

## GPS Signal Description

1. The baseband signal **transmitted** by the satellite is given as

$$S(t) = S_{PPS}(t) + jS_{SPS}(t) \quad (1)$$

- $S_{SPS}(t) = \sum_{i=-\infty}^{\infty} c_{sps}([i]_{L\_sps}).d([i]_{CD\_sps}).rect_{T_{c,sps}}(t - iT_{c,sps})$  — Standard Positioning Service
- $S_{PPS}(t) = \sum_{i=-\infty}^{\infty} c_{pps}([i]_{L\_pps}).d([i]_{CD\_pps}).rect_{T_{c,pps}}(t - iT_{c,pps})$  — Precision Positioning Service

2. Let  $x_{in}[n]$  be the incoming signal at the **receiver** end and is given as

$$x_{in}[n] = A(t)s_T(t - \tau(t))e^{j(2\pi f_D(t)t + \phi(t))}|_{t=nT_s} + n(t)|_{t=nT_s} \quad (2)$$

where

- $A(t)$  is Amplitude
- $s_T(t)$  is Complex baseband signal
- $\tau(t)$  is code delay(time varying)
- $f_D(t)$  is Doppler shift(time varying)
- $\phi(t)$  is carrier phase shift(time varying)
- $n(t)$  is Random noise with zero mean
- $T_s$  is Sampling period
- $f_s$  is Sampling frequency

## Pseudo code for GPS Signal Acquisition

### 1.1 Functions for computing the PRN codes of GPS satellite

1. (a) g1\_lfsr()

```

state = 0x3FFF
Declare an array out[1023]
for i=0 to i=1022
    out[i] = (state >> 9) & 0x1
    new_bit = ((state >> 9) ⊕ (state >> 2)) & 0x1
    state = ((state << 1) | new_bit) & 0x3FFF
end for

```

return out

- (b) g2\_lfsr(tap0,tap1)

```

state = 0x3FFF
Declare an array out[1023]
tap0 = tap0-1
tap1 = tap1-1
for i=0 to i=1022
    out[i] = ((state >> tap0) ⊕ (state >> tap1)) & 0x1
    new_bit = ((state >> 9) ⊕ (state >> 8) ⊕ (state >> 7) ⊕ (state >> 5) ⊕ (state >> 2) ⊕ (state >> 1)) & 0x1
    state = ((state << 1) | new_bit) & 0x3FFF
end for

```

return out

- (c) combine\_g1\_g2(g1,g2)

```

declare out[1023]
for i=0 to i=1022
    out[i] = g1[i] ⊕ g2[i]
end for

```

return out

## 1.2 Main function

1. PRN Code frequency  $f_c$  is 1.023Mhz
2. Sampling frequency  $f_s$  is 2.048Mhz
3. The number of samples  $\mathbf{N}$  for 1ms is 2048  

```
/* Array to store Phase selector values for 32 satellites - 2 values per satellite*/
```
4. Static array  $\mathbf{SVs}[64] = [2, 6, 3, 7, 4, 8, 5, 9, 1, 9, 2, 10, 1, 8, 2, 9, 3, 10, 2, 3, 3, 4, 5, 6, 6, 7, 7, 8, 8, 9, 9, 10, 1, 4, 2, 5, 3, 6, 4, 7, 5, 8, 6, 9, 1, 3, 4, 6, 5, 7, 6, 8, 7, 9, 8, 10, 1, 6, 2, 7, 3, 8, 4, 9]$
5. Static array  $\mathbf{g1}[1023]$
6. static array  $\mathbf{g2}[32][1023]$
7.  $\mathbf{g1} = \mathbf{g1\_lfsr}()$  /\* Fuction call \*/
8.  $\mathbf{k}=0$
9.  $\mathbf{visible\_satellites} = 0$
10. **for**  $\mathbf{sv}=01$  to  $\mathbf{sv}=32$ :  

```
/* Generating PRN code */
    i tap0 = SVs[k++]
    ii tap1 = SVs[k++]
    iii g2[sv] = g2_lfsr(tap0,tap1) /* Fuction call */
    iv gold_code = combine_g1_g2(g1,g2) /* Fuction call */
    v For  $\mathbf{i} = 0$  to  $\mathbf{i} = 1022$ 
        if gold_code[i] > 0
            gold_code[i] = -1
        else
            gold_code[i] = 1
    /* Upsampling the PRN code */
    vi for  $\mathbf{i} = 0$  to  $\mathbf{i} = \mathbf{N}-1$ 
         $p_{sv}[\mathbf{i}] = \mathbf{gold\_code}[\mathbf{i}, \frac{f_c}{f_s}]$ 
    vii for  $\mathbf{i} = 0$  to  $\mathbf{i} = \mathbf{N}-1$ 
         $\mathbf{c}[\mathbf{sv}][\mathbf{i}] = p_{sv}[\mathbf{i}]$ 
end for
```
11. Calculate received signal power using the formula  

$$P_x = 0$$
**for**  $\mathbf{i}=0$  to  $\mathbf{N}-1$   

$$P_x = P_x + |x_{in}[\mathbf{i}]|^2$$
12. The power of incoming signal should be  $P_x > \vartheta$   

$$\vartheta = \frac{\sum_{i=1}^4 X_i}{4}$$
 $X_i$  represents Signal powers at gain = {0,27,47} and noise
13. Capture 2ms samples of incoming signal  $x_{in}[n]$
14.  $\mathbf{max\_values}[5] = \{0\}$
15.  $\mathbf{max\_row\_indices}[5] = \{0\}$
16.  $\mathbf{max\_indices}[5] = \{0\}$

17. **for** **sv**=01 to **sv**=32

```

    max = 0
    max_index = 0
    for n = 0 to n = N-1
         $z_{\mathbf{sv}}[n] = \sum_{m=0}^{N-1} c[\mathbf{sv}][m]x_{in}[n+m]$ 
         $z_{\mathbf{sv}}[\mathbf{n}] = \{\text{Re}(z_{\mathbf{sv}}[\mathbf{n}])\}^2$ 
        if  $z_{\mathbf{sv}}[\mathbf{n}] > \text{max}$ 
            max =  $z_{\mathbf{sv}}[\mathbf{n}]$ 
            max_index = n
        end for
    for i = 0 to i = 4
        if max > max_values[i]
            for j = 4 to j = i-1
                j = j-1
                max_values[j] = max_values[j-1]
                max_row_indices[j] = max_row_indices[j-1]
                max_indices[j] = max_indices[j-1]
            end for
            max_values[i] = max
            max_row_indices[i] = sv
            max_indices[i] = max_index
            break the loop
        end if
    end for
end for

```

18. **for** **sv** = 0 to **sv** = 4

```

    Code phase  $\hat{\tau}_{\mathbf{sv}} = \text{max\_indices}[\mathbf{sv}]$ 
    For i = 0 to i = N-1
         $x[\mathbf{i}] = x_{in}[\mathbf{i} + \hat{\tau}_{\mathbf{sv}}]$ 
    max_of_max=0
    for  $f_D = f_{min}$  to  $f_D = f_{max}$  in  $f_{step}$  steps:
        Shift the signal  $x[n]$  by  $f_D$ 

```

$$x_{sh}[n] = x[n] \cdot e^{-j2\pi f_D n T_s} \quad (3)$$

```

    Apply FFT to  $x_{sh}[n] \rightarrow X_{sh}[k]$ 
    for n = 0 to n = N-1
         $P_{\mathbf{sv}}^*[n] = c[\text{max\_row\_indices}[\mathbf{sv}]][\mathbf{n}]$ 
    Compute conjugate of FFT of  $p_{\mathbf{sv}}[n] = P_{\mathbf{sv}}^*[k]$ 
    Multiply  $X_{sh}[k]$  and  $P_{\mathbf{sv}}^*[k]$ .

```

$$Y[k] = X_{sh}[k] \cdot P_{\mathbf{sv}}^*[k] \quad (4)$$

```

    Compute IFFT for  $Y[k]$ 

```

$$R_{\mathbf{sv}}[n] = \text{IFFT}_k\{Y[k]\} \quad (5)$$

```

    max_value =  $R_{\mathbf{sv}}[0]$ 
    max_fd = 0
    For i = 0 to i = N-1
         $R_{\mathbf{sv}}[\mathbf{i}] = \{\text{Re}(R_{\mathbf{sv}}[\mathbf{i}])\}^2$ .
        if ( $R_{\mathbf{sv}}[\mathbf{i}] > \text{max\_value}$ ) &\& ( $R_{\mathbf{sv}}[\mathbf{i}] > \text{max\_of\_max}$ )
            max_value =  $R_{\mathbf{sv}}[\mathbf{i}]$ 
            max_fd = i
        end if
    max_of_max = max_value
    Doppler Frequency offset  $f_{sv_D} = \text{max\_fd}$ 

```