### Macroeconomics B, El060

Class 3

Real exchange rate and terms-of-trade

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## What you will get from today class

- Comparing price levels: the real exchange rate.
  - Consumption allocation between traded and non-traded goods (Harms IV.4.1-4.4, Obstfeld and Rogoff (secondary) 4.4).
  - Impact on the current account.
- Different traded goods and the terms-of-trade.
  - Consumption allocation (Harms IV.4.5).
  - Impact on current account.
- Link with nominal exchange rate, and special cases (Harms VII.1-3).
- Real exchange rate and productivity (Harms VII.4, OR 4.1-4.2.3).

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### A question to start

When a country's currency appreciates (even when correcting for different price levels), it looses competitiveness and runs a trade deficit.

real appreciation

Do you agree? Why or why not?

dynamic

fall in real investment

actively depreciate

import dependent reverse causality

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REAL EXCHANGE RATE:

**DEFINITION AND PATTERNS** 

## Nominal and real exchange rates

- Nominal exchange rate of Switzerland, E: how many Swiss franc does it take to get a Euro?
  - A higher value is a nominal depreciation. of the CHF
  - In an analysis always be clear of whether you define the exchange rate that way, or the other way around (both are perfectly fine, but beware of confusion).
- Nominal exchange rate is the (inverse of) international purchasing power of a currency. How does it link to its domestic purchasing power (inverse of price level)?
- Real exchange rate Q. P is the Swiss price level, in Swiss franc,  $P^*$  is the European price level, in Euro:

# Q=1 PPP

$$Q = \frac{EP^*}{P} = \frac{\frac{CHF}{Euro} * Euro}{CHF}$$

- $Q = \frac{EP^*}{P} = \frac{\frac{CHF}{Euro} * Euro}{CHF}$  A higher value is a real depreciation, so the nominal exchange rate is not just the mirror of domestic purchasing powers.
- No specific unit of measure (unlike nominal exchange rate), expressed as an index

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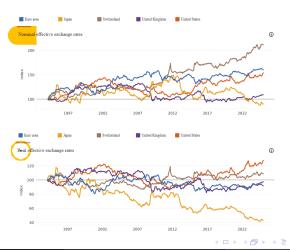
#### Bilateral and effective rates

- Swiss franc Euro is a bilateral exchange rate.
- A (geometric) weighted-average across a countries trading partners gives an effective (trade weighted exchange rate).
  - Weights can be based on exports, imports, or a mix.
- Database of the Bank for International Settlements: https://data.bis.org/topics/EER go under "tables & dashboards".
  - Can select countries, real or nominal rates.
  - Easy charts and data downloads. Exchange rate as indices, were an increase is an appreciation (inverse of my definition).

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#### Advanced economies

 Trends of nominal appreciations (esp. Switzerland), but less so in real terms. Nominal appreciation reflects low domestic inflation (esp. Japan).



## Emerging economies

 Heterogeneous: several nominal depreciations (incl. crises), some steady, some increases (China). Same real pattern, but smaller magnitudes (exc. China).



TRADED VS. NON — TRADED GOODS

# Consumption basket

#### r given

- Small open economy with representative consumer.
- Overall consumption  $C_t$  is a (constant elasticity of substitution) basket of a traded good  $C_t^T$  and a non-traded good  $C_t^N$ :

$$C_t = \left[ (\gamma)^{\eta} \left( C_t^{\mathsf{T}} \right)^{1-\eta} + (1-\gamma)^{\eta} \left( C_t^{\mathsf{N}} \right)^{1-\eta} \right]^{\frac{1}{1-\eta}}$$

- The higher  $\eta$ , the less substitutables are the two goods.
- Price of the traded good normalized to 1. Relative price of the non-traded good is  $\frac{P_t^N}{t}$ . Total expenditure:

$$P_t C_t = C_t^T + P_t^N C_t^N$$

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### Allocation between the two goods

- Minimize the expenditure, subject to the constraints of a given real basket  $C_t$ .
- Demands reflects the weight in the basket, and the relative price:

$$C_t^T = \gamma \left[ \frac{1}{P_t} \right]^{-\frac{1}{\eta}} C_t \quad ; \quad C_t^N = (1 - \gamma) \left[ \frac{P_t^N}{P_t} \right]^{-\frac{1}{\eta}} C_t$$

- The higher  $\eta$ , the lower the sensitivity of demand to the price (goods are not so substitutables).
- Price index is the minimum expenditure to get  $C_t = 1$ :

$$P_{t} = \left[\gamma + (1 - \gamma) \left[P_{t}^{N}\right]^{\frac{\gamma - 1}{\eta}}\right]^{\frac{\gamma}{\eta - 1}}$$

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### Real exchange rate

- Real exchange rate is the ratio of the price level abroad to the domestic price level, all denominated in terms of traded good.
- The rest of the world consumes only the traded good:

$$Q_{t} = \frac{P_{t}^{T}}{P_{t}} = \left[\gamma + (1 - \gamma) \left[P_{t}^{N}\right]^{\frac{\eta - 1}{\eta}}\right]^{\frac{\eta}{\eta - 1}}$$

- Increase is a real depreciation for the domestic country.
- An increase in the price of the non-traded good  $P_t^N$  reduces  $Q_t$  and is a real exchange rate appreciation.

#### PN up then Q down



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### Intertemporal dimension

Two periods economy, with utility:

$$U_1 = \frac{(C_1)^{1-\sigma}}{1-\sigma} + \beta \frac{(C_2)^{1-\sigma}}{1-\sigma}$$

- Outputs are endowments. Investment in a bonds denominated in traded good units, with return r.
- Budget constraints, in terms of traded goods:

$$B_2 + P_1 C_1 = Y_1^T + P_1^N Y_1^N$$
  
 $P_2 C_2 = Y_2^T + P_2^N Y_2^N + (1+r) B_2$ 

# Dynamic of consumption basket

Standard Euler condition:

$$C_{2} = \left[\beta \left(1 + r\right) \frac{P_{1}}{P_{2}}\right]^{\frac{1}{\sigma}} C_{1}$$

$$C_{2} = \left[\beta \left(1 + r^{C}\right)\right]^{\frac{1}{\sigma}} C_{1}$$

- The real interest rate is the relative price of current consumption. A higher rate shifts consumption to the future, especially if  $\sigma$  is low (utility is not very concave).
- Two different real interest rates.
  - r in terms of units of traded good. Reflects the price of a traded good today, in terms of a traded good tomorrow.
  - $r^{C}$  in terms of the consumption basket. Reflects the price of a basket today, in terms of a basket tomorrow. If today the non-traded good is PNelatively expensive  $(P_{1}^{T} > P_{2}^{T})$  this makes the basket relatively

expensive today  $(P_1>P_2)$ , hence a higher real interest rate.

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# Dynamics of traded good consumption

• Combine the Euler (dynamics of C) and the static demand for the traded good (link between C and  $C^T$ ):

$$C_2^T = [\beta (1+r)]^{\frac{1}{\sigma}} \left[ \frac{P_1}{P_2} \right]^{\frac{1}{\sigma} - \frac{1}{\eta}} C_1^T$$

- Usual effect of the real interest rate r.
- Subtle effects of the real exchange rate dynamics  $(P_1/P_2)$ . If the price of the non-traded good increases through time, the real exchange rate is appreciating between today and tomorrow  $P_1 < P_2$ .
  - Non-traded good is relatively cheap today.
  - Low consumption real interest rate  $r^{C}$ , shifts consumption basket to the present: higher  $C_1/C_2$ , and  $C_1^{T}/C_2^{T}$ . Driven by intertemporal sensitivity  $1/\sigma$ .
  - Take advantage of cheaper non-traded good in period 1 by shifting consumption composition towards non-traded today, and traded tomorrow. Reduces  $C_1^T/C_2^T$ . Driven by substitutability  $1/\eta$ .

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## Traded consumption and current account

Traded consumption in period 1 is:

$$C_1^T = \frac{1}{1 + (\beta)^{\frac{1}{\sigma}} (1+r)^{\frac{1-\sigma}{\sigma}} \left[\frac{P_2}{P_1}\right]^{\frac{1}{\eta} - \frac{1}{\sigma}}} \left[Y_1^T + \frac{Y_2^T}{1+r}\right]$$

• Consumption and supply of non-traded goods are always equal:  $C_t^N = Y_t^N$ . Intertemporal constraint then only includes traded goods:

$$C_1^T + \frac{C_2^T}{1+r} = Y_1^T + \frac{Y_2^T}{1+r}$$

• The current account  $CA_1 = Y_1^T - C_1^T$  is:

$$CA_{1} = Y_{1}^{T} - \frac{1}{1 + (\beta)^{\frac{1}{\sigma}} (1 + r)^{\frac{1 - \sigma}{\sigma}} \left[\frac{P_{2}}{P_{1}}\right]^{\frac{1}{\eta} - \frac{1}{\sigma}}} \left[Y_{1}^{T} + \frac{Y_{2}^{T}}{1 + r}\right]$$

• It reflects the dynamics of the real exchange rate,  $P_2/P_1$ , not its level.

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### A simpler case

• We still need to solve for  $P_2/P_1$ . Set  $\beta(1+r)=1$ , and  $\eta=1$  (Cobb-Douglas consumption basket)

$$C_t = \left(C_t^T\right)^{\gamma} \left(C_t^N\right)^{1-\gamma}$$

Consumption allocation shows constant spending shares:

$$C_{t}^{T} = \gamma P_{t}C_{t} ; P_{t}^{N}C_{t}^{N} = (1 - \gamma) P_{t}C_{t}$$

$$P_{t}^{T} = \frac{1}{(\gamma)^{\gamma} (1 - \gamma)^{1 - \gamma}} \left(P_{t}^{N}\right)^{1 - \gamma}$$

• Using the fact that  $\frac{C_t^N}{t} = Y_t^N$ , the price of the non-traded good increases when its supply shrinks (details in the technical appendix):

$$\frac{\frac{P_2^N}{P_2^N}}{P_1^N} = \left(\frac{Y_1^N}{Y_2^N}\right)^{\frac{\sigma}{1-\gamma+\sigma\gamma}} \quad ; \quad \frac{P_2}{P_1} = \left(\frac{Y_1^N}{Y_2^N}\right)^{\frac{(1-\gamma)\sigma}{1-\gamma+\sigma\gamma}}$$

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# Current account (1)

• The ratio of current account to traded output is  $(1 + g^N) = Y_2^N / Y_1^N$  and  $1 + g^T = Y_2^T / Y_1^T$ ):

$$\frac{\textit{CA}_{1}}{\textit{Y}_{1}^{\textit{T}}} = 1 - \frac{1}{1 + \beta \left( 1 + \textit{g}^{\textit{N}} \right)^{\frac{(1 - \gamma)(1 - \sigma)}{1 - \gamma + \sigma \gamma}}} \left( 1 + \beta \left( 1 + \textit{g}^{\textit{T}} \right) \right)$$

 For simplicity starts from a case where all outputs are constant, and the current account is zero.

$$\begin{array}{lcl} \frac{\partial}{\partial g^T} \left( \frac{CA_1}{Y_1^T} \right) & = & -\frac{\beta}{1+\beta} < \textcolor{red}{\mathbf{0}} \\ \\ \frac{\partial}{\partial g^N} \left( \frac{CA_1}{Y_1^T} \right) & = & \textcolor{blue}{(1-\sigma)} \frac{\beta}{1+\beta} \frac{(1-\gamma)}{1-\gamma+\sigma\gamma} \end{array}$$

 Permanent increases in either output have not effects on the current account or real exchange rate dynamics.

# Effect of endowment growth

- Higher  $g^T$  leads to a current account deficit, but no change in the real exchange rate dynamics.
  - As in last week, smooth consumption.
- Higher  $g^N$  leads to:
  - Real depreciation path  $(P_2 < P_1)$
  - Current account deficit,  $\sigma > 1$ , utility more concave than log (corresponds to  $\frac{1}{\sigma} - \frac{1}{n} < 0$ ).
  - Non-traded relative scarce and expensive today, dominant impact is shift of consumption in period 1 from non-traded to traded good, hence deficit \$
- Equally higher  $g^T$  and  $g^N$  leads to a current account deficit:

$$\frac{\partial}{\partial g^T} \left( \frac{CA_1}{Y_1^T} \right) + \frac{\partial}{\partial g^N} \left( \frac{CA_1}{Y_1^T} \right) = \frac{\beta}{1+\beta} \frac{-\sigma}{1-\gamma+\sigma\gamma} < 0$$

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### TERMS OF TRADE

# Different traded goods

- Two traded goods: one is produced at home (index H) and the other abroad (index F). No non-traded good.
- Consumption of the traded goods is a basket:

$$C_t = \left[ \left( \theta \right)^{\nu} \left( C_t^H \right)^{1-\nu} + \left( 1 - \theta \right)^{\nu} \left( C_t^F \right)^{1-\nu} \right]^{\frac{1}{1-\nu}}$$

• Normalize the foreign price to 1. The terms-of-trade are the ratio of the home good to the foreign one:

$$Q_t^{tot} = \frac{P_t^H}{P_t^F} = P_t^H$$



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# Consumption allocation

• Total expenditure is  $P_t C_t = Q_t^{tot} C_t^H + C_t^F$ . Optimal allocation minimizes it, subject to a target value for  $C_t$ , leading to (same steps as for the traded / non-traded analysis):

$$C_t^H = \theta \left[ \frac{Q_t^{tot}}{P_t} \right]^{-\frac{1}{\nu}} C_t \quad ; \quad C_t^F = (1 - \theta) \left[ \frac{1}{P_t} \right]^{-\frac{1}{\nu}} C_t$$

$$P_t = \left[ \theta \left[ Q_t^{tot} \right]^{\frac{\nu - 1}{\nu}} + (1 - \theta) \right]^{\frac{\nu}{1 - \nu}}$$

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### Intertemporal choice

• Maximization of intertemporal log utility ( $\sigma = 1$ ):

$$U_1 = ln(C_1) + \beta ln(C_2)$$

 Output of domestic traded good is an endowment. Invest in a bond denominated in the foreign good. The budget constraints are:

$$B_2 + P_1 C_1 = Q_1^{tot} Y_1^H$$
  
 $P_2 C_2 = Q_2^{tot} Y_2^H + (1+r) B_2$ 

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#### Euler condition

Allocation given by the Euler condition:

$$C_2 = \beta (1 + r) \frac{P_1}{P_2} C_1$$

$$C_2 = \beta (1 + r^C) C_1$$

- The real interest rate in terms of the consumption basket  $r^{C}$  (relative price of the period 1 consumption basket) reflects the dynamics of the terms of trade.
- If the Home good becomes more valuable,  $Q_2^{tot} > Q_1^{tot}$ , the price of the consumption basket increases through time,  $P_2 > P_1$ .
- This makes the current basket relatively cheap, i.e. an decrease in the real interest rate.

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#### Current account

 Current account is the difference between the value of the Home good endowment and that of the overall traded consumption basket:

$$CA_1 = Q_1^{tot} Y_1^H - P_1 C_1$$

The current account reflects the dynamics of the terms of trade:

$$\frac{\mathit{CA}_1}{\mathit{Q}_1^{tot}\mathit{Y}_1^H} \ = \ \frac{1}{1+\beta} \left[ \beta - \frac{1}{1+r} \frac{\mathit{Q}_2^{tot}\mathit{Y}_2^H}{\mathit{Q}_1^{tot}\mathit{Y}_1^H} \right]$$

- Rising value of the Home endowment  $Q_2^{tot}Y_2^H > Q_1^{tot}Y_1^H$  leads to a deficit:
  - Smooth consumption, as endowment tilted to the future.
  - Rising terms-of-trade leads to a decrease in the real interest rate (in terms of the traded basket).
- Solving for the terms-of-trade requires extra steps (Foreign demand, goods market clearing).

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### COMBINING VARIOUS DIMENSIONS

#### Nested indices

• The overall consumption basket consists of non-traded and traded goods, with the later being itself a basked of domestic and imported goods (set  $\eta = \nu = 1$  for simplicity).

$$C_t = \left(C_t^T\right)^{\gamma} \left(C_t^N\right)^{1-\gamma} \quad ; \quad C_t^T = \left(C_t^H\right)^{\theta} \left(C_t^F\right)^{1-\theta}$$

- Prices are expressed in Home currency, and denoted by  $P_t^H$ ,  $P_t^F$ ,  $P_t^T$ ,  $P_t^N$  and  $P_t$ .
- Consumption allocation and price indices are:

$$C_{t}^{T} = \gamma \frac{P_{t}C_{t}}{P_{t}^{T}} ; \quad C_{t}^{N} = (1 - \gamma) \frac{P_{t}C_{t}}{P_{t}^{N}}$$

$$C_{t}^{H} = \theta \frac{P_{t}^{T}C_{t}^{T}}{P_{t}^{H}} ; \quad C_{t}^{F} = (1 - \theta) \frac{P_{t}^{T}C_{t}^{T}}{P_{t}^{F}}$$

$$P_{t} = (\gamma)^{-\gamma} (1 - \gamma)^{-(1 - \gamma)} \left(P_{t}^{T}\right)^{\gamma} \left(P_{t}^{N}\right)^{1 - \gamma}$$

$$P_{t}^{T} = (\theta)^{-\theta} (1 - \theta)^{-(1 - \theta)} \left(P_{t}^{H}\right)^{\theta} \left(P_{t}^{F}\right)^{1 - \theta}$$

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### Foreign country

The allocation is similar in the Foreign country, with indices:

$$C_t^* = \left(C_t^{T*}\right)^{\gamma} \left(C_t^{N*}\right)^{1-\gamma} \quad ; \quad C_t^{T*} = \left(C_t^{H*}\right)^{1-\theta} \left(C_t^{F*}\right)^{\theta}$$

- The weight  $\theta$  applies to the domestic traded good. If  $\theta > 0.5$  the basket is tilted towards the domestic traded good.
- Foreign prices prices, expressed in Foreign currency, are denoted by  $P_t^{H*}$ ,  $P_t^{F*}$ ,  $P_t^{T*}$ ,  $P_t^{N*}$  and  $P_t^*$ . The indices are:

$$P_t^* = (\gamma)^{-\gamma} (1 - \gamma)^{-(1 - \gamma)} \left(P_t^{T*}\right)^{\gamma} \left(P_t^{N*}\right)^{1 - \gamma}$$

$$P_t^{T*} = (\theta)^{-\theta} (1 - \theta)^{-(1 - \theta)} \left(P_t^{F*}\right)^{\theta} \left(P_t^{H*}\right)^{1 - \theta}$$

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# Real exchange rate and terms-of-trade

- Nominal exchange rate between the Home and Foreign:  $E_t$  (increase is a Home currency nominal depreciation).
- Real exchange rate and terms-of-trade (earnings of an export / cost of an import):

$$Q_t^{rer} = \frac{E_t P_t^*}{P_t} \quad ; \quad Q_t^{tot} = \frac{E_t P_t^{H*}}{P_t^F}$$

The real exchange rate is:

$$Q_t^{rer} = \left(\frac{\left(E_t P_t^{F*}\right)^{\theta} \left(E_t P_t^{H*}\right)^{1-\theta}}{\left(P_t^{H}\right)^{\theta} \left(P_t^{F}\right)^{1-\theta}}\right)^{\gamma} \left(\frac{E_t P_t^{N*}}{P_t^{N}}\right)^{1-\gamma}$$

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# Law of one price and Purchasing Power Parity

Law of one price: a good sells for the price in all countries:

$$P_t^H = E_t P_t^H ; \quad \frac{P_t^F}{E_t} = P_t^{F*}$$

 Purchasing Power Parity: the consumer price indices are the same in all countries, one converted in the same currency:

$$P_t = E_t P_t^*$$

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### Some particular cases

• If the basket is symmetric ( $\theta = 0.5$ ), and the law of one price holds, the real exchange rate reflects the price of non-traded goods:

$$Q_t^{rer} = \left(\frac{E_t P_t^{N*}}{P_t^N}\right)^{1-\gamma}$$

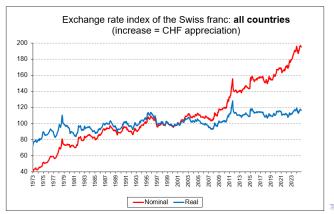
- A country with more expensive non-traded goods, for instance due to higher overall income, has a more appreciate (real) currency.
- If the countries have a bias towards domestic goods ( $\theta > 0.5$ ) and the law of one price holds, the real exchange rate is affected by the terms-of-trade:

$$Q_t^{rer} = \left( \left( \frac{1}{Q_t^{tot}} \right)^{2\theta - 1} \right)^{\gamma} \left( \frac{E_t P_t^{N*}}{P_t^N} \right)^{1 - \gamma}$$

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#### Does PPP hold?

- Not in absolute terms, reflecting in part different prices of non-traded goods.
- More so in relative terms (first difference): the real exchange rate varies, but is stationary. In other words, prices take time to adjust to the nominal exchange rate.



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### **ENDOGENOUS OUTPUT**

## Technology

- Small open economy with traded and non-traded good. Price of traded good set a  $\frac{1}{t}$ , with price of non-traded good equal to  $\frac{P_t^N}{t}$ 
  - Higher value raises the consumer price index: a real appreciation.
- Production uses labor and capital, with productivity shifter:

$$Y_t^T = A_t^T \left(K_t^T\right)^{\alpha_T} \left(L_t^T\right)^{1-\alpha_T} \quad ; \quad Y_t^N = A_t^N \left(K_t^N\right)^{\alpha_N} \left(L_t^N\right)^{1-\alpha_N}$$

• Profit maximization implies (k = K/L):

$$r = \alpha_T A_t^T \left( k_t^T \right)^{\alpha_T - 1}; \quad \mathbf{w} = (1 - \alpha_T) A_t^T \left( k_t^T \right)^{\alpha_T}$$

$$r = P_t^N \alpha_N A_t^N \left( k_t^N \right)^{\alpha_N - 1}; \quad \mathbf{w} = P_t^N (1 - \alpha_N) A_t^N \left( k_t^N \right)^{\alpha_N}$$

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### Solution for price

• Capital mobility gives the world real interest rate r. This gives  $k_t^T$ , and in turn w:

$$k_{t}^{T} = \left(\frac{\alpha_{T}A_{t}^{T}}{r}\right)^{\frac{1}{1-\alpha_{T}}}$$
;  $\mathbf{w} = (1-\alpha_{T})A_{t}^{T}\left(\frac{\alpha_{T}A_{t}^{T}}{r}\right)^{\frac{\alpha_{T}}{1-\alpha_{T}}}$ 

 Putting these in the two relation for the non-traded sector gives the price of the non-traded good:

$$P_t^N = \frac{\left(A_t^T\right)^{\frac{1-\alpha_N}{1-\alpha_T}}}{A_t^N} \left(r\right)^{\frac{\alpha_N-\alpha_T}{1-\alpha_T}}$$



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# Impact of productivity

- Harrod • Increase in productivity in the traded sector  $A_t^T$ : Balassa Samuel Higher capital ratio.
  - Higher wage, thanks to a) direct productivity effect and b) higher capital ratio.
  - Non-traded firms must match the higher wage.

PN up Requires them to increase the price, especially if they are more reliant on labor that traded goods producers  $(\frac{1-\alpha_N}{1-\alpha_T}>1)$ .

- Increase in productivity in the non-traded sector  $A_{\star}^{N}$ :
  - No impact on the traded sector.
- PN down Wage is unchanged. Non-traded producers fully pass-on the higher productivity into lower prices
  - Dutch disease, if there are several traded good sectors, with a gain in only some of them.
    - Productivity gain leads to a real exchange appreciation.
    - Producers of the traded goods that did not see a gain have to raise wages, but cannot increase their price (set by world markets).

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#### Two countries

- Follow similar steps in the Foreign country.
- The ratio of prices is then:

$$ln\left(\frac{P_t^{N*}}{P_t^{N}}\right) = \frac{1 - \alpha_N}{1 - \alpha_T} ln\left(\frac{A_t^{T*}}{A_t^{T}}\right) - ln\left(\frac{A_t^{N*}}{A_t^{N}}\right)$$

- The real exchange rate is affected by productivity, but differently depending on which sector sees an increase (Balassa-Samuelson effect).
  - Difference between traded and non-traded sectors.
  - Cross-country difference. A global productivity boom does not impact the real exchange rate. Not surprising, as the real exchange rate is about cross-country differences.