

GPS Signal Description

1. The baseband signal **transmitted** by the satellite is given as

$$S(t) = S_{PPS}(t) + jS_{SPS}(t) \quad (1)$$

- $S_{SPS}(t) = \sum_{i=-\infty}^{\infty} c_{sps}([i]_{L_sps}).d([i]_{CD_sps}).rect_{T_{c,sps}}(t - iT_{c,sps})$ — Standard Positioning Service
- $S_{PPS}(t) = \sum_{i=-\infty}^{\infty} c_{pps}([i]_{L_pps}).d([i]_{CD_pps}).rect_{T_{c,pps}}(t - iT_{c,pps})$ — Precision Positioning Service

2. Let $x_{in}[n]$ be the incoming signal at the **receiver** end and is given as

$$x_{in}[n] = A(t)s_T(t - \tau(t))e^{j(2\pi f_D(t)t + \phi(t))}|_{t=nT_s} + n(t)|_{t=nT_s} \quad (2)$$

where

- $A(t)$ is Amplitude
- $s_T(t)$ is Complex baseband signal
- $\tau(t)$ is code delay(time varying)
- $f_D(t)$ is Doppler shift(time varying)
- $\phi(t)$ is carrier phase shift(time varying)
- $n(t)$ is Random noise with zero mean
- T_s is Sampling period
- f_s is Sampling frequency

Pseudo code for GPS Signal Acquisition

1.1 Functions for computing the PRN codes of GPS satellite

1. (a) g1_lfsr()

```
state = 0x3FFF
Declare an array out[1023]
for i=0 to i=1022
    out[i] = (state >> 9) & 0x1
    new_bit = ((state >> 9) ⊕ (state >> 2)) & 0x1
    state = ((state << 1) | new_bit) & 0x3FFF
end for
return out
```

- (b) g2_lfsr(tap0,tap1)

```
state = 0x3FFF
Declare an array out[1023]
tap0 = tap0-1
tap1 = tap1-1
for i=0 to i=1022
    out[i] = ((state >> tap0) ⊕ (state >> tap1)) & 0x1
    new_bit = ((state >> 9) ⊕ (state >> 8) ⊕ (state >> 7) ⊕ (state >> 5) ⊕ (state >> 2) ⊕ (state >> 1)) & 0x1
    state = ((state << 1) | new_bit) & 0x3FFF
end for
return out
```

- (c) combine.g1.g2(g1,g2)

```
declare out[1023]
for i=0 to i=1022
    out[i] = g1[i] ⊕ g2[i]
end for
return out
```

1.2 Main function

1. PRN Code frequency f_c is 1.023Mhz
2. Sampling frequency f_s is 2.048Mhz
3. The number of samples \mathbf{N} for 1ms is 2048
4. Static array $\mathbf{SVs}[64] = [2, 6, 3, 7, 4, 8, 5, 9, 1, 9, 2, 10, 1, 8, 2, 9, 3, 10, 2, 3, 3, 4, 5, 6, 6, 7, 7, 8, 8, 9, 9, 10, 1, 4, 2, 5, 3, 6, 4, 7, 5, 8, 6, 9, 1, 3, 4, 6, 5, 7, 6, 8, 7, 9, 8, 10, 1, 6, 2, 7, 3, 8, 4, 9]$ /* Array to store Phase selector values for 32 satellites - 2 values per satellite*/
5. Static array $\mathbf{g1}[1023]$
6. static array $\mathbf{g2}[32][1023]$
 /* Generating PRN code, BPSK modulation and upsampling for all 32 satellites */
7. $\mathbf{g1} = \mathbf{g1_lfsr}()$ /* Fucntion call */
8. $\mathbf{k}=0$
9. $\mathbf{visible_satellites} = 0$
10. **for** $\mathbf{sv}=01$ to $\mathbf{sv}=32$:
 tap0 = $\mathbf{SVs}[\mathbf{k}++]$
 tap1 = $\mathbf{SVs}[\mathbf{k}++]$
 $\mathbf{g2}[\mathbf{sv}] = \mathbf{g2_lfsr}(\mathbf{tap0}, \mathbf{tap1})$ /* Fucntion call */
 $\mathbf{gold_code} = \mathbf{combine_g1_g2}(\mathbf{g1}, \mathbf{g2})$ /* Fucntion call */

 /*BPSK modulation of PRN code */
for $\mathbf{i} = 0$ to $\mathbf{i} = 1022$
 if $\mathbf{gold_code}[\mathbf{i}] > 0$
 $\mathbf{gold_code}[\mathbf{i}] = -1$
 else
 $\mathbf{gold_code}[\mathbf{i}] = 1$
 /* Upsampling the PRN code */
for $\mathbf{i} = 0$ to $\mathbf{i} = \mathbf{N}-1$
 $\mathbf{c}[\mathbf{2i}] = \mathbf{gold_code}[\mathbf{i}]$
 $\mathbf{c}[\mathbf{2i} + 1] = \mathbf{gold_code}[\mathbf{i}]$

end for

 $\mathbf{c}[2046] = 0$
 $\mathbf{c}[2047] = 0$
11. Capture 2ms samples of incoming signal $x_{in}[n]$
12. Calculate received signal power using the formula

$$P_x = 0$$
for $\mathbf{i}=0$ to $\mathbf{N}-1$

$$P_x = P_x + (x_{in}[n] \times x_{in}^*[n])$$
13. The power of incoming signal should be $P_x > \text{threshold}$. If true, **go to** step 14. else, **stop** the process
14. Initialize the array $\mathbf{max_power}[5] = \{0\}$
15. Initialize the array $\mathbf{visible_satellites_withMaxPower}[5] = \{0\}$

```

16. Initialize the array codePhase[5] = {0}

/* Find out the code phase for 5 satellites having maximum power */

17. for sv=01 to sv=32

    Initialize max = 0
    Initialize max_index = 0
    for n = 0 to n = N-1
        z[n] = 0
        for m = 0 to m = N-1
            index = (m + n) % N
            if c[sv][m] > 0
                z[n] = z[n] + xin[index]
            else
                z[n] = z[n] - xin[index]

        end for
        z[n] = z[n] × z*[n]
        if z[n] > max
            max = z[n]
            max_index = n
        end for

/* Update max_power, visible_satellites_withMaxPower and codePhase arrays */
for i = 0 to i = 4
    if max > max_power[i]
        for j = 4 to j = i-1
            max_power[j] = max_power[j-1]
            visible_satellites_withMaxPower[j] = visible_satellites_withMaxPower[j-1]
            codePhase[j] = codePhase[j-1]
            j = j-1
        end for
        max_power[i] = max
        visible_satellites_withMaxPower[i] = sv
        codePhase[i] = max_index
        break the loop
    end if
end for

end for

/* Finding the Doppler shift for 5 satellites */

18. for sv = 0 to sv = 4

    Code phase  $\hat{\tau}$  = codePhase[sv]
    Initialize max_of_max=0

    Compute conjugate of FFT of  $p_{sv}[n] \rightarrow P_{sv}^*[k]$ 
    for  $f_D = f_{min}$  to  $f_D = f_{max}$  in  $f_{step}$  steps:
        Shift the signal  $x[n]$  by  $f_D$ , for n = 0 to N-1

$$x_{sh}[n] = x_{in}[n + \hat{\tau}] \cdot e^{-j2\pi f_D n T_s} \quad (3)$$


        Apply FFT to  $x_{sh}[n] \rightarrow X_{sh}[k]$ 

```

```

for n = 0 to n = N-1
     $P_{\mathbf{sv}}[n] = c[\text{visible\_satellites\_withMaxPower}[\mathbf{sv}]] [n]$ 
end for
Multiply  $X_{sh}[k]$  and  $P_{\mathbf{sv}}^*[k]$ .

```

$$Y[k] = X_{sh}[k] \cdot P_{\mathbf{sv}}^*[k] \quad (4)$$

```

Compute IFFT for  $Y[k]$ 

```

$$R[n] = IFFT_k\{Y[k]\} \quad (5)$$

```

Initialize max_value = 0

```

```

Initialize max_fd = 0

```

```

for i = 0 to i = N-1

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     $R[\mathbf{i}] = \text{Re}(R[\mathbf{i}])$ 

```

```

    if ( $R_{\mathbf{sv}}[\mathbf{i}] > \text{max\_value}$ )

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```

        max_value =  $R[\mathbf{i}]$ 

```

```

    end if

```

```

end for

```

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if (max_value > max_of_max)

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```

    max_of_max = max_value

```

```

    max_fd =  $f_D$ 

```

```

end if

```

```

end for

```

```

Doppler Frequency offset  $f_{D_{sv}} = \text{max\_fd}$ 

```

```

end for

```