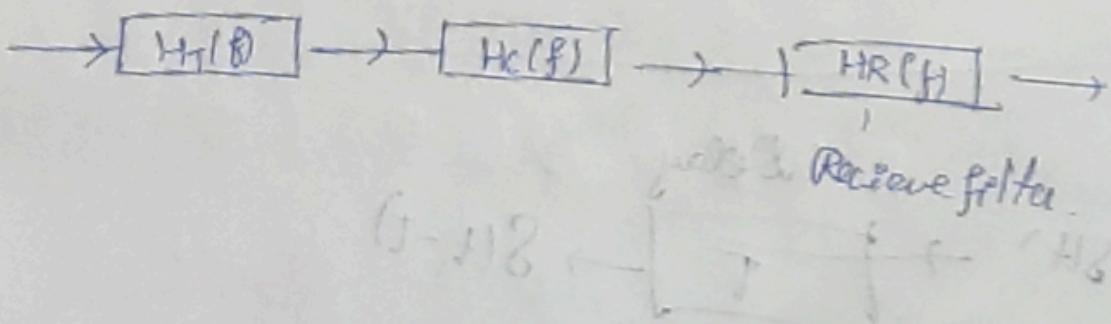
$$\int \sin^2(x_0) \, df = \int |x(t)|^2 dt$$

$$\Rightarrow \text{Average power} = \frac{1}{2T} \left( \int_{-T}^T |x(t)|^2 dt \right)$$

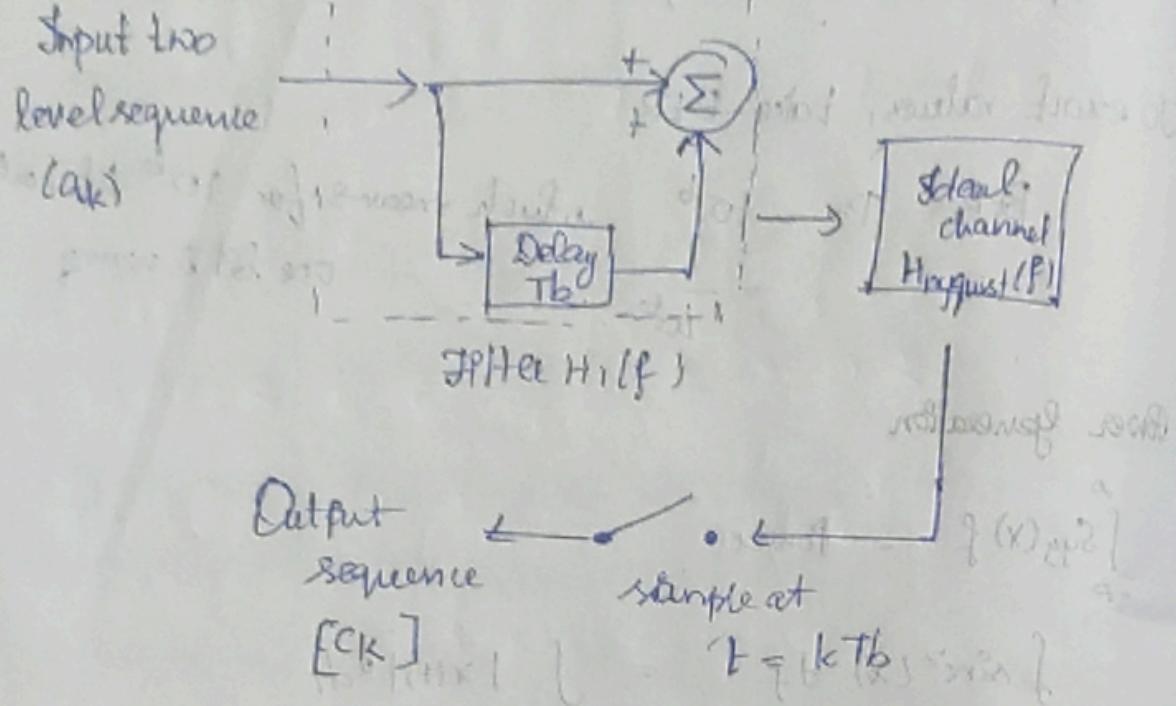
## 03/12/2020 Dictionary Encoding +

## Correlative Encoding

$\Rightarrow$  Controlled ISI  $\rightarrow$  Required Minimum Bandwidth



## Duobinary signalling scheme



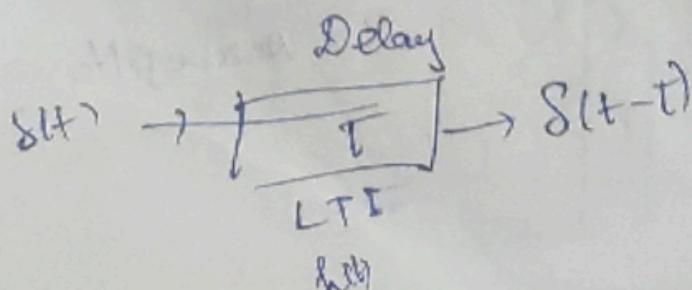
The current bit exactly overlaps / superposition with the previous bits:

so if  $\Sigma \rightarrow 2 \rightarrow$  then current bit  $c_1$  previous bit  $c_1$

$\rightarrow -2 \rightarrow -1$  previous bit  $c_0$  current bit  $c_0$

$\rightarrow 1 \rightarrow -1$  previous bit  $c_0$  current bit  $c_1$

$\rightarrow -1 \rightarrow 1$  previous bit  $c_1$  current bit  $c_1$



$$H(f) = H_c(f) \left[ 1 + \exp(-j2\pi f T_b) \right]$$

Nyquist  $\rightarrow$  Ideal filter for bandwidth restriction

$$= H_c(f) e^{-j2\pi f T_b} \left[ e^{j2\pi f T_b} + e^{-j2\pi f T_b} \right]$$

$$= H_c(f) e^{-j2\pi f T_b} [2 \cos(\pi f T_b)]$$

$$H(f) = 2H_c(f) \cos(\pi f T_b) e^{-j2\pi f T_b}$$

$$\left( H_c(f) = 1 \quad |f| \leq \frac{R_b}{2} \right)$$

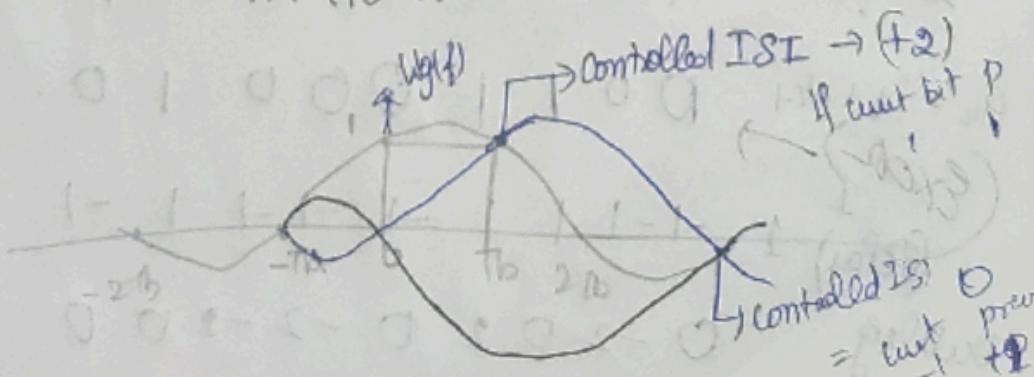
$$H(f) = 2 \cos(\pi f T_b) \exp(-j2\pi f T_b) \quad |f| \leq \frac{R_b}{2}$$

1 0 1 - 1 - 1 1 - 1 elsewhere

$$h(t) = \frac{\sin\left(\frac{\pi t}{T_b}\right)}{\pi t/T_b} + \frac{\sin\left(\frac{\pi(t-T_b)}{T_b}\right)}{\pi(t-T_b)/T_b}$$

$$= \frac{\sin(\pi t/T_b)}{\pi t/T_b} - \frac{\sin(\pi(t-T_b)/T_b)}{\pi(t-T_b)/T_b}$$

$$= \frac{Tb^2 \sin(\pi t/T_b)}{\pi t(Tb-t)}$$



## DuoBipolar encoding.

Data seq: 1 0 1 0 1 0 0 1 1 -

$b_k$ : 1 -1 1 -1 1 -1 -1 1 -

[Data =  
represents]

Initial +1

$a_k = b_k + b_{k-1}$  & 0 0 0 0 0 -2 0 2,

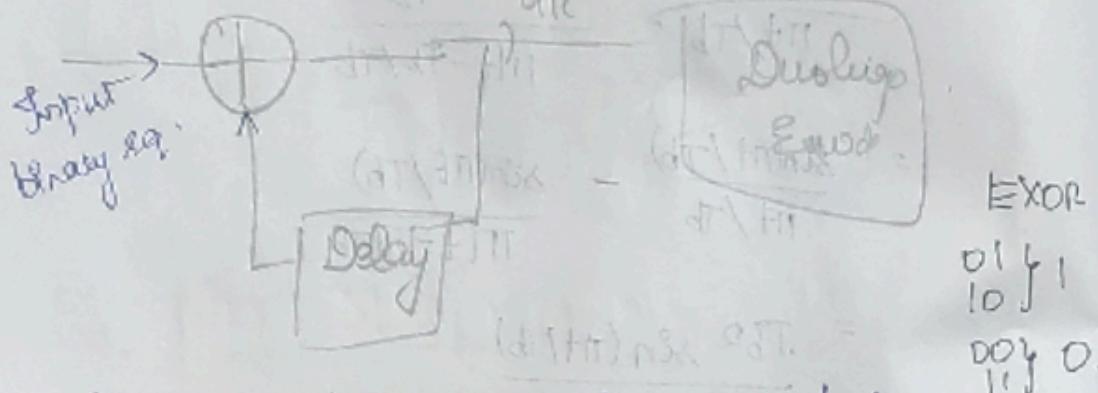
If  $c_k > +1$  Data 1  $\left( \begin{array}{l} a_k \\ a_{k-1} \end{array} \right) \rightarrow (0, 1)$

(ie  $a_k$  Data 0.

+1  $\leftarrow c_k + 1$  count by inverted at +1 case  $\rightarrow (1, 0)$

1 -1 1 -1 1 -1 1 -1 1

1 0 1 0 1 0 0 1 1



Sequence 1 0 1 0 1 0 0 1 1

$a_k = b_k + a_{k-1}$  0 0 1 1 0 0 0 1 0

(Exor 1  
(Delay))

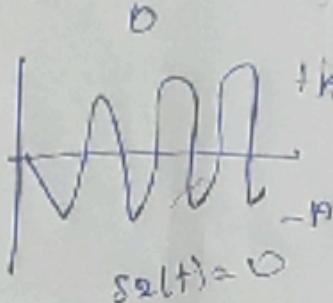
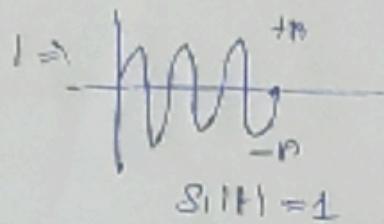
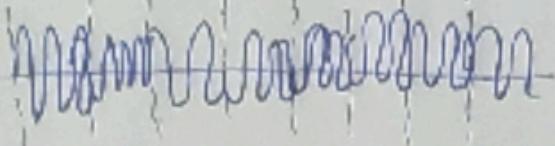
-1 -1 1 1 -1 -1 -1 1 -

DuoBip

0 -2 0 2 0 -2 -2 0 0

09/09/2020 Bandpass signalling: 0 1 0 1 0 1

1 0 1 0 0 1 1



- $\{s_i(t)\}$  represents the set of waveforms to be represented in the signalspace.  $\{s_1(t), s_2(t), \dots, s_M(t)\}$ .

The set of Orthogonal (real) basis functions.

$$\{\phi_1(t), \phi_2(t), \dots, \phi_N(t)\} \quad N \leq M$$

$$\int_0^T \phi_i(t) \phi_j(t) dt = \begin{cases} 1 & \text{if } i=j \\ 0 & \text{if } i \neq j \end{cases}$$

T = duration of symbol

Energy of the basis function = 1

$$\text{Let } S_i(t) = \sum_{j=1}^M s_{ij} \phi_j(t)$$

- Each of the waveform must be a linear combination of the basis functions.

$$0 \leq t \leq T$$

- If  $\phi_j$  is second in,

$$i = 1, 2, 3, \dots, M$$

$$S_{ij} = \int_0^T S_i(t) \phi_j(t) dt$$

$\Rightarrow \begin{matrix} i = 1, 2, \dots, M \\ j = 1, 2, \dots, N \end{matrix}$