

**Q1.** Consider the equation  $x^2 - 2x - n = 0$ , where  $n \in \mathbb{N}$  and  $n \in [5, 100]$ . The total number of different values of  $n$  so that the given equation has integral roots is

**Q2.** If  $\pi < 0 < \pi$ , the equation  $(\cos 3\theta + 1)x^2 + (2\cos 2\theta - 1)x + (1 - 2\cos \theta) = 0$  has more than 2 roots for

- (a) No value of  $\theta$
- (b) One value of  $\theta$
- (c) Two values of  $\theta$
- (d) Infinite values of  $\theta$

**Q3.** If  $\alpha, \beta$  are the roots of the equation  $2x^2 + 4x - 5 = 0$ , the equation whose roots are  $\frac{1}{2\alpha - 3}$  and  $\frac{1}{2\beta - 3}$  is

- (a)  $x^2 + 10x - 11 = 0$
- (b)  $11x^2 + 10x + 1 = 0$
- (c)  $x^2 + 10x + 11 = 0$
- (d)  $11x^2 - 10x + 1 = 0$

**Q4.** The number of natural number  $n$  for which the equation  $(x - 8)x = x(n - 10)$  has no real solution is equal to

- (a) 2
- (b) 3
- (c) 4
- (d) 5

**Q5.** The value of  $a$  for which the sum of cubes of the roots of equation  $x^2 - ax + (2a - 3) = 0 \forall a \in \left[\frac{1}{2}, 4\right]$  attains its minimum value

- (a) greater than 4
- (b) less than 2

(c) Greater than  $\frac{3}{2}$

(d) less than  $\frac{1}{2}$

**Q6.** If  $\frac{\alpha+5i}{2}$  is a root of the equation  $2x^2 - 6x + k = 0$  then the value of  $\frac{k}{10}$  is ( $\alpha, k \in R$ )

**Q7.** If  $\alpha$  and  $\beta$  are the roots of the quadratic equation,  $x^2 + x \sin \theta - 2 \sin \theta = 0, \theta \in \left(0, \frac{\pi}{2}\right)$ , then  $\frac{\alpha^{12} + \beta^{12}}{(\alpha^{-12} + \beta^{-12})(\alpha - \beta)^{24}}$  is equal to:

(a)  $\frac{2^{12}}{(\sin \theta - 8)^6}$

(b)  $\frac{2^6}{(\sin \theta + 8)^{12}}$

(c)  $\frac{2^{12}}{(\sin \theta + 8)^{12}}$

(d)  $\frac{2^{12}}{(\sin \theta - 4)^{12}}$

**Q8.** If for a positive integer  $n$ , the quadratic equation  $x(x+1) + (x+1)(x+2) + \dots + (x+(n-1))(x+n) = 10n$  has 2 consecutive integral solutions then  $n$  is equal to

(a) 12

(b) 9

(c) 10

(d) 11

**Q9.** If  $\alpha$  and  $\beta$  are roots of the equation,  $x^2 - 4\sqrt{2}kx + 2e^{4 \ln k} - 1 = 0$  for some  $k$ , and  $\alpha^2 + \beta^2 = 66$ , then  $\alpha^3 + \beta^3$  is equal to

(a)  $248\sqrt{2}$

(b)  $280\sqrt{2}$

(c)  $-32\sqrt{2}$

(d)  $-280\sqrt{2}$

