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Colab Link: [Vectors_and_Perceptron.ipynb](#)

1. What is the magnitude of $\vec{w} = [0.5, 0.5]$?

```
[6] def magnitude(vector):  
    return math.sqrt(sum(pow(element, 2) for element in vector))  
  
w = np.array([0.5, 0.5])  
magnitude(w)  
  
0.7071067811865476
```

0.707

2. Multiple the following two vectors ($\vec{x} * \vec{w}^T$), where $\vec{x} = [0.5, 0.5]$ and $\vec{w} = [0.75, 1.25]$

```
[28] x*w.transpose()  
  
array([0.375, 0.625])
```

[0.375, 0.625]

3. Multiple the following two vectors ($\vec{x}^T * \vec{w}$) using the vectors from the previous problem.

```
✓  
0s [9] x.transpose()*w  
  
array([0.375, 0.625])
```

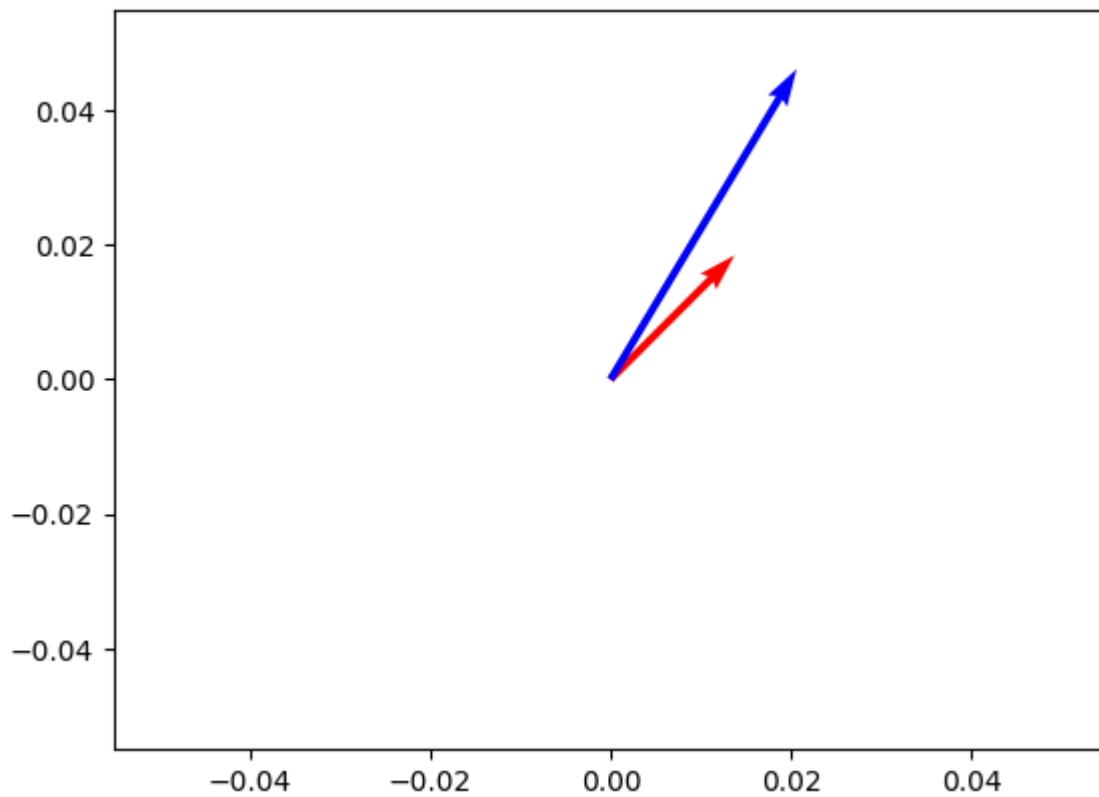
[0.375, 0.625]

4. What is the dot product of \mathcal{X} and \mathcal{W} using the values from the previous problem?

```
✓ 0s [▶] np.dot(x,w)  
[→] 1.0
```

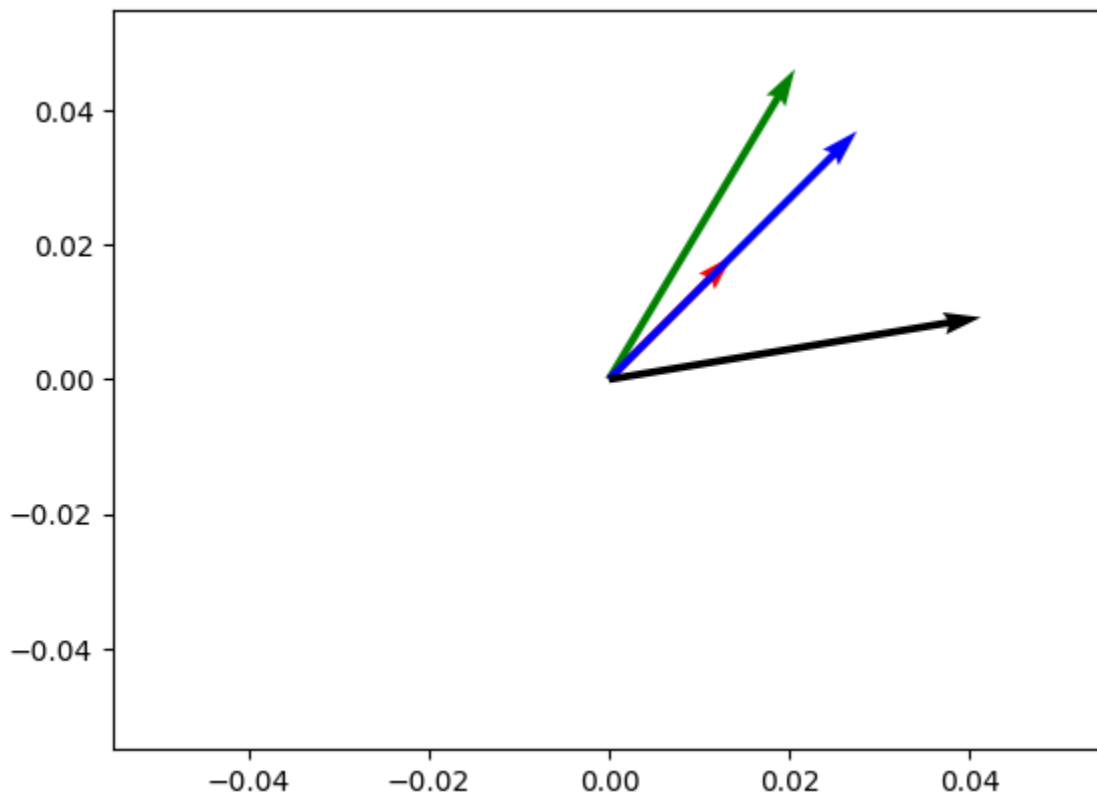
1.0

5. What is the angle between \mathcal{X} and \mathcal{W} using the values from the previous problem? Draw the vectors and label the angle that you found.



Red is \mathcal{X} and Blue is \mathcal{W} . The angle between them is 14 degree

6. Add the following vectors, and draw the resultant and the original vectors.
 $\vec{x} = [0.5, 0.5]$ and $\vec{w} = [0.75, -1]$



Red and **Green** vectors are the original vectors.
Blue and **Black** vectors are the resultant vectors.

7. What is the difference between prediction and classification?

Prediction is the process of estimating a value based on previous data.
While classification is the process of assigning a label to an input based on its features

8. Using the perceptron learning algorithm and a single neuron, find the weights that correctly predict the "OR" function. Continue updating the weights using the algorithm discussed in class until you converge on a correct solution. Show all of your work. The initial weights are $w_0 = 0$, $w_1 = 0.5$, $w_2 = -0.5$ and the learning parameter $v = 0.25$. You may also assume that $x_0 = 1$.

x_1	x_2	OR
0	0	0
0	1	1
1	0	1
1	1	1

$$1^{st} \quad \bar{y} = f(0 \times 1 + 0.5 \times 0 + -0.5 \times 0) = f(0) = 0 = y$$

$$2^{nd} \quad \bar{y} = f(0 \times 1 + 0.5 \times 0 + -0.5 \times 1) = f(-0.5) = 0 \neq y$$

$$w_0 = w_0 + v(0 - 1) = -0.25$$

$$w_1 = w_1 + v(0 - 1) = 0.5$$

$$w_2 = w_2 + v(0 - 1) = -0.75$$

$$3^{rd} \quad \bar{y} = f(0 \times 1 + 0.5 \times 1 + -0.5 \times 0) = f(0.5) = 1 = y$$

$$w_0 = w_0, w_1 = w_1, w_2 = w_2$$

$$4^{th} \quad \bar{y} = f(0 \times 1 + 0.5 \times 1 + -0.5 \times 1) = f(0) = 0 \neq y$$

$$w_0 = w_0 + v(0 - 1) = -0.5$$

$$w_1 = w_1 + v(0 - 1) = 0.25$$

$$w_2 = w_2 + v(0 - 1) = -1$$

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