

1. What is the magnitude of $\vec{w} = [0.5, 0.5]$?

$$|\vec{w}| = \sqrt{0.5^2 + 0.5^2} = \boxed{0.707}$$

2. Multiple the following two vectors ($\vec{x} * \vec{w}^T$), where $\vec{x} = [0.5, 0.5]$ and $\vec{w} = [0.75, 1.25]$

$$\begin{aligned} [0.5, 0.5] \times \begin{bmatrix} 0.75 \\ 1.25 \end{bmatrix} &= [0.5 \cdot 0.75 + 0.5 \cdot 1.25] \\ &= \boxed{[1]} \end{aligned}$$

3. Multiple the following two vectors ($\vec{x}^T * \vec{w}$) using the vectors from the previous problem.

$$\begin{bmatrix} 0.5 \\ 0.5 \end{bmatrix} \times [0.75, 1.25] = \begin{bmatrix} 0.375 & 0.625 \\ 0.375 & 0.625 \end{bmatrix}$$

4. What is the dot product of \vec{x} and \vec{w} using the values from the previous problem?

$$\vec{x} \cdot \vec{w} = 0.5 \cdot 0.75 + 0.5 \cdot 1.25$$

$$= \boxed{1}$$

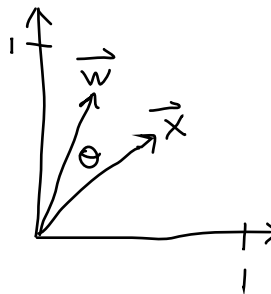
5. What is the angle between \vec{x} and \vec{w} using the values from the previous problem? Draw the vectors and label the angle that you found.

$$|\vec{x}| |\vec{w}| \cos \theta = \vec{x} \cdot \vec{w}$$

$$\cos \theta = \frac{1}{|\vec{x}| |\vec{w}|}$$

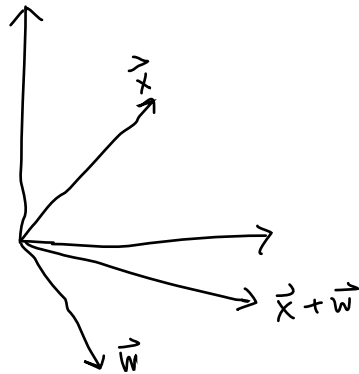
$$\cos \theta = \frac{1}{1.03}$$

$$\boxed{\theta = 14.036^\circ}$$



6. Add the following vectors, and draw the resultant and the original vectors.
 $\vec{x} = [0.5, 0.5]$ and $\vec{w} = [0.75, -1]$

$$\vec{x} + \vec{w} = [0.5 + 0.75, 0.5 - 1] = [1.25, -0.5]$$



7. What is the difference between prediction and classification?

Prediction refers to predicting missing values for a dataset.

Classification is a type of prediction, where categorical variables are predicted to split the data into groups.

8. Using the perceptron learning algorithm and a single neuron, find the weights that correctly predict the "OR" function. Continue updating the weights using the algorithm discussed in class until you converge on a correct solution. Show all of your work. The initial weights are $w_0 = 0, w_1 = 0.5, w_2 = -0.5$ and the learning parameter $\nu = 0.25$. You may also assume that $x_0 = 1$.

x_1	x_2	OR
0	0	0
0	1	1
1	0	1
1	1	1

First iteration:

Input: [0,0], y: 0, t: 0

No update since $y = t$

Input: [1,0], y: 1, t: 1

No update since $y = t$

Input: [0,1], y: 0, t: 1

$$w_0 = 0 - 0.25(0 - 1) \cdot 1 = 0.25$$

$$w_1 = 0.5 - 0.25(0 - 1) \cdot 0 = 0.5$$

$$w_2 = -0.5 - 0.25(0 - 1) \cdot 1 = -0.25$$

Input: [1,1], y: 0, t: 1

$$w_0 = 0.25 - 0.25(0 - 1) \cdot 1 = 0.5$$

$$w_1 = 0.5 - 0.25(0 - 1) \cdot 1 = 0.75$$

$$w_2 = -0.25 - 0.25(0 - 1) \cdot 1 = 0$$

Second iteration:

Input: [0,0], y: 0, t: 0

No update since $y = t$

Input: [1,0], y: 1, t: 1

No update since $y = t$

Input: [0,1], y: 1, t: 1

No update since $y = t$

Input: [1,1], y: 1, t: 1

No update since $y = t$

$$w_0=0.5, w_1 = 0.75, w_2 = 0$$