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# THE NAVIC STANDARD

## Through Python

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G. V. V. Sharma



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# Introduction

This book introduces the NAVIC communication standard through Python exercises



## Chapter 1

# Computing the Position and Velocity of the satellite from the RINEX file

### 1.1. Introduction

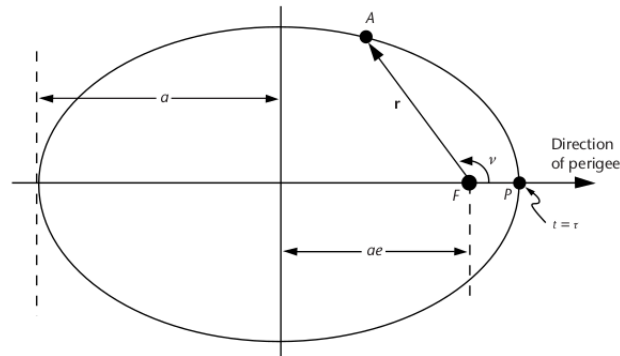
In order to achieve the navigation services we have to find the position and velocity of satellite in its orbit. In order to find the position and velocity we have the source called RINEX file Which contains all the orbital parameters of the satellite in its orbit. In this document we compute the position and velocity of GPS and NAVIC satellites. The RINEX files is different for both the satellites but the algorithm for finding the position and velocity is same.

### 1.2. Determination of satellite position

RINEX files will be available in official websites for all the satellites. The RINEX files contains all the information of the orbital parameters of the particular satellite. The Orbital elements of satellite from rinex file is given in below table.

### 1.2.1. Orbital parameters in rinex file

$\sqrt{a}$	Square root of semimajor axis
e	Eccentricity
$\Delta n$	Mean motion difference from computed value
$M_0$	Mean anomaly at reference time
$\Omega_0$	Longitude of ascending node n of orbit plane at weekly epoch
$i_0$	Inclination angle a at reference time
w	Argument of perigee
$\dot{\Omega}$	Rate of right ascension
IDOT	Rate of inclination angle
$t_{oe}$	Ephemeris reference time
IODE	Issue of data, ephemeris
$C_{uc}$	Amplitude of cosine harmonic h correction term to the argument of latitude
$C_{us}$	Amplitude of sine harmonic correction term to the argument of latitude
$C_{rc}$	Amplitude of cosine harmonic correction term to the orbit radius
$C_{rs}$	Amplitude of sine harmonic correction term to the orbit radius
$C_{ic}$	Amplitude of cosine harmonic correction term to the angle of inclination
$C_{is}$	Amplitude of sine harmonic correction term to the angle of inclination



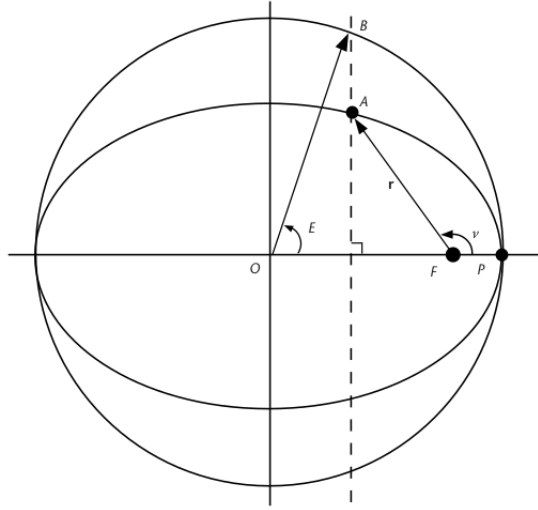
In the above Figure

1. The elliptical orbit has a focus at point F, which corresponds to the center of the mass of the Earth.
2. The time  $t_0$  at which the satellite is at some reference point A in its orbit is known as the epoch.
3. The point, P, where the satellite is closest to the center of the Earth is known as perigee.
4. The time at which the satellite passes perigee,  $t$ , is another Keplerian orbital parameter.

The three Keplerian orbital elements that define the shape of the elliptical orbit and time relative to perigee are as follows:

1.  $a$  = Semimajor axis of the ellipse
2.  $e$  = eccentricity of the ellipse
3.  $t$  = time of perigee passage





In order to find the position of satellite let us understand the keplerian orbital elements.

**True anomaly :** The angle in the orbital plane measured counterclockwise from the direction of perigee to the satellite.

**Eccentric anomaly :** Geometrically, the eccentric anomaly is constructed from the true anomaly first by circumscribing a circle around the elliptical orbit. Next, a perpendicular is dropped from the point A on the orbit to the major axis of the orbit, and this perpendicular is extended upward until it intersects the circumscribed circle at point B. The angle measured at the center of the circle, O, counter-clockwise from the direction of perigee to the line segment.

$$E = 2 \arctan\left(\sqrt{\frac{1+e}{1-e}} \tan\left(\frac{v}{2}\right)\right) \quad (1.1)$$

**Mean anomaly :** The importance of transforming from the true to the mean anomaly is that time

varies linearly with the mean anomaly.

$$M = M_o + n * (t - t_o) \quad (1.2)$$

Where,

$M_o$  is Mean anomaly at the time of epoch.

$M$  is the mean anomaly at time  $t$ .

$$n = \sqrt{\frac{\mu}{a^3}} \quad (1.3)$$

$$\mu = 398,600.5 * 10^8 m^3/s^2 \quad (1.4)$$

In the case of GPS or Navic, the Keplerian parameters are defined in relation to the ECEF coordinate system. In this case, the xy-plane is always the Earth's equatorial plane. The following three Keplerian orbital elements define the orientation of the orbit in the ECEF coordinate system:

**Inclination of orbit :** Inclination is the dihedral angle between the Earth's equatorial plane and the satellite's orbital plane.

**longitude of the ascending node :** The orbital element that defines the angle between the +x-axis and the direction of the ascending node is called the right ascension of the ascending node (RAAN). Because the +x-axis is fixed in the direction of the prime meridian ( $0^\circ$  longitude) in the ECEF coordinate system, the right ascension of the ascending node is actually the longitude of the ascending node,  $\Omega$ .

**Argument of perigee :** Measures the angle from the ascending node to the direction of perigee

in the orbit.

Notice that  $\Omega$  is measured in the equatorial plane, whereas  $\omega$  is measured in the orbital plane.

The following formulas are used for computing the position, velocity of the satellite in the elliptical

orbit. Where the inputs are taken from the rinex file.

$$\Omega = 7.2921151467 * 10^{-5} \text{rad/sec} \quad (1.5)$$

$$a = \sqrt{a^2} \quad (1.6)$$

$$t_k = t - t_o e \quad (1.7)$$

$$n = n_o + \Delta n \quad (1.8)$$

$$M_k = M_o + n t_k \quad (1.9)$$

$$E_k = M_k + e \sin(E_k) \quad (1.10)$$

$$\sin(v_k) = \frac{1 - e^2 \sin E_k}{1 - e \cos E_k} \quad (1.11)$$

$$\cos(v_k) = \frac{\cos(E_k) - e}{1 - e \cos(E_k)} \quad (1.12)$$

$$\phi_k = v_k + w \quad (1.13)$$

$$\delta \phi_k = C_{us} \sin(2\phi_k) + C_{uc} \cos(2\phi_k) \quad (1.14)$$

$$\delta r_k = C_{rs} \sin(2\phi_k) + C_{rc} \cos(2\phi_k) \quad (1.15)$$

$$\delta i_k = C_{is} \sin(2\phi_k) + C_{ic} \cos(2\phi_k) \quad (1.16)$$

$$u_k = \phi_k + \delta \phi_k \quad (1.17)$$

$$r_k = a(1 - e \cos E_k) + \delta r_k \quad (1.18)$$

$$i_k = i_0 + \frac{di}{dt} t_k + \delta i_k \quad (1.19)$$

$$\Omega_k = \Omega_0 + \Omega - \Omega_e(t_k) - \Omega_e t_{oe} \quad (1.20)$$

$$x_p = r_k \cos(u_k) \quad (1.21)$$

$$y_p = r_k \sin(u_k) \quad (1.22)$$

$$x_s = x_p \cos \Omega_k - y_p \cos i_k \sin \Omega_k \quad (1.23)$$

$$y_s = x_p \sin \Omega_k - y_p \cos i_k \cos \Omega_k \quad (1.24)$$

$$z_s = y_p \sin i_k \quad (1.25)$$

By computing the above formulas  $[x_s, y_s, z_s]$  are the position of satellite in ECEF coordinate frame. The velocity of the satellite is obtained by differentiating the above position equations with respect to time. The final equation is as follows:

$$x_v = -x_p \dot{\Omega}_k \sin \Omega_k + x_p \cos \Omega_k - y_p \sin \Omega_k \cos i_k \\ - y_p (\dot{\Omega}_k \cos \Omega_k \cos i_k - \frac{di_k}{dt} \sin \Omega_k \sin i_k)$$

$$y_v = -x_p \dot{\Omega}_k \cos \Omega_k + x_p \sin \Omega_k - y_p \cos \Omega_k \cos i_k \\ - y_p (\dot{\Omega}_k \sin \Omega_k \cos i_k - \frac{di_k}{dt} \cos \Omega_k \sin i_k)$$

$$z_v = y_p \frac{di_k}{dt} \cos i_k + y_p \sin i_k$$

By computing the above formulas  $[x_v, y_v, z_v]$  is the velocity vector of satellite in ECEF coordinate frame.

## Computations of error corrections :

### 1. Clock Correction :

One of the largest sources of error in calculating range is satellite clock error. To get the accuracy of the receiver position signal transmission and reception time must be precisely known. Because of the travel time of light, one nanosecond of inaccuracy in the clock causes 30 centimeter error in position. Satellite clock correction coefficients - clock bias, clock drift, and clock drift rate are obtained from the RINEX Navigation file. Calculation of the satellite clock error is given by

$$\Delta t_{clk} = a_{f0} + a_{f1}(t - t_{oc}) + a_{f2}(t - t_{oc})^2 \quad (1.26)$$

where ,

$\Delta t_{clk}$  is clock offset in seconds.

$t$  is IRNSS system time at transmission in seconds.

$t_{oc}$  is clock data reference time.

$a_{f0}$  is clock bias.

$a_{f1}$  is clock drift.

$a_{f2}$  is clock drift rate.

## 2. Relativistic Correction :

Because of the high speed of satellites and weaker gravity, clocks on the satellites run a little faster than the clock on the Earth. Error found because the relativity is in nanoseconds. The computation of relativistic clock error is given by

$$\delta_{rel} = Fe\sqrt{a} \sin(E) \quad (1.27)$$

where ,

$a$  is semimajor axis of the ellipse.

$e$  is eccentricity of the ellipse.

$F$  is  $-4.442807633 \times 10^{-10}$

$E$  is Eccentric anomaly.  $\delta_{rel}$  is relativistic clock correction

## 1.3. Computing the position and velocity of the GPS satellite using python

Installations :

1. pip3 install pymap3d
2. pip3 install georinex

3. pip3 install itertools
4. pip3 install argparse

**Algorithm for finding the position and velocity of satellite From Rinex file :**

1. Get the rinex file for GPS satellite from the official website.
2. The Rinex file contains the observational file and navigation file.
3. Convert the Rinex file to CSV file using the python

The below python function will convert the GPS RINEX file to CSV file.

```
./rinex_to_csv/funcs.py
```

4. Remove the empty rows in csv file.The python function for removing empty rows is

```
./rinex_to_csv/funcs.py
```

5. Convert the csv file to list in python so that each row is corresponds to the parameters of the satellite. Function for converting the csv file to list is given as :

```
./rinexread/funcs.py
```

6. Process the above list with the formulas mentioned in chapter 2

The python function for finding the position of satellite is given as :

```
./position/funcs.py
```

7. The velocity of the satellite is computed by the function

```
./velocity/funcs.py
```

8. The distance between the satellite and receiver is obtained by the python package called **pymap3d**, using this package convert ECEF to spherical coordinate frame. So that we obtain the distance between satellite and receiver.

9. These position and velocity of the satellite is used for computing the doppler shift.

The above algorithm will work for both GPS and Navic satellite. If there is a problem in converting Navic RINEX file to csv file then follow the instructions below:

1. go to the mentioned folder in your laptop.

```
./home/mannava/.local/lib/python3.10/site-packages/georinex/nav3.py
```

2. Go to the line 220 in nav3.py file and modify the below changes.

```
elif numval == 29: # only one trailing spare fields
    cf = cf[:-2]
elif numval == 28: # only one trailing spare fields
    cf = cf[:-3]
elif numval == 27: # only one trailing spare fields
    cf = cf[:-4]
elif numval == 26: # only one trailing spare fields
    cf = cf[:-5]
```



