

clustering

Clustering:

Clustering is the grouping of a particular set of objects based on their characteristics, aggregating them according to their similarities.

Advantages:

The main advantage of clustering over classification is that, it is adaptable to changes and helps single out useful features that distinguish different groups.

Disadvantages:

Application:

- clustering analysis is broadly used in market research, pattern recognition, data analysis and image processing.
- clustering can also help marketers discover distinct groups in their customer base.
- In the field of biology, it can be used to derive plant and animal taxonomies.
- clustering also helps in classifying documents on the web for information discovery.

Centroid based clustering: 72 page → centroid medoid

In centroid-based clustering, clusters are represented by a central vector, which may not necessarily be a member of the data set.

k-means clustering is centroid based clustering.

k-means is an iterative clustering algorithm in which items are moved among sets of clusters until the desired set is reached.

The cluster mean of $k_i = \{t_{i1}, t_{i2}, \dots, t_{im}\}$ is defined as,

$$m_i = \frac{1}{m} \sum_{j=1}^m t_{ij}$$

Example 5.4

Suppose that we are given the following items to cluster:

$\{2, 4, 10, 12, 3, 20, 30, 11, 25\}$

Given, $k=2$,

$$m_1 = 2$$

$$m_2 = 4$$

$$\left[\begin{array}{l} m_1 + m_2 \\ \Rightarrow 2 + 4 = \frac{6}{2} = 3 \end{array} \right] \left\{ \begin{array}{l} k_1 \text{ is including} \\ \text{number} \leq 3 \end{array} \right.$$

m_1	m_2	k_1	k_2
2	4	$\{2, 3\}$	$\{4, 10, 11, 12, 20, 25, 30\}$
$\frac{3+2}{2} = 2.5$	16	$\{2, 3, 4\}$	$\{10, 11, 12, 20, 25, 30\}$
3	18	$\{2, 3, 4, 10\}$	$\{11, 12, 20, 25, 30\}$
4.75	19.6	$\{2, 3, 4, 10, 11, 12\}$	$\{20, 25, 30\}$
7	25	$\{2, 3, 4, 10, 11, 12\}$	$\{20, 25, 30\}$

So, the last two steps are identical.

This will yield identical means, and thus the means have converged.

Our answer is thus

$$K_1 = \{2, 3, 4, 10, 11, 12\}$$

$$\text{and } K_2 = \{20, 25, 30\}$$

Dendrogram:

(i) Single link:

Smallest distance between an element in one cluster and an element in the other.

We thus have $\text{dis}(k_i, k_j) = \min(\text{dis}(t_{ij}, t_{jm})) \forall t_{ij} \in k_i \notin k_j \text{ and } \forall t_{jm} \in k_j \notin k_i$.

(ii) Complete link:

Largest distance between an element in one cluster and an element in the other.

We thus have $\text{dis}(k_i, k_j) = \max(\text{dis}(t_{ij}, t_{jm})) \forall t_{ij} \in k_i \notin k_j \text{ and } \forall t_{jm} \in k_j \notin k_i$.

(iii) Average:

Average distance between an element in one cluster and an element in the other.

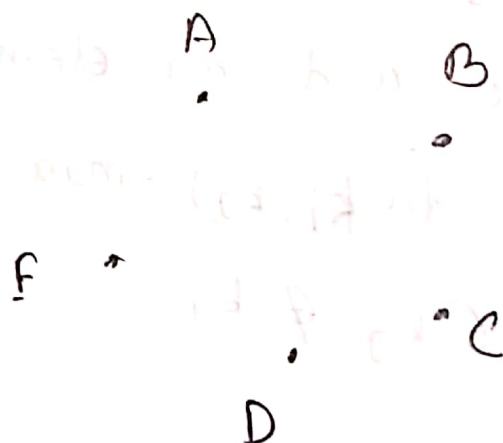
We thus have $\text{dis}(k_i, k_j) = \text{mean}(\text{dis}(t_{ij}, t_{jm})) \forall t_{ij} \in k_i \notin k_j \text{ and } t_{jm} \in k_j \notin k_i$.

and $t_{ij} \in k_i \notin k_j$ and $t_{jm} \in k_j \notin k_i$.

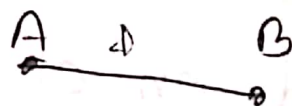
Example 5.3

Item	A	B	C	D	E
A	0	1	2	2	3
B	1	0	2	4	3
C	2	2	0	1	5
D	2	4	1	0	3
E	3	3	5	3	0

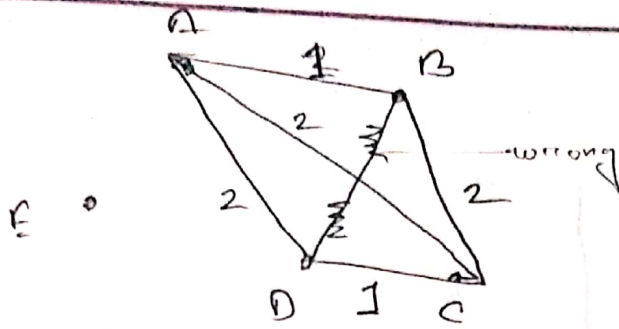
Single Link:



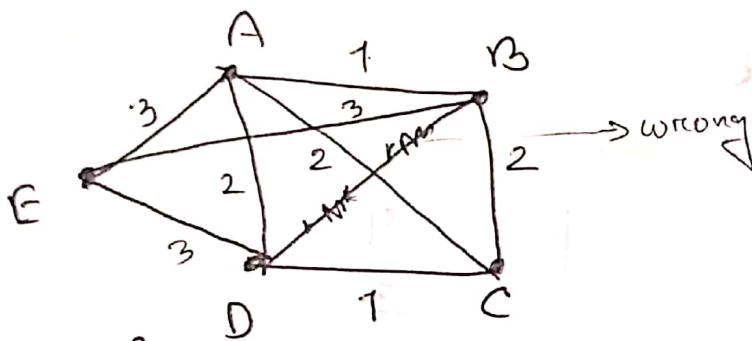
for threshold 0



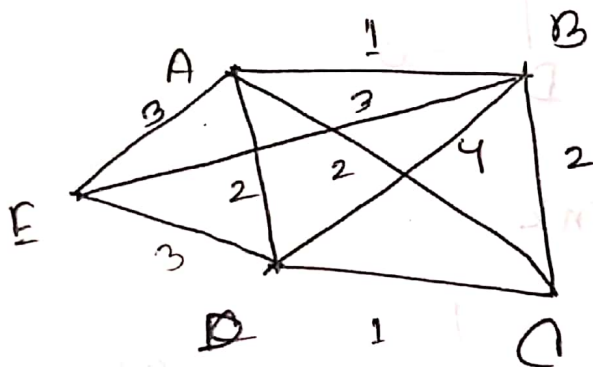
for threshold 1



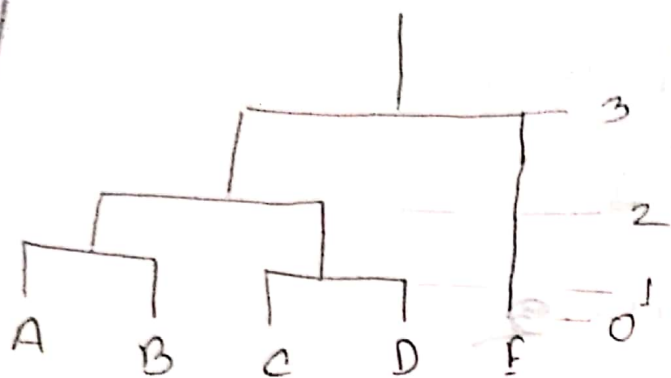
for threshold 2



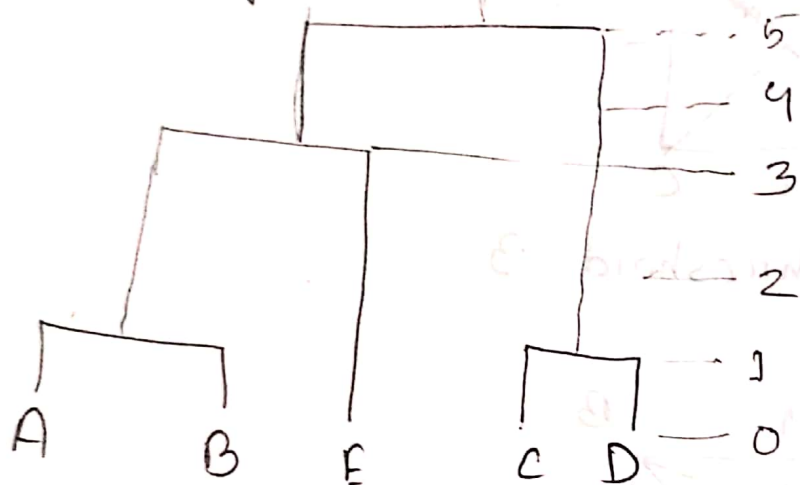
for threshold 3



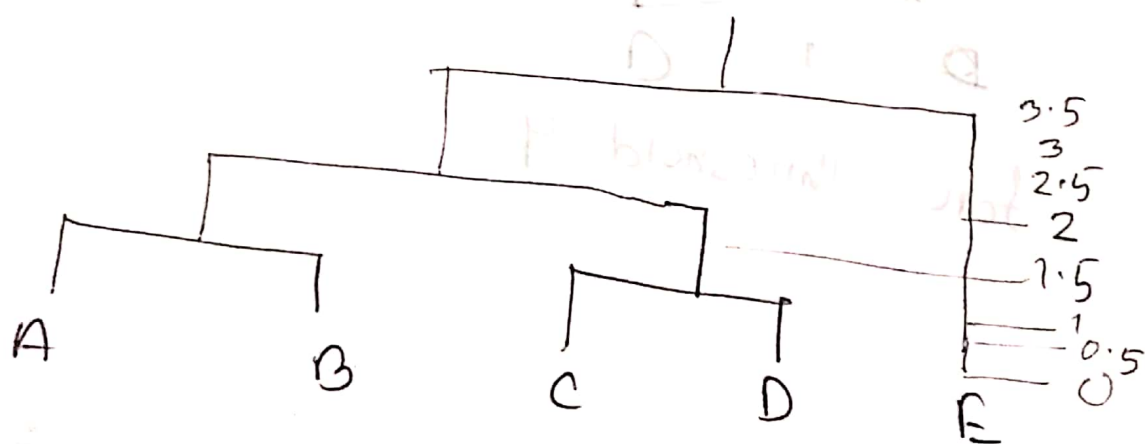
for threshold 4



(a) single link



(b) complete link



(c) Average link

K nearest neighbor Algorithm:

$$K_1 = \{A\}$$

The distance between A to B = $1 \leq 2$

$$\therefore K_1 = \{A, B\}$$

The distance between A to C = $2 \leq 2$

$$B \text{ to } C = 2 \leq 2$$

$$\therefore K_1 = \{A, B, C\}$$

$$A \text{ to } D = 2 \leq 2$$

$$B \text{ to } D = 4 \not\leq 2$$

$$C \text{ to } D = 1 \leq 2$$

$$\therefore K_1 = \{A, B, C, D\}$$

$$A \text{ to } E = 3$$

$$B \text{ to } E = 3$$

$$C \text{ to } E = 5$$

$$D \text{ to } E = 3$$

$$\therefore K_1 = \{A, B, C, D\}$$

$$\therefore K_2 = \{E\}$$

BIRCH:

Balanced iterative reducing and clustering using hierarchies) is designed for clustering a large amount of metric data. It applies only to numeric data.

□ A clustering feature (CF) is a triple (N, \bar{I}, ss) where the number of the points in the cluster is N , \bar{I} is the sum of the points in the cluster, and ss is the sum of the square squares of the points in the cluster.

□ CF tree:

A CF tree is a balanced tree with a branching factor (maximum number of children a node may have) B .

Each internal node contains a CF triple for each of its children. Each leaf node also represents a cluster and contains a CF entry for each subcluster in it.

A ~~subcluster~~ subcluster in a leaf node must have a diameter no greater than a given threshold value T .

DBSCAN!

(density-based spatial clustering of applications with noise) is to create clusters with a minimum size and density.

Density is defined as a minimum number of points within a certain distance of each other.