

$$1 - \omega_1^2 L_1 C_1 = \frac{\omega_1}{\omega_2} [\omega_2^2 L_1 C_1 - 1] \quad \text{--- (5)}$$

from (1)

$$L_1 C_1 = \frac{1}{\omega_0^2} \quad \text{--- (6)}$$

$$\therefore 1 - \frac{\omega_1^2}{\omega_0^2} = \frac{\omega_1}{\omega_2} \left(\frac{\omega_2^2}{\omega_0^2} - 1 \right)$$

$$\Rightarrow 1 - \frac{f_1^2}{f_0^2} = \frac{f_1}{f_2} \left(\frac{f_2^2}{f_0^2} - 1 \right)$$

$$\frac{f_0^2 - f_1^2}{f_0^2} = \frac{f_1}{f_2} \left(\frac{f_2^2 - f_0^2}{f_0^2} \right)$$

$$f_0^2 f_2 - f_1^2 f_2 = f_1 f_2^2 - f_0^2 f_1$$

$$f_0^2 (f_2 / f_1) = f_1 f_2 (f_2 / f_1)$$

$$f_0^2 = f_1 f_2$$

$$\boxed{f_0 = \sqrt{f_1 f_2}}$$

$$\text{--- (7)}$$

The frequency of resonance of the individual arms should be the geometric mean of the two freq's of cut-off.

2 marks
 16 free filter is terminated in a load $R = R_k$.

The value of the circuit components are determined in terms of R, f_1 & f_2 .

At lower cut-off freq

① $\frac{1}{\omega_1 C_1} - \omega_1 L_1 = 2R$

$$\frac{1 - \omega_1^2 L_1 C_1}{\omega_1 C_1} = 2R$$

$$1 - \omega_1^2 L_1 C_1 = 2R \omega_1 C_1$$

from ① $\frac{1 - \frac{\omega_1^2}{\omega_0^2}}{\frac{\omega_1^2}{\omega_0^2}} = 2R \omega_1 C_1 \Rightarrow 1 - \frac{f_1^2}{f_0^2} = 4\pi R f_1 C_1$

sub $f_0 = f_1 f_2$ from ②

$$1 - \frac{f_1}{f_2} = 4\pi R f_1 C_1 \Rightarrow \frac{f_2 - f_1}{f_2} = 4\pi R f_1 C_1$$

$$C_1 = \frac{f_2 - f_1}{4\pi R f_1 f_2} \quad \text{--- ③}$$