## Macroeconomics A

Lecture 6: Credit Frictions

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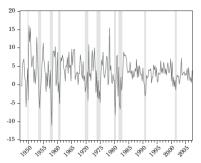
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## The "Great Moderation", 1980 – 2007

- ► Macroeconomic volatility during 1980 2007 much lower than before
- ▶ Lucas (2003): "[...] macroeconomics in this original sense has succeeded: its central problem of depression prevention has been solved, for all practical purposes, and has in fact been solved for many decades."
- Why? Commonly given reasons:
  - ► Independent CBs and good MP
  - Structural change from manufacturing (volatile) to services (believed to be less volatile)
  - ► More information available (IT revolution)
  - Luck

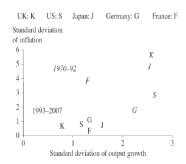
# The "Great Moderation", 1980 – 2007

GDP Growth, 1947-2007 (quarterly, annual rate in percent) (US)



Source: National Income and Product Accounts.

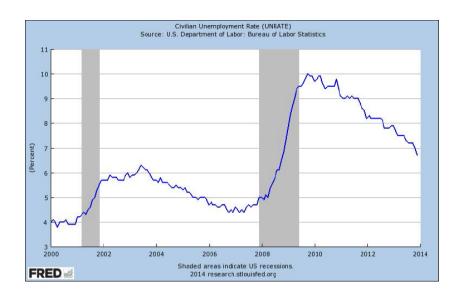
Note: Shaded periods represent NBER-designated recessions



Source: Bean, EJ, 2009.

### Increase in debt





#### Credit frictions

No role for financial sector and asset prices in the models so far. Recent experience (financial crisis 2008-2010) says there must be a link between finance and macro.

- ➤ The financial crisis can be analysed from many different angles (labor: banker's pay and incentives, intl macro: savings glut, micro: coordination failures/bank runs, political economy).
- We are going to model one mechanism that gives a role for asset prices in the transmission of shocks. This is by far not the only explanation for what happened!
- ➤ This mechanism gives an answer to the question: why were the real effects of the bursting of the housing bubble so big?

## Quantitative model of the financial accelerator

- Original model of financial accelerator due to Kiyotaki and Moore (1998).
- Study a simplified version of Bernanke, Gertler, Gilchrist (1999), which is closer to NK and aims to be quantitative model.
- ► Three types of agents: households, entrepreneurs, retailers
- Households: Supply labor, save, and consume goods. Standard.
- Entrepreneurs: Borrow to invest, accumulate net worth, supply some labor,
- Retailers: Buy the homogenous good produced by entrepreneurs and differentiate them before selling on to households. Retail prices are sticky.

# Credit markets and asymmetric information

- ► Fundamental problem that borrowers have more information about (and more control over) the projects they undertake than the lenders who finance them.
- Assume lender cannot verify the outcome of an investment project without some monitoring cost.
- Known as costly state verification (CSV) problem.
- ► Leads to a positive *external finance premium* (= cost of financing from outside the firm relative to opportunity cost)
- Ability to borrow is constrained by net worth

## Entrepreneurs

- ► Risk-neutral (otherwise very hard)
- ▶ Die with probability  $1 \gamma$  (so that they never accumulate enough net worth to become self-financing)
- Borrow money (in addition to using their net worth) to acquire capital
- Also supply some labor to the general labor market

# Idiosyncratic risk for entrepreneurs

Let's first look at the entrepreneur's problem and financing frictions in a simplified setting.

► Entrepreneurs can do a "project" in every period, which yields a total nominal payoff of

$$\omega R^k QK$$

if K units of capital are used. Q is the price of one unit of capital. Hence,  $\omega R^k$  is the gross nominal return on capital.  $R^k$  is the aggregate component (common for all firms) and  $\omega$  is the firm-specific component.

- ▶  $\omega$  drawn from a continuous distribution with CDF F(x), PDF f(x), an expectation  $\mathbb{E}(\omega) = 1$ .
- $\blacktriangleright$  Ex ante, neither the entrepreneur nor the lender observe  $\omega$  prior to undertaking project
- Ex post, the entrepreneur observes  $\omega$ . The lender would have to incur a monitoring cost, which is a fraction  $\mu$  of the ex post project payoff, in order to see  $\omega$ .

# Borrowing decision and contract offered by lender

- Suppose an entrepreneur has net worth N at the beginning of the period.
- ▶ The price of capital goods is *Q*.
- For the entrepreneur to acquire K units of capital, an amount QK N must be borrowed once net worth has been used.
- If the entrepreneur's idiosyncratic shock is  $\omega$ , the total project payoff is  $\omega R^k QK$
- ▶ The financial contract we consider specifies a threshold  $\overline{\omega}$ .
  - if  $\omega \geq \overline{\omega}$  then a fixed amount  $\overline{\omega}R^kQK$  is repaid
  - if  $\omega < \overline{\omega}$  then the borrower defaults, and after the lender has inspected the project and determined  $\omega$ , an amount  $(1-\mu)\omega R^k QK$  can be seized.
- ► This type of contract is known as *risky debt* and can be shown to contain a contract that is optimal from the borrower's pespective (see micro/mechanism design class).

#### Lender's return

- ► Suppose the lender is able to diversify lending across a large representative sample of entrepreneurs with net worth *N*.
- As entrepreneurs' idiosyncratic draws are independent, the law of large numbers applies and the actual return on lending amount QK N is:

$$\left(\overline{\omega}(1-F(\overline{\omega}))+(1-\mu)\int_0^{\overline{\omega}}\omega f(\omega)d\omega\right)R^kQK$$

Suppose the lender's outside option for lending is to earn a risk-free interest R. Assuming perfect competition between lenders, we get that the above must equal R(QK - N).

# Division of gross profits

 Define the lender's gross share of aggregate revenues (before monitoring costs) as

$$\Gamma(\overline{\omega}) \equiv \int_0^{\overline{\omega}} \omega f(\omega) d\omega + \overline{\omega} \int_{\overline{\omega}}^{\infty} f(\omega) d\omega$$

and

$$G(\overline{\omega}) \equiv \int_0^{\overline{\omega}} \omega f(\omega) d\omega$$

- ▶ Then the monitoring costs are  $\mu G(\overline{\omega})$ .
- ▶ Lender's net share of revenues =  $\Gamma(\overline{\omega}) \mu G(\overline{\omega})$
- ▶ Borrower's net share of revenues  $= 1 \Gamma(\overline{\omega})$

# Optimal contracting problem

- Maximize borrower's payoff in the aggregate (or expectation of individual's payoff: is the same because of LLN) subject to lender wanting to participate (gets at least his outside option)
- ▶ Choice variables: terms of the loan: default threshold  $\overline{\omega}$  and amount lent  $B \equiv QK N$ . For given Q and N, maximizing over K is equivalent to maximizing over B.
- ► Formally:

$$\max_{K,\overline{\omega}} (1 - \Gamma(\overline{\omega})) R^k QK \tag{1}$$

s.t. 
$$(\Gamma(\overline{\omega}) - \mu G(\overline{\omega}))R^k QK = R(QK - N)$$
 (2)

▶ Define the external finance premiunm  $s \equiv R^k/R$  and  $k \equiv QK/N$  and rewrite the problem as

$$\max_{k,\overline{\omega}} (1 - \Gamma(\overline{\omega})) sk \tag{3}$$

s.t. 
$$(\Gamma(\overline{\omega}) - \mu G(\overline{\omega}))sk = k - 1$$
 (4)

# Solving this

First-order conditions from the Lagrangian:

$$\Gamma'(\overline{\omega}) = \lambda(\Gamma'(\overline{\omega}) - \mu G'(\overline{\omega}))$$
$$((1 - \Gamma(\overline{\omega})) + \lambda(\Gamma(\overline{\omega}) - \mu G(\overline{\omega}))) s = \lambda$$

and the constraint must bind:

$$(\Gamma(\overline{\omega}) - \mu G(\overline{\omega}))sk = k - 1$$

Under some regularity conditions, you can show that these equations imply a solution of the form

$$k = \psi(s)$$

where  $\psi(s)$  is increasing in s.

# Interpretation

#### Rewrite as

$$QK = \psi(s)N.$$

The borrower can raise more capital K when

- ▶ the average return on project  $R^k$  increases compared to lender's outside option R (i.e. increase in s):
- ▶ the borrower's net worth *N* increases: higher collateral
- $\triangleright$  when the price of capital  $Q_t$  decreases

The full model makes  $R^k$  stochastic, and allows for contracts contingent on  $R^k$ . Result very similar, with  $s = \mathbb{E}(R^k/R)$ .

# Putting this into general equilibrium

▶ Entrepreneurs' aggregate production function is

$$Y_t = A_t K_t^{\alpha} L_t^{1-\alpha}$$

(Individual production function includes idiosyncratic  $\omega$  component)

Expected gross return to holding one more unit of capital is

$$\mathbb{E}(R_{t+1}^k) = \mathbb{E}\left(\frac{MPK_{t+1} + Q_{t+1}(1-\delta)}{Q_t}\right)$$

which is the supply curve for capital.

▶ Demand curve for capital is found by inverting the result from the optimal contract:

$$\mathbb{E}(R_{t+1}^k) = s\left(\frac{N_{t+1}}{Q_t K_{t+1}}\right) R_{t+1}$$

Note: in "standard" RBC model: supply of capital from households consumption-saving decision, demand from firms. Here: households lend to banks, who then lend to entrepreneurs.

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# Putting this into general equilibrium

Entrepreneur's net worth:

$$N_{t+1} = \gamma \int (\mathsf{Entrep}.i.\mathsf{s} \; \mathsf{profits})_t di + W_t^e$$

where  $W_t^e$  is the entrepreneurs' labor income, and  $\gamma$  is the probability of not dying.

- lacktriangle Households: like in standard RBC, with capital (return  $R_{t+1}$ )
- Entrepreneurs' output  $Y_t$  is sold to the retail sector firms, which are like the monopolistically competitive firms in the NK model (with Calvo prices etc) and who turn this into a the households' consumption goods c(i). Households as in NK model.

# What do we get from all this?

#### Financial accelerator mechanism:

- Consider a negative demand shock to the economy
- Reduces the quantity (or price) of output that can be sold
- ► This reduces the MPK, and hence the asset value of capital used to produce output
- ▶ This reduces the net worth of entrepreneurs who hold capital
- ► This reduces the amount of capital that they can take in future investments, external finance premium s increases
- ► This reduces investment, and aggregate demand

Note: all this requires entrepreneurs to be constrained in their financing!

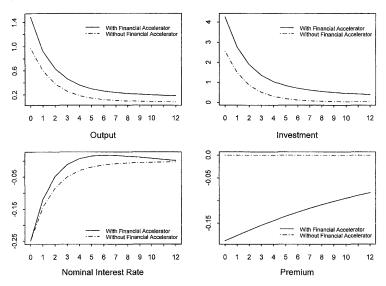
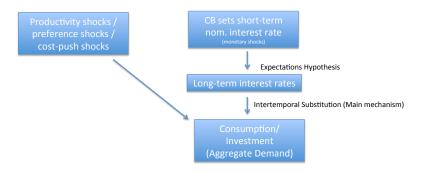
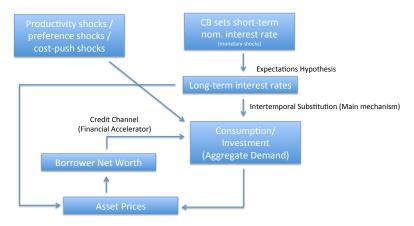


Fig. 3. Monetary shock - no investment delay. All panels: time horizon in quarters.

### Overview



## Overview



# You can play this even further

If you have a channel of how an asset price shock will be amplified, you get even more of a kick

- Bank capital channel: Banks have to maintain a particular maximum leverage ratio (size of the balance sheet vs. core capital)
- If the value of your assets decrease, you have to write it off; capital requirements will not be met anymore
- You have to sell off assets. This, in turn, reduces asset prices (pecuniary externality)
- Then the value of your assets decreases again...

Margin/Haircut spiral: in times of crisis, banks increase 'haircuts', i.e. value assets as a collateral less  $\Rightarrow$  tightens borrowing constraint further

## Overview

