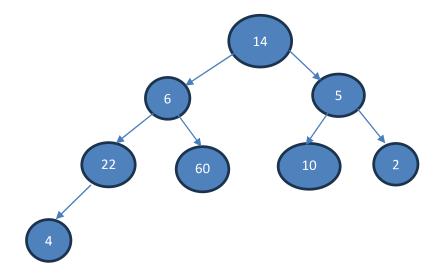
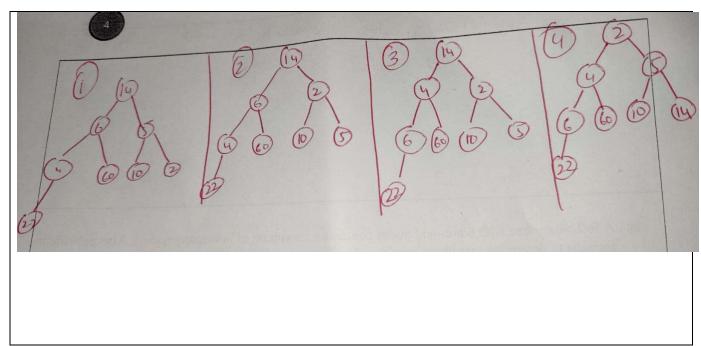
THUMAL ON THUMBER OF THE OFFICE OF THE OFFIC	Course: Program: Duration: Paper Date: Section: Exam:	Data Structures BS(CS, DS, SE, R) 180 Minutes 23-dec- 2023 ALL Final Exam	Course Code: Semester: Total Marks: Page(s): Section: Roll No:	CS 2001 Fall 2023 70 10		
Instruction/Notes:	Answer in the space provided. You can use rough sheets, which will not be marked. Do not use pencil or red ink to answer the questions. In case of confusion or ambiguity make a reasonable assumption. Questions are not allowed.					
Question 1: [CLO	1]			[Marks: 2*5]		
merement stack pe	onter for stack I	and decrement stack pointer	for stack 2.	n operation wi		
merement stack pe	ointer for stack I	and decrement stack pointer	for stack 2.	r operation wi		
b. A full binary	y tree with 6 nor	n-leaf nodes contains a maximum number of nodes at a spe	num of how many nodes?	Also provide t		

c. Build min heap from this given tree using BuildHeap method and show all of your working





- d. Suppose an initially empty stack *S* has performed a total of 25 push operations, and 10 pop operations, 3 of which generated a StackEmpty exception that was caught and ignored. What is the current size of *S*?
- 25-7 = 18 as for three operation nothing is pooed from the stack

Name:	Roll #:

e. Which of the hash table collision-handling schemes could tolerate a load factor above 1 and which could not? Load factor is the ratio of number of elements present in the hash table and size of hash table.

Chaining			

Question 2: [CLO 2]

a. Give an estimate of $\underline{T(N)}$ for each line of the following code. Also, give time complexity (in Big-Oh notation). Compute the tight bounds.

[Marks:5+5+5+2.5+2.5]

```
long compute(int x) {
    long ans = 1;
    for (int i = 1; i <= x; i++)
        ans *= x;
    return ans;
}
void print(int n) {
    for (int i = 0; i < n; i++)
    {
        for (int j = 1; j < (n - i); j++)
            cout << " ";

        for (int k = 0; k <= i; k++)
            cout << endl;
    }
    cout << endl;
}
cout << endl;
}</pre>
```

b. For each node u in an undirected graph, let twodegree[u] be the sum of the degrees of u's neighbors. Explain how to compute the entire array of twodegree[\cdot] values in O(|V|+|E|) time, given a graph in adjacency list format.

First compute the degree of each node by traversing the adjacency list in the first pass. Again traverse the adjectancy list and now sum the degrees of all the neighbours of a node. This way two degree of all the vertices can be computed in O(|V|+|E|) time.

<u>Name:</u>	Roll #:
	we circularly linked lists, L and M such that both the lists contain distinct algorithm for telling if L and M are really the same list of nodes but with
	L ends and find the first element of List M in L. d M until M ends(traverse L from the point where first element of M is
found)	
3. If all the elements match	n then return true otherwise return false
d. How long would it take to	o remove the $\lceil \log n \rceil$ smallest elements from a heap that contains n entries
using the removeMin() of	peration?
$O(\log(n)*\log(n)) = O((\log(n))^2)$	

Name:_	Roll #:
e	Explain how to use an AVL tree to sort n elements in $O(n\log n)$ time in the worst case.
Insert	all the n element in an AVL tree and then perform an inorder traversal

Question 3: [CLO 3]

a. Write a <u>recursive</u> C++ function bool IsHeap(...) in a <u>Binary tree</u> class, that determines if the Binary tree is a MIN-HEAP or not in **O(n) time.** Note its Binary tree (BT) not a BST.

[Marks: 15+15]

You code should sure that the Binary tree meets both requirements of heap to be classified as a binary minheap.

- i) Heap structure property (Complete Binary Tree)
- ii) Heap Order property

Provide the code of any helper function that you use in your bool IsHeap(...) function. Write a wrapper function if needed.

```
        class Bnode {
        template <class T>

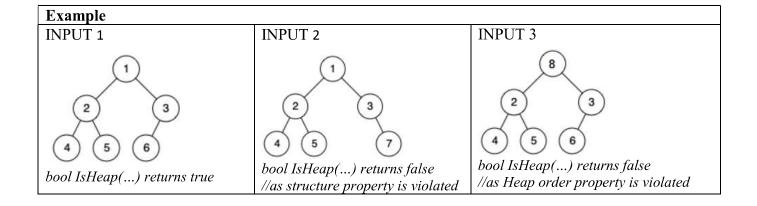
        public:
        class BinaryTree {

        Bnode * left;
        public:

        Bnode * right;
        BTree();

        bool IsHeap(...)
        private:

        Bnode * root;
        };
```



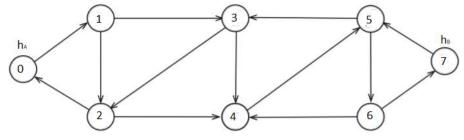
Name:_____ Roll #: _____

```
int countNodes(struct Node* root)
             if (root == NULL)
                   return (0);
             return (1 + countNodes(root->left) + countNodes(root->right));
bool isComplete(Bnode* root, int index, int number_nodes)
             // An empty tree is complete
      if (root == NULL)
             return true;
      if (index >= number_nodes)
             return false:
      // Recur for left and right subtrees
      return (isComplete(root->left,2*index+1,number_nodes) && isComplete(root->right,
2*index + 2, number_nodes));
bool isHeapProperty(Bnode* root)
      if (root->left == NULL && root->right == NULL)
             return true;
      if (root->right == NULL) {
             return (root->key >= root->left->key);
      else {
             if (root->key >= root->left->key && root->key >= root->right->key)
                   return ((isHeapProperty(root->left)) && (isHeapProperty(root>right)));
             else
                   return false;
             }
}
bool IsHeap(Bnode* root) {
      int node_count = countNodes(root);
      int index = 0;
      if (isComplete(root, index, node_count) && isHeapProperty(root))
             return true;
      return false;
}
bool IsHeap(root) {
     return IsHeap(root) {
```

Name:	Roll #:

b. Two spy, Ahmad and Baber have been stationed in the enemy territory at houses h_A and h_B respectively. Ahmed needs to hand over a secret information to Baber. It is decided that Ahmed and Baber will meet each other at a third location, a hotel, where the information will be exchanged. The secret agency has already prepared a road map of the enemy territory. It contains the homes h_A, h_B, and the n hotels in the area: h1, h2, ..., hn. This map formulates a graph where each location (houses and hotels) are its vertices and if one location is directly reachable via a road from the other then there is an edge between them. Each edge (road) poses a risk of being caught. The total risk of a path is simply the number of edges on that path.

The agency wishes to tell Ahmed and Baber which hotel, h, to meet at so that the total risk, for both of them combined, is minimized. Such a hotel would be the *safest hotel*. Note that both Ahmed and Baber would need to travel to h to make the delivery possible. The problem is that the map is too large for manual processing. Therefore, you have been tasked to write a C++ program that can find and return the id of the safest hotel given the graph G and locations h_A and h_B . Your goal is to write a function in Graph class that takes no more than O((|V|+|E|)) time to accomplish this task. If you use any helper function then also provide its code. You can assume that graph is represented as adjacency list and all the vertices are labelled 0 to |V|-1. Consider the example below: Vertex 0 is h_A and vertex 7 is h_B , here the safest hotel is vertex 3 and the minimum total risk is 4.



```
#include class Graph{
    int V; // No. of vertices
    list<int> *adjList; //adjacency lists of neighbours (std list)

public:
    Graph(int V); // Constructor
    ... SafestHotel(...) // think of input parameter and return type
};
```

Name:_____ Roll #: _____

```
void BFS(int s, int* d) {
             bool* visited = new bool[V];
             for (int i = 0;i < V; i++)</pre>
                    visited[i] = false;
             d[s] = 0;
             queue<int> q;
             q.push(s);
visited[s] = true;
             while (!q.empty()) {
                    int v = q.front();
                    q.pop();
                    list<int>::iterator it;
                    for (it = adjList[v].begin(); it != adjList[v].end();it++) {
                           int u = *it;
                           if (visited[u] == false) {
                                  visited[u] = true;
                                  d[u] = d[v] + 1;
                                  q.push(u);
                           }
                    }
             }
      }
```

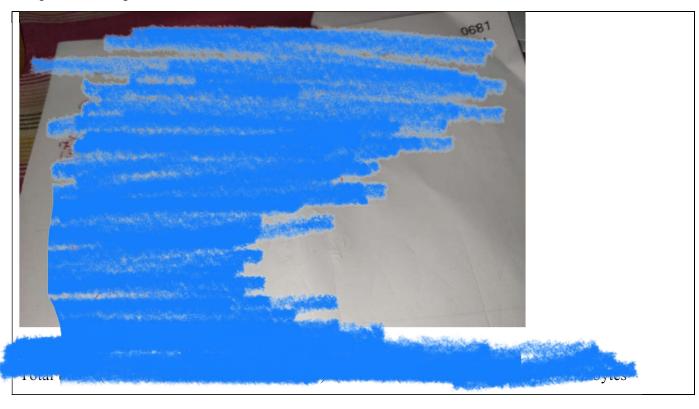
Name: _____Question 4: [CLO 4]

Roll #: _____

Question 4: [CLO 4] [Marks: 5+5]
a. Suppose a file contains the following characters along with their frequencies.

D: 100, L: 150, E: 120, N: 30, K: 130, W: 40, O: 10

How many bytes will be required to store this file if Huffman encoding scheme is used. Show your complete working.



b. Consider the following Hash tables, T1 and T2 of same sizes.

Hash function for table T1 is simple mod functions t1 = hf1(key % T1_size)

The hash function for table T2 is **t2= hf2(reverse_key % T2_size)** which reverses the key first and then takes mod with table size T2.

The keys 72,86,71,52,23 and 17 are inserted into an initially empty hash using open addressing and linear probing. After filling out both tables give a valid reason with hash function is better and why.

	0	1	2	3	4	5	6	7
T1	72	23	17		52		86	71

	0	1	2	3	4	5	6	7
T2	23	71	52	72	86			17

Number of collisions faced by hf1 is 3 and hf2 is 1 so second hash function is better than first hash function

Name:	Roll #:

Rough Sheet