



🇮🇳 A.P. 🇮🇳 T.S. 🇮🇳 KARNATAKA 🇮🇳 TAMILNADU 🇮🇳 MAHARASTRA 🇮🇳 DELHI 🇮🇳 RANCHI

## A right Choice for the Real Aspirant

## ICON Central Office - Madhapur - Hyderabad

**Sec: Sr. Super 60\_ STERLING & NUCLEUS\_BT    Paper - 2 (Adv-2021-P2-Model)    Date: 06-08-2023**

Time: 02.00Pm to 05.00Pm

# RPTA-01

**Max. Marks: 180**

# KEY SHEET

# PHYSICS

1	AC	2	BD	3	AB	4	BD	5	ABCD	6	ACD
7	1.50	8	1.12	9	4	10	8	11	4.66 or 4.67	12	8.90 or 8.91
13	D	14	A	15	C	16	B	17	5	18	3
19	5										

# CHEMISTRY

20	ABD	21	B	22	BCD	23	ABD	24	C	25	CD
26	14	27	83	28	7	29	5	30	8	31	2020
32	C	33	A	34	C	35	C	36	6	37	5
38	2										

# MATHEMATICS

39	AB	40	AD	41	ABCD	42	ABC	43	BD	44	BCD
45	15	46	8	47	3	48	3	49	1.5	50	6
51	A	52	C	53	B	54	D	55	2	56	4
57	1										

## SOLUTIONS

### PHYSICS

1. Let the system be water at  $100^{\circ}\text{C}$

$$\text{Heat released by steam} = (4) \left( \frac{L}{1000} \right) (500) + 4L = 6L$$

$$\text{Heat required by ice} = (10) \left( \frac{L}{1000} \right) (200) + 10 \left( \frac{L}{6} \right) + 10 \left( \frac{L}{500} \right) (100) = 5.67L$$

Using 0.33 L of available heat 0.33g converts into steam.

2. Let  $\frac{\ell}{KA} = R$

$$\text{The resistances will be } R, R \text{ and } 3R \quad \frac{3T - T_0}{R} + \frac{2T - T_0}{R} + \frac{T - T_0}{3R} = 0$$

$$T_0 = \frac{16T}{7} \text{ which is greater than } T \text{ and } 2T.$$

Heat flows towards the junction in only one rod.

3. Volume of the liquid  $= (\pi R^2 h)(1 + \gamma\theta)$

$$\text{Area of the base} = \pi R^2 (1 + 2\alpha\theta)$$

$$\therefore \text{Height from the bottom} = \frac{\text{volume}}{\text{Area}} = h \left( \frac{1 + \gamma\theta}{1 + 2\alpha\theta} \right)$$

Depth from the top = height of the cylinder – height of the liquid

$$= H(1 + \alpha\theta) - h \left( \frac{1 + \gamma\theta}{1 + 2\alpha\theta} \right) = H(1 + \alpha\theta) - h(1 + (\gamma - 2\alpha)\theta)$$

4.  $\Delta Q = nC\Delta T$   $C$  can be positive or negative depending on the process.

When  $C$  is negative, temperature decreases.

5. Average KE per degree of freedom  $= \frac{1}{2} KT$

Energies greater than  $\frac{5}{2} KT$  and less than  $\frac{5}{2} KT$  are possible.

6.  $\frac{1}{2}(nM)v^2 = n \left( \frac{3}{2} R \right) \Delta T \quad \therefore \Delta T = \frac{Mv^2}{3R}$

$$Pv = nRT \quad \therefore \frac{\Delta P}{P} = \frac{\Delta T}{T}$$

7.  $V_M = \frac{V_0 + 2V_0}{2} = \frac{3V_0}{2} \quad \therefore \frac{V_M}{V_0} = 1.50$

8.  $2P_0V_0 = nRT_0$

Middle point will be at maximum temperature

$$\left( \frac{3P_0}{2} \right) \left( \frac{3V_0}{2} \right) = nRT_M \quad \therefore \frac{T_M}{T_0} = \frac{9}{8} = 1.12$$

9. The outer shell emits power  $P$  in both directions.

Sphere has to emit radiation of power  $P' = P + P = 2P$

10.  $P \propto T^4$  and  $P' \propto T'^4$

$$\therefore \frac{P'}{P} = \left(\frac{T'}{T}\right)^4 = 2 \text{ and } \left(\frac{T'}{T}\right)^{12} = 8$$

11.  $u_1 = \sqrt{\frac{2RT}{4 \times 10^{-3}}}$   $v_3 = \sqrt{\frac{3RT}{28 \times 10^{-3}}}$   $\therefore \left(\frac{u_1}{v_3}\right)^2 = 4.66 \text{ or } 4.67$

12.  $u_2 = \sqrt{\frac{8RT}{\pi 4 \times 10^{-3}}}$   $v_1 = \sqrt{\frac{2RT}{28 \times 10^{-3}}}$

$$\left(\frac{u_2}{v_1}\right)^2 = 8.90 \text{ or } 8.91$$

13.  $\frac{yA}{\ell}(\ell\alpha\theta + x) = \frac{2y2A}{2\ell}(2\ell2\alpha\theta - x)$   $\therefore x = \frac{7\ell\alpha\theta}{3}$

14.  $F = \frac{Ay}{\ell}(\ell\alpha\theta + x) = \frac{10Ay\alpha\theta}{3}$

15.  $x = \left(\frac{3}{2}R\right)T = \frac{3}{2}P_0V_0$

$$y = \frac{3}{2}[4P_0V_0 - P_0V_0] \quad \therefore \frac{y}{x} = 3$$

16. Heat is absorbed when the product  $PV$  increases.

When pressure increases at  $V_0$ ,  $Q_1 = \frac{3}{2}(2P_0V_0 - P_0V_0)$

When volume increases at  $2P_0$ ,  $Q_2 = \frac{5}{2}(4P_0V_0 - 2P_0V_0)$

$$\therefore \text{heat absorbed} = \frac{13P_0V_0}{2}$$

$$\Delta w = P_0V_0 \quad \therefore \text{Efficiency} = \frac{P_0V_0}{\left(\frac{13P_0V_0}{2}\right)} = \frac{2}{13}$$

17. Mean free path  $\propto \frac{T}{P}$   $y = 2.5x$   $\therefore \sqrt{\frac{10y}{x}} = 5$

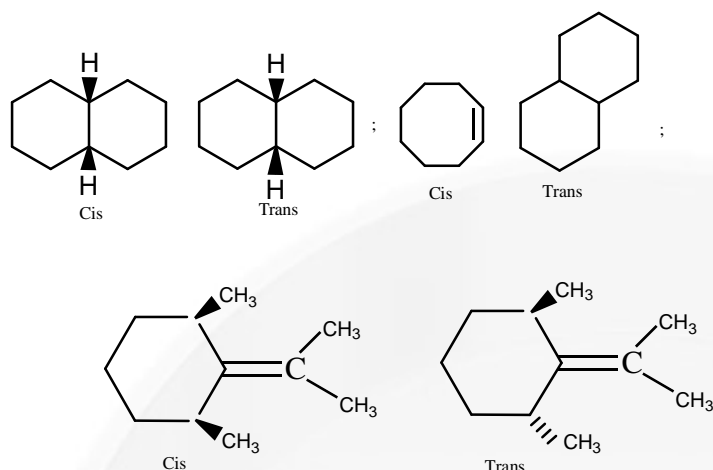
18.  $PV = nRT = \frac{3n}{4}R(T + \Delta T)$

$$\therefore \frac{T}{\Delta T} = 3$$

19.  $\Delta Q = \left[ (5)\left(\frac{3}{2}R\right) + (4)\left(\frac{5}{2}R\right) + 3\left(\frac{10}{2}R\right) \right] 2$   
 $= 65R \quad \therefore x = 5$

**CHEMISTRY**

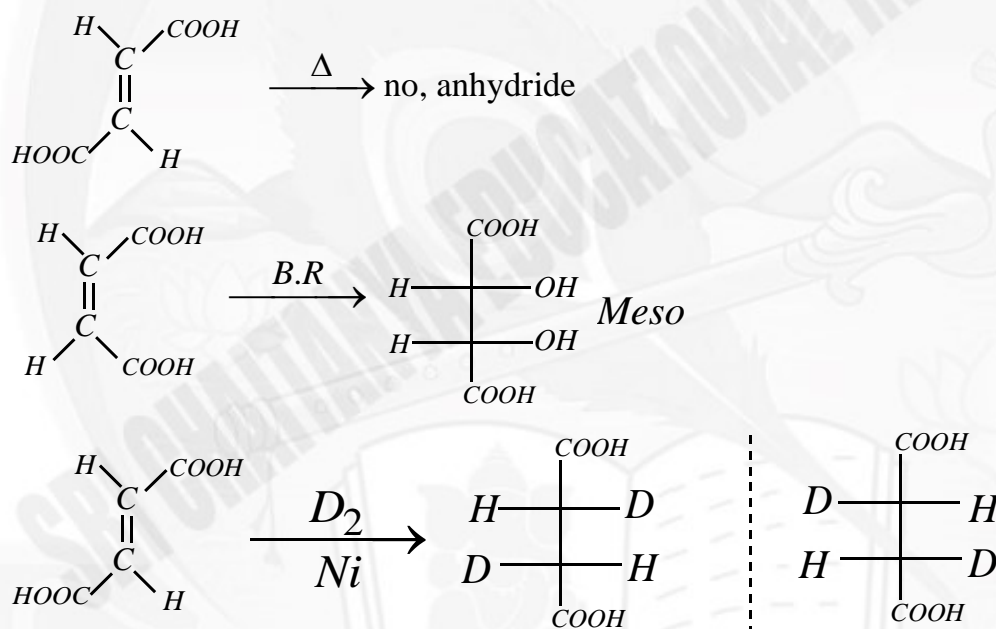
20.



21.

CONCEPTUAL

22.



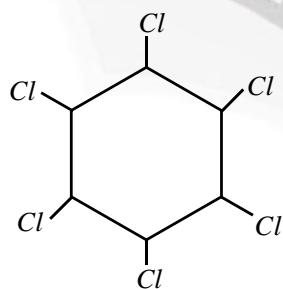
23.

*a, b, d* are without any symmetry element.

24.

Only salicylic acid is carboxylic acid.

25.



has 9 stereoisomers and  
only one enantiomeric pair  
and 7 meso compounds.

26 & 27. Enolizable  $H_3 = 14$ 

Chiral centres = 5

 $sp^2$  carbons = 25

28.

CONCEPTUAL

29. OPTICALLY ACTIVE = 2 ; MESO COMPOUNDS = 2

30. CONCEPTUAL

31. CONCEPTUAL

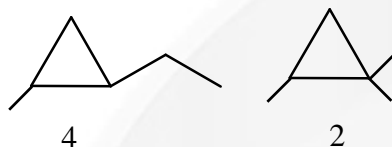
32&33. In "13"  $\longrightarrow$  "c" is without symmetry elements.

In "14"  $\longrightarrow$  "y" is without symmetry elements.

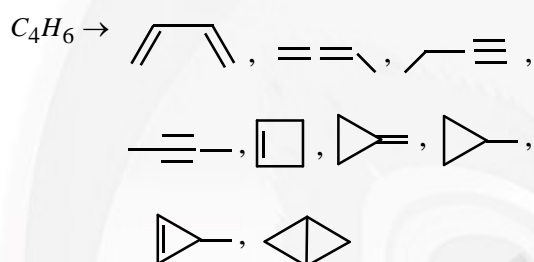
34. C is chiral

35. Only three double bonds can exhibit geometrical isomerism.

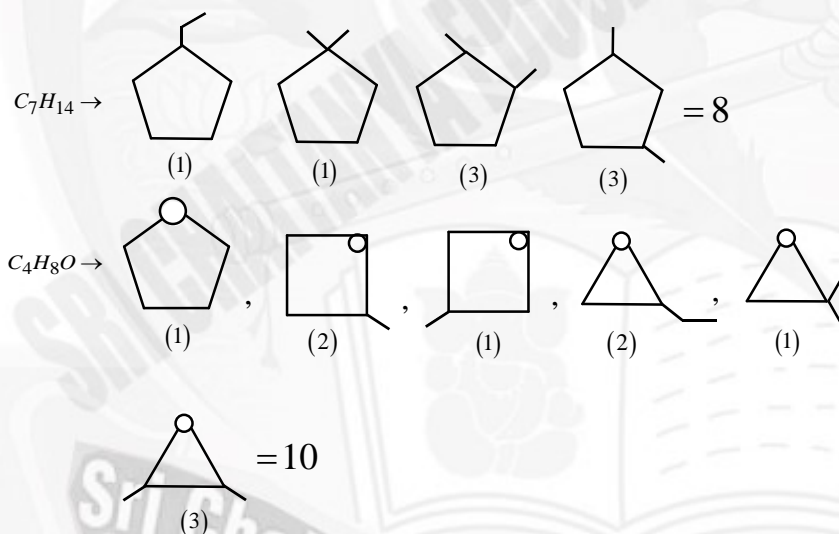
36.



37.

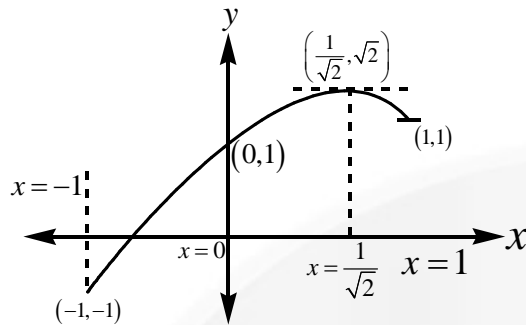


38.



**MATHEMATICS**

39.



Clearly domain of  $f$  is  $[-1, 1]$ . Verify all alternatives from graph.

40.  $f(x)$  is defined only when

$$3 - e^{2x} \geq 0 \Rightarrow 3 \geq e^{2x} \Rightarrow e^{2x} \leq 3 \Rightarrow 2x \leq \log_e 3$$

$$\frac{1}{f(x)} \text{ is defined only when } 3 - e^{2x} > 0 \Rightarrow 3 > e^{2x} \Rightarrow e^{2x} < 3 \Rightarrow 2x < \log_e 3$$

41. Put  $x = 0 = y \Rightarrow f(0) = 0$ 

$$f^1(0) = \lim_{h \rightarrow 0} \frac{f(h) - f(0)}{h} = (f^1(0))^3$$

$$\Rightarrow f^1(0) = 0 \text{ or } 1 (\because f^1(0) \geq 0)$$

$$\Rightarrow f(x) = k(a)x + k$$

$$\Rightarrow f(x) = 0 \text{ or } (\because f(0) = 0)$$

$$42. f(x) = \begin{cases} -x-3 & x < 0 \\ x-3 & 0 \leq x < 1 \\ -x > 2 > a & 1 \leq x < 2 \end{cases} \quad g(x) = \begin{cases} 2 > x & x < 0 \\ 2-x & 0 \leq x < 2 \\ 1-2 & 2 \geq 2 \end{cases}$$

$$h(x) = \begin{cases} -1 & x < 0 \\ -1 & 0 \leq x < 1 \\ 0-h > 3-x & 1 \leq x < 2 \\ a-L-1 > x & x \geq 2 \end{cases}$$

$$a-L > 2 = -1 \Rightarrow a-L = -3$$

$$43. R.H.L \ f(0^+) = \lim_{x \rightarrow 0^+} 3 - \left[ \cot^{-1} \left( \frac{2x^3 - 3}{x^2} \right) \right]$$

$$= 3 - \lim_{x \rightarrow 0^+} \left[ \cot^{-1} \left( \frac{2x^3 - 3}{x^2} \right) \right]$$

$$= 3 - 3 = 0$$



$$L.H.L \, f(0^-) = \lim_{x \rightarrow 0^-} \left\{ x^2 \right\} \cos \left( \frac{1}{e^x} \right) = 0$$

$$44. \quad f(x) = \left[ \tan^2 x \right]$$

$$\text{AT } x=0 \text{ as } x \rightarrow 0^- \tan x < 0 \Rightarrow \tan^2 x > 0$$

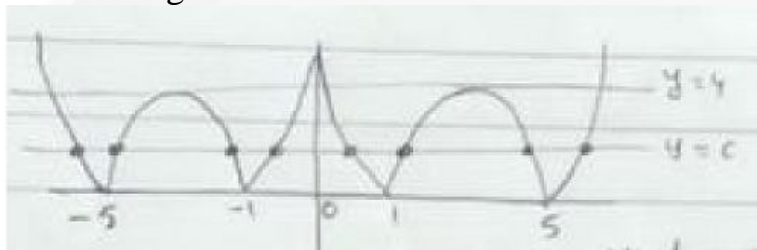
$$x \rightarrow 0^+ \tan x > 0 \Rightarrow \tan^2 x > 0$$

$$f(0^-) = f(0^+)$$

$$f(x) \text{ at constant at } x=0$$

$$45 \text{ \& } 46. \text{ For domain of } g(x), f(x) > 0 \Rightarrow x \notin [1, 5]$$

$$\text{Sum of integers} = 1 + 2 + 3 + 4 + 5 = 15$$



$$47. \quad f(x) = \begin{cases} -2 & -2 \leq x < -1 \\ -1 & -1 \leq x \leq -\frac{1}{2} \\ 2x^2 - 1 & -\frac{1}{2} < x \leq 2 \end{cases}$$

$$f(|x|) = \begin{cases} 2x^2 - 1 & -2 \leq x \leq 2 \end{cases}$$

$$|f(x)| = \begin{cases} 2 & -2 \leq x \leq -1 \\ 1 & -1 \leq x \leq -\frac{1}{2} \\ -(2x^2 - 1) & -\frac{1}{2} < x \leq \frac{1}{\sqrt{2}} \\ 2x^2 - 1 & -\frac{1}{\sqrt{2}} < x \leq 2 \end{cases}$$

$$g(x) = \begin{cases} 2x^2 - 1 & -2 \leq x < -1 \\ 2x^2 - 1 & -1 \leq x \leq -\frac{1}{2} \\ 0 & -\frac{1}{2} < x < \frac{1}{\sqrt{2}} \\ ax^2 - 2 & \frac{1}{\sqrt{2}} \leq x \leq 2 \end{cases}$$

$|f(x)|$  is non differentiable at 3 points.

$g(x)$  is non differentiable at 3 points.

48. CONCEPTUAL

49 & 50

$$\text{Let } x^2 = 4\cos^2 \theta + \sin^2 \theta$$

$$\text{Then } f(x) = \sqrt{3}|\sin \theta| + \sqrt{3}|\cos \theta|$$

$$\min = \sqrt{3}(1) = \sqrt{3}$$

$$\max = \sqrt{3}\sqrt{2} = \sqrt{6}$$

50. CONCEPTUAL

$$51. \quad f(x) = \begin{cases} \frac{\pi}{2} & x \neq 0 \\ 0 & x = 0 \end{cases}$$

$$g(x) = \begin{cases} 1 & \sin^2 x = 1 \Rightarrow x = \pm \frac{\pi}{2} \\ 0 & \sin^2 x < 1 \end{cases}$$

Range  $g|x=1$  is  $\{0,1\}$

$$h(x) = \sin^{-1} \left\{ \frac{1}{2} \left( \cos \pi \left( g(x) + \cos 2 \left( f(x) \right) \right) \right) \right\}$$

Is discontinuous.

52. CONCEPTUAL

$$53. \quad \text{Since } f\left(x + \frac{7}{4}\right) = f\left(\frac{7}{4} - x\right) \forall x \in \mathbb{R}$$

So,  $f(x)$  is symmetric about  $x = \frac{7}{4}$

$$\text{Hence } \frac{-b}{2a} = \frac{7}{4} \Rightarrow \frac{-b}{a} = \frac{7}{2}$$

Also  $f(x) = 7x + a$  has only one real solution, so

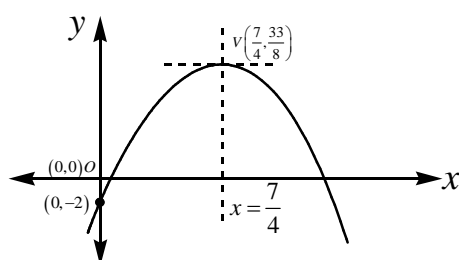
$$ax^2 + bx + a = 7x + a \Rightarrow ax^2 + x(b-7) = 0 \text{ has discriminant zero.}$$

$$\Rightarrow (b-7)^2 - 4(a)(0) = 0 \Rightarrow b = 7$$

Putting  $b = 7$  in equation (1), we get  $a = -2$

$$\text{So, } f(x) = -2x^2 + 7x - 2 \text{ Hence, } (a+b) = (-2+7) = 5$$

54. Clearly from the graph of  $f(x) = -2x^2 + 7x - 2$ ,





Minimum value of  $f(x)$  in  $\left[0, \frac{3}{2}\right]$  is  $F_{\min}(x=0) = -2$

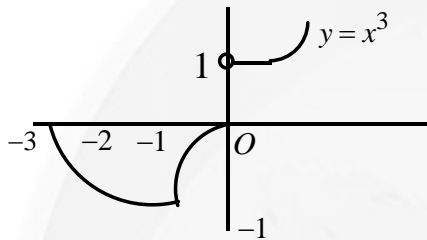
55.  $2[x] = [x] + 2\{x\}$

$$\{x\} = \frac{[x]}{2} \rightarrow 0 < \frac{[x]}{2} < 2 \Rightarrow [x] = 0, 1$$

For  $[x] = 0 \rightarrow x = 0$

$$[x] = 1 \rightarrow x = 1 + \frac{1}{2} = \frac{3}{2}$$

56.



All is not differentiable at 5 points.

57.

