

P5. $r(A, B, C, D)$ is a relation with f.d: $(A \rightarrow B, B \rightarrow C)$.
Find lossless join dependency preserving BCNF.

The given relation is $r(A, B, C, D)$ and the

Functional Dependency (FD) is $A \rightarrow B, B \rightarrow C$.
To find out the lossless join & dependency preserving BCNF for the given relation, the following 3 steps can be followed.

Step 1: Check candidate key: Candidate keys are minimal Superkeys. To find them, we need to check if removing any attribute from the superkey makes it lose the ability to uniquely identify tuples.

① $\Rightarrow \{A\}$ is a candidate key because removing any attribute from it will make it to lose its uniqueness property.

② $\Rightarrow \{B\}$ is also a candidate key due to same reason mentioned above.

Step 2: Check for BCNF violation: To ensure the relation is in BCNF we need to check if it satisfies the BCNF condition. A relation is in BCNF if for every non-trivial functional dependency $X \rightarrow Y$, X is a superkey. In our case, both FD are non-trivial.

Step 3: Lossless Join: To ensure that the decomposition is lossless, we need to check if the intersection of the attributes of the new relation $R_1(A, B)$ with FD $A \rightarrow B$ & $R_2(B, C, D)$ with FD $B \rightarrow C$, it contains the superkey of either of the relation. In our case, it contains the attribute B , which is superkey, so this decomposition is lossless.

Dependency Preservation: If each FD from the original relation can be derived from the FD of the new relation, then the decomposition preserves the dependency.

So, we can conclude that the decomposition is a lossless join, in BCNF and dependency preserving BCNF decomposition.

Q.6. $R(A, B, C, D)$ is a relation with FD $(A \rightarrow BC)$. Find ² lossy join, dependency preserving BCNF.

Ans As from FD $(A \rightarrow BC)$, A can determine both B & C attributes. So, we can say A is candidate key.

A relation is BCNF, if for every non-trivial dependency $X \rightarrow Y$, X is a super key. for the given FD $A \rightarrow BC$ it is non-trivial. Here A, is candidate as well as super key. So, there is no violation of BCNF.

Q7. Student (name, c.no, roll, grade),

FD : name \rightarrow CNo \rightarrow grade

name \rightarrow roll

roll \rightarrow name.

Candidate key = $\{ \text{name, CNo}, \text{CNo, roll} \}$

Prime attribute = Name, CNo, roll

Non-Prime attribute = grade.

Is it BCNF : $X \rightarrow Y$, where X is candidate key
name, CNo \rightarrow grade \rightarrow already BCNF
roll, CNo \rightarrow grade \rightarrow already BCNF
name \rightarrow roll \rightarrow Not BCNF
roll \rightarrow name \rightarrow Not BCNF

check for 3NF:

name \rightarrow roll

roll \rightarrow name

Both name, roll are the Prime attribute

So, relation is in 3NF, which is the highest form.

P8. $r(A, B, C, D)$ is a relation with FD $(AB \rightarrow C, C \rightarrow AD)$
Find lossy join, dependency preserving BCNF.

From $AB \rightarrow C$ here AB is the super key

$C \rightarrow AD$ here C is the super key

So, AB & C both are super key, they are the candidate key also.

$AB^+ = ABCD$ (it can determine all attributes)

$C^+ = ADC$ (it can not determine B so can not be a candidate key).

check for BCNF:

$X \rightarrow Y$ where X is a candidate key

$AB \rightarrow C$ AB is a candidate key

$C \rightarrow AD$ C is not a candidate key so it does not meet BCNF requirement.

To make it BCNF we need to perform decomposition.

- So,
1. Create a new relational dependency $r_1(C, AD)$
 2. Remove the functional dependency FD $(C \rightarrow AD)$ from the original relation.

3. Now, the new relation will be

$r_2(A, B, C) \rightarrow$ New original relation

$r_1(C, AD)$ - New decomposed relation