

# CS492: Probabilistic Programming

# Basics of Clojure and

# tiny bit of Anglican

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KAIST

Does anyone use Clojure, Scheme, or Lisp?

Does anyone use Clojure, Scheme, or Lisp?

What are the cons and pros of such a lang.?

# Clojure

- Re-design of Scheme for Java virtual machine, with concurrency in mind.
- Untyped.
- Highly expressive.
- Cousin language for Anglican, the probabilistic programming language used in this course.

# Learning outcome

- Can write simple Clojure programs with recursion, loop, list, and map.
- Can write simple Anglican programs with no conditioning, and perform inference.
- All by copy-paste-modify programming.

# Clojure in a nutshell

1. Prefix instead of infix notation:

`(+ 3 3)`, not `3+3`

2. Use `let` to bind variables to values.

`(let [x (* 3 3) y (* 4 4)] (+ x y))`

3. Anonymous function using `fn`:

`(let [f (fn [x] (* x x))] (+ (f 3) (f 4)))`

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**[Q] Write a program that computes  $1^2 + 2^2 + \dots + 5^2$ .**

# Clojure in a nutshell

1. Prefix instead of infix notation:

```
(let [f (fn [x] (* x x))]
```

```
  (+ (f 1)
```

```
    (f 2)
```

```
    (f 3)
```

```
    (f 4)
```

```
  (let [g (fn [x y] (+ x y))]
    (g (f 5) (f 6)))
```

3. Anonymous function using fn:

```
(let [f (fn [x] (* x x))] (+ (f 3) (f 4)))
```

[Q] Write a program that computes  $1^2 + 2^2 + \dots + 5^2$ .



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(let [f (fn [x] (* x x))]
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```
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```
     (f 4)
```

```
  (let [f (fn [x] (* x x))]
```

```
    (f 5)))
```

2. Use

s.

(+ x y))

3. Anonymous function using fn:

```
(let [f (fn [x] (* x x))] (+ (f 3) (f 4)))
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[Q] Write a program that computes  $1^2 + 2^2 + \dots + 5^2$ .

# Clojure in a nutshell

## 4. Separate function definition:

```
(defn f [n] ...)
```

E.g.

```
(defn f [n]
  (if (= n 0)
      0
      (+ n (f (- n 1)))))

(println (f 10))
```

[Q] Write a program that computes  $1^2 + 2^2 + \dots + 5^2$ .

# Closure in a nutshell

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Recursion  
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[Q] Write a program that computes  $1^2 + 2^2 + \dots + 5^2$ .

# Chaining in a nutshell

```
Lecture2 — vi sum.clj — 55x14
× ...me/Work/Teaching/2017-18/ProbProg18/Lectures/Lecture2 — vi sum.clj
...k/Teaching/2017-18/ProbProg18/Lectures/Lecture2 — java • lein repl +

(ns lecture2)

(defn sq [x] (* x x))

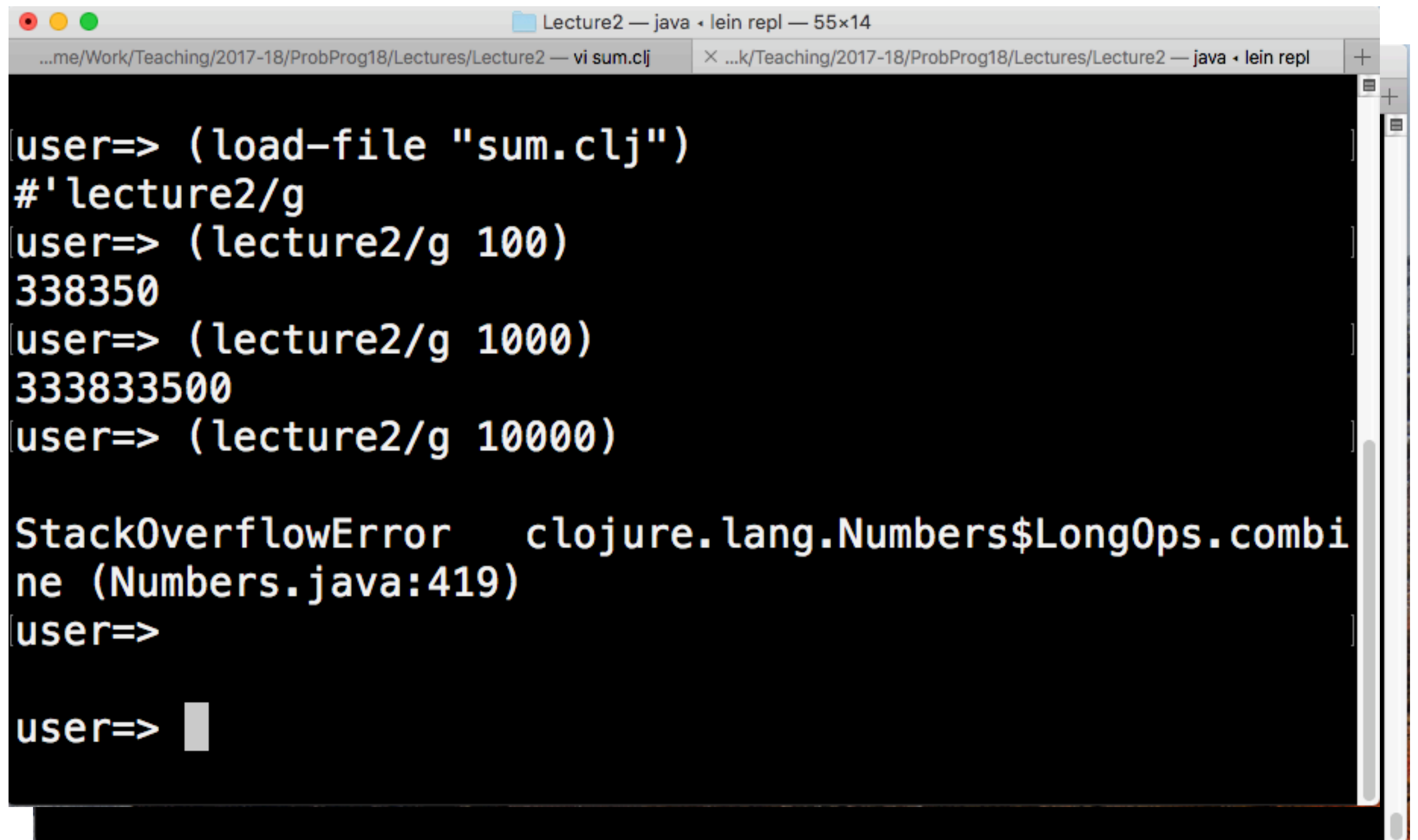
(defn g [n]
  (if (= n 0)
      0
      (+ (sq n) (g (- n 1)))))

~
~
~

sum.clj 1,1 All
"sum.clj" 9L, 101C written
```

[Q] Write a program that computes  $1^2 + 2^2 + \dots + 5^2$ .

NB: I installed leiningen. Then, I ran “lein repl”. You can install Clojure and run “clj” instead.

A screenshot of a Clojure REPL window. The window has a title bar with a folder icon and the text "Lecture2 — java • lein repl — 55x14". Below the title bar are two tabs: "...me/Work/Teaching/2017-18/ProbProg18/Lectures/Lecture2 — vi sum.clj" and "× ...k/Teaching/2017-18/ProbProg18/Lectures/Lecture2 — java • lein repl". The main area of the window is a black terminal with yellow text. The text shows a sequence of commands and their outputs: [user=> (load-file "sum.clj")] returns #'lecture2/g; [user=> (lecture2/g 100)] returns 338350; [user=> (lecture2/g 1000)] returns 333833500; [user=> (lecture2/g 10000)] results in a StackOverflowError: clojure.lang.Numbers\$LongOps.combine (Numbers.java:419). The prompt [user=>] is shown again at the bottom.

```
[user=> (load-file "sum.clj")]
#'lecture2/g
[user=> (lecture2/g 100)]
338350
[user=> (lecture2/g 1000)]
333833500
[user=> (lecture2/g 10000)]

StackOverflowError    clojure.lang.Numbers$LongOps.combine
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[user=>

user=> █
```

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StackOverflowError   clojure.lang.Numbers$LongOps.combine (Numbers.java:419)
[user=>]
[user=> ]
```

No StackOverflow.

[Q] Write a program that computes  $1^2 + 2^2 + \dots + 52^2$ .

# Clojure in a nutshell

## 5. Tail recursion.

[Q] Write a program that computes  $1^2 + 2^2 + \dots + n^2$ .



# Closure in

No further work  
after recursive call.

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```
(defn f [n]
  (if (= n 0)
      0
      (+ n
         (f (- n 1)))))
```

Not tail recursive

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(defn g [n r]
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[Q] Write a program that computes  $1^2 + 2^2 + \dots + 5^2$ .

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5. Tail recursion. 1) Use accumulator.

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```
(defn f [N] (g N 0))
```

Tail recursive. **Acc. r**  $n^2$

[Q] Write a program that computes  $1^2 + 2^2 + \dots + 5^2$ .

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No further work  
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5. Tail recursion. 1) Use accumulator. 2) Inform the compiler using loop and recur.

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Tail recursive. Acc. r

[Q] Write a program that computes  $1^2 + 2^2 + \dots + 5^2$ .

# Chaining in a nutshell

```
Lecture2 — vi sum_loop.clj — 55x14
...Work/Teaching/2017-18/ProbProg18/Lectures/Lecture2 — java • lein repl  X .../Teaching/2017-18/ProbProg18/Lectures/Lecture2 — vi sum_loop.clj +
(ns lecture2b)

(defn sq [x] (* x x))

(defn g [n]
  (loop [i n r 0]
    (if (= i 0)
        r
        (recur (- i 1) (+ (sq i) r)))))

~
sum_loop.clj [+] 11,0-1 All
```

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333383335000
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333338333350000
[user=> (lecture2b/g 1000000)]
333333833333500000
[user=> ]
```

[Q] Write a program that computes  $1^2 + 2^2 + \dots + 5^2$ .

# Exercise 1:

## Fibonacci sequence

[Q] Write a Clojure function that takes  $n \geq 2$  and computes the  $n$ -th Fibonacci number  $F_n$ :

$$F_1 = 1, \quad F_2 = 1, \quad F_{n+2} = F_n + F_{n+1}$$

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[Hint]

```
(defn fib [n]
  (loop [i . . . . .]
    (if (= i n)
      .
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```



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(defn fib [n]
  (loop [i 2 r0 1 r1 1]
    (if (= i n)
      r1
      (recur (+ i 1)
              r1
              (+ r0 r1)))))
```

# Exercise 2: Random Fibonacci sequence $R_n$

$$R_1 = 1, \quad R_2 = 1,$$

$$R_{n+2} = R_n + R_{n+1} \text{ or } R_{n+1} - R_n, \text{ each with prob. } 1/2$$

[Q] What does the distribution of  $R_n$  look like?

# Anglican in a nutshell

- I. Define an Anglican query using defquery.

```
(defquery baby-rfib [n]
  (let [b (sample (flip 0.5))
        new-n (if b n (+ n 1))]
    (loop [i 2 r0 1 r1 1]
      (if (= i new-n)
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query name

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```

query name

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query body

# Anglican in a nutshell

Creating and sampling  
from distribution object

ery using defquery.

query name

arguments

query body

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(defquery baby-rfib [n]
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query name

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[Q] Write an Anglican query for generating  $R_n$  for given  $n$ .

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(defquery rfib [n]
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        ...
        ...
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```

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(defquery rfib [n]
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    (if (= i n)
      r1
      (let [b (sample (flip 0.5))
            r2 (if b (+ r1 r0) (- r1 r0))]
        (recur (+ i 1)
               r1
               r2))))))
```

[Q] Write an Anglican query for generating  $R_n$  for given  $n$ .

# Anglican in a nutshell

2. Perform inference using doquery.

```
(doquery :importance rfib [20])
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Clojure keyword.

Chooses an inference algorithm.

# Anglican in a nutshell

2. Perform inference using doquery.

(doquery :importance **rfib** **[20]**)



Clojure keyword.

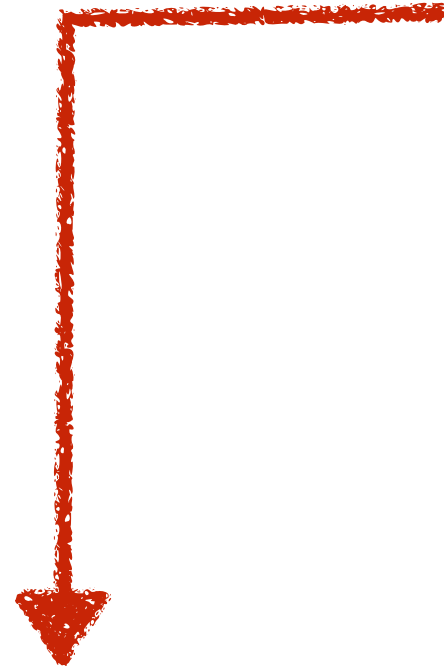
Chooses an inference algorithm.

**query name,**  
**arguments**



# Anglican in a nutshell

2. Perform inference using doquery. query name,  
arguments

 (doquery :importance rfib [20])

 Clojure keyword.  
Chooses an inference algorithm.

Returns a lazy infinite list  
of samples.  
Only a finite prefix used.

# Anglican in a nutshell

2. Perform inference using doquery.

```
(let [s (doquery :importance rfib [20])]  
  (take 2 s))
```

# Anglican in a nutshell

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(let [s (doquery :importance rfib [20])]  
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```
( { :log-weight 0.0,  
    :result 1,  
    :predict []}  
  
  { :log-weight 0.0,  
    :result -17,  
    :predict []} )
```

# Anglican in a nutshell

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List

# Anglican in a nutshell

## 2. Perform inference using doquery.

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List  
of maps



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    :predict []}  
  
  { :log-weight 0.0,  
    :result -17,  
    :predict []} )
```

List  
of maps  
with three keys

# Anglican in a nutshell

## 2. Perform inference using doquery.

```
(let [s (doquery :importance rfib [20])]  
  (take 2 s))
```

```
( { :log-weight 0.0,  
    :result 1,  
    :predict []}  
  
  { :log-weight 0.0,  
    :result -17,  
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```

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- To move on, we need to understand map and list datatypes of Clojure.

- To move on, we need to understand map and list datatypes of Clojure.
- Two key questions:
  1. How to construct a datatype?
  2. How to destruct (or decompose) it?

# Map in Clojure

1. Constructed using `{..}` or `assoc` typically.

```
{:a 0, :b 1, 3 10},
```

```
(assoc {:a 0, :b 1} 3 10)
```

2. Accessed (or destructured) by `get` & keyword.

```
(get {:a 0, :b 1, 3 10} 3)
```

```
(get {:a 0, :b 1, 3 10} :a)
```

```
(:a {:a 0, :b 1, 3 10})
```

# List in Clojure

1. Created using `list` and `conj` typically.

`(list 1 2 3)`, `(conj (list 2 3) 1)`

2. Destructured by `first`, `rest`, and `take`.

`(first (list 1 2 3))`,

`(rest (list 1 2 3))`,

`(take 2 (list 1 2 3))`

# List in Clojure

## 3. Changed using map and filter.

```
(map inc (list 1 2 3)),
```

```
(map + (list 1 2 3) (list 10 11 12))
```

```
(filter (fn [x] (>= x 2)) (list 1 2 3))
```

## 4. reduce.

```
(reduce + 0.0 (list 1 2 3 4))
```

## 5. drop, empty?, many other functions. Google.

# List in Clojure

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(reduce + 0.0 (list 1 2 3 4))
```

5. drop, empty?, many other functions. Google.

[Q] Write a program that computes  $1^2 + 2^2 + \dots + n^2$ .



```
(def sq [x] (* x x))
```

```
(defn f [n]  
  (reduce + 0.0 (map sq (range 0 (inc n))))))
```

### 3. Changed using map and filter.

```
(map inc (list 1 2 3)),
```

```
(map + (list 1 2 3) (list 10 11 12))
```

```
(filter (fn [x] (>= x 2)) (list 1 2 3))
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- Map: {..}, assoc, get, and access by keyword.
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Masters' tools.

Core functions

# Summary

- Map: {..}, assoc, get, and access by keyword.
- List: list, conj, first, rest, take, map, filter, reduce, drop, empty?, etc.

[Q1] Write a fun. rev that reverses a list.

[Q2] Write a fun. conc that concatenates two lists.

```
(defn rev [l]  
  (reduce conj (list) l))
```

y

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```
(defn rev [l]  
  (reduce conj (list) l))
```

```
(defn conc [l1 l2]  
  (reduce conj l2 (rev l1)))
```

- Map: {..}, assoc, get, and access by keyword.
- List: list, conj, first, rest, take, map, filter, reduce, drop, empty?, etc.

[Q1] Write a fun. rev that reverses a list.

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# Anglican in a nutshell

1. Define an Anglican query using `defquery`.
2. Perform inference using `doquery`.

```
(let [s (doquery :importance rfib [20])]
  (take 2 s))
```

```
( { :log-weight 0.0,
    :result 1,
    :predict [] }
  { :log-weight 0.0,
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List  
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# Anglican in a nutshell

3. Pick :result entries and analyse them.

```
(doquery :importance rfib [20])
```

# Anglican in a nutshell

3. Pick `:result entries` and analyse them.

```
(let [s (doquery :importance rfib [20])  
      r (map :result (take 1000 s))]
```

)

# Anglican in a nutshell

3. Pick :result entries and **analyse them**.

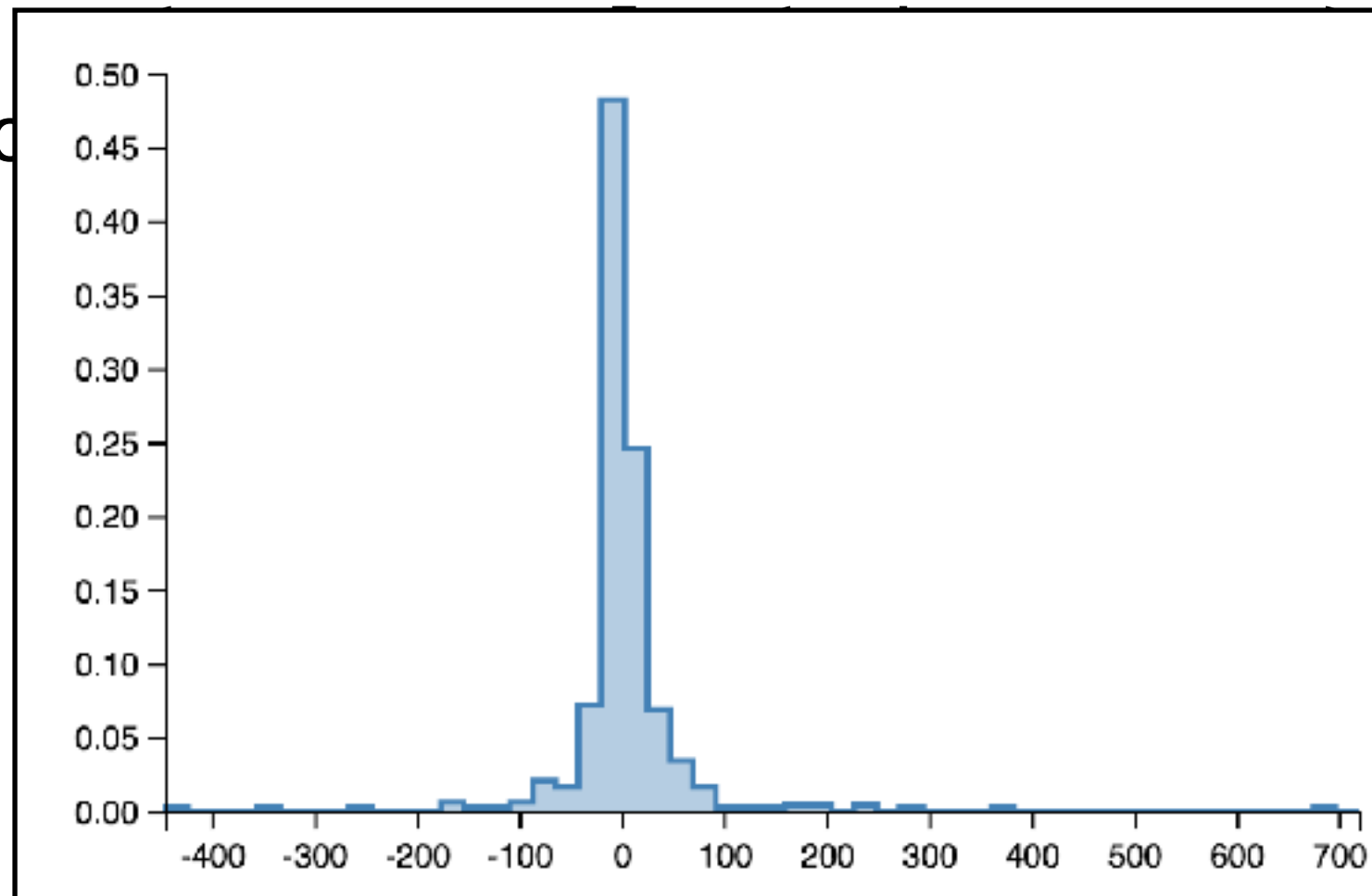
```
(let [s (doquery :importance rfib [20])  
      r (map :result (take 1000 s))]  
  (plot/histogram r  
                  :bins 50  
                  :normalize :probability))
```

# Anglican in a nutshell

3. Pick :result entries and analyse them.

```
(let [s (doquery :importance rfib [20])
```

```
(plot
```



```
ability))
```

# Anglican in a nutshell

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(let [s (doquery :importance rfib [20])  
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[Q1] Compute the average of generated  $R_{20}$  using 1000 samples. This is called empirical mean.

# Anglican in a nutshell

3. Pick `:result` entries and analyse them.

```
(let [s (doquery :importance rfib [20])  
      r (map :result (take 1000 s))]  
  (/ (reduce + 0.0 r) 1000.0))
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[Q1] Compute the average of generated  $R_{20}$  using 1000 samples. This is called empirical mean.

# Anglican in a nutshell

3. Pick `:result` entries and analyse them.

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[Q1] Compute the average of generated  $R_{20}$  using 1000 samples. This is called empirical mean.

[Q2] Compute the variance of generated  $R_{20}$ .

# Anglican in a nutshell

3. Pick :result entries and analyse them.

```
(let [s (doquery :importance rfib [20])  
      r (map :result (take 1000 s))  
      m (/ (reduce + 0.0 r) 1000.0)  
      f (fn [x] (Math/pow (- x m) 2))]  
  (/ (reduce + 0.0 (map f r)) 1000.0))
```

[Q1] Compute the average of generated  $R_{20}$  using 1000 samples. This is called empirical mean.

[Q2] Compute the variance of generated  $R_{20}$ .



# Exercise 3:

[Part 1] Generate a list of Fibonacci numbers (list  $F_1 F_2 \dots F_n$ ) for a given  $n$ .

[Part 2] Generate a list of indices  $0 < i \leq 10000$  such that  $i$  is the sum of digits of  $F_i$ .

Assume `get-digits` for converting a number to a list of its digits. `(get-digits 23)=(list 2 3)`.

Assume `range`. `(range 1 6) = (list 1 2 3 4 5)`.

# Part I

```
(defn fib [n]
  (loop [i 2 s (list 1 1)]
    (if (= i n)
      (rev s)
      (recur (+ i 1)
              (conj s (+ (first s)
                          (second s)))))))
```

# Part 2

```
(defn ck [fibn-and-i]
  (let [fibn (first fibn-and-i)
        i    (second fibn-and-i)]
    (= (reduce + 0 (get-digits fibn))
       i)))
```

```
(def idx-fib-seq
  (map (fn [s i] (list s i))
       (fib 10000)
       (range 1 10001)))
```

```
(def indices
  (map second (filter ck idx-fib-seq)))
```

# Topics covered

- Functions, recursion, loop, list, and map in Clojure.
- `defquery`, and `doquery` in Anglican.

# Announcement

1. Homework 0 in the course webpage.
  - It will teach you how to use Gorilla and to try examples in the web browser.
2. Form a group and tell us by the midnight of 13 March 2018 (Tuesday).