



Word Embeddings

Lena Voita

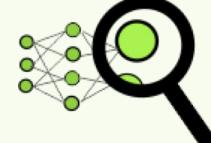
Lecture-blog and lots of additional materials are here:

https://lena-voita.github.io/nlp_course/word_embeddings.html

NLP Course For You



What is going to happen:

- Why do we need word representations?
- One-hot Vectors
- Distributional Semantics
- Count-Based Methods
- Word2Vec (Prediction-based Method)
- GloVe
- Evaluation
-  Analysis and Interpretability

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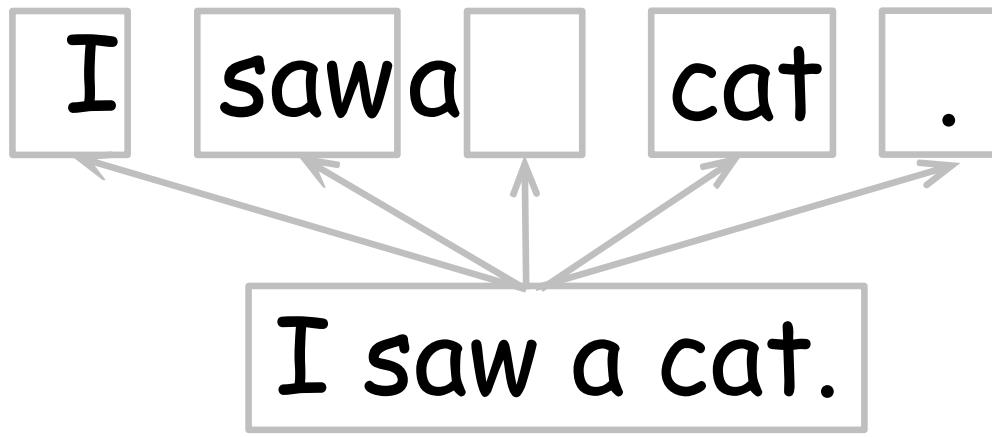
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Why do we need word representations?

I saw a cat.

Text (your input)

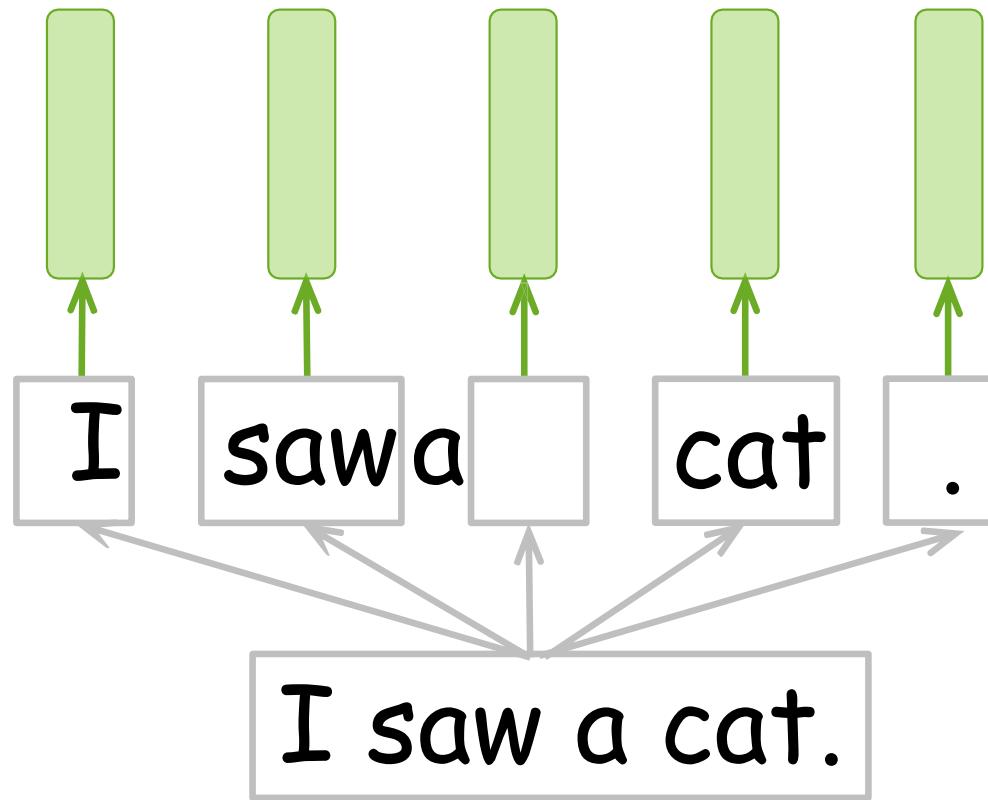
Why do we need word representations?



Sequence of tokens

Text (your input)

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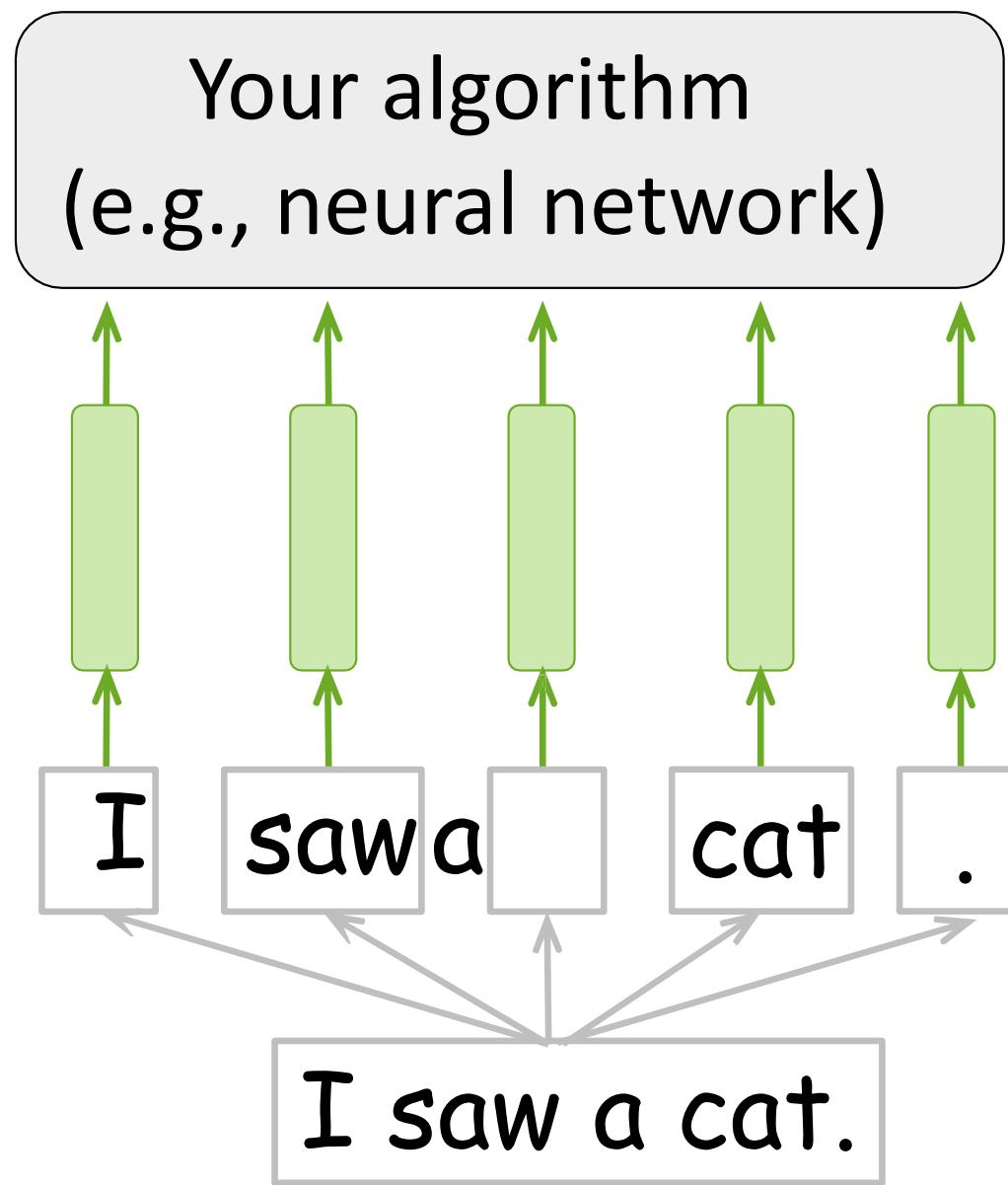


Word representation - vector
(input for your model/algorithm)

Sequence of tokens

Text (your input)

Why do we need word representations?



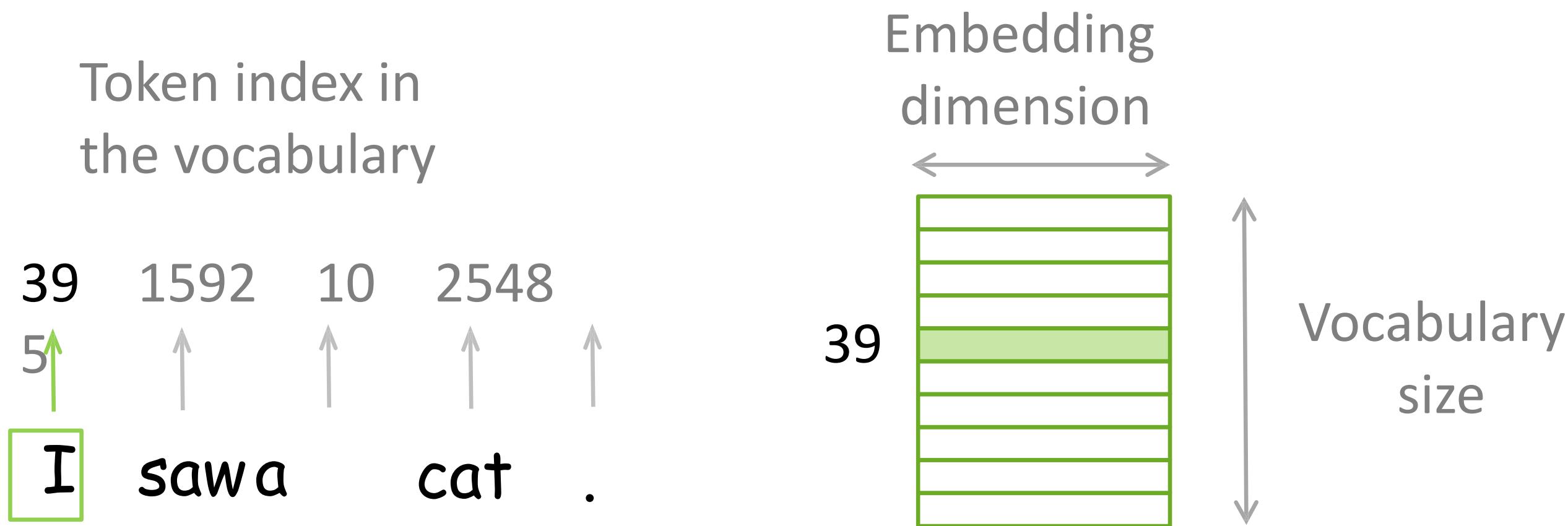
Any algorithm for solving a task

Word representation - vector
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Sequence of tokens

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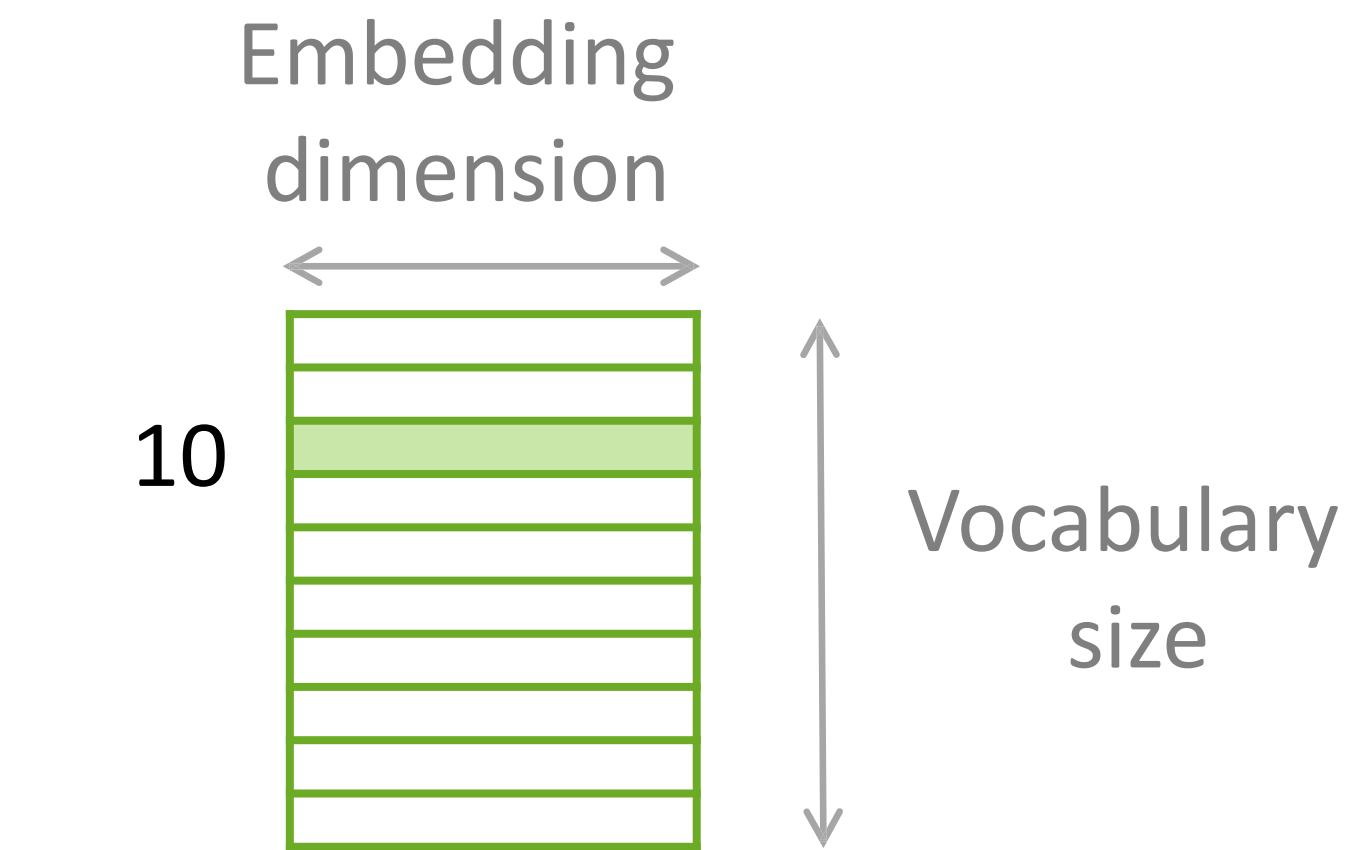
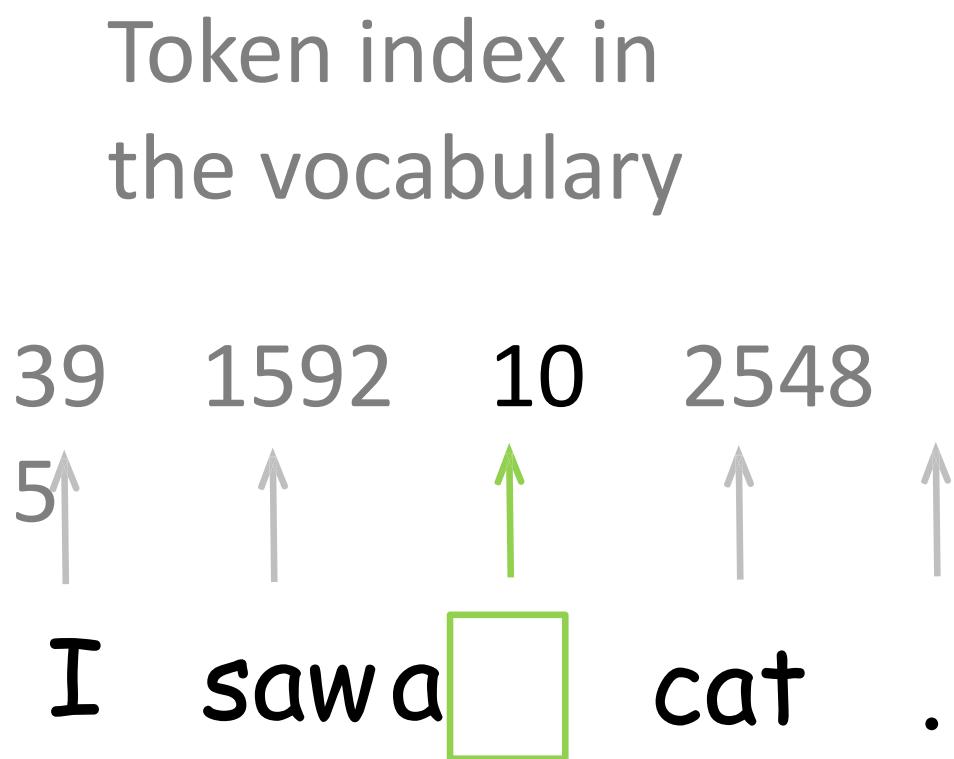
How it works: Look-up Table



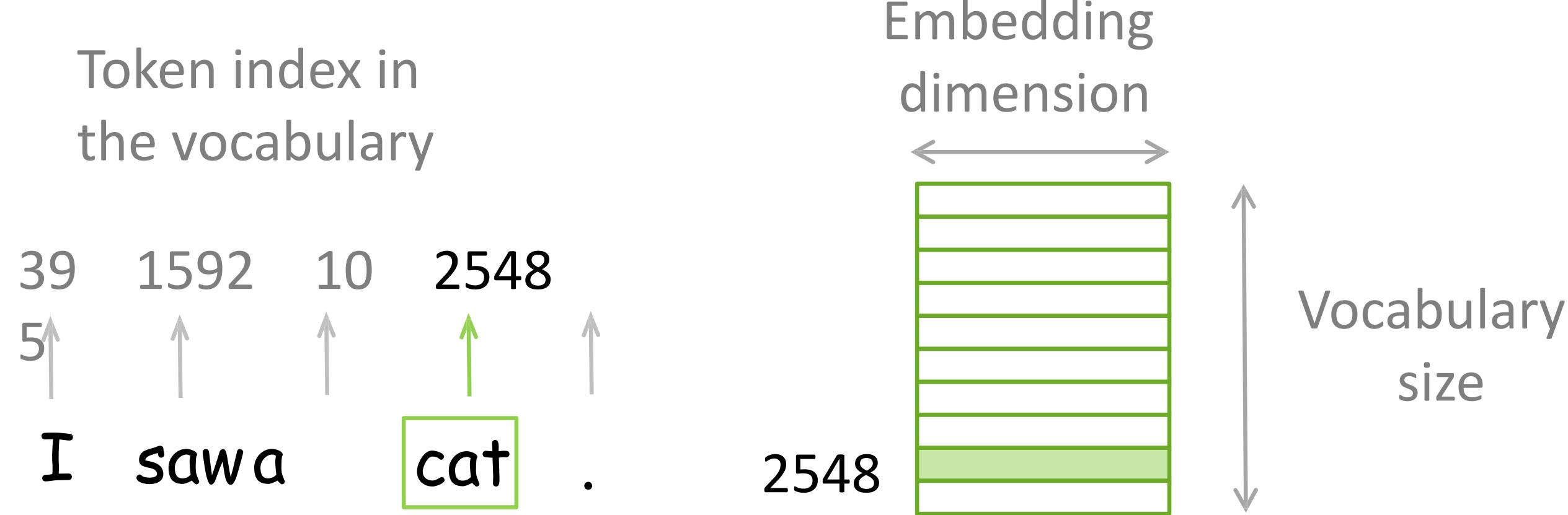
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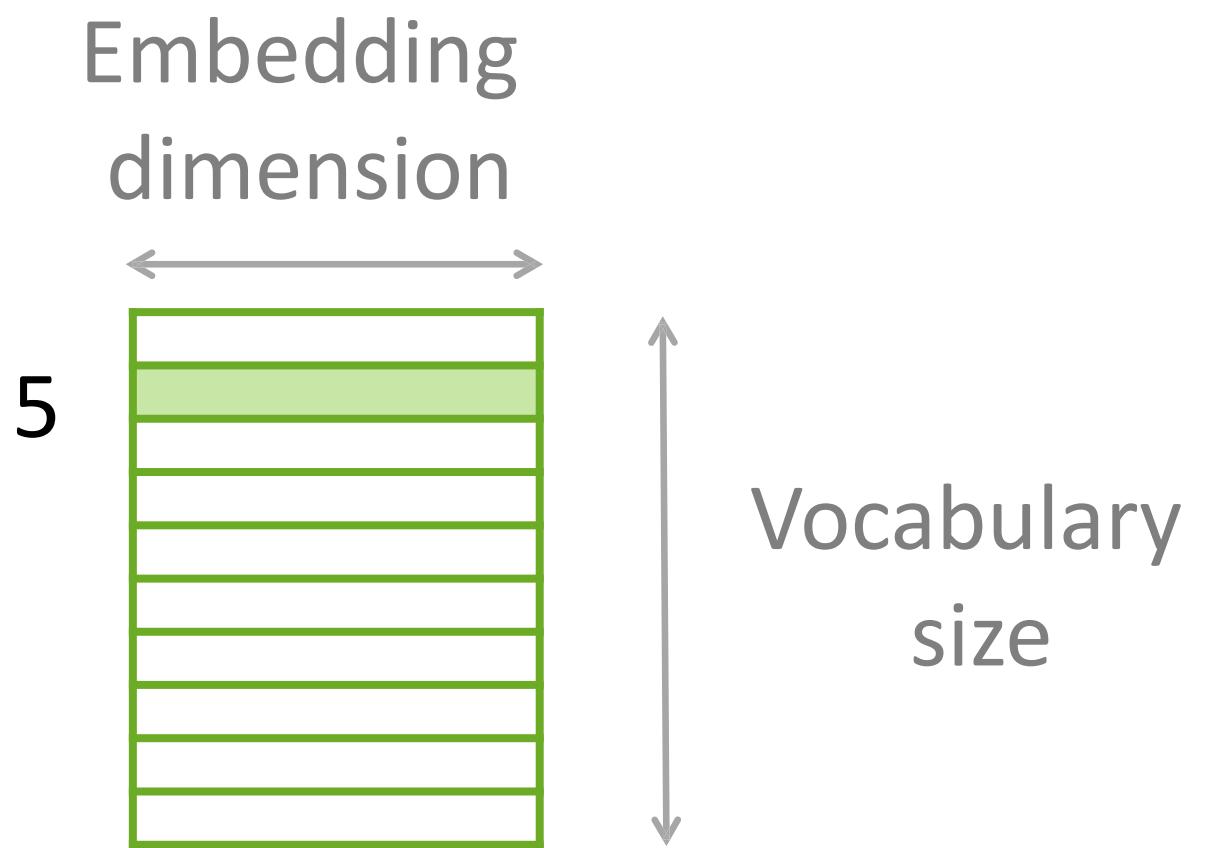
How it works: Look-up Table

Token index in the vocabulary

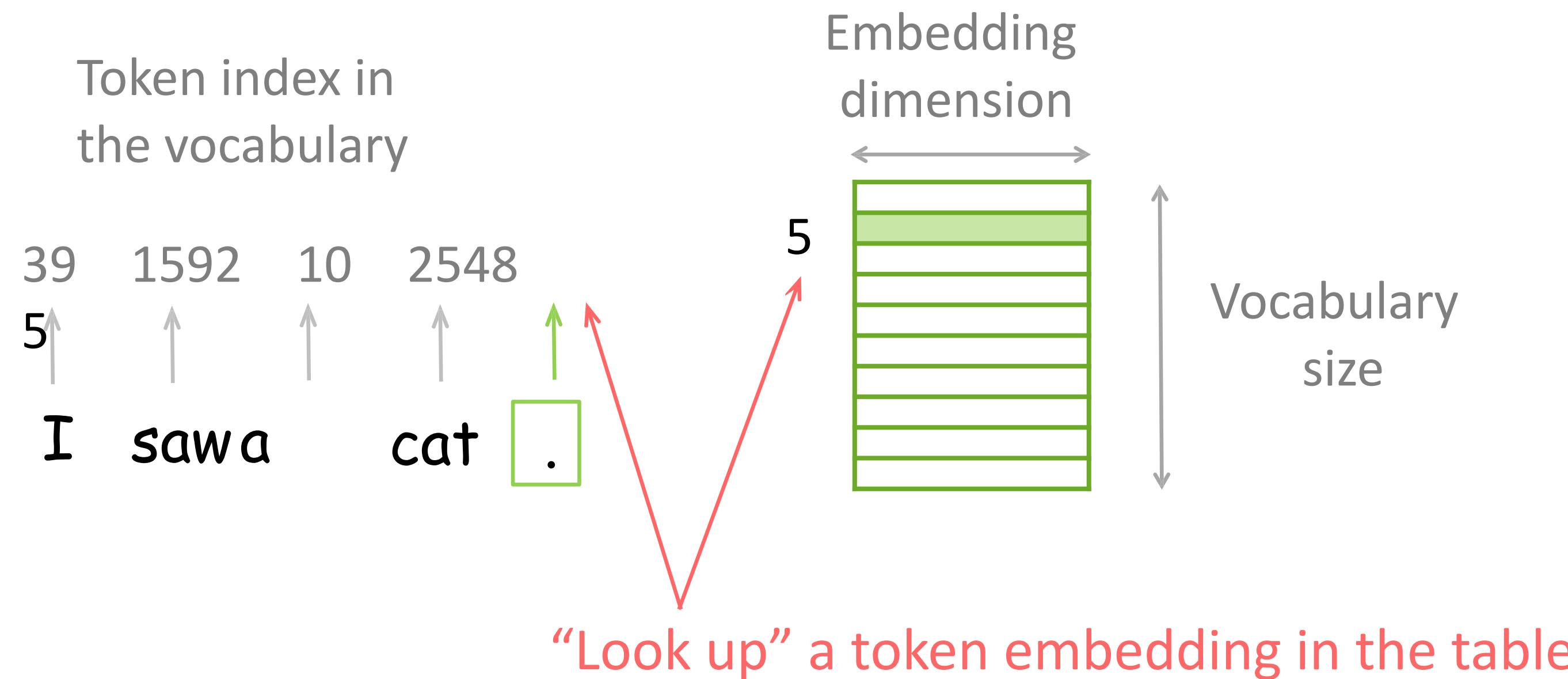
39 1592 10 2548

5 ↑ ↑ ↑ ↑ ↑

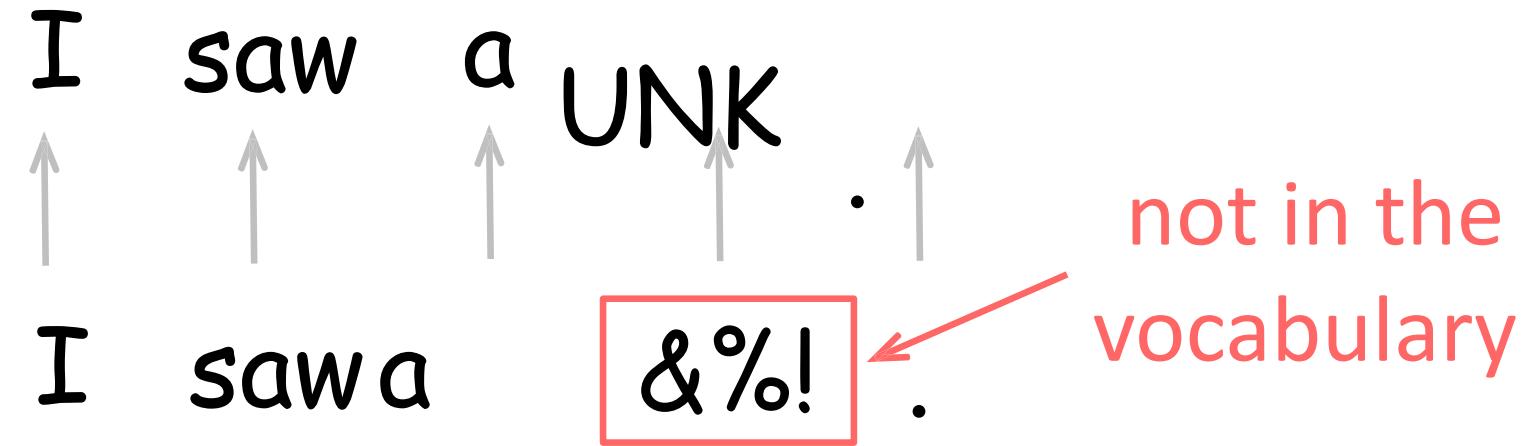
I saw a cat .



How it works: Look-up Table



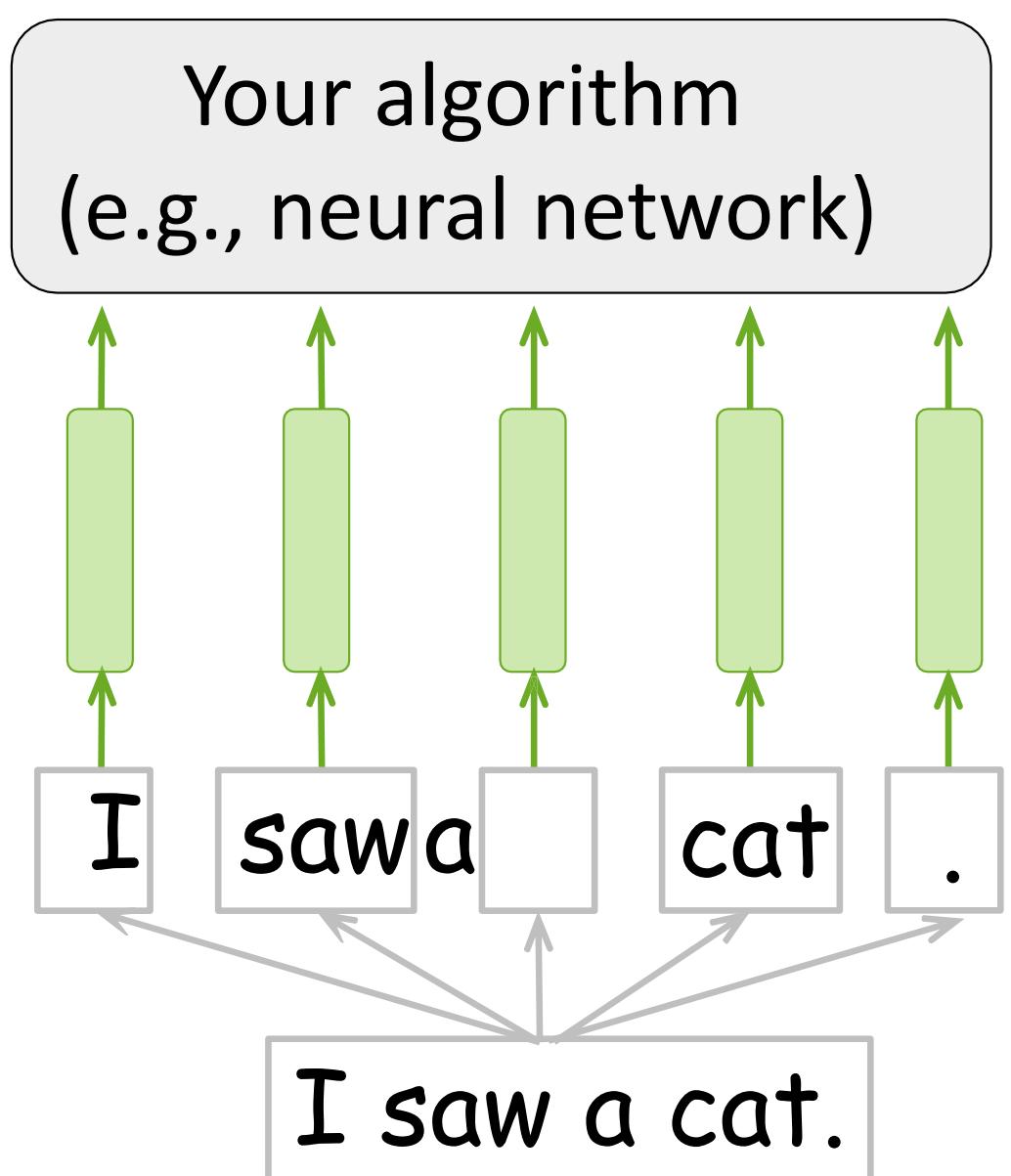
Note UNKs: Out-of-Vocabulary Tokens



Vocabulary is chosen in advance

Therefore, some tokens may be “unknown” – you can use a special token for them

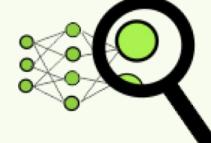
How can we get word representations?



In the following:

How can we get these representations?

What is going to happen:

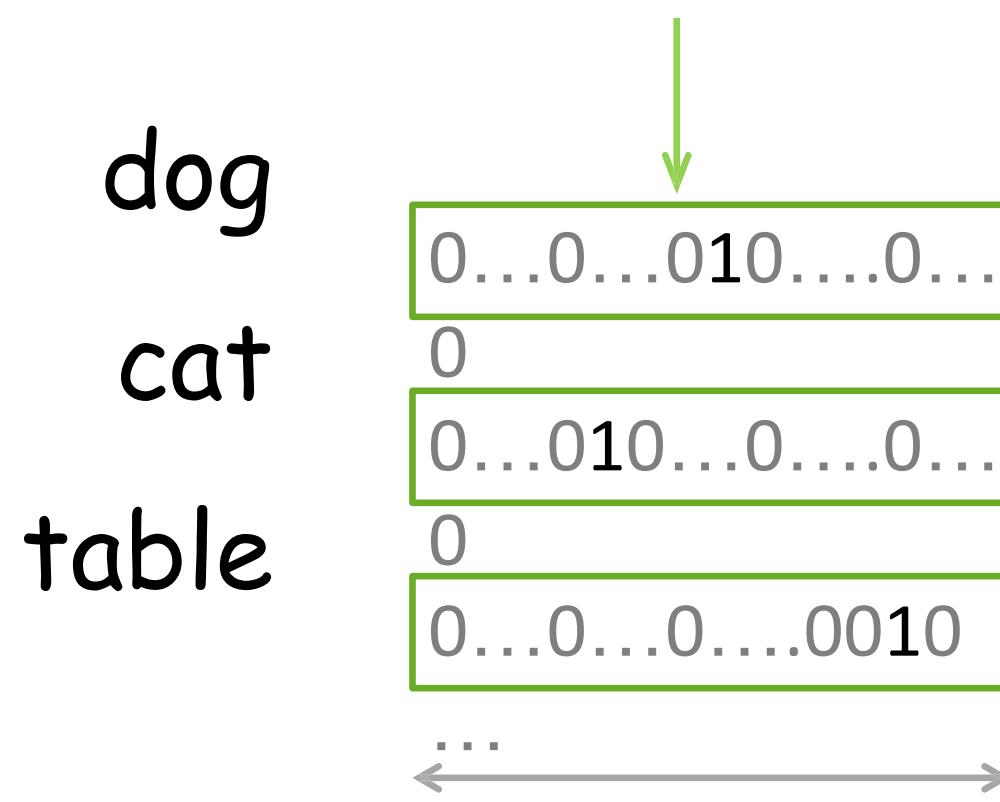
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One-Hot Vectors: Represent Words as Discrete Symbols

One is 1, the rest are 0



One-Hot Vectors: Represent Words as Discrete Symbols

One is 1, the rest are 0

dog

0...0...010....0...

cat

0...010....0....0...

table

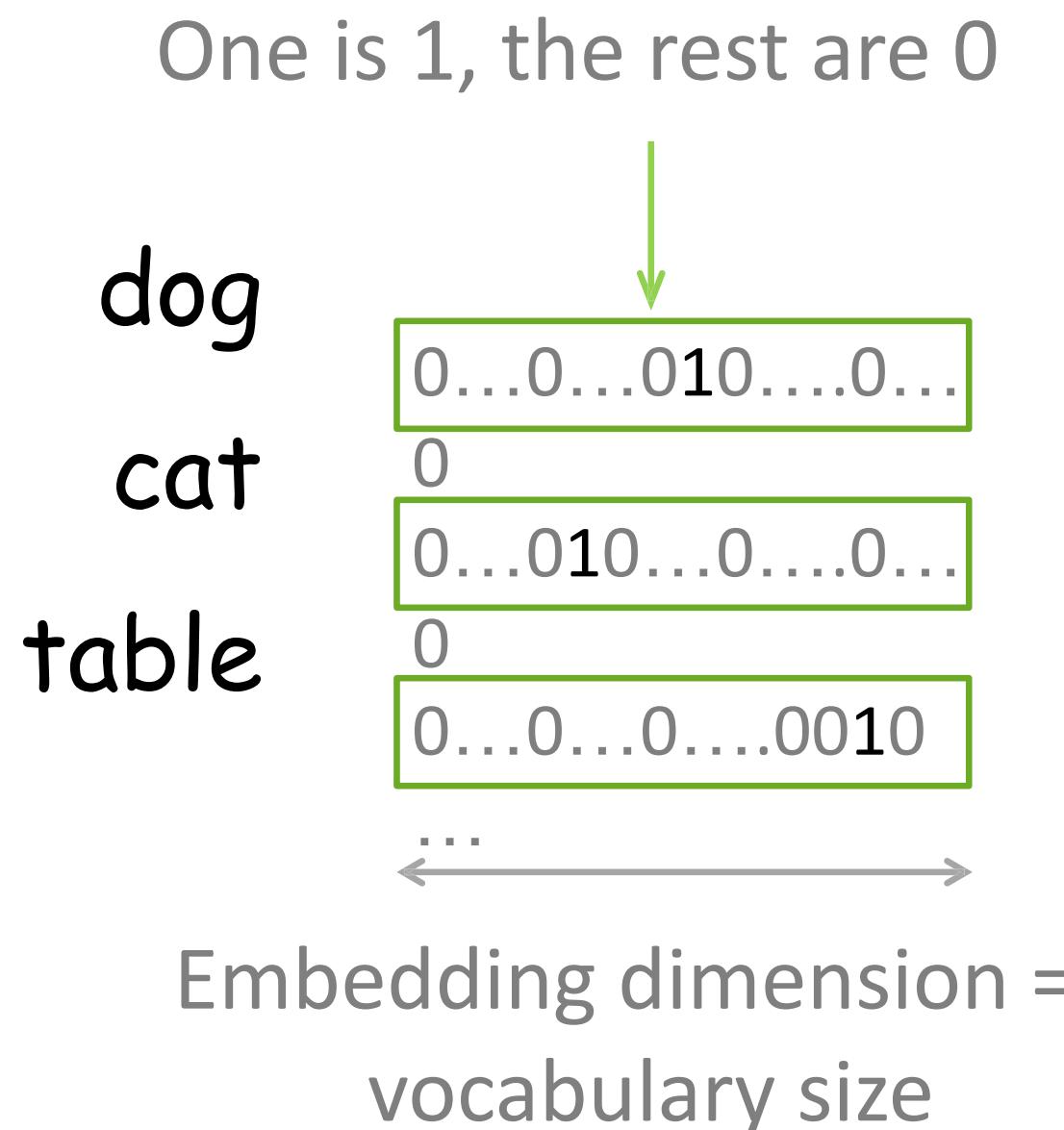
0...0...0....0010



Embedding dimension =
vocabulary size

Any problems?

One-Hot Vectors: Represent Words as Discrete Symbols



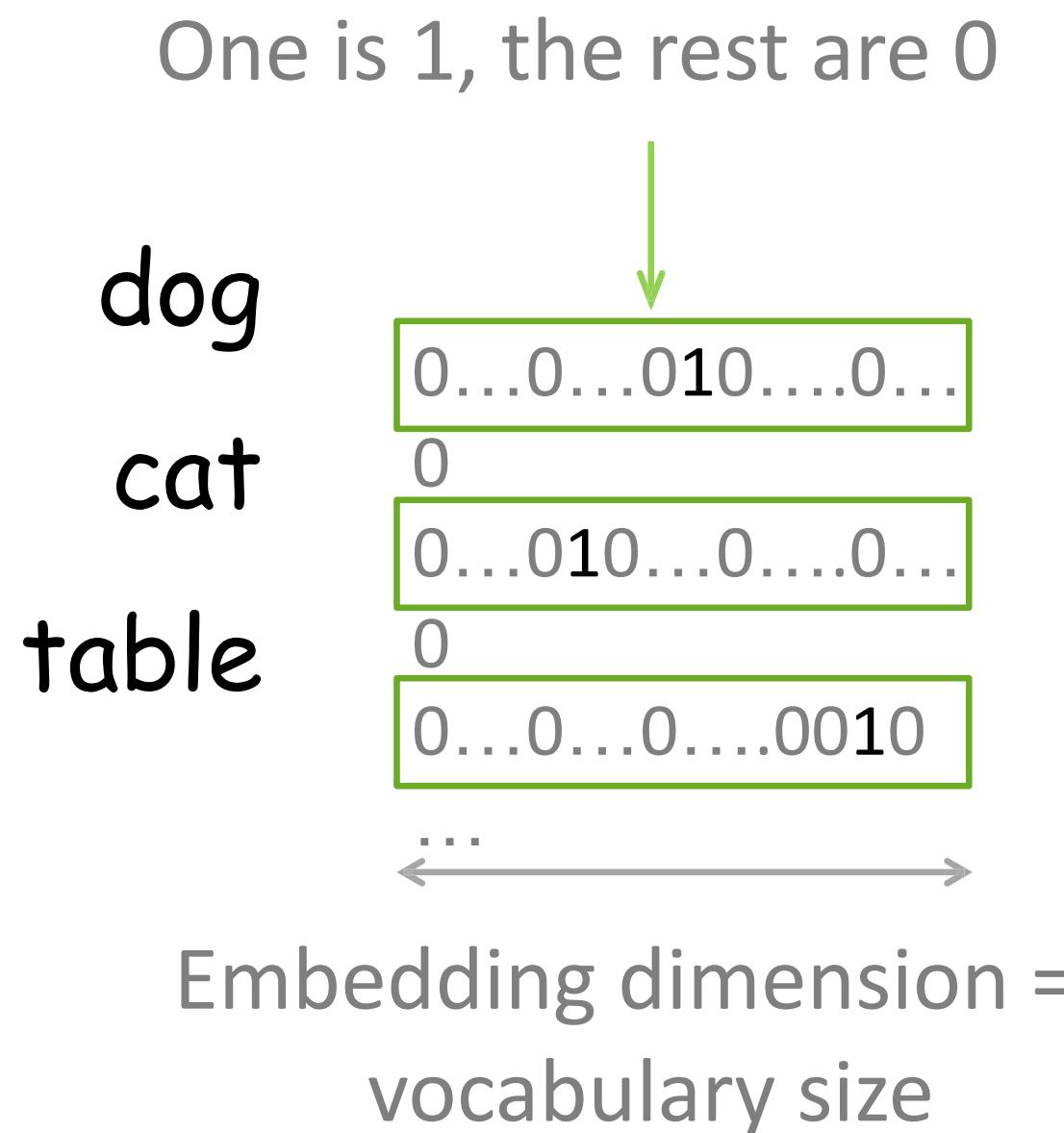
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- Vector size is too large
- Vectors know nothing about meaning

e.g., cat is as close to

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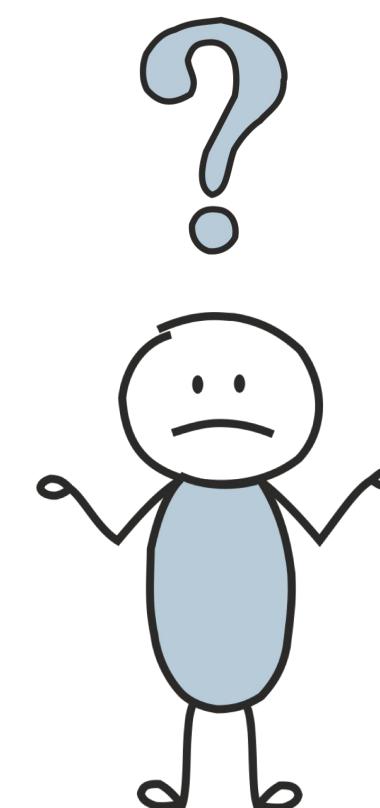
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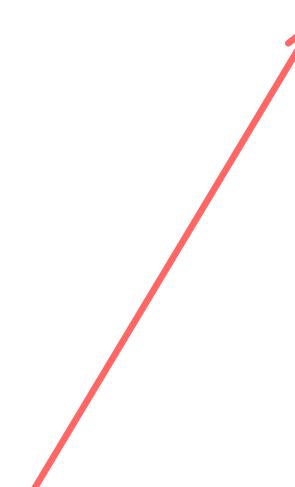
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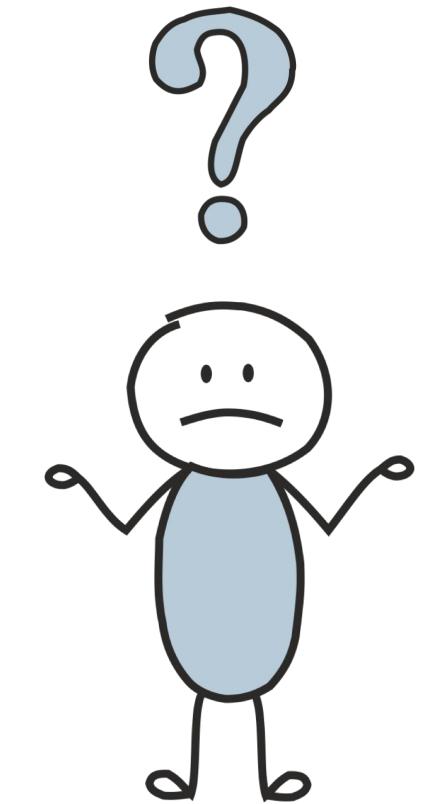
What is meaning?



What is meaning?

Do you know what the word **tezgüino** means ?

(We hope you do not)



What is meaning?

Now look how this word is used in different contexts:

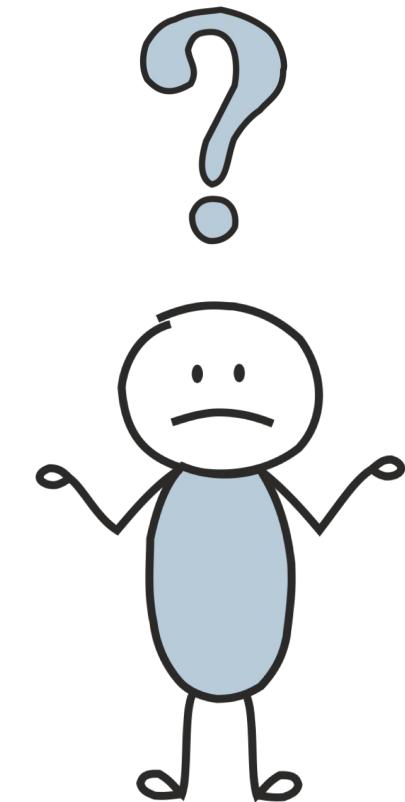
A bottle of **tezgüino** is on the table.

Everyone likes **tezgüino**.

Tezgüino makes you drunk.

We make **tezgüino** out of corn.

Can you understand what **tezgüino** means ?



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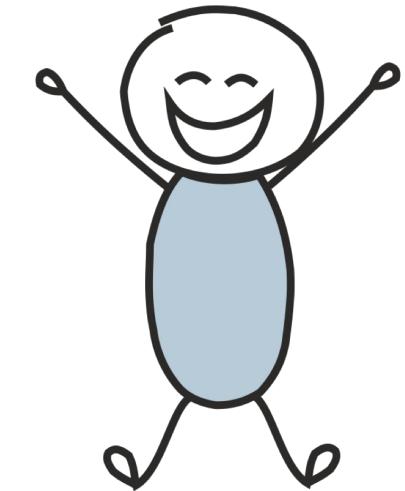
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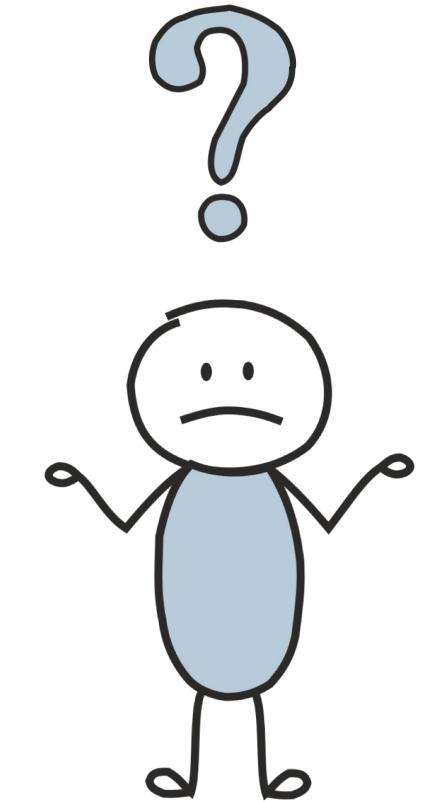
Tezgüino is a kind of alcoholic beverage made from corn.



With context, you can understand the meaning!

What is meaning?

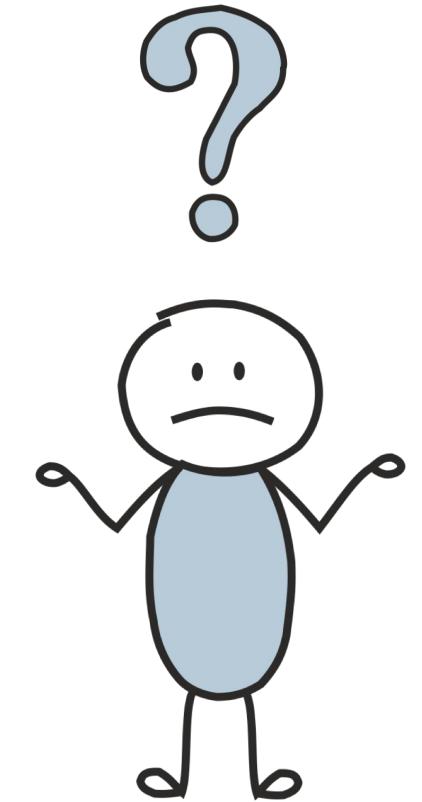
How did you do this?



What is meaning?

- (1) A bottle of _____ is on the table.
- (2) Everyone likes _____
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What other words fit into these contexts ?



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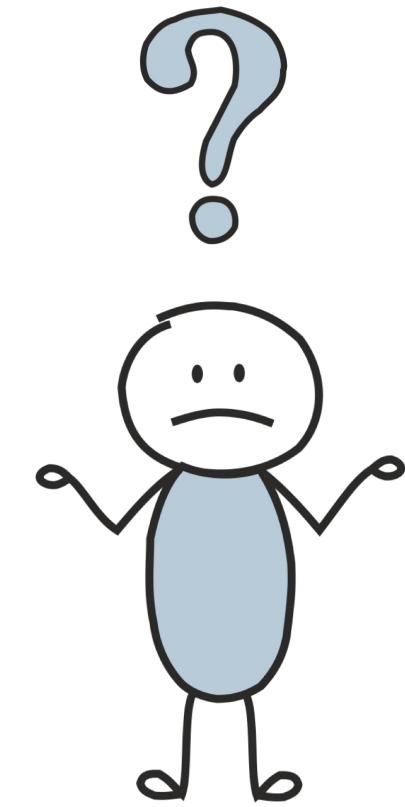
(1) (2) (3) (4)

← contexts

...

tezgüino1	1	1	1
loud0	0	0	0
motor oil	1	0	0
tortillas0	1	0	1
wine	1	1	1

← rows show contextual
properties: 1 if a word can
appear in the context, 0 if not



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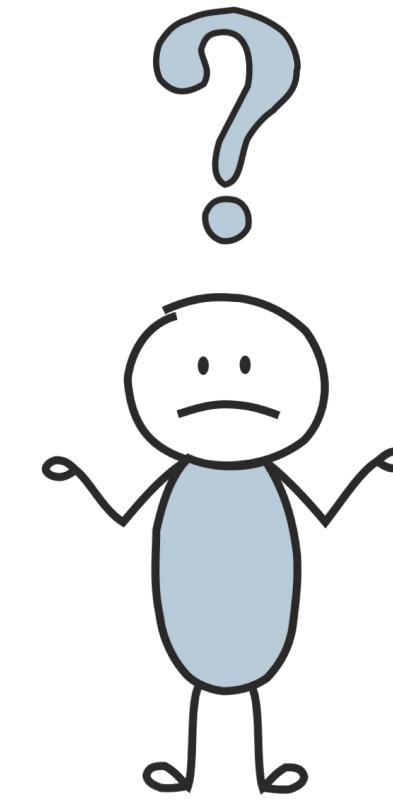
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rows are
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meanings of the
words are similar

Is this true?

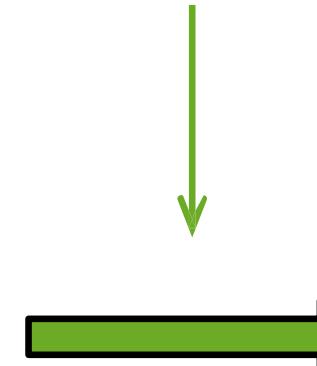
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This is the distributional hypothesis

rows are
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meanings of the
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Distributional Hypothesis

Words which frequently appear in similar contexts have similar meaning.

(Harris 1954, Firth 1957)

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This can be used in practice to build word vectors!

Distributional Hypothesis

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Main idea:

We have to put information about contexts into word vectors.

What comes next: different ways to do this

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Count-Based Methods



Count-Based Methods Idea

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Count-Based Methods: Idea

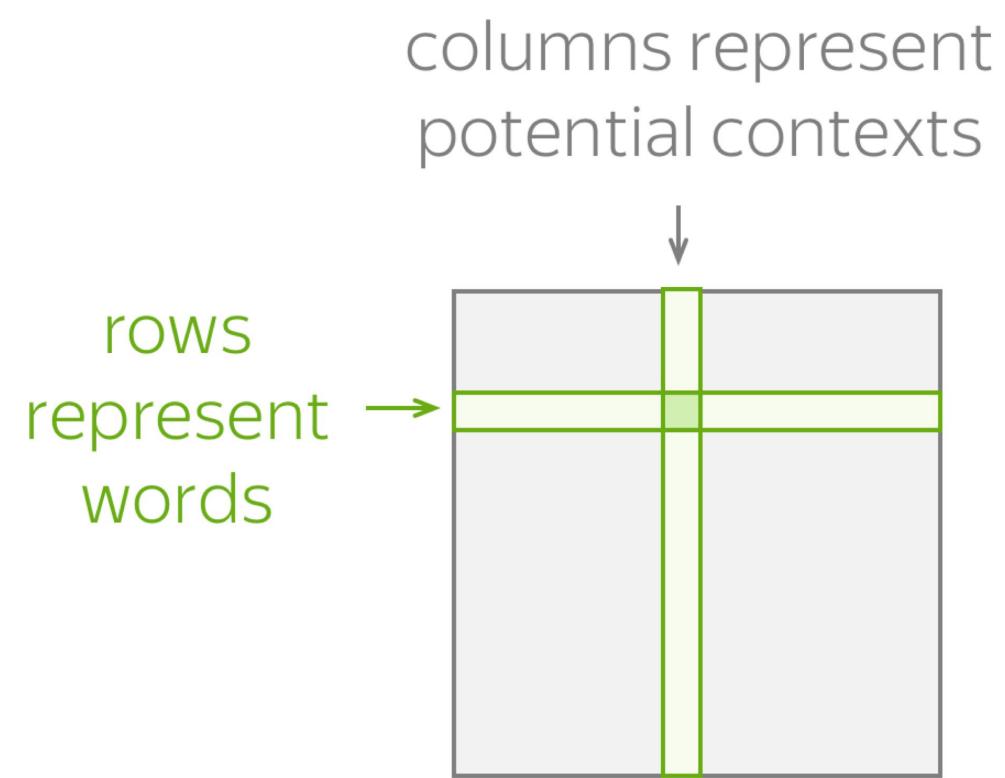
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Count-based methods take this idea quite literally :)

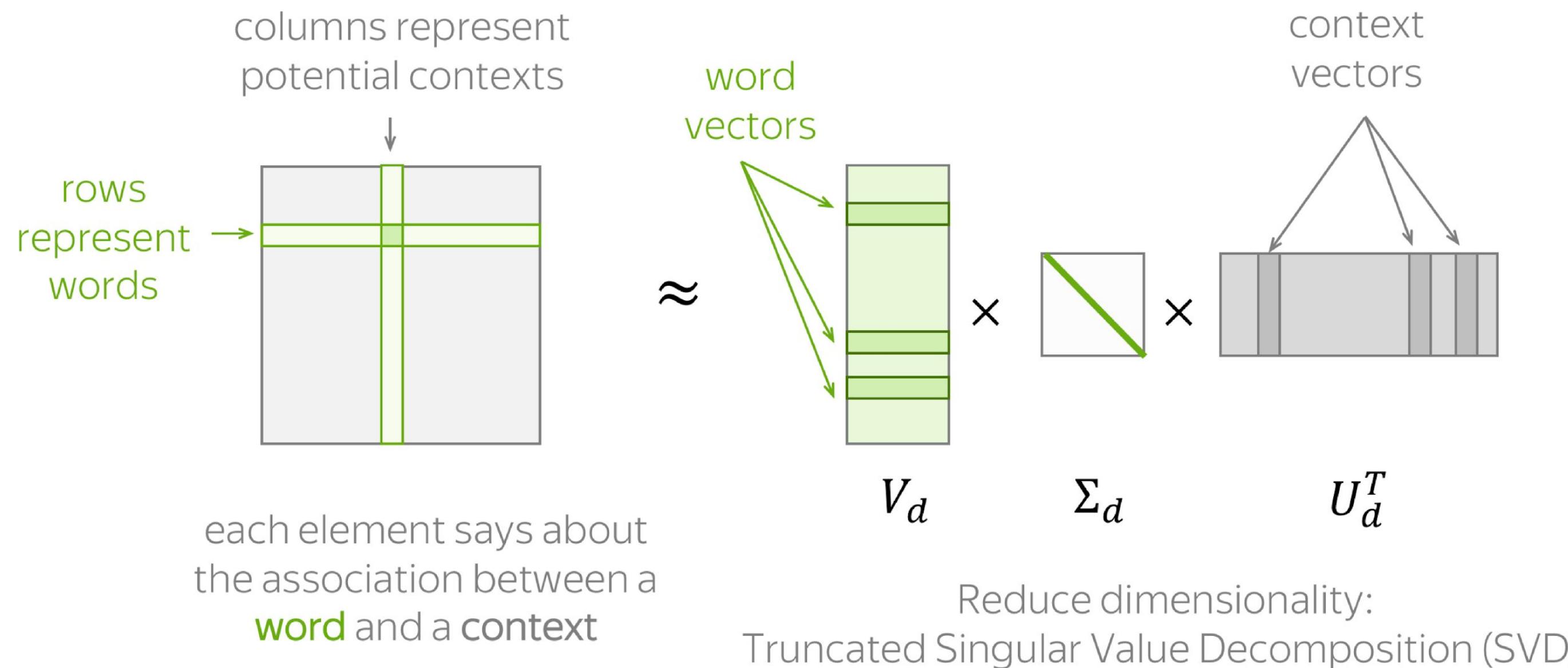
How: Put this information manually based on global corpus statistics.

Count-Based Methods: The General Pipeline

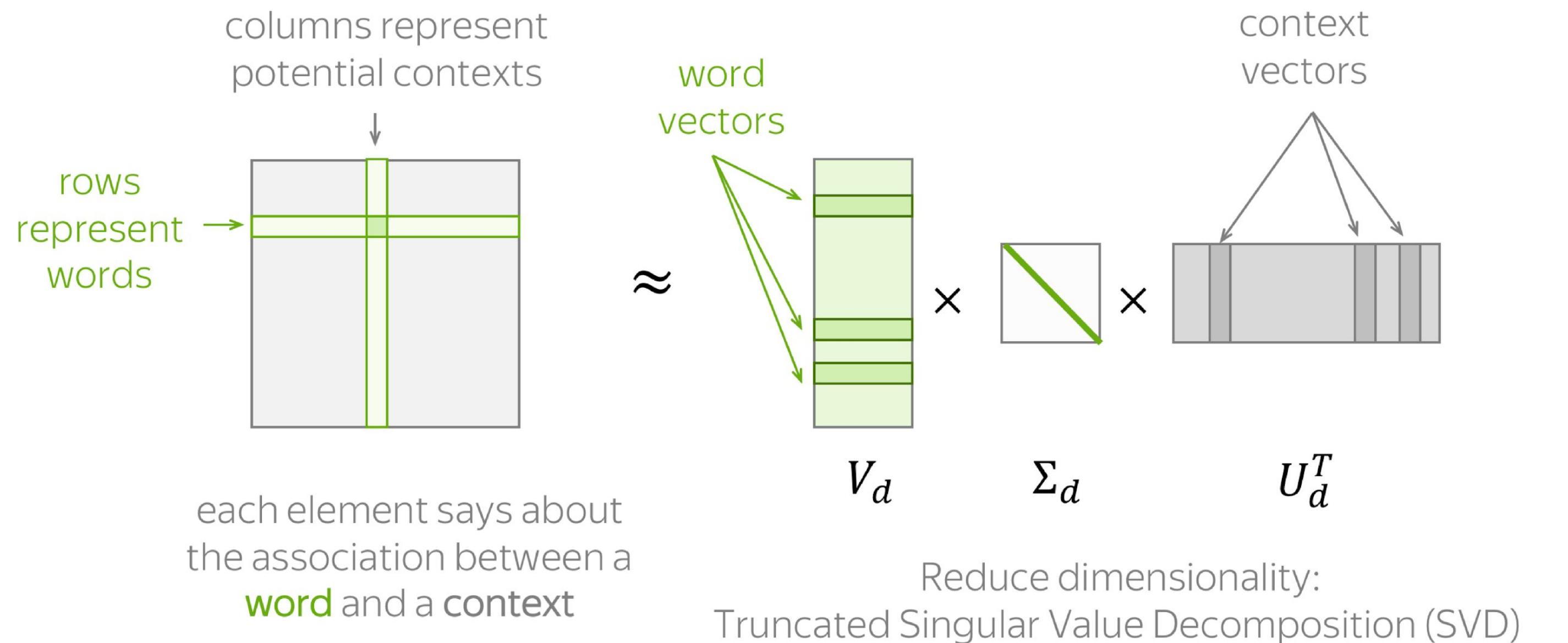


each element says about the association between a **word** and a context

Count-Based Methods: The General Pipeline



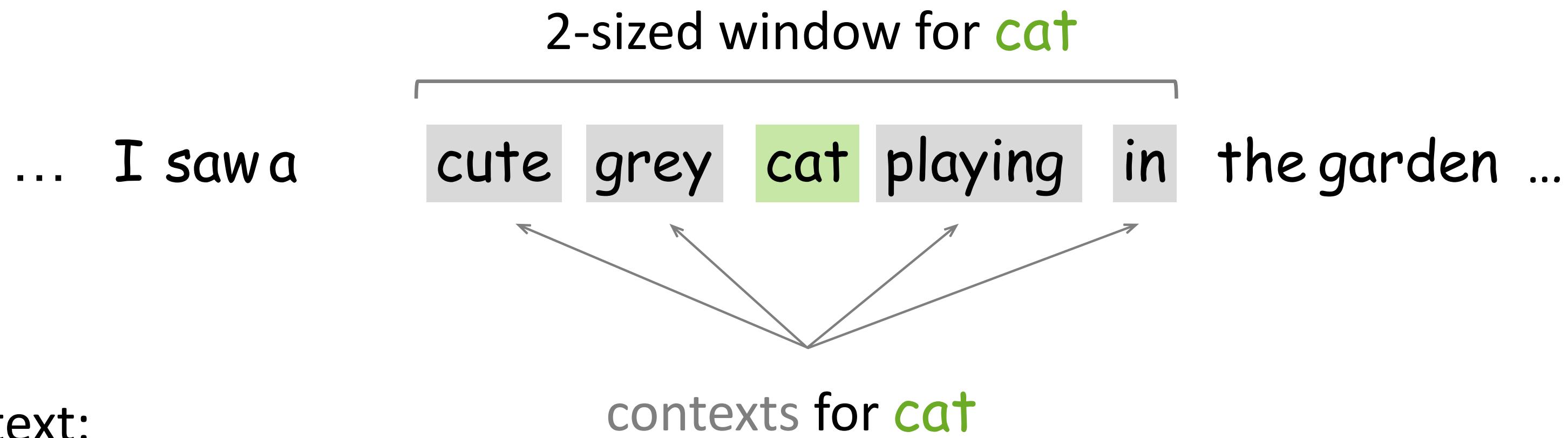
Count-Based Methods: The General Pipeline



Need to define:

- what is context
- how to compute matrix elements

Simple: Co-Occurrence Counts



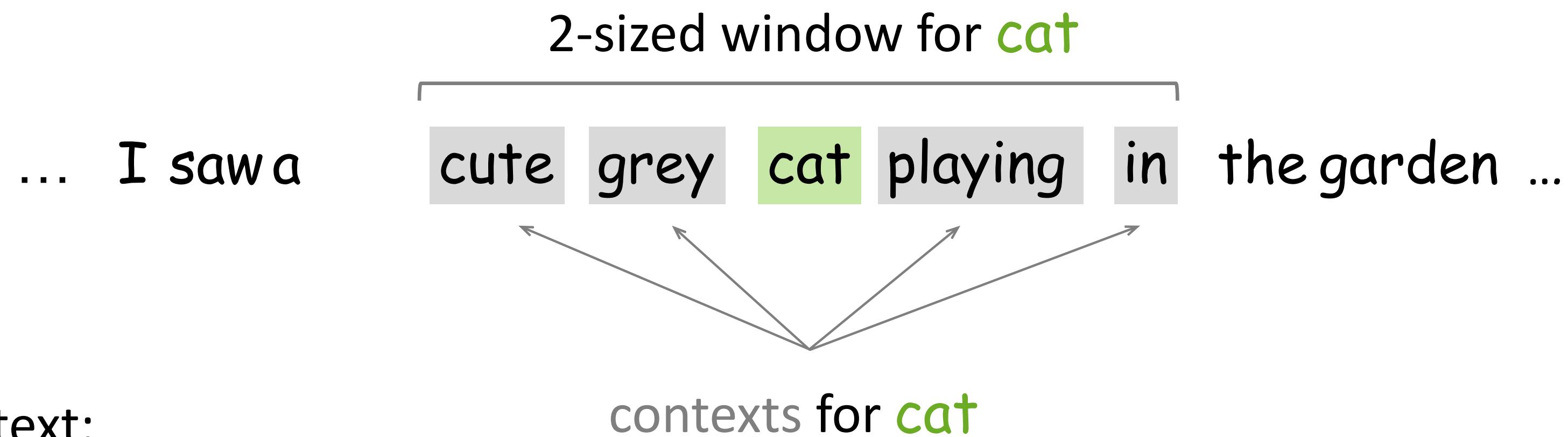
Context:

- surrounding words
in a L-sized window

Matrix element:

- $N(w, c)$ – number of times word w appears in context c

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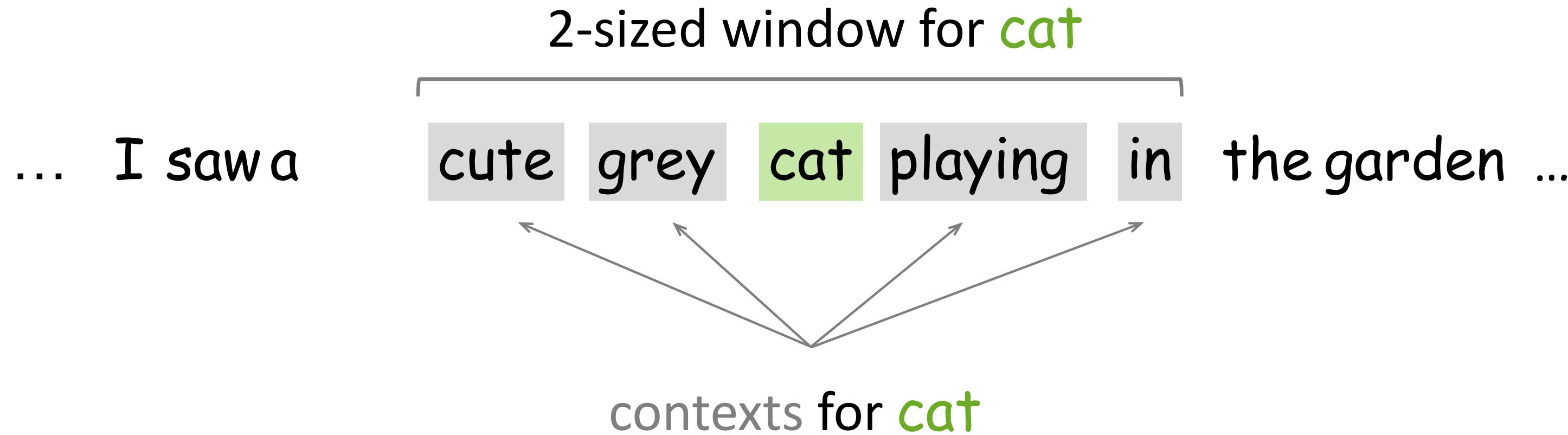
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NLP Course For You



The (once) famous HAL model (1996) is also a modification of this approach. Learn more from [this exercise](#) in the Research Thinking section.

Positive Pointwise Mutual Information (PPMI)



Context:

- surrounding words
in a L-sized window

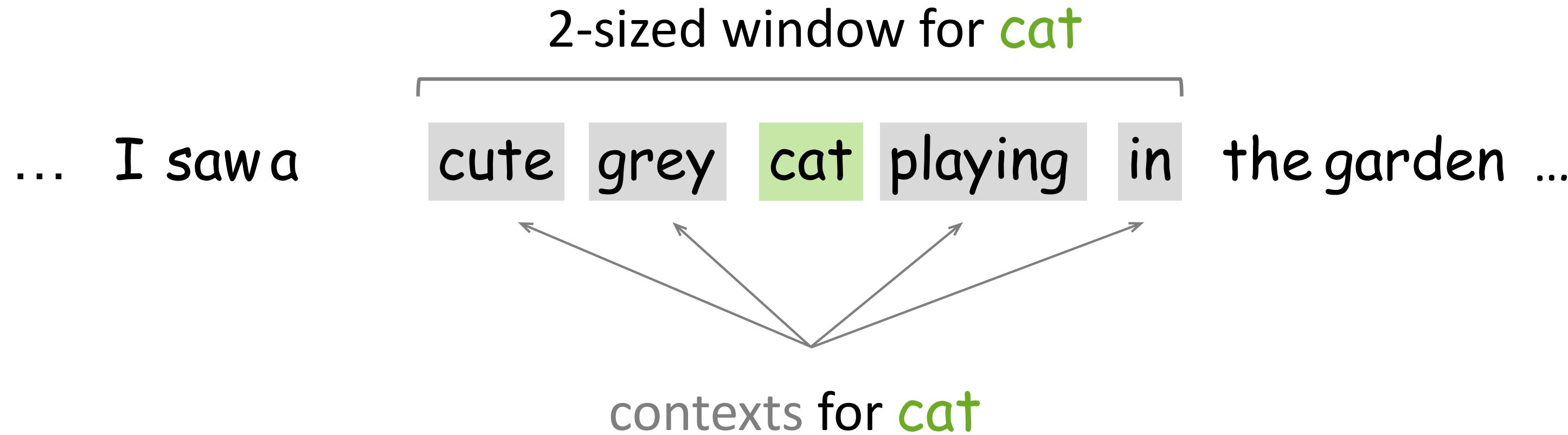
Matrix element:

- $\text{PPMI}(w, c) = \max(0, \text{PMI}(w, c))$,

where

$$\text{PMI}(w, c) = \log \frac{P(w, c)}{P(w)P(c)} = \log \frac{P(w, c)}{P(w) + P(c) - P(w, c)}$$

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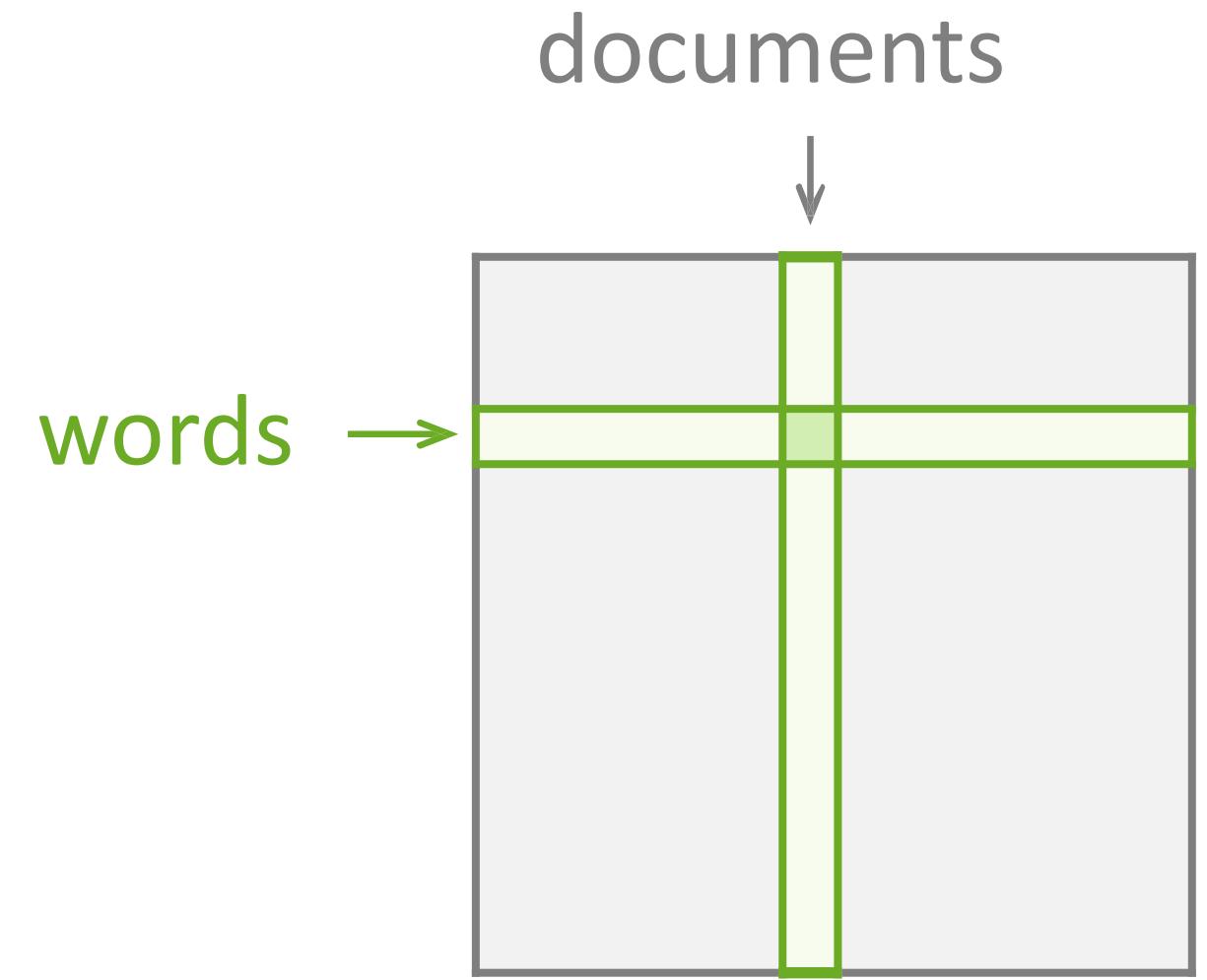
How much one variable tells about another

Latent Semantic Analysis (LSA):

Understanding Documents

Context:

- document d (from a collection D)



Each element is the association between a **word** and a document

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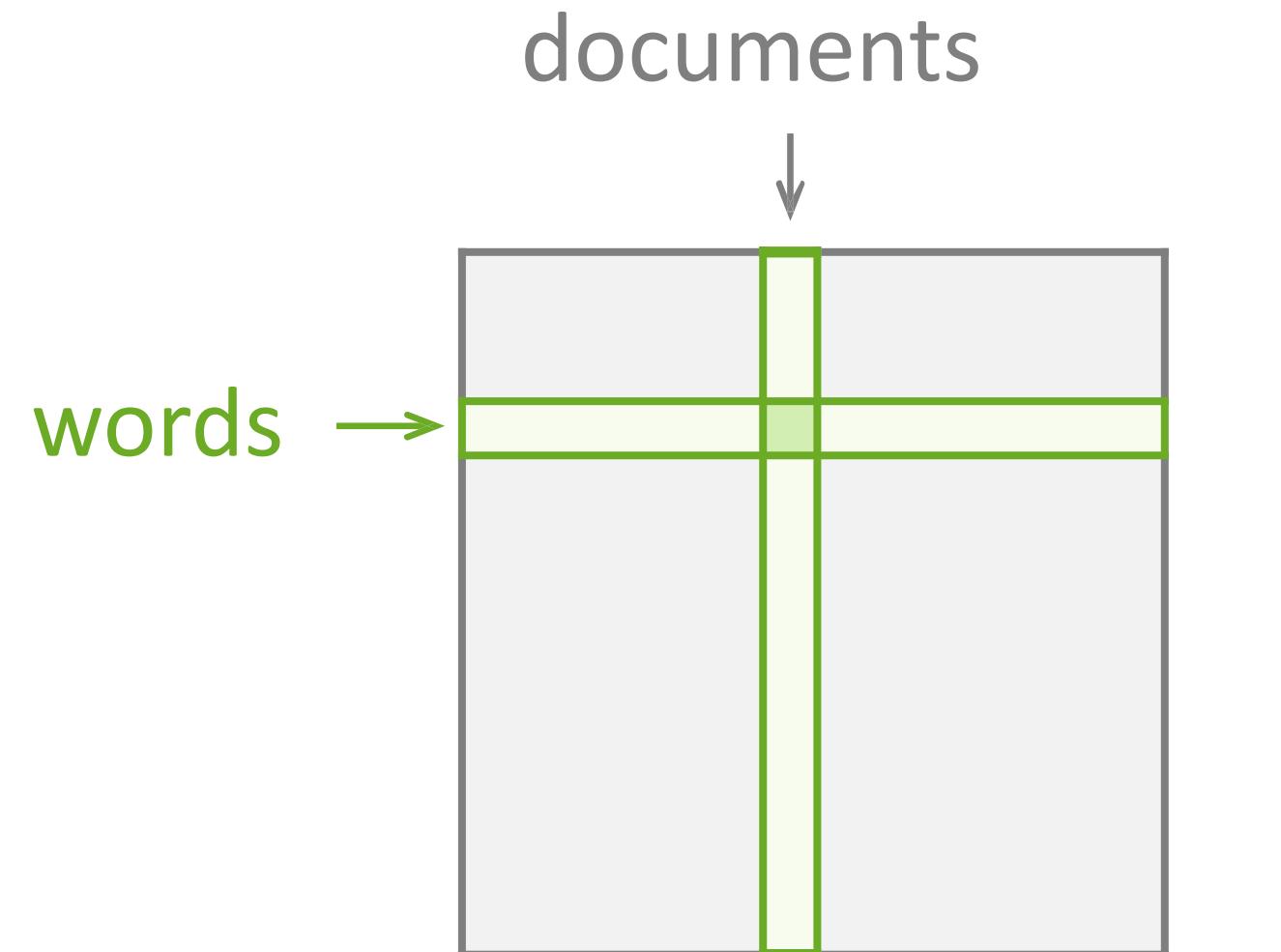
- $\text{tf-idf}(w, d, D) = \text{tf}(w, d) \cdot \text{idf}(w, D)$

$$N(w, d)$$

term frequency

$$\log \frac{|D|}{|\{d \in D : w \in d\}|}$$

inverse document frequency



Each element is the association between a **word** and a document

Count-Based Methods: Idea

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Word2Vec

(Prediction-Based Method)



What's inside:

Word2Vec

- Idea
- Objective Function
- Training Procedure
- Faster Training: Negative Sampling
- Word2Vec versions: Skip-Gram vs CBOW
- Final Notes

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Word2Vec uses this idea differently from count-based methods:

How: Learn word vectors by teaching them to predict contexts.

Word2Vec: Idea

| How: Learn word vectors by teaching them to predict contexts.

- Learned parameters: word vectors
- Goal: make each vector “know” about the contexts of its word
- How: train vectors to predict possible contexts from words (or, alternatively, words from contexts)

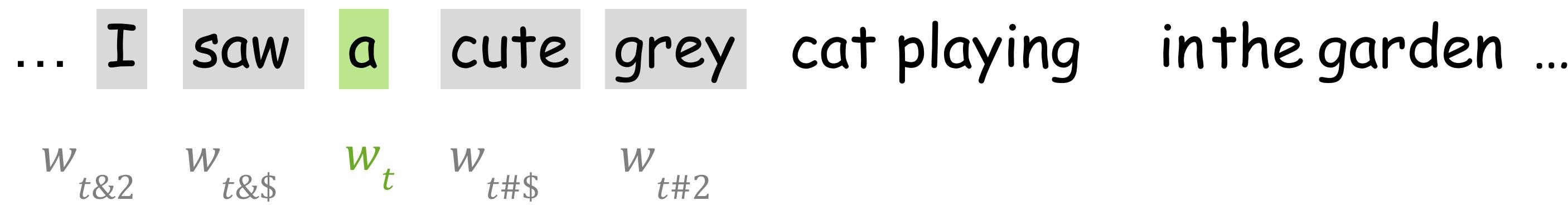
Word2Vec: High-Level pipeline

- take a huge text corpus

...I saw a cute grey cat playing in the garden ...

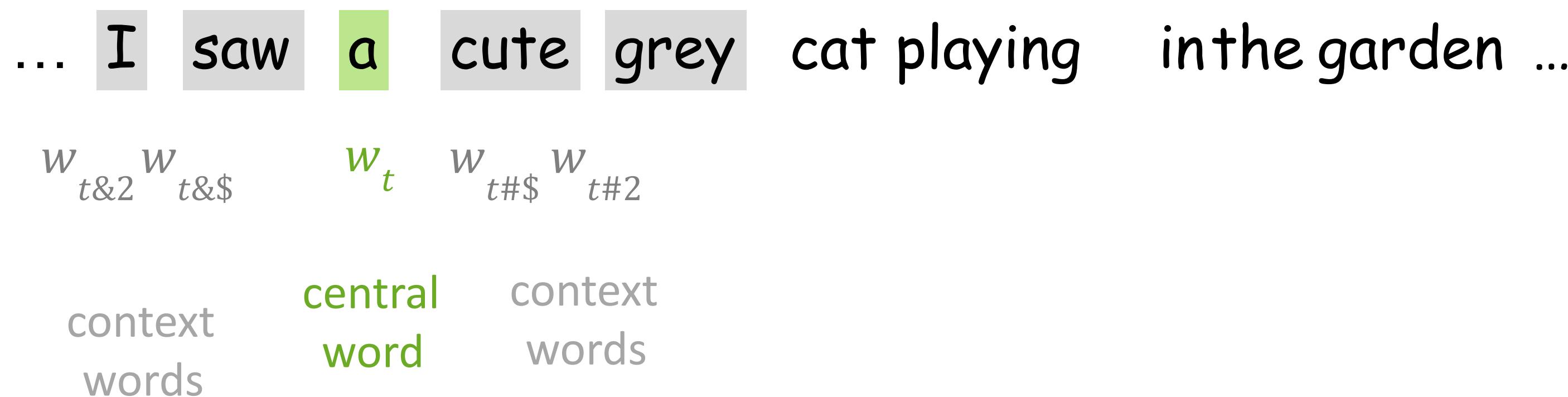
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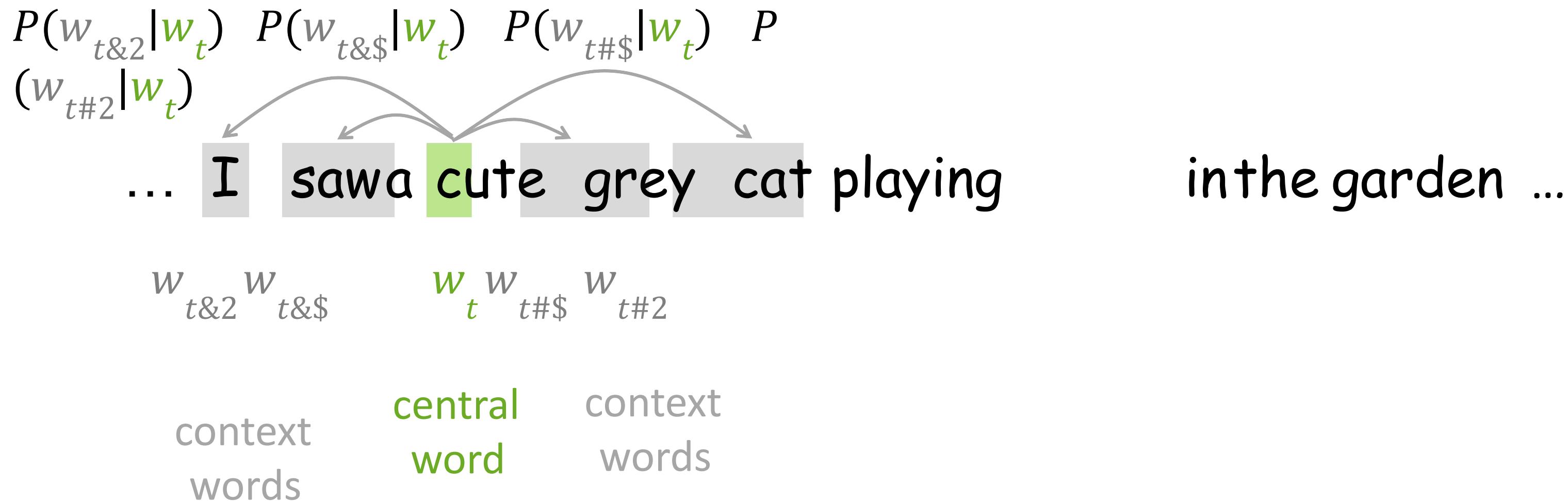
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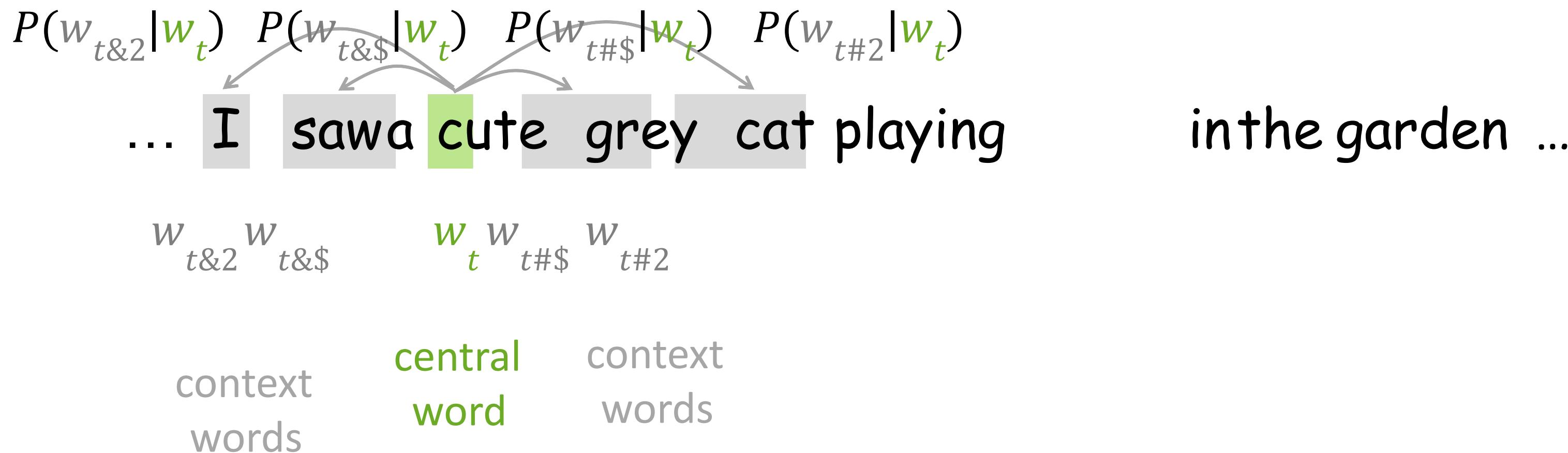
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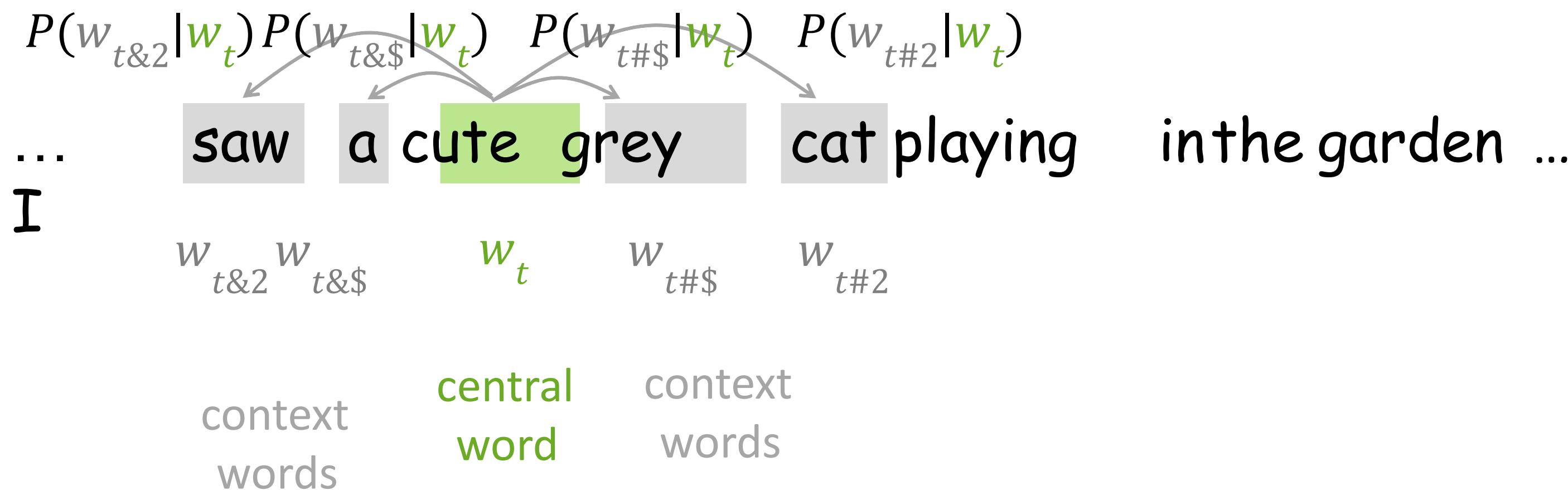
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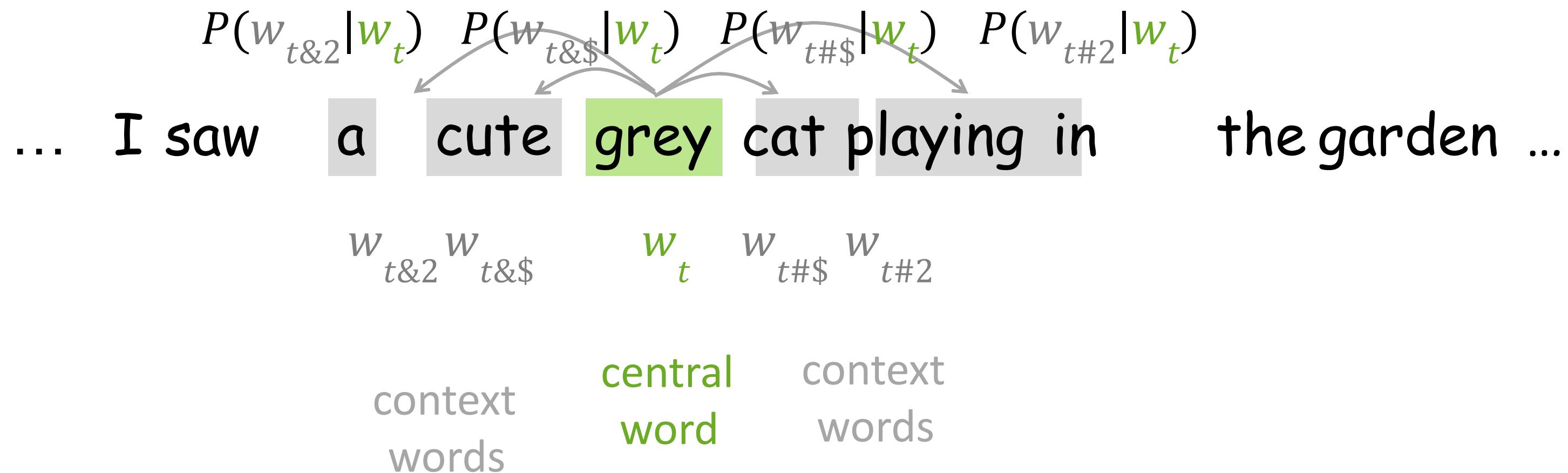
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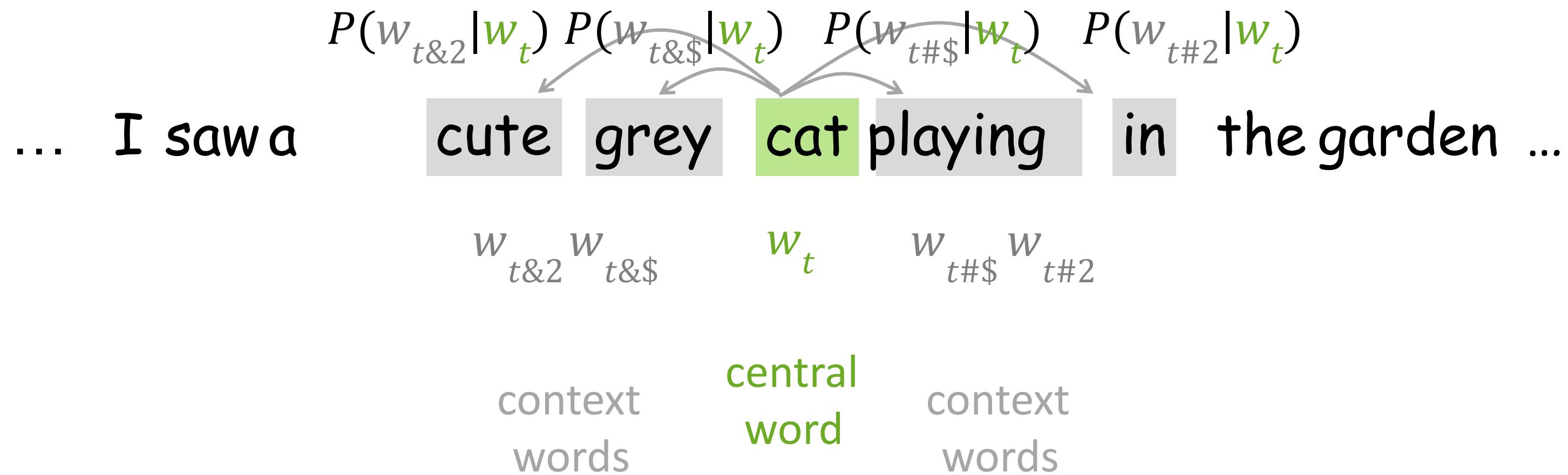
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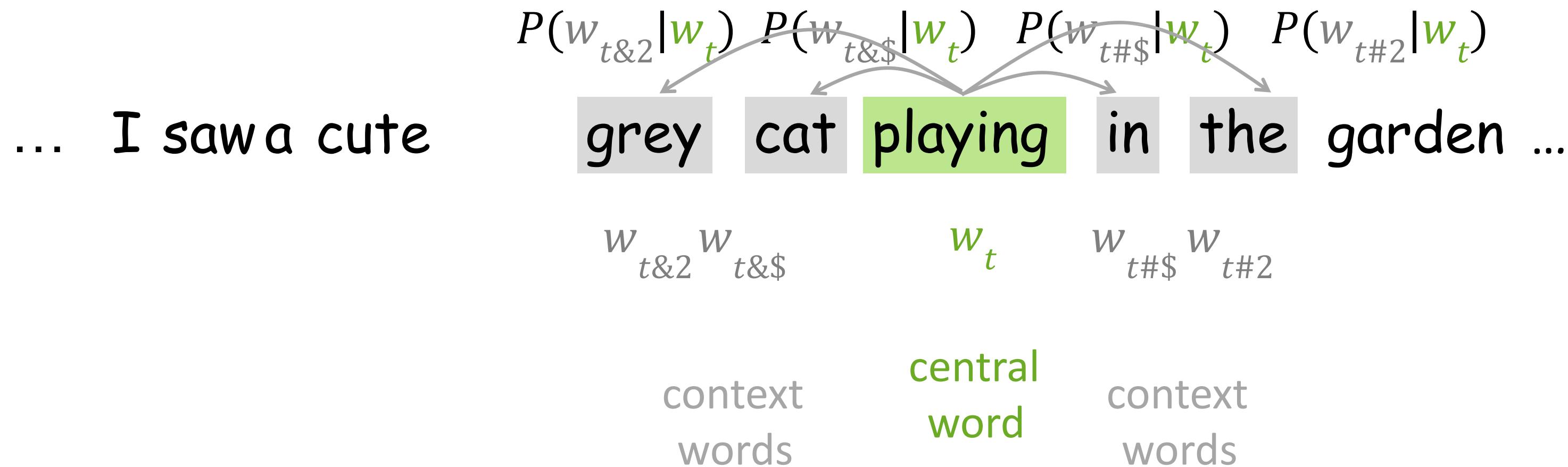
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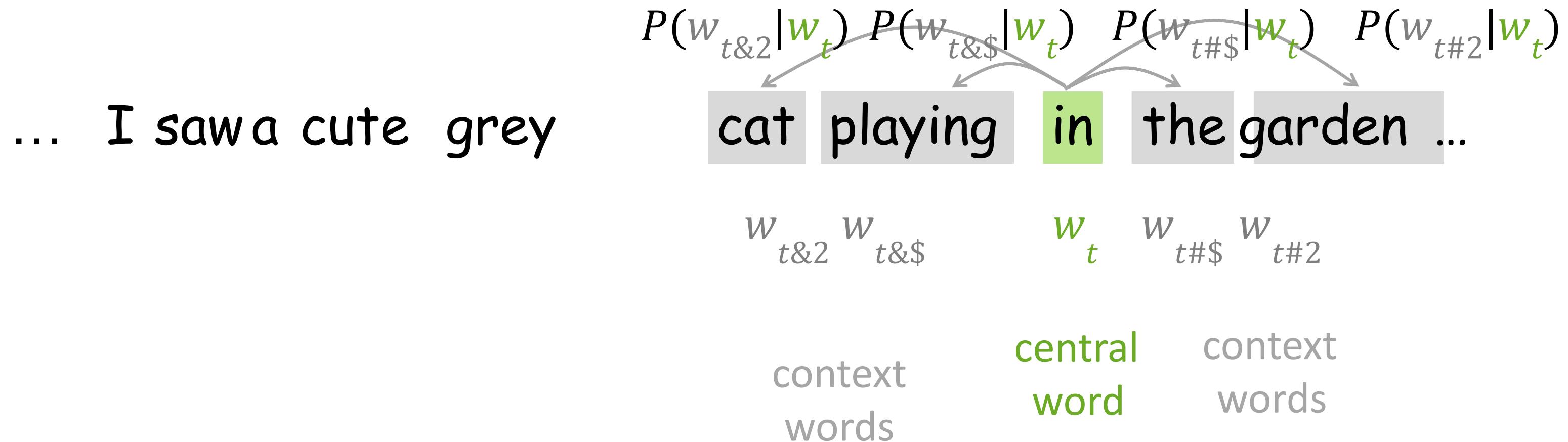
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$$\text{Likelihood} = \prod_{t=1}^T P(w_t | w_{t-1}, \theta)$$

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We want our model to think that the training data is “likely”

Objective Function: Negative Log-Likelihood

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$$\text{Likelihood} = L(\theta) = \prod_{t=1}^T \prod_{j=1}^{m+m} P(w_{t+j} | w_t, \theta)$$

" are all variables to optimize

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To do this, it uses negative (log-)likelihood as its loss function:

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agrees with our plan above



Objective Function: Negative Log-Likelihood

Word2Vec tries to find the parameters that maximize the data likelihood:

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$$P(w_{t+1} | w_t, \theta)$$

How to compute this?

compute probability of the context word given the central

How to compute $P(w_{t\%} | w_t)$?

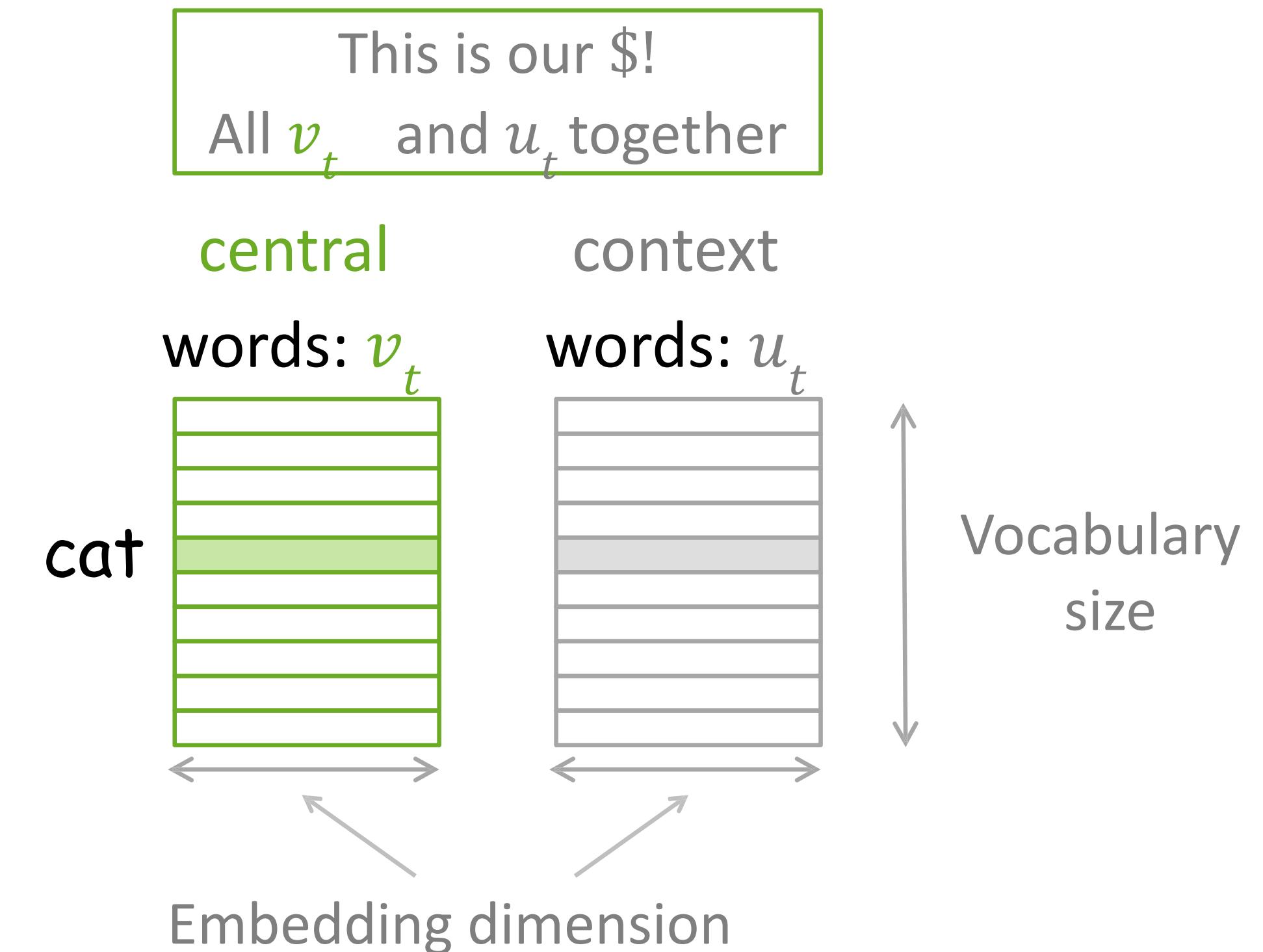
For each word w , we will have two vectors:

- v_w when it is a central word
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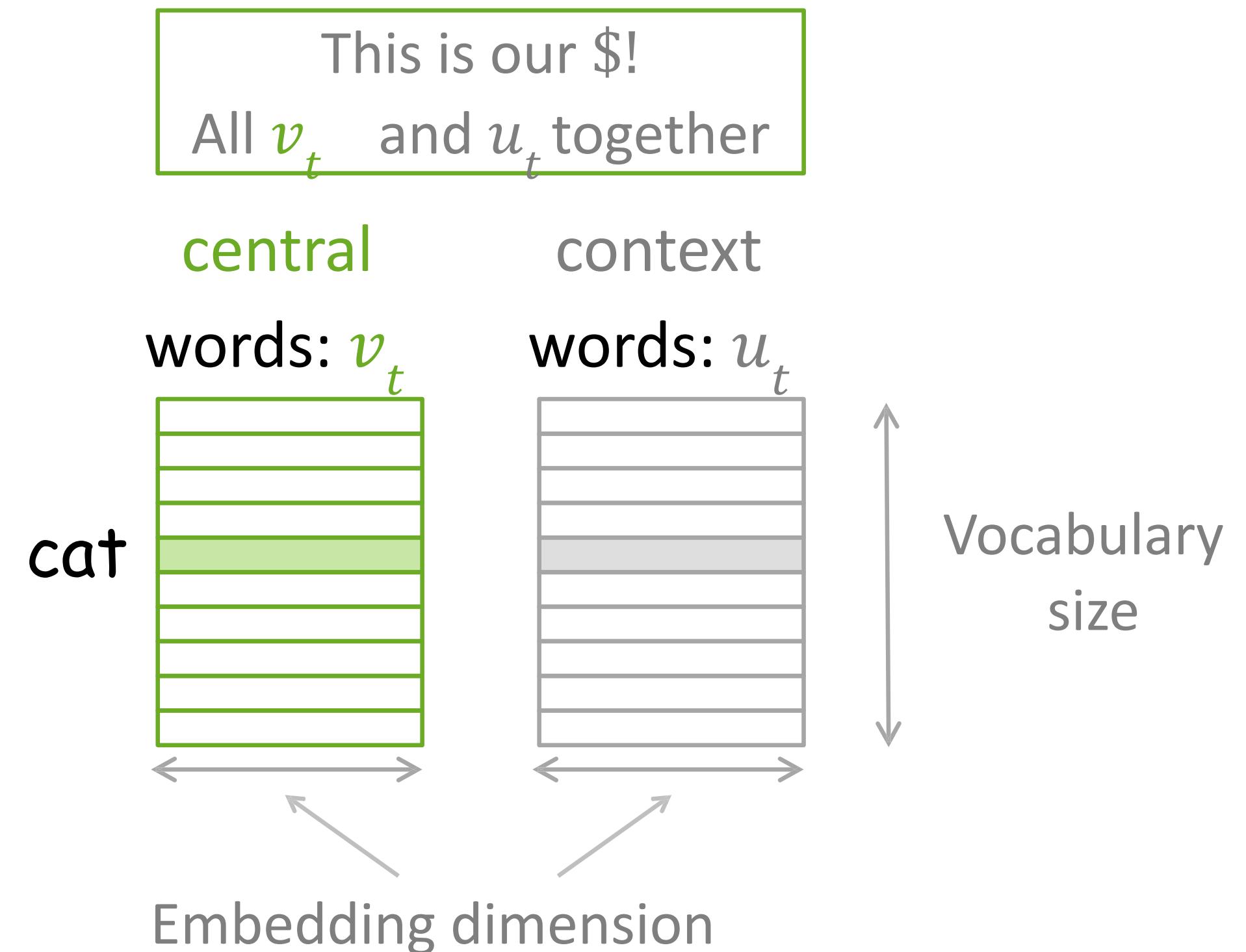


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Once the vectors are trained, usually we throw away context vectors and use only word vectors.



How to compute $P(w_{t56} | w_t, 9)$?

For the central word c and context word o (o - outside):

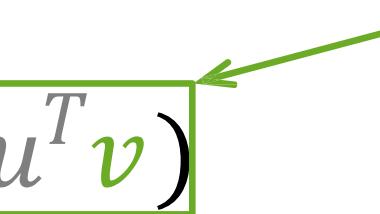
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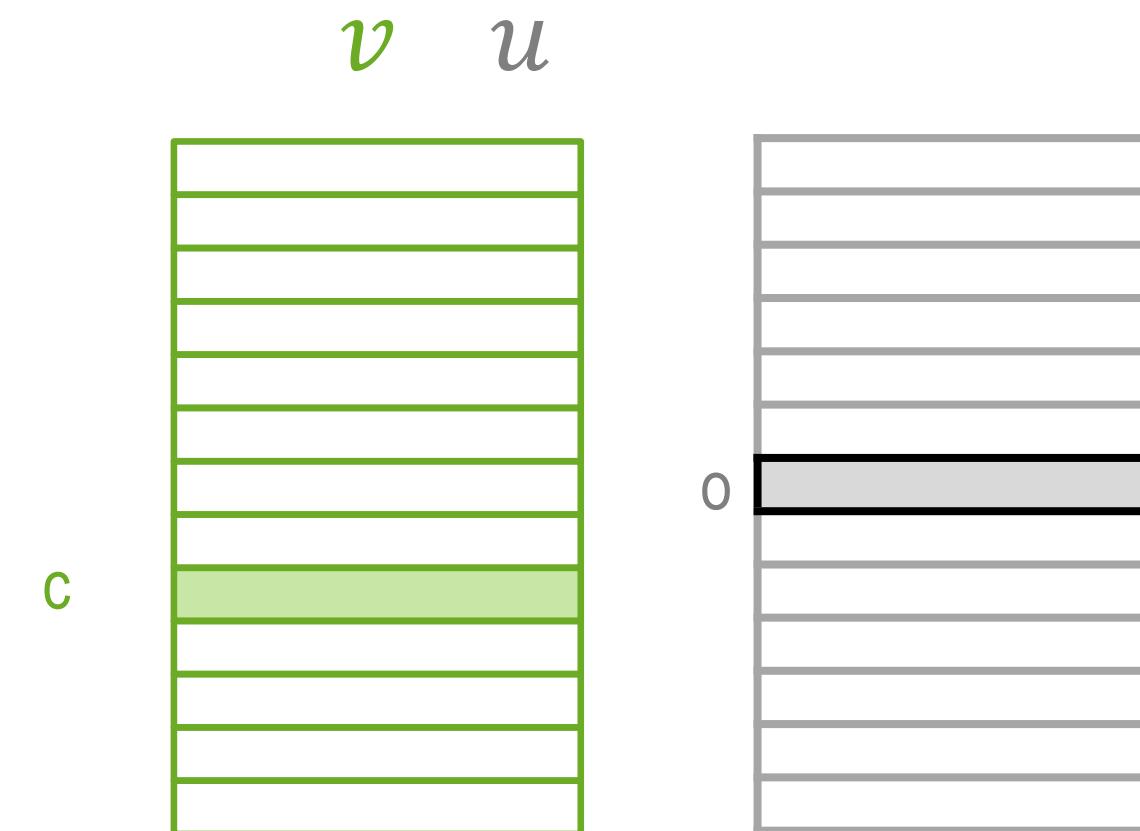
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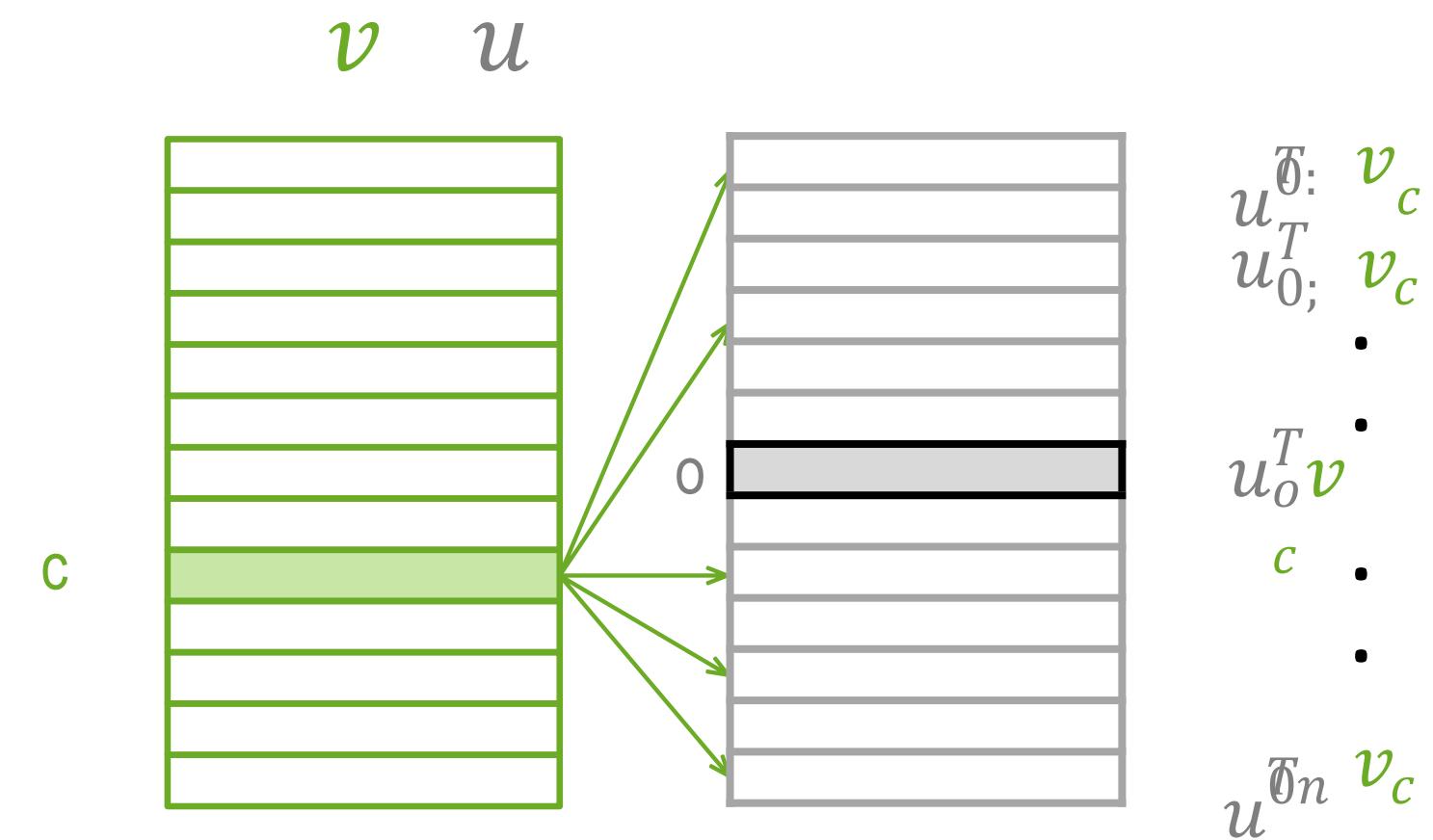
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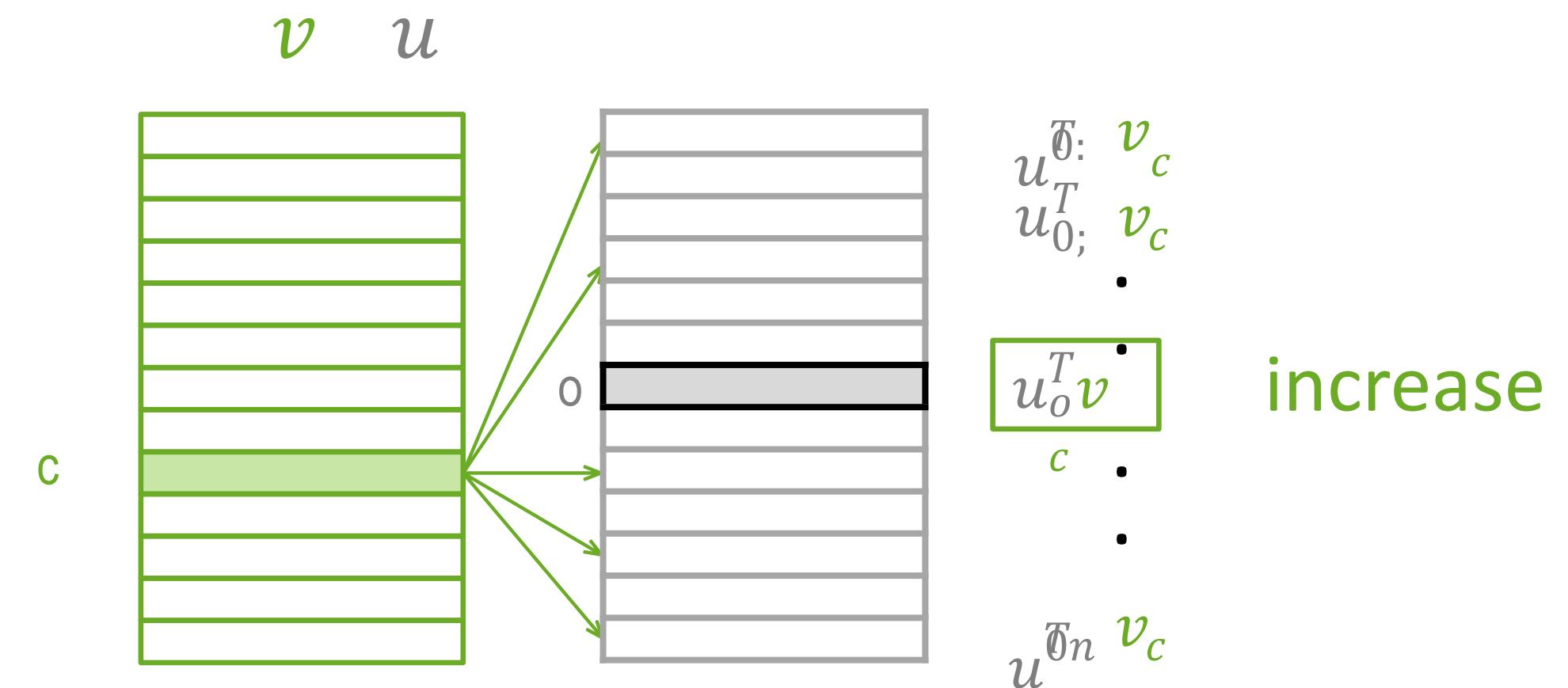
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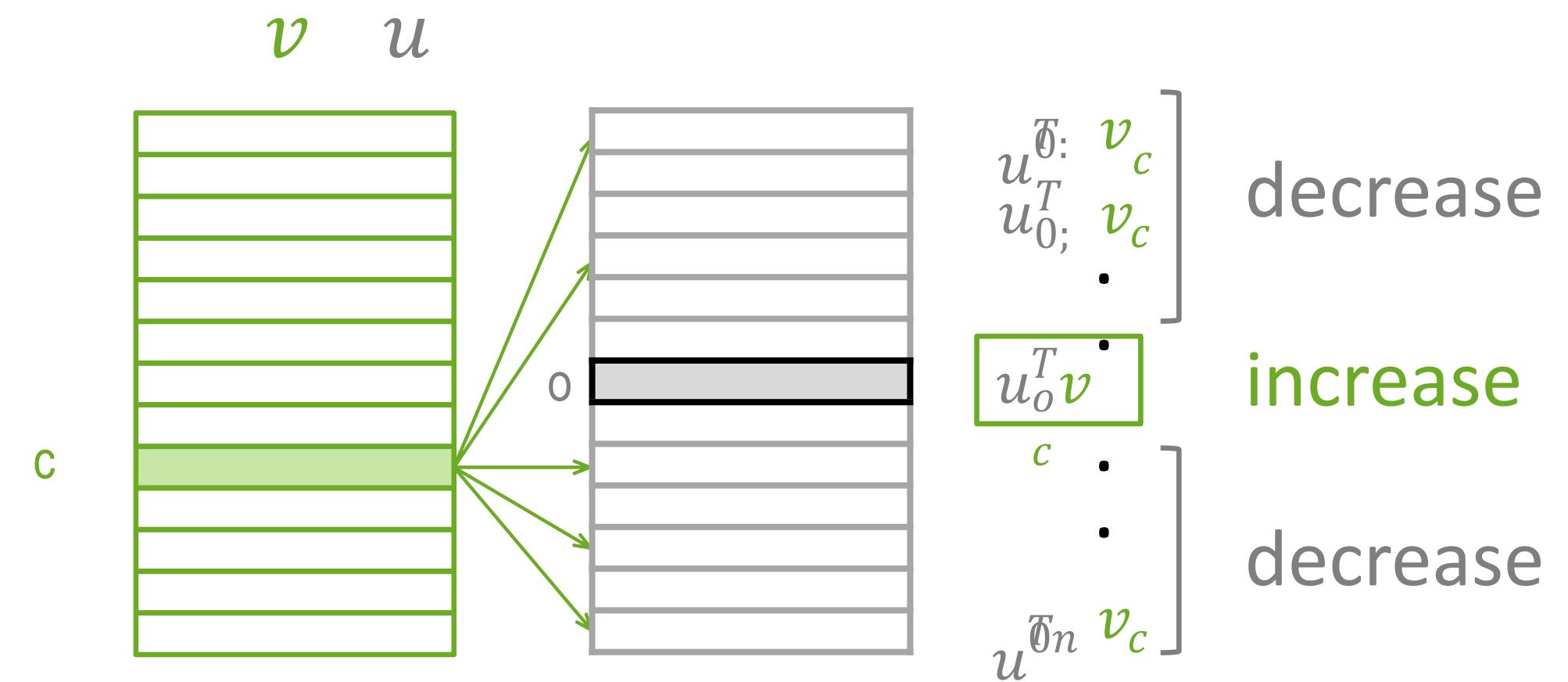
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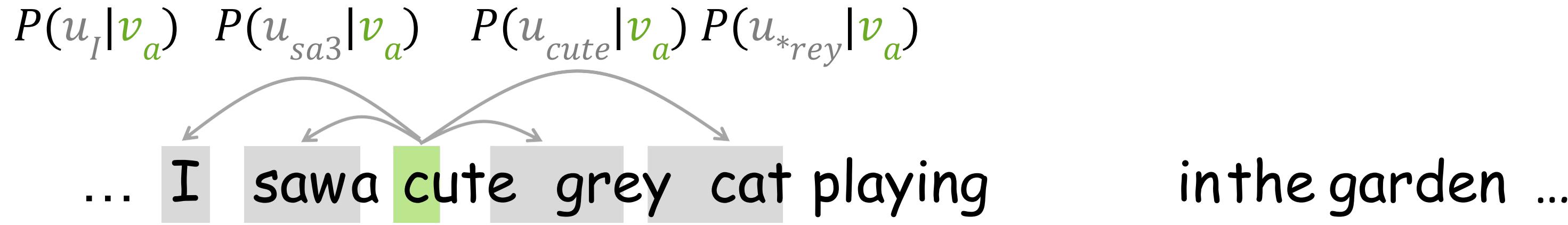
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- maps arbitrary values x_i to a probability distribution p_i
- “max” because amplifies probability of largest x_i
- “soft” because still assigns some probability to smaller x_i
- often used in Deep Learning!

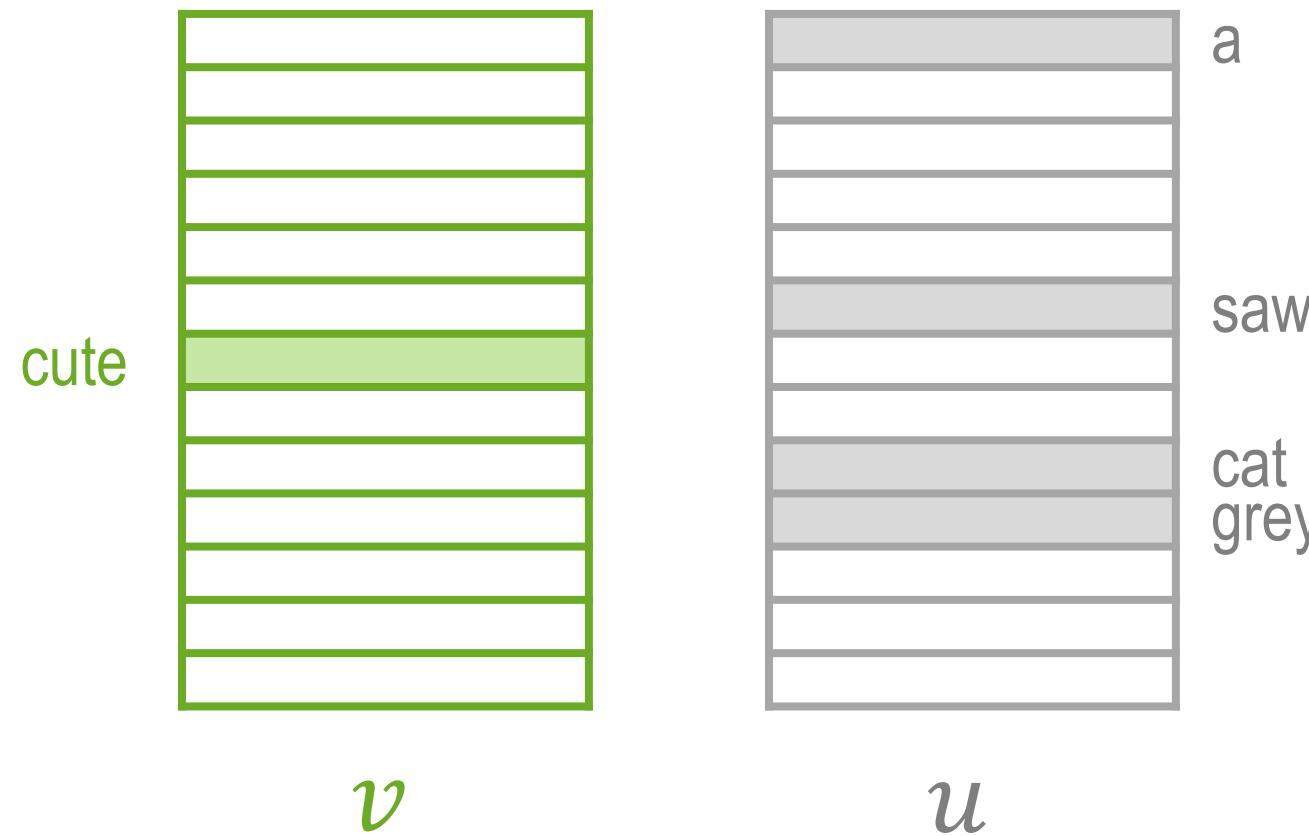
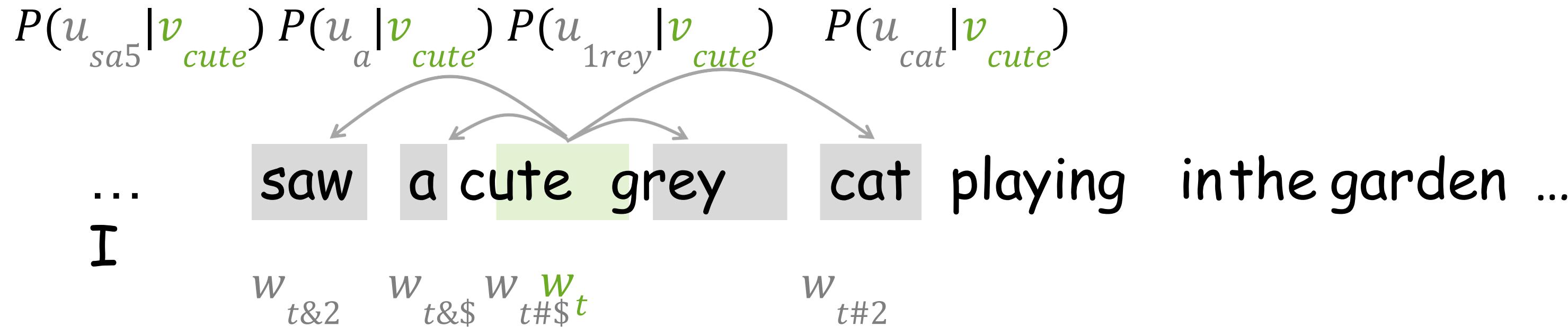
Two vectors for each word



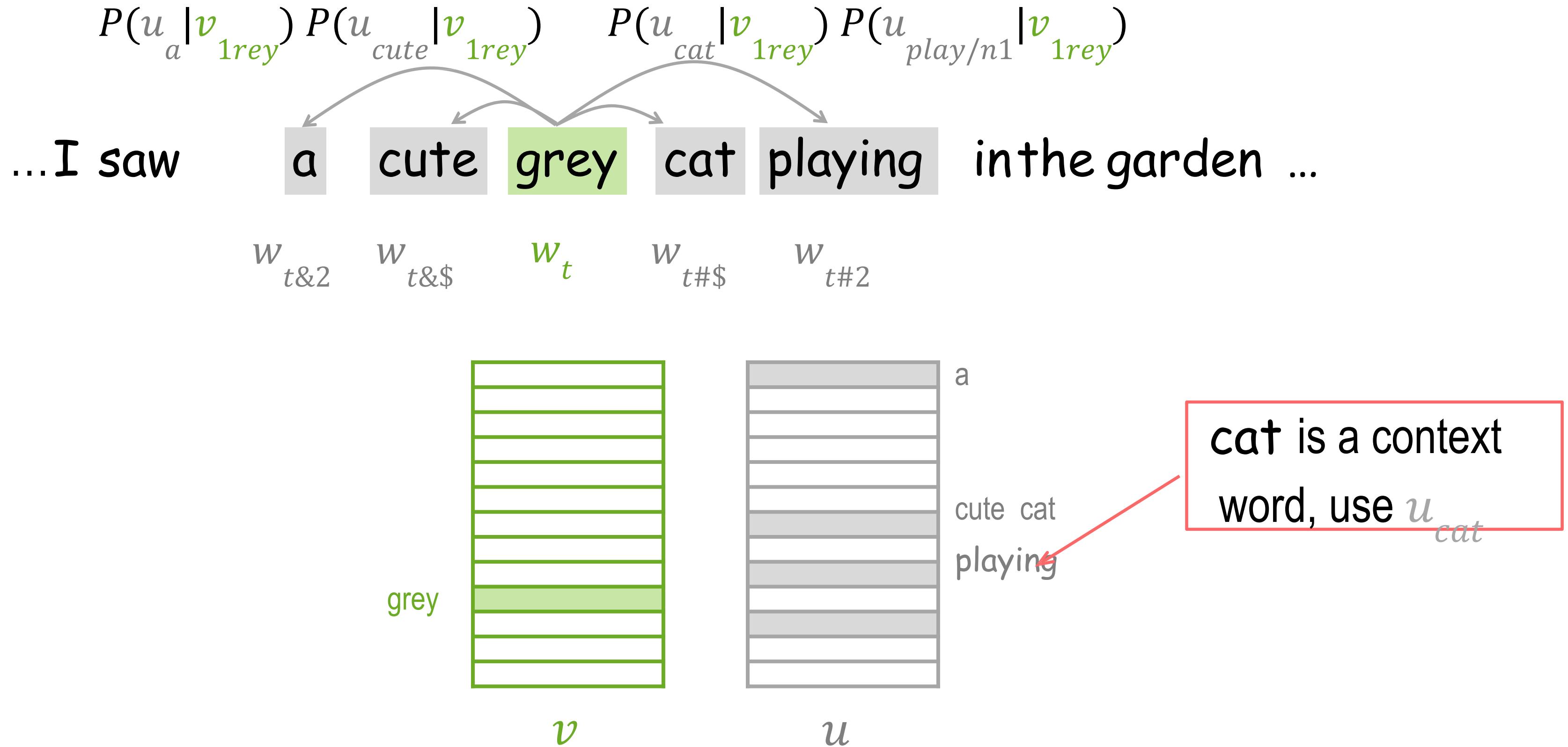
$w_{t\&2}$ $w_{t\&\$}$ w_t $w_{t\#\&}$ $w_{t\#\#}$



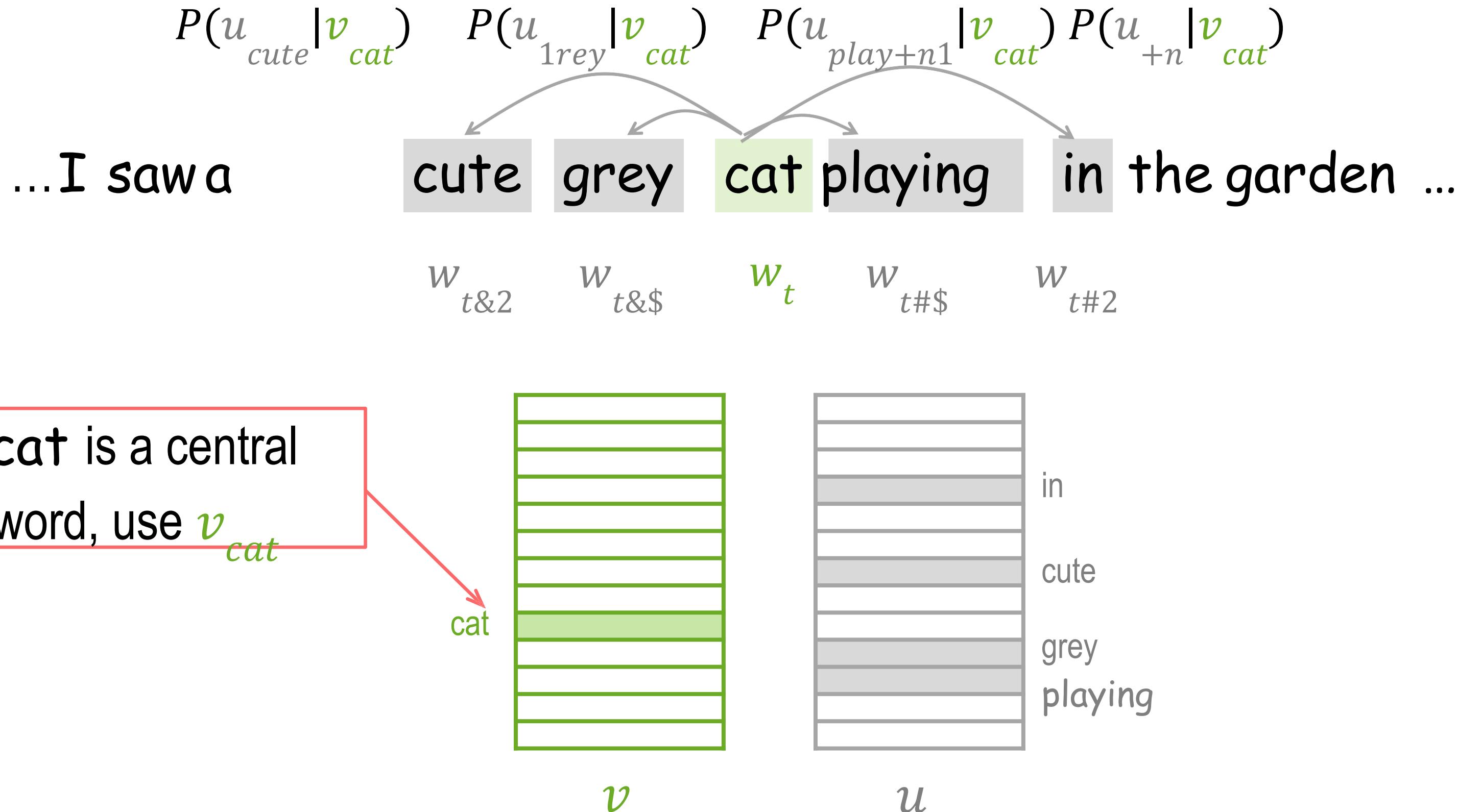
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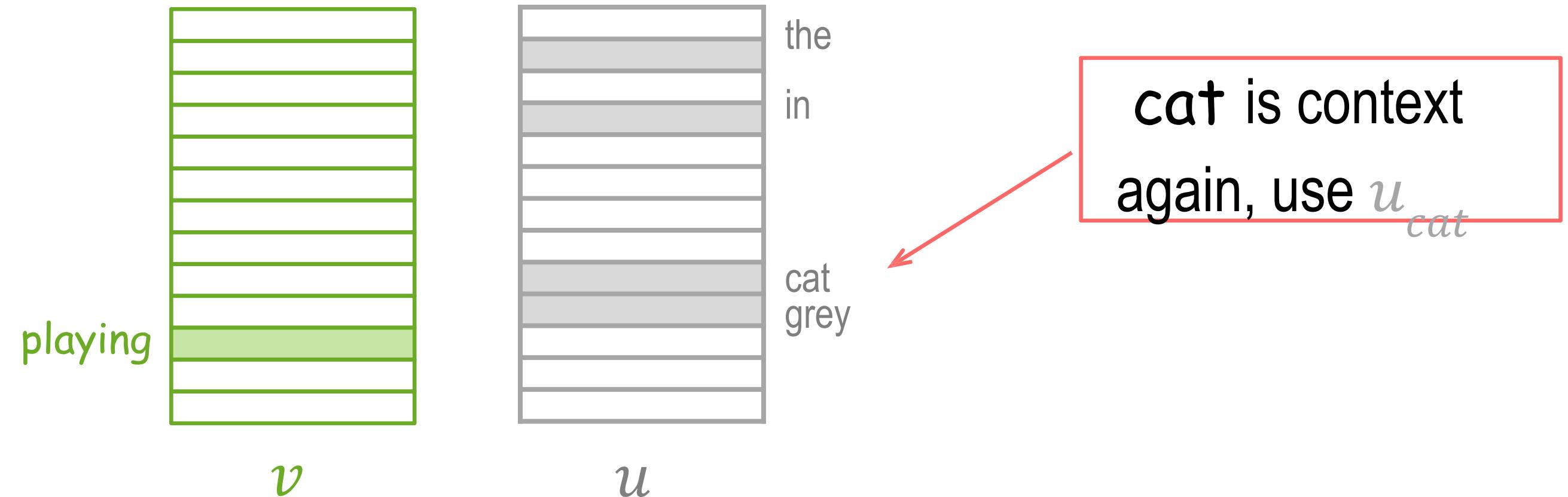


Two vectors for each word

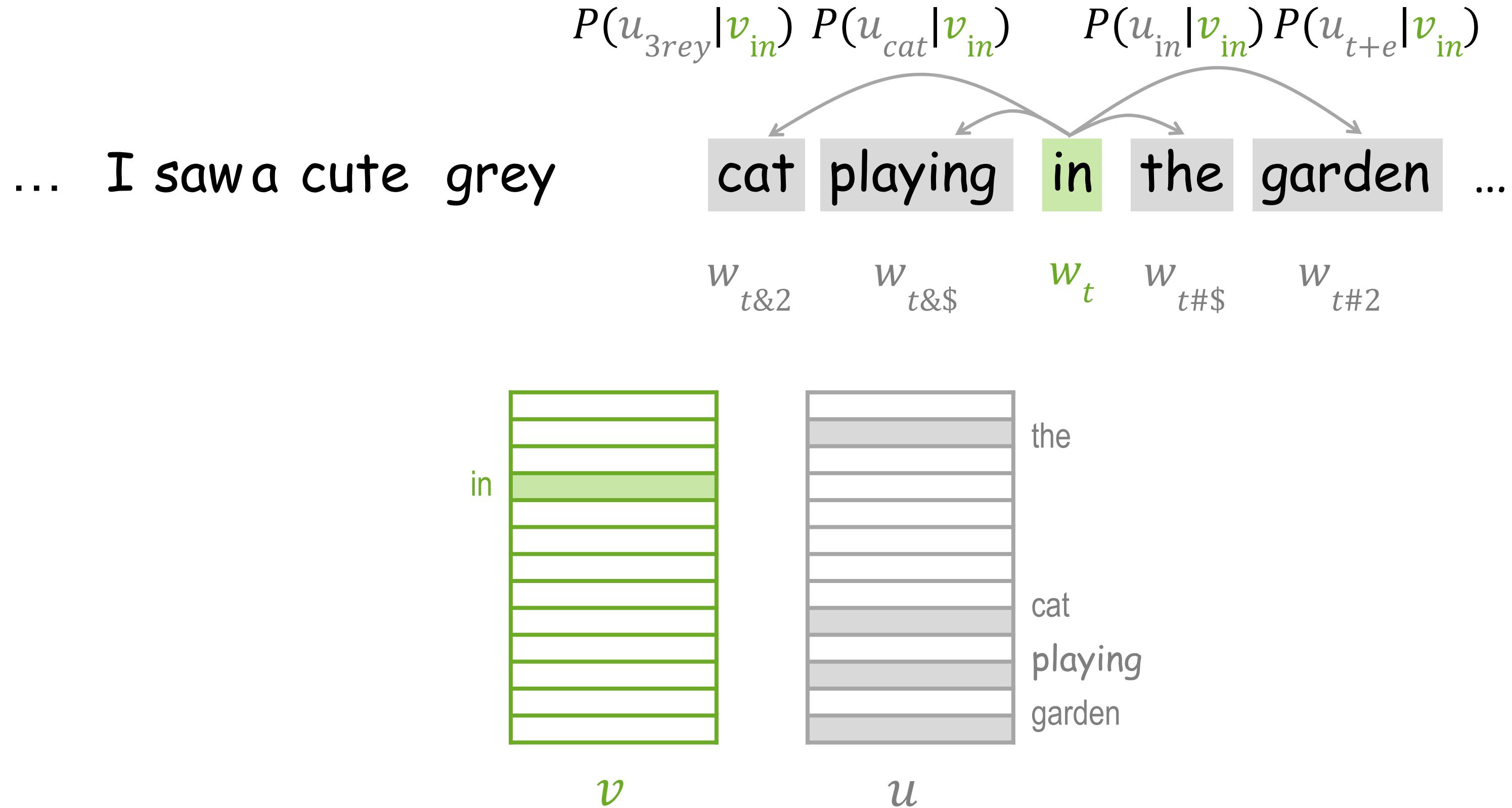
...I saw a cute grey cat **playing** in the garden ...

$P(u_{4rey} | v_{play2n4})$ $P(u_{cat} | v_{play2n4})$ $P(u_{2n} | v_{play2n4})$ $P(u_{t+e} | v_{play2n4})$

$$w_{t\&2} \quad w_{t\&\$} \quad w_t \quad w_{t\#\$} \quad w_{t\#2}$$



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One training step in detail

$$\text{Loss} = J(w) = -\frac{1}{T} \log L(w) = -\frac{1}{T} + \log P(w) \quad (t93 | w, ")$$

$t-1$ $m232m,$
 356

556

One training step in detail

$$\text{Loss} = J(w) = -\frac{1}{T} \log L(w) = -\frac{1}{T} \sum_{t=1}^T \log P(w_t)$$

Loss for word w_t in window t

$$L(w_t) = -\frac{1}{T} \sum_{t=1}^T \log P(w_t)$$

One training step in detail

$$\text{Loss} = J \left(\frac{1}{T} \sum_{t=1}^T \log L(w_t) \right) = -\frac{1}{T} \sum_{t=1}^T \log P(w_t)$$

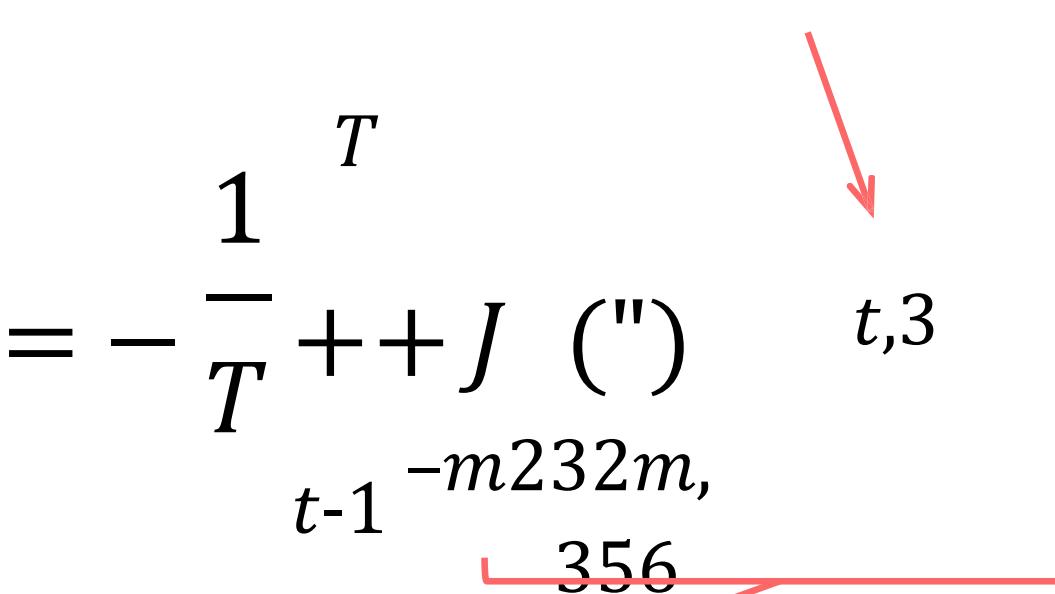
$$\text{Loss for word } w_t = -\frac{1}{T} \sum_{t=1}^T \log P(w_t)$$

pick one window

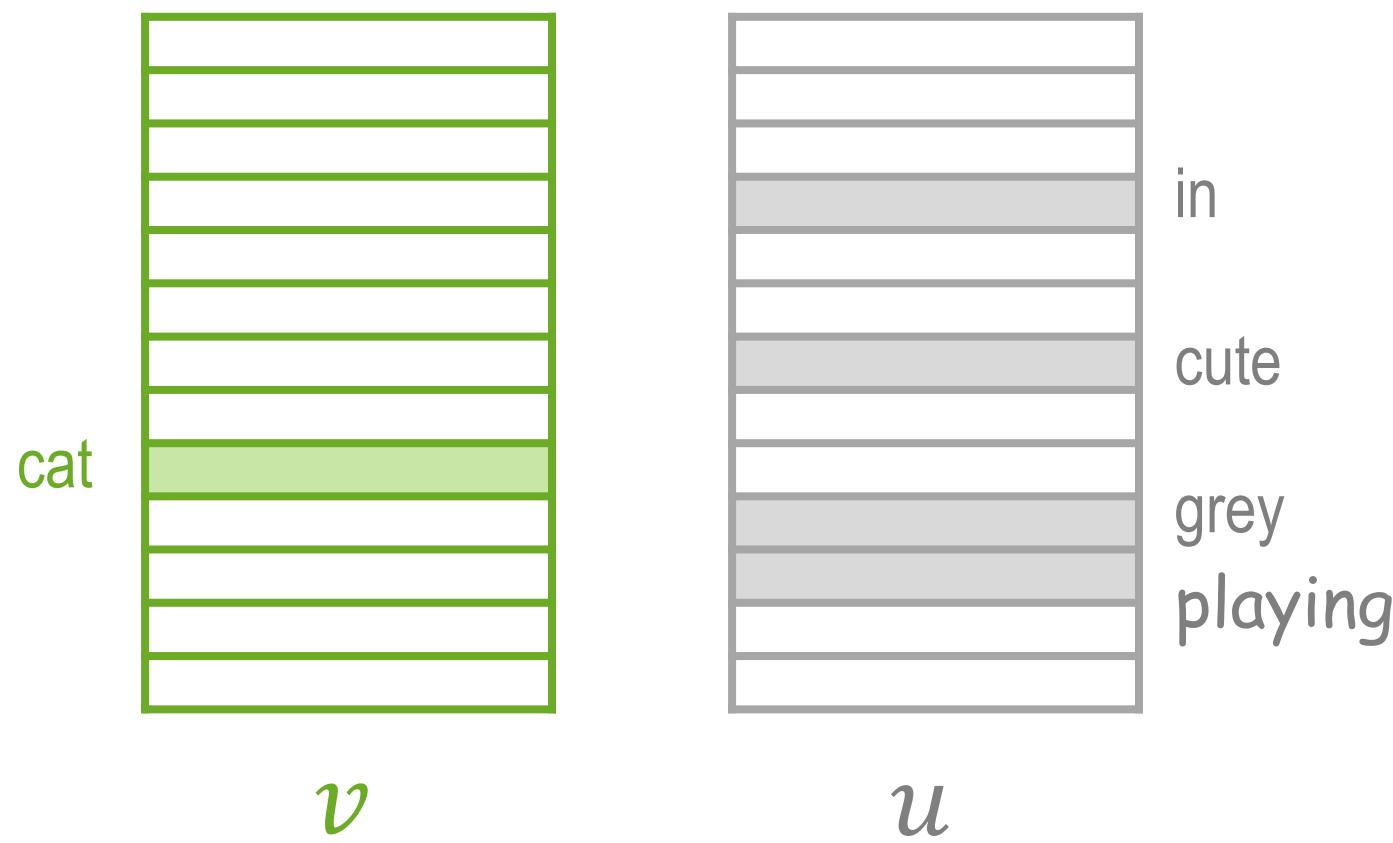
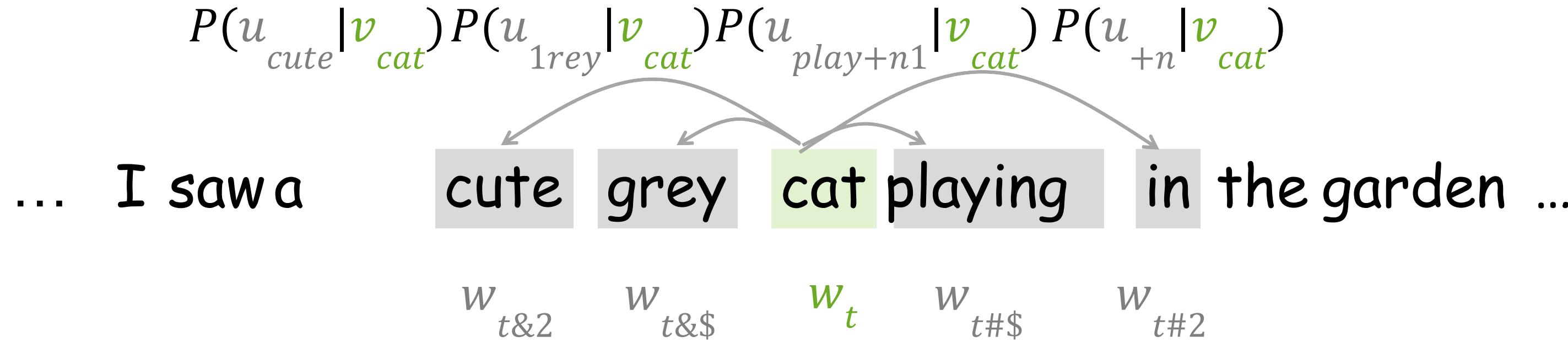
...I saw a

cute grey cat playing in the garden ...

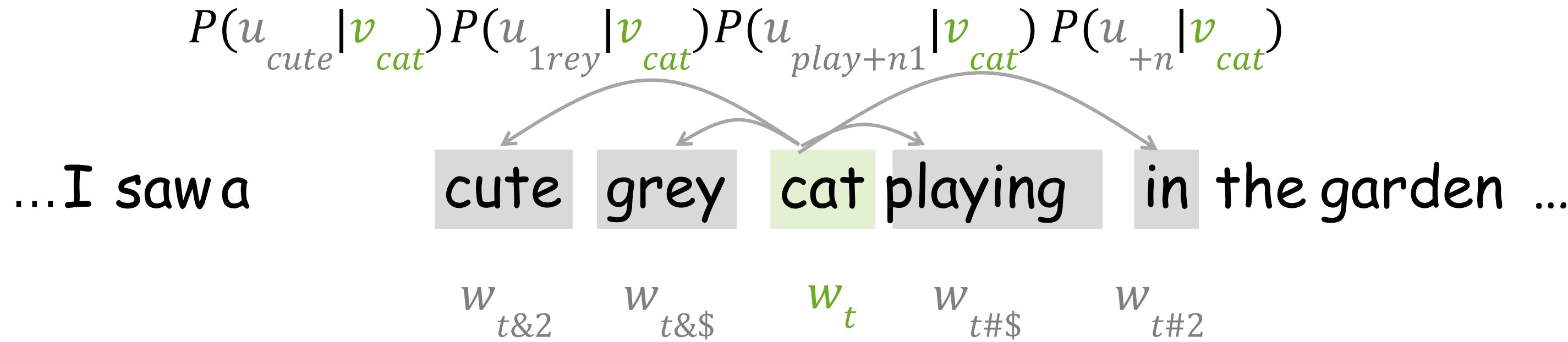
w_{t-1} w_t w_{t+1} w_{t+2} w_{t+3}



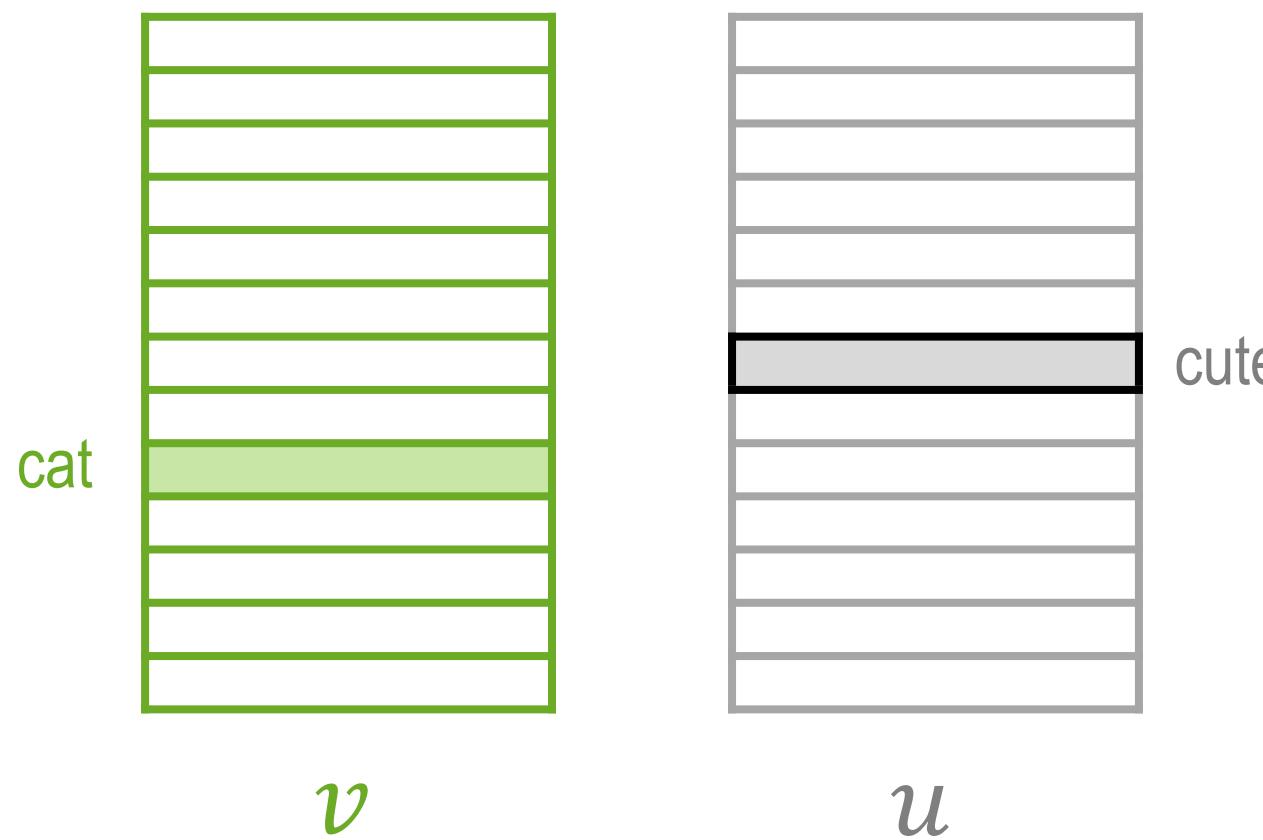
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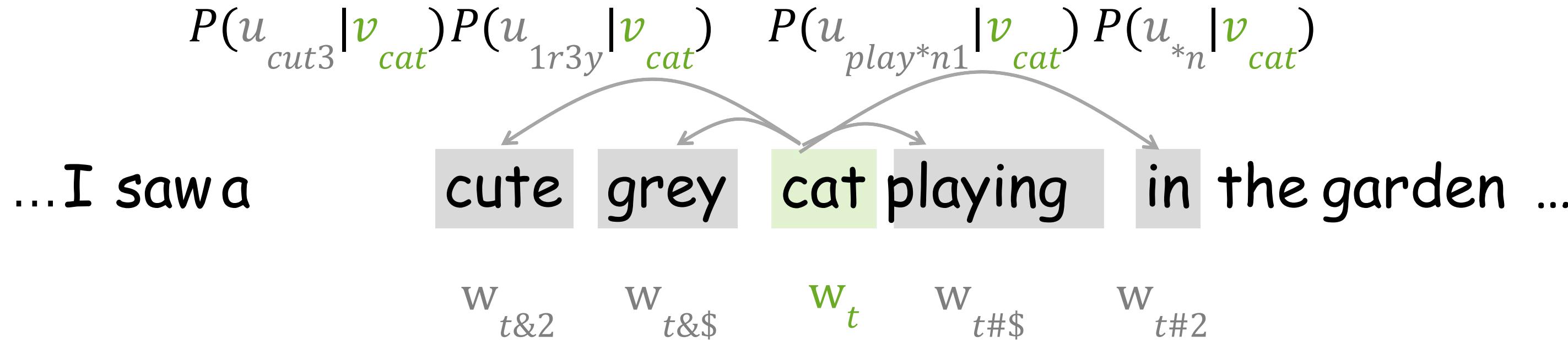
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Pick one of the context words

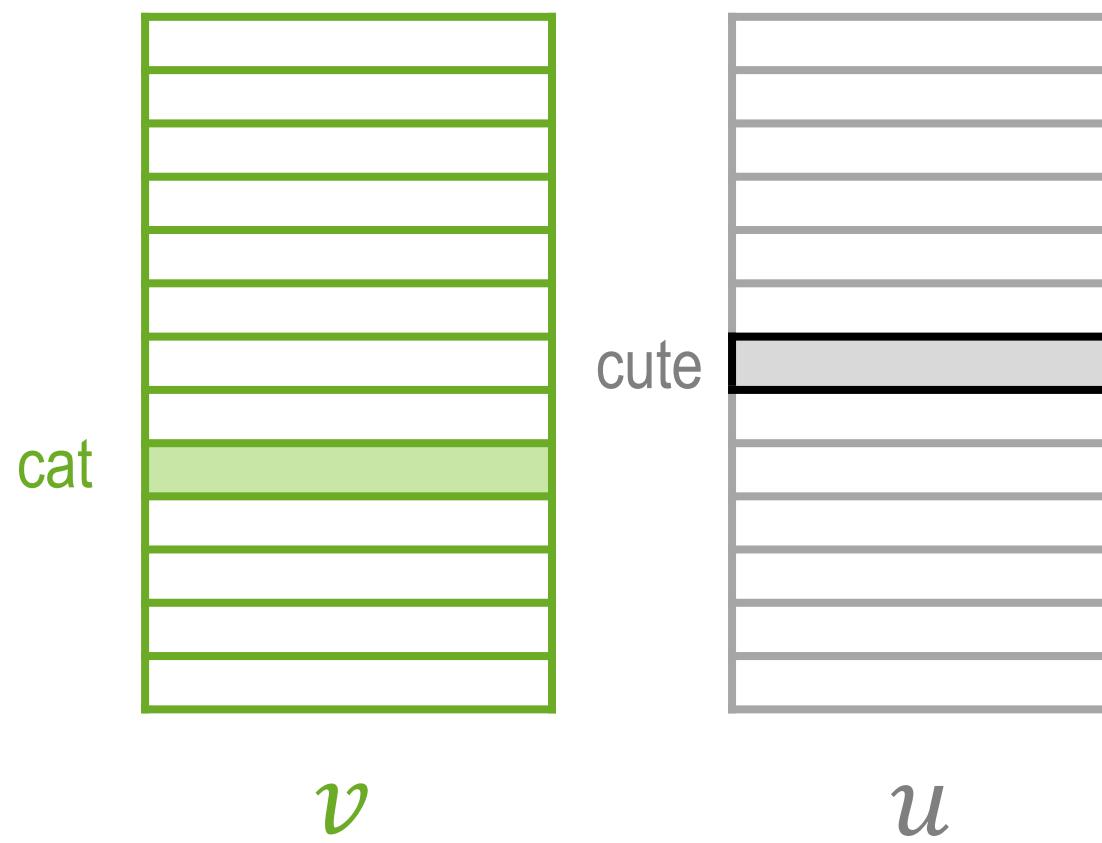


One training step in detail



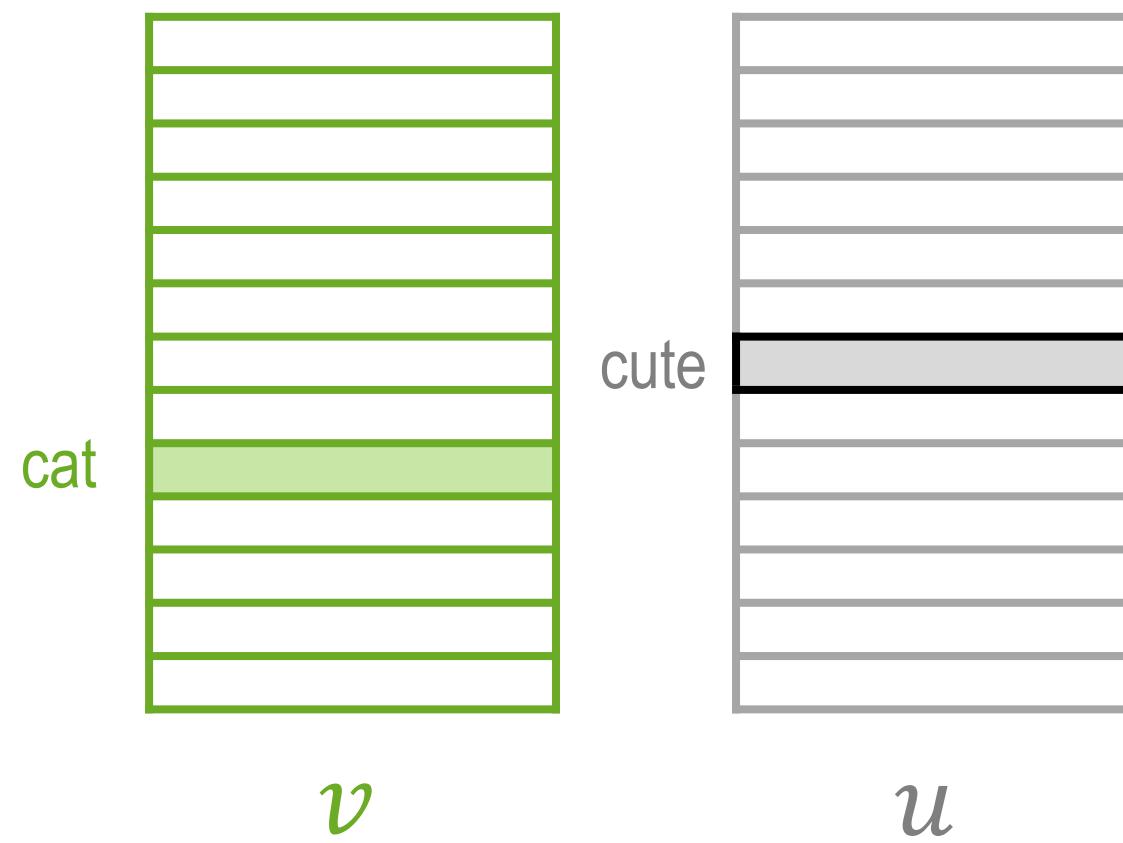
Look at the loss component for this step:

$$-\log P(\text{cut} \rightarrow \text{cat}) = -\log \frac{\exp(u_{cut3}^T v_{cat})}{\sum_{F \in V} \exp(u_F^T v_{cat})}$$



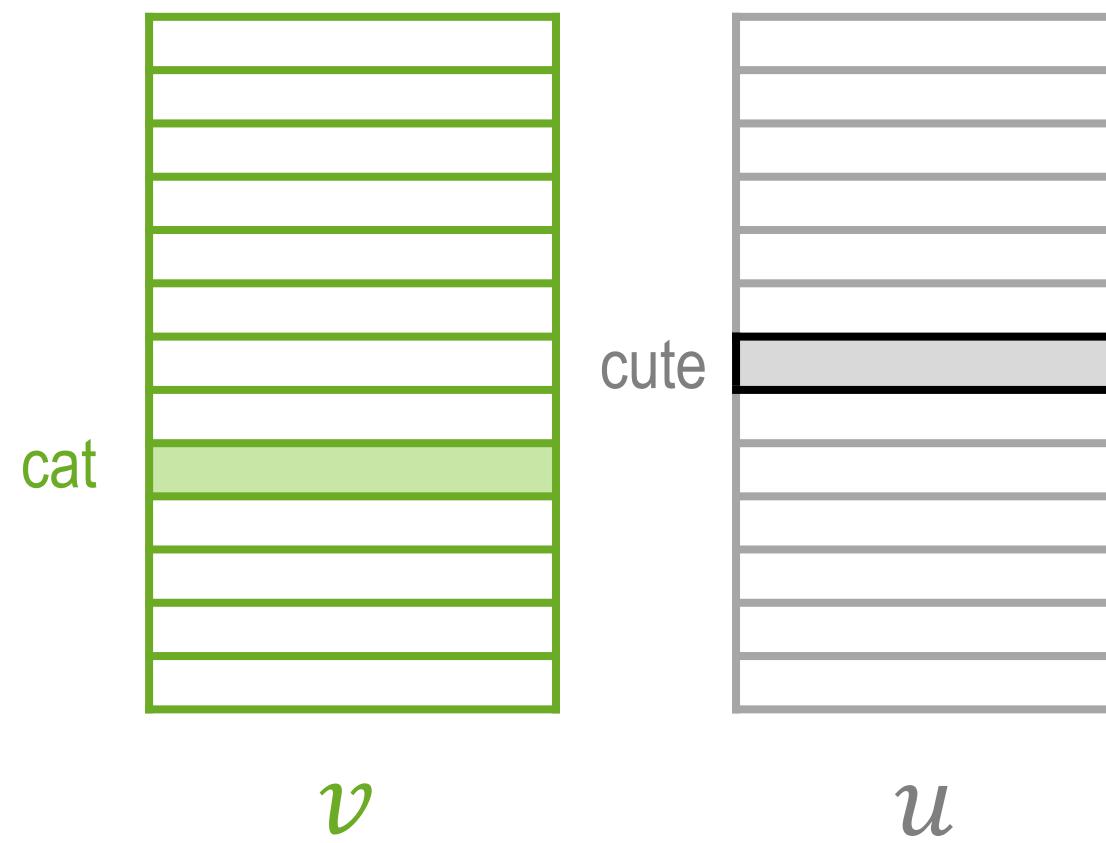
One training step in detail

$$-\log P(\text{cute} | \text{cat}) = -\log \frac{\exp(u_{\text{cute}}^T v_{\text{cat}})}{\sum_{7 \in V} \exp(u_7^T v_{\text{cat}})}$$



One training step in detail

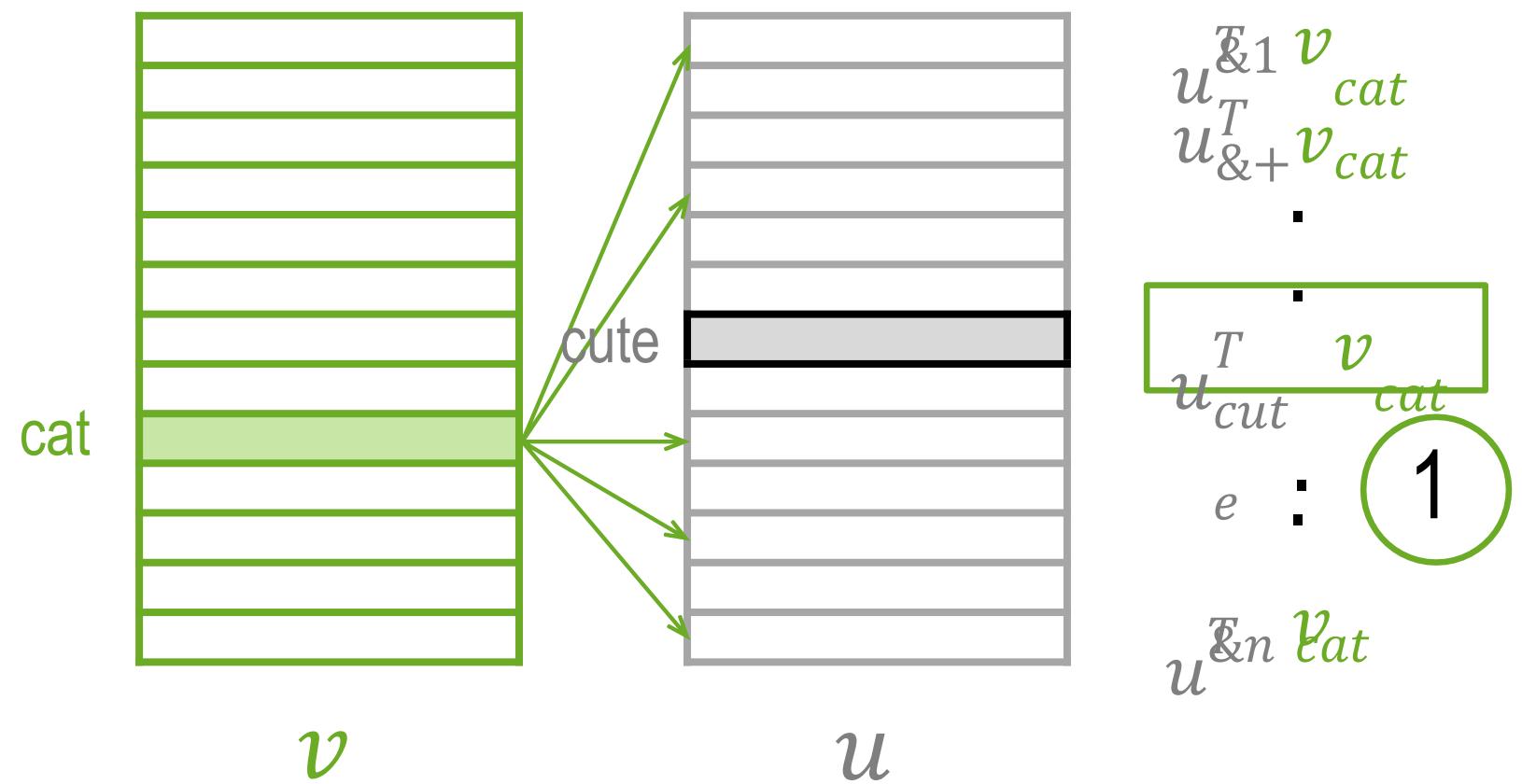
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$$-\log P(\text{cute} | \text{cat}) = -\frac{\exp(u_{\text{cute}}^T v_{\text{cat}})}{\sum_{e \in V} \exp(u_e^T v_{\text{cat}})} = -u_{\text{cute}}^T v_{\text{cat}} + \log \sum_{e \in V} \exp(u_e^T v_{\text{cat}})$$

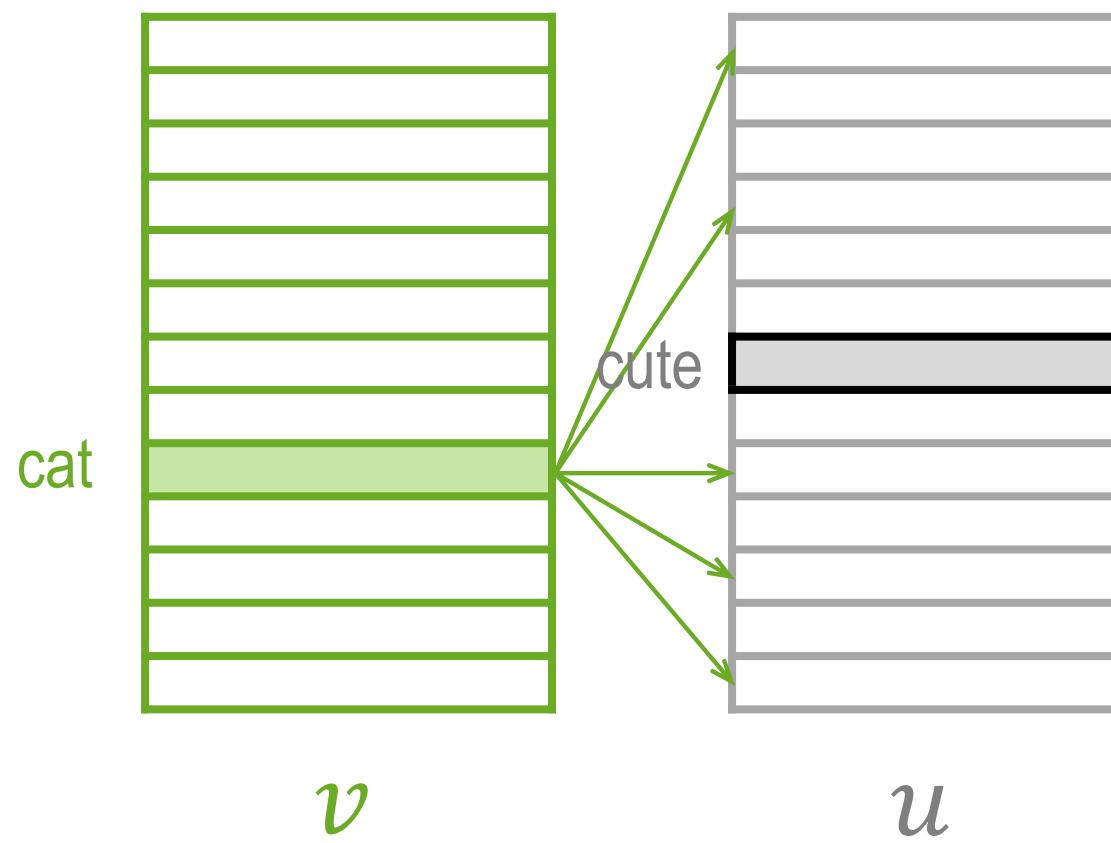
1. Take dot product of v_{cat} with all u



One training step in detail

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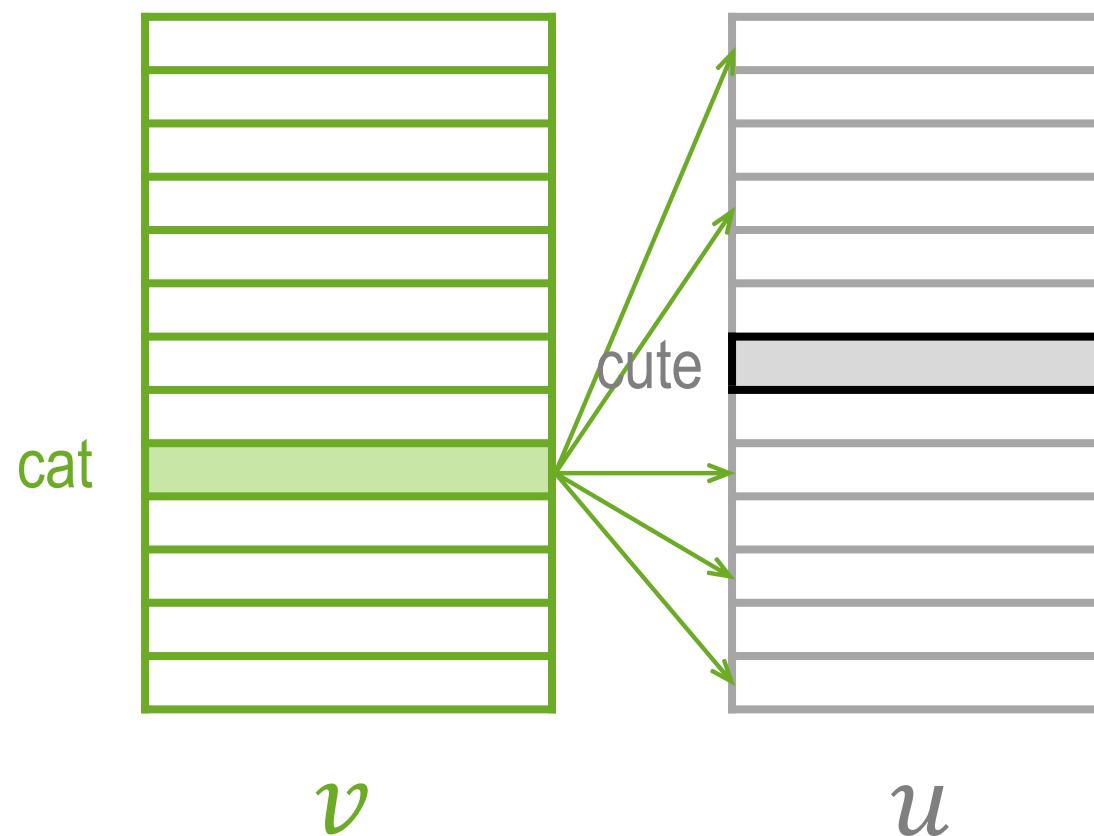
2. exp

$$\begin{aligned} u_{\&1}^T v_{\text{cat}} &\rightarrow \exp(u_{\&1}^T v_{\text{cat}}) \\ u_{\&+}^T v_{\text{cat}} &\rightarrow \exp(u_{\&+}^T v_{\text{cat}}) \\ &\vdots \\ u_{\text{cut}}^T v_{\text{cat}} &\rightarrow \boxed{\exp(u_{\text{cut}}^T v_{\text{cat}})} \\ e : 1 & \\ u_{\&n}^T v_{\text{cat}} &\rightarrow \exp(u_{\&n}^T v_{\text{cat}}) \end{aligned}$$

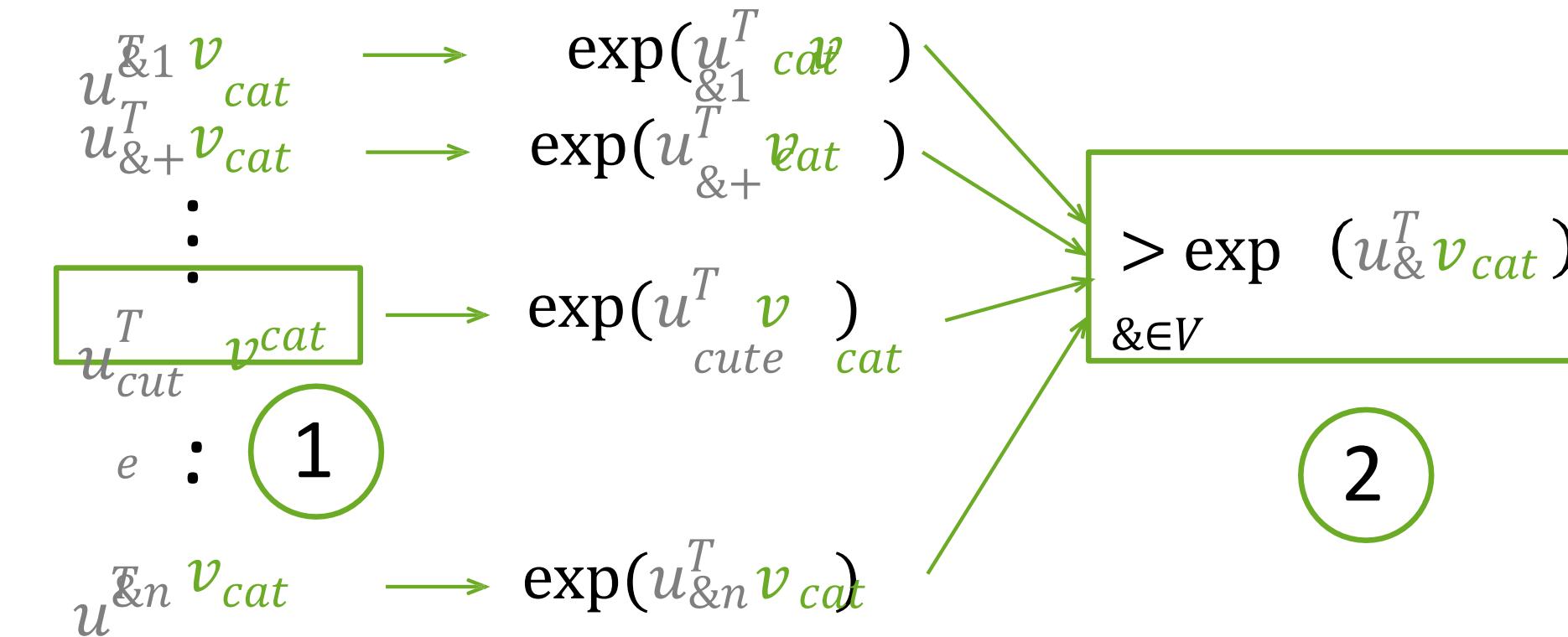
One training step in detail

$$-\log P(\text{cute} | \text{cat}) = -\frac{\exp(u_{\text{cute}}^T v_{\text{cat}})}{\sum_{e \in V} \exp(u_e^T v_{\text{cat}})} = -u_{\text{cute}}^T v_{\text{cat}} + \log \left(\sum_{e \in V} \exp(u_e^T v_{\text{cat}}) \right)$$

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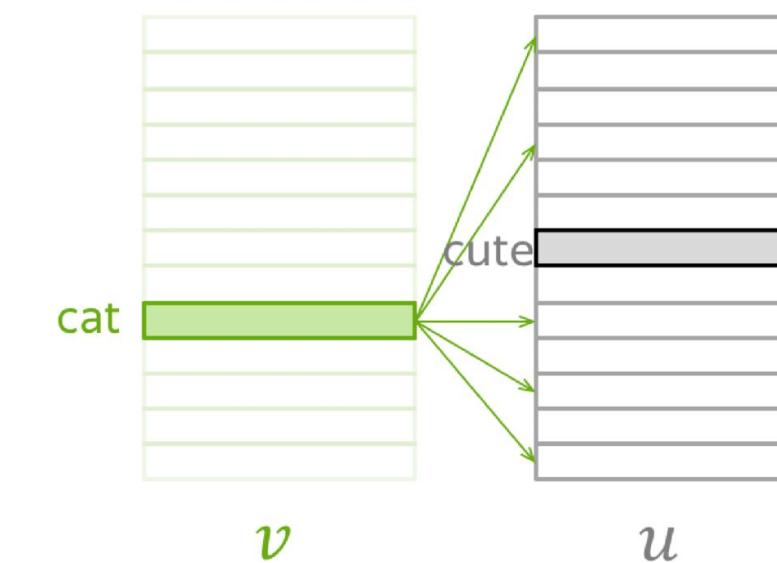
3. sum all

One training step in detail

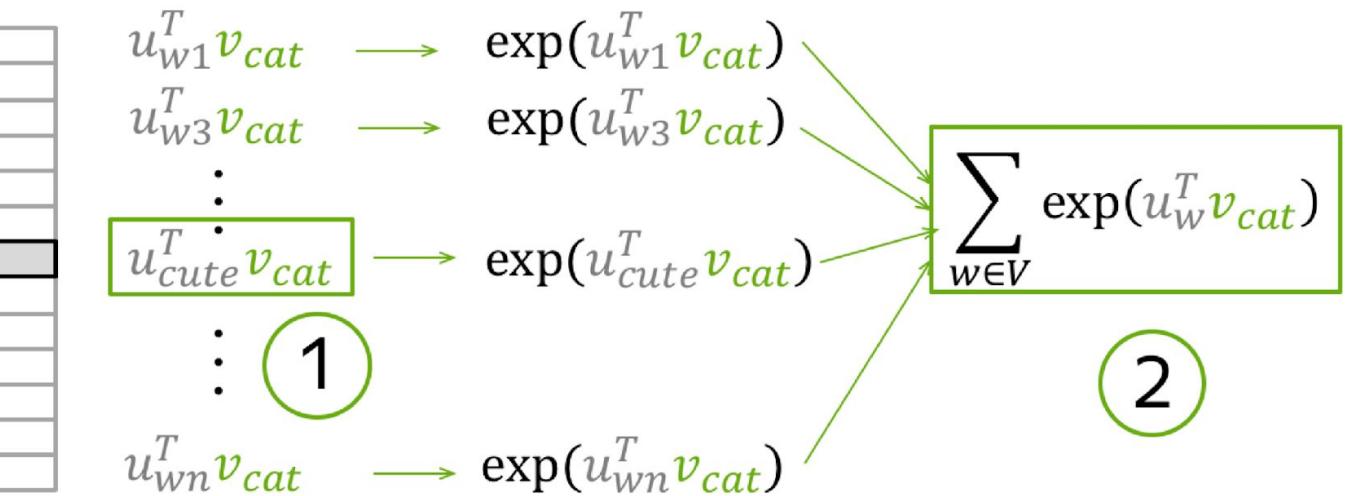
$$-\log P(\text{cute} | \text{cat})$$

$$= -u^T v_{\text{cat}} + \log \sum_{w \in V} \exp(u_w^T v_{\text{cat}})$$

1. Take dot product of v_{cat} with all u



2. exp



3. sum all

4. get loss (for this one step)

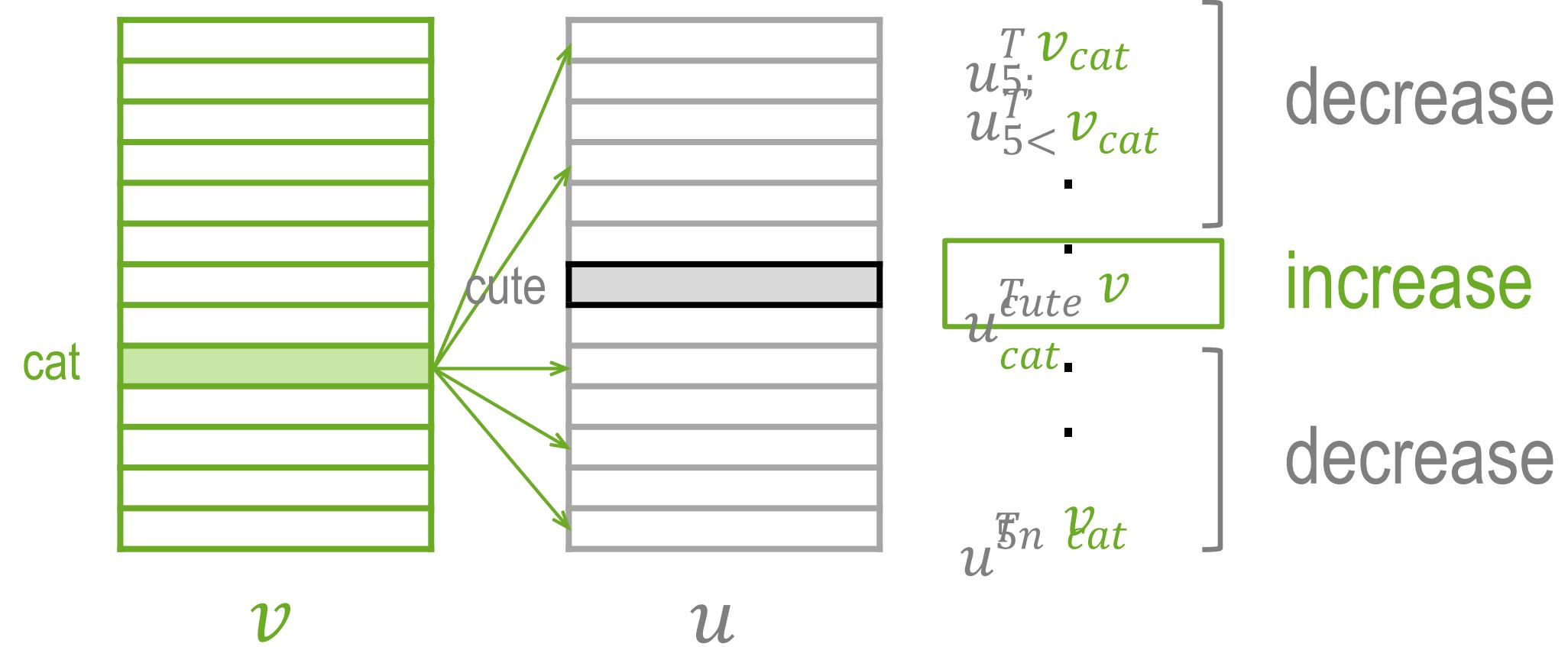
$$J_{t,\$}(\) = -\underbrace{u_{\text{cute}}^T v_{\text{cat}}}_{\%} + \log \underbrace{\sum_{w \in V} \exp(u_w^T v_{\text{cat}})}_{(2)}$$

5. evaluate the gradient, make an update

$$\begin{aligned} v_{\text{cat}} &:= -\alpha \frac{\langle J_{t,\$} \rangle}{\langle v_{\text{cat}} \rangle} \\ v_{\text{cat}} &:= \frac{\langle J_{t,\$} \rangle}{\langle v_{\text{cat}} \rangle} \quad \forall w \in V \\ u_4 &:= u_4 - \alpha \frac{\langle J_{t,\$} \rangle}{\langle u_4 \rangle} \end{aligned}$$

Recap: One Update Intuition

$$-\log P(\text{cute} | \text{cat}) = -\mathbf{u}_{\text{cute}}^T \mathbf{v}_{\text{cat}} + \log \sum_{\mathbf{v} \in V} \exp(\mathbf{u}^T \mathbf{v})$$



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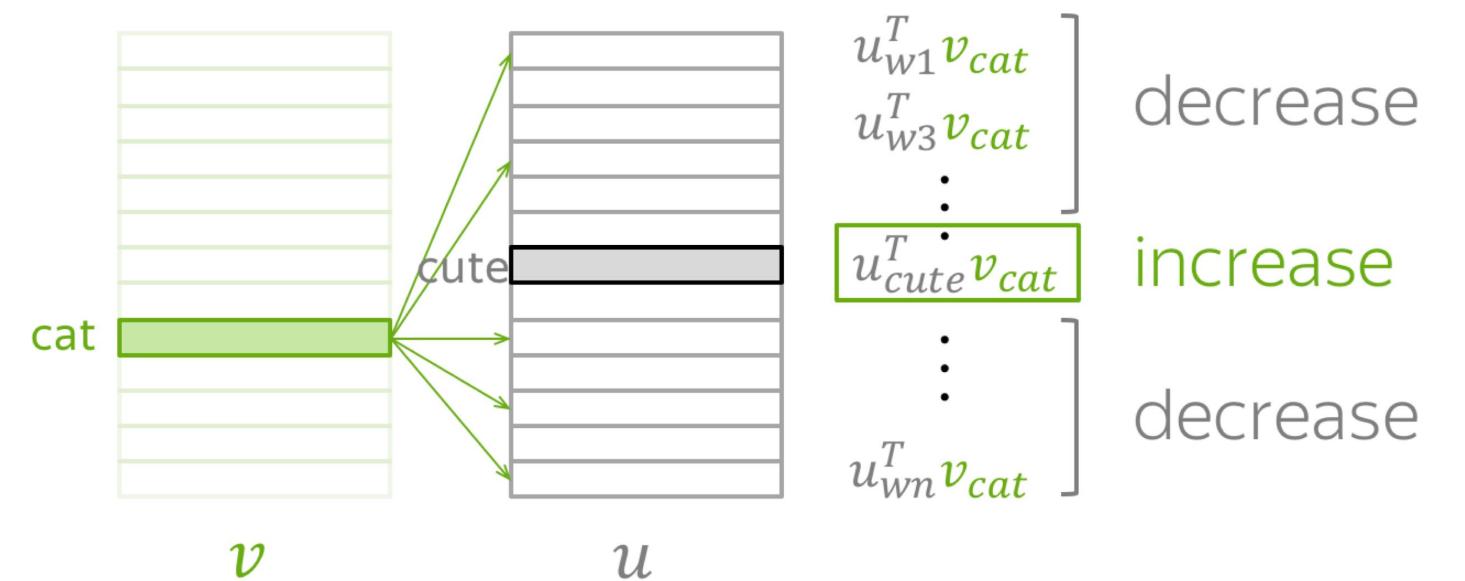
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What happens at each training step

Dot product of v_{cat} :

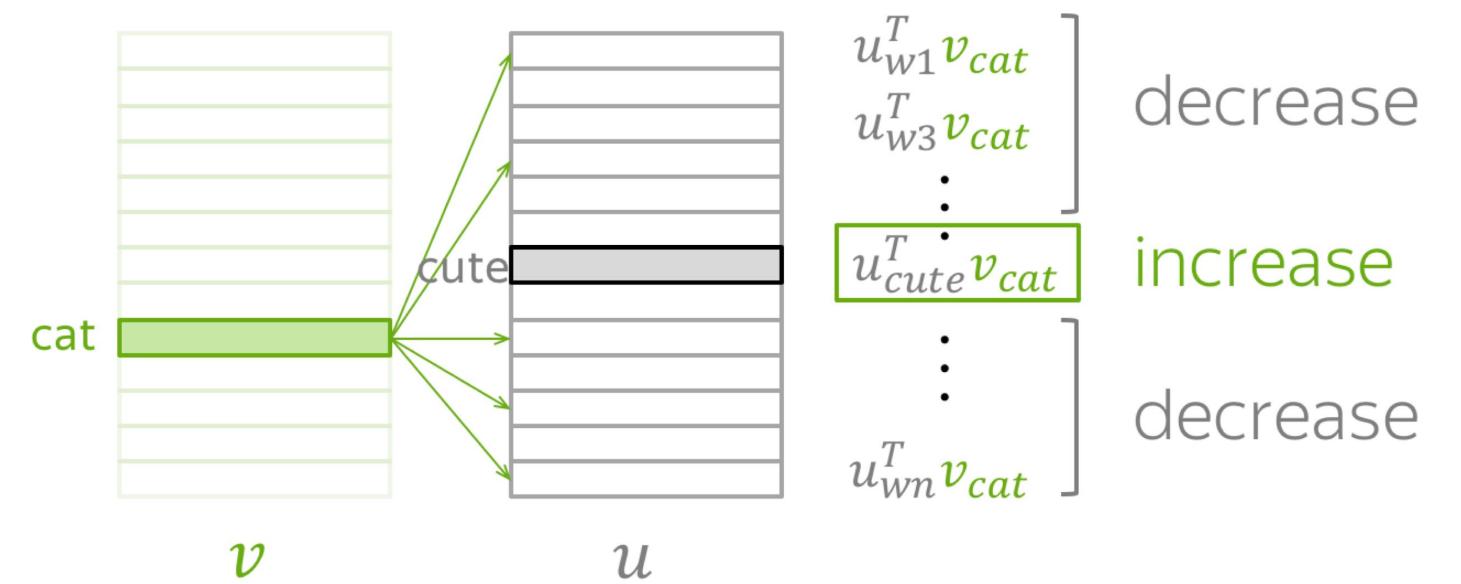
- with u_{cute} - increase,
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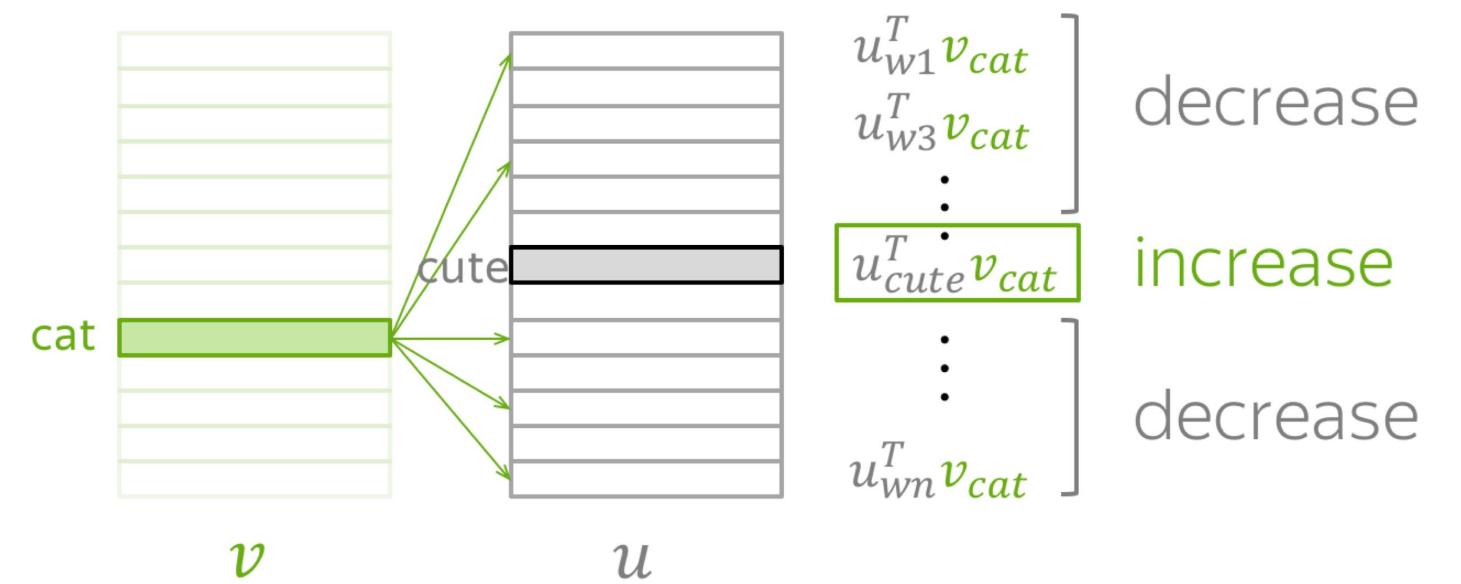


Parameters to be updated:

What happens at each training step

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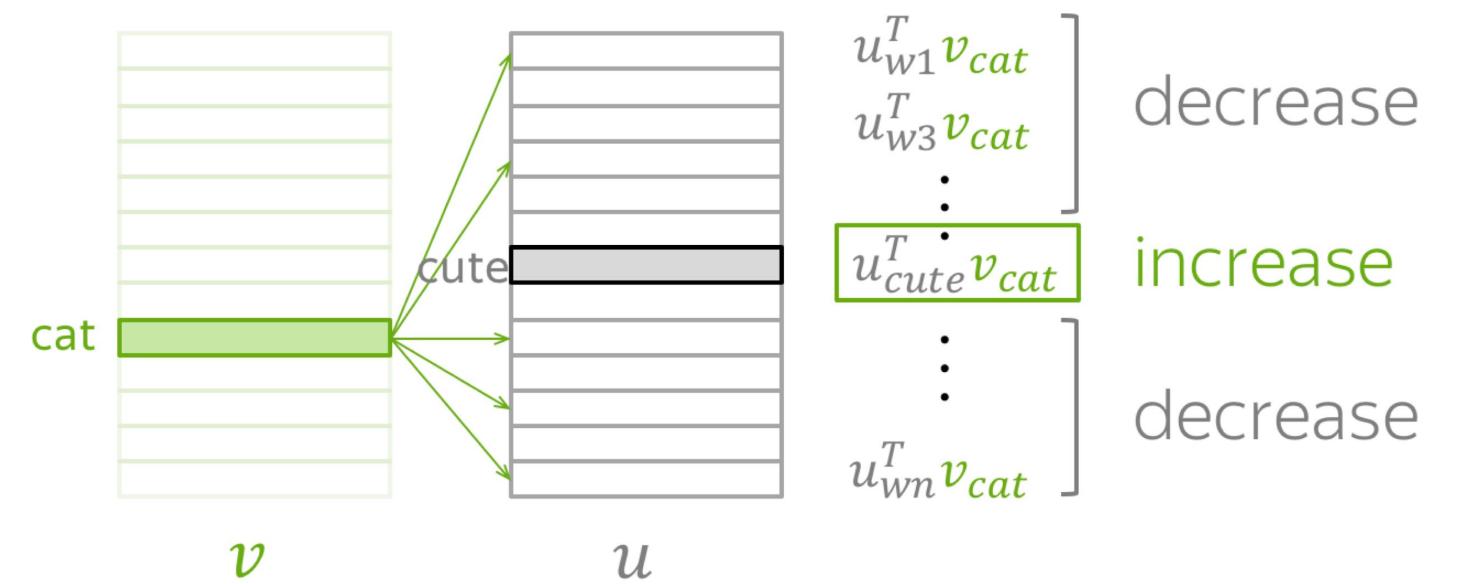
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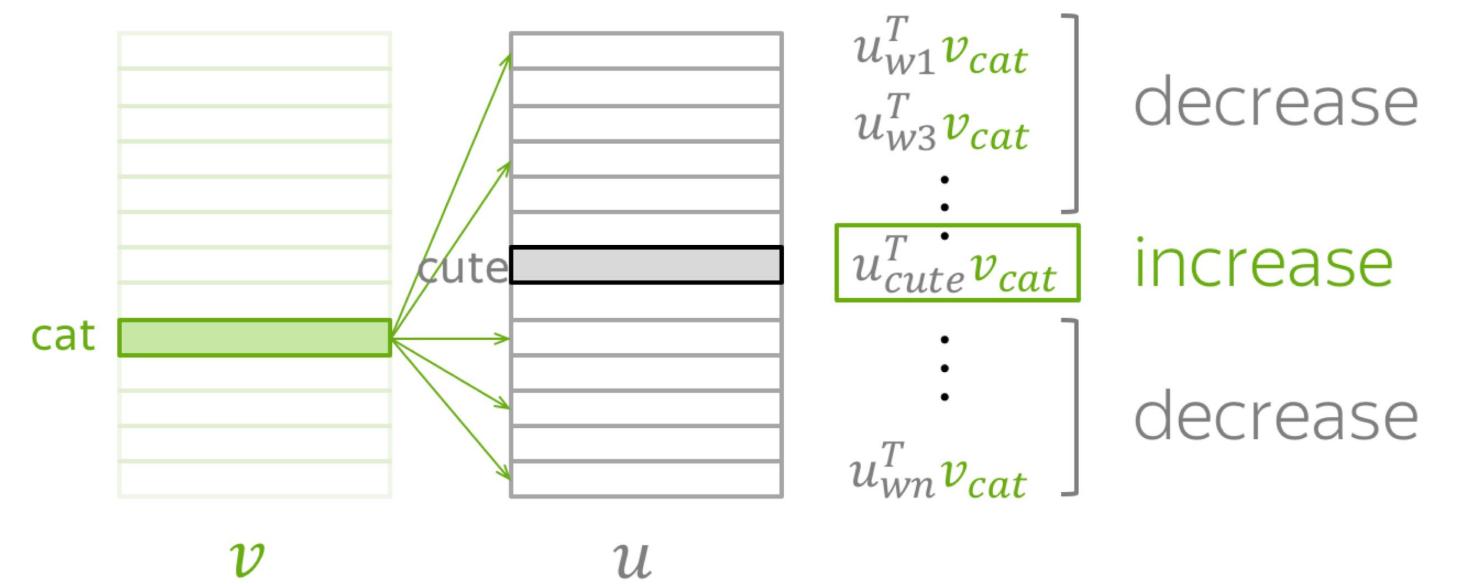
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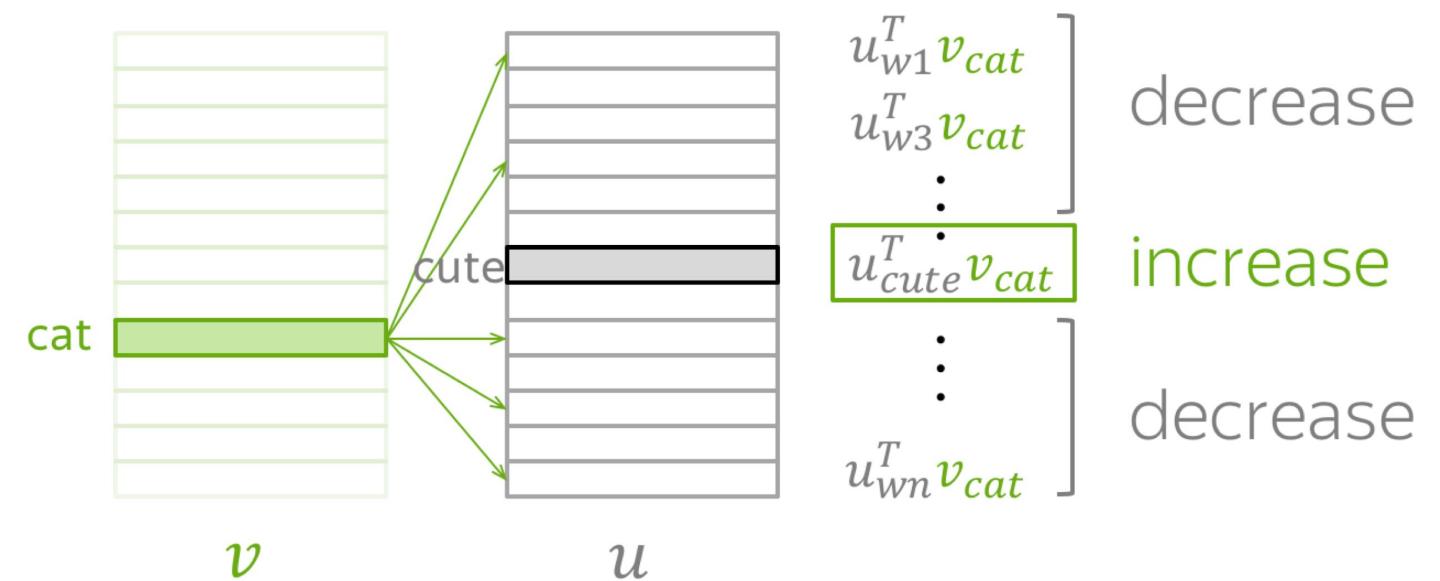
Parameters to be updated:

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- |V| + 1 vectors

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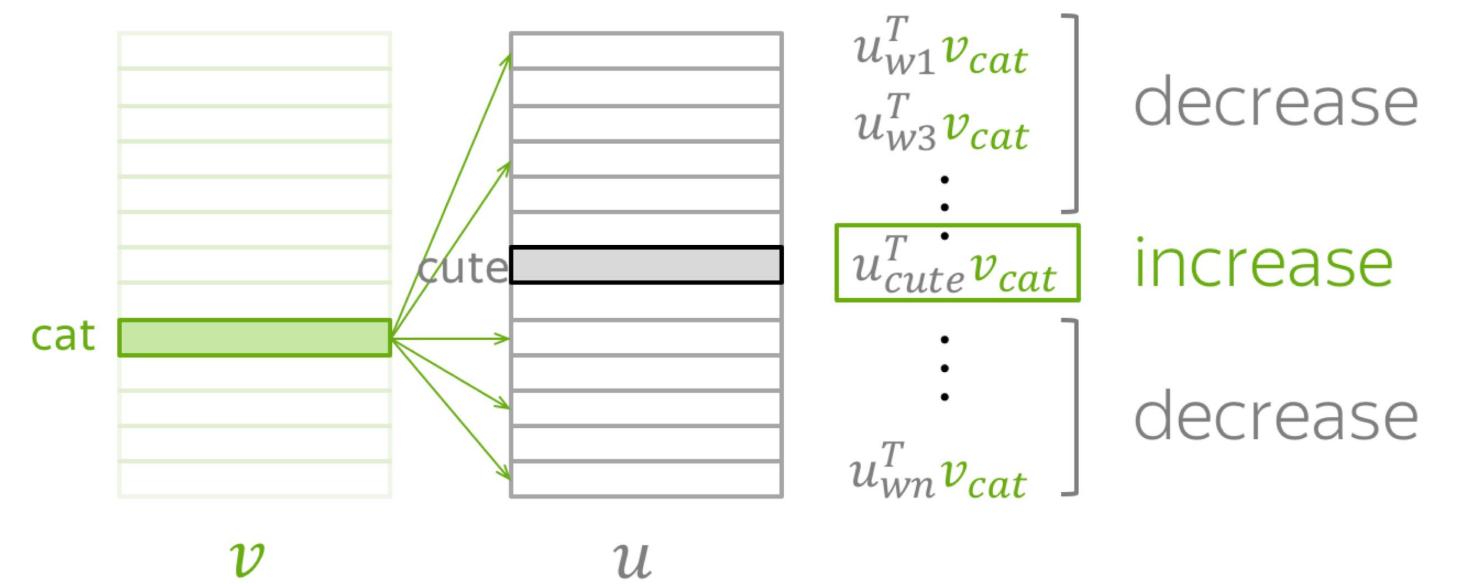
$|V| + 1$ vectors

Many parameters
at each step –
slow training

What happens at each training step

Dot product of v_{cat} :

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Parameters to be updated:

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- u_w for all w in the vocabulary

bad

$|V| + 1$ vectors

Let's do better: Negative Sampling

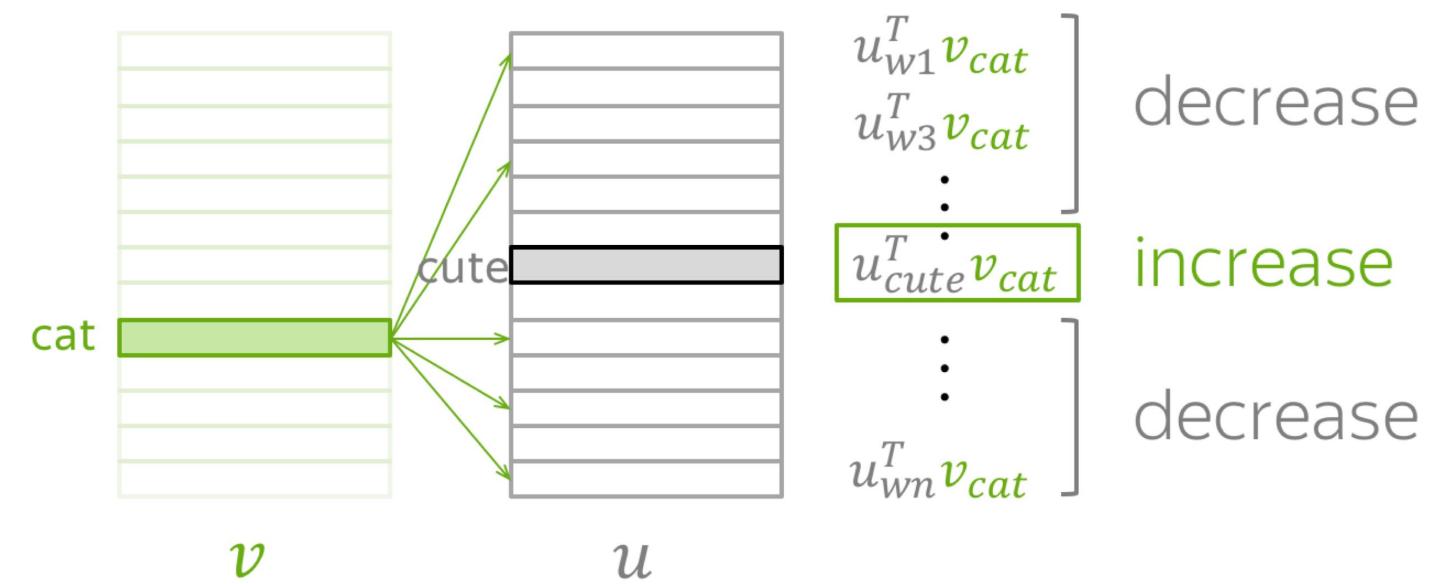
Dot product of v_{cat} :

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Dot product of v_{cat} :

- with u_{cute} - increase,
- with a subset of other u - decrease



Parameters to be updated:

bad

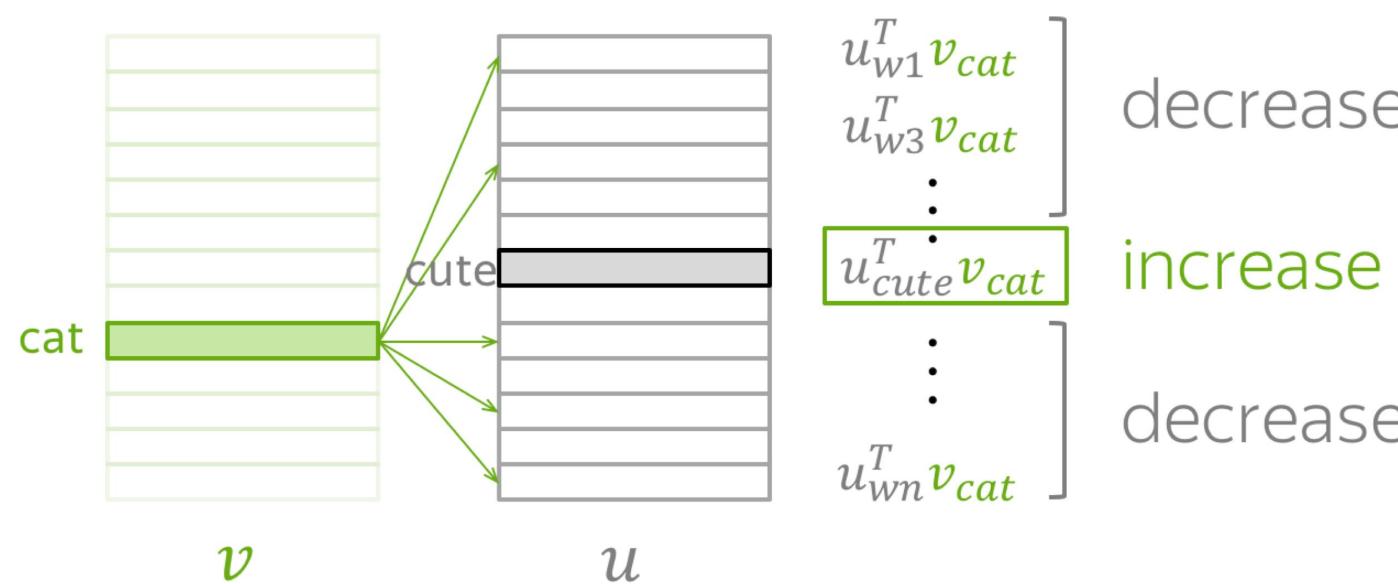
- v_{cat}
- u_w for all w in the vocabulary

$|V| + 1$ vectors

Let's do better: Negative Sampling

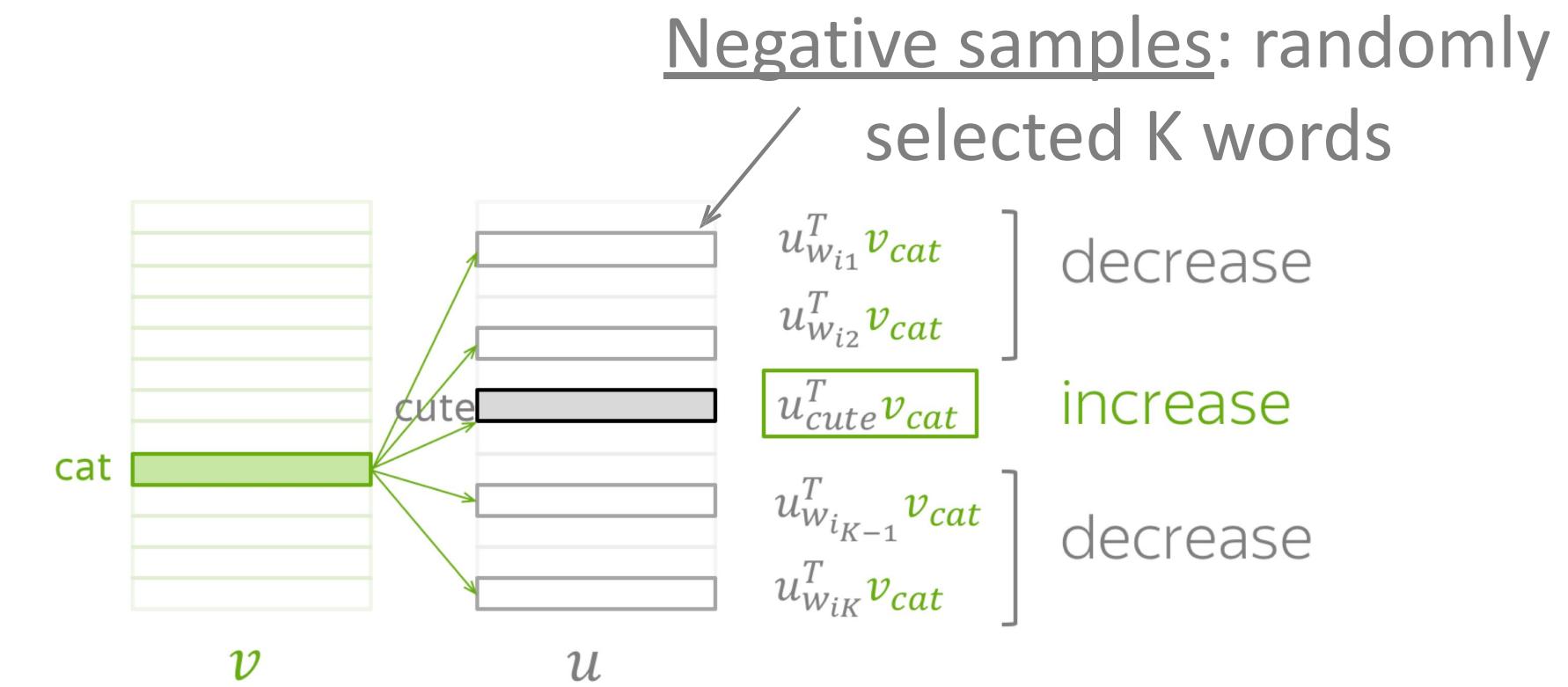
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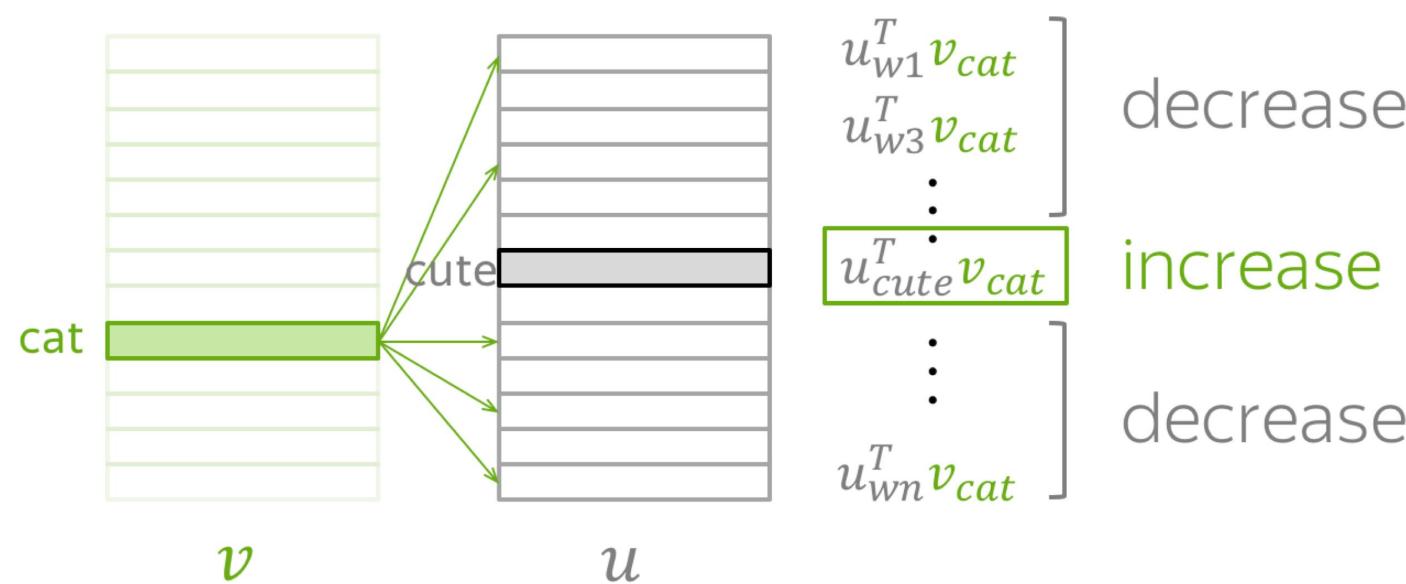
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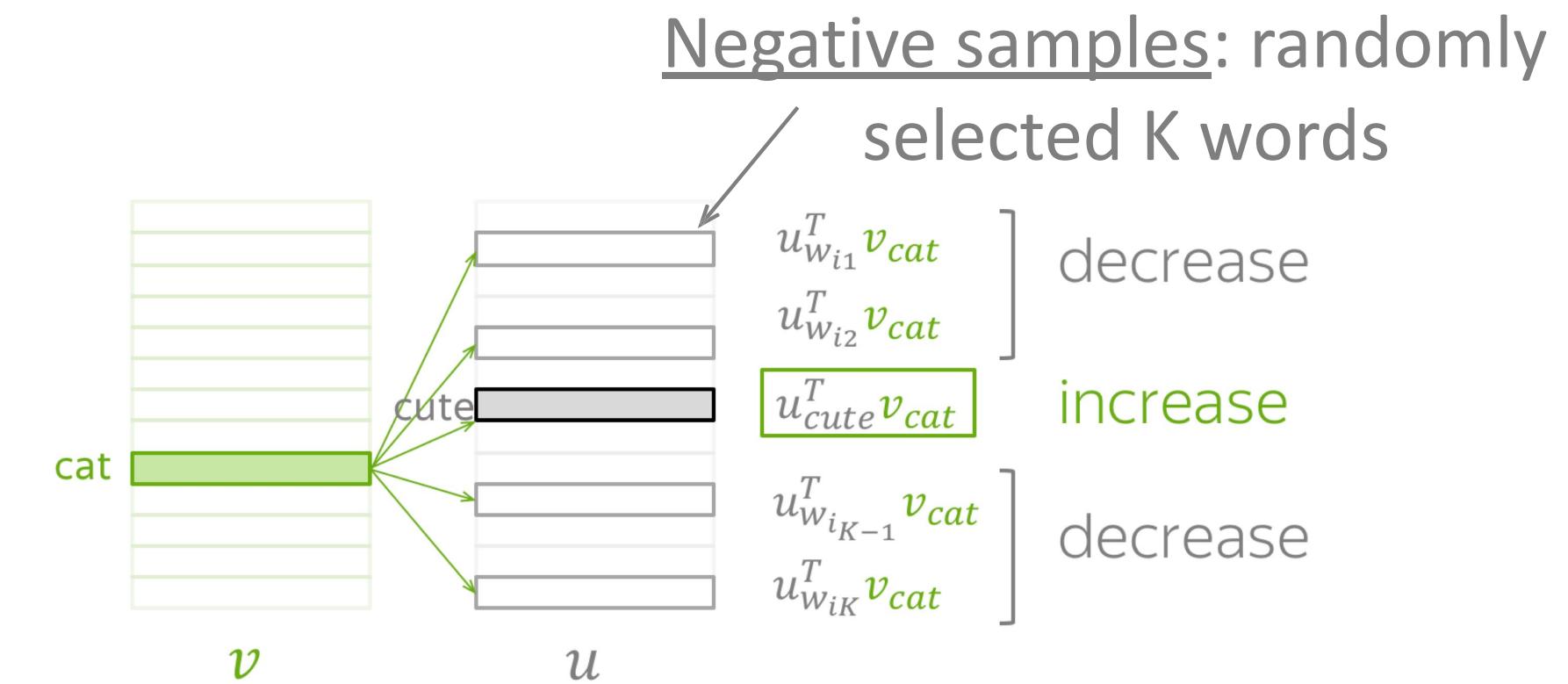
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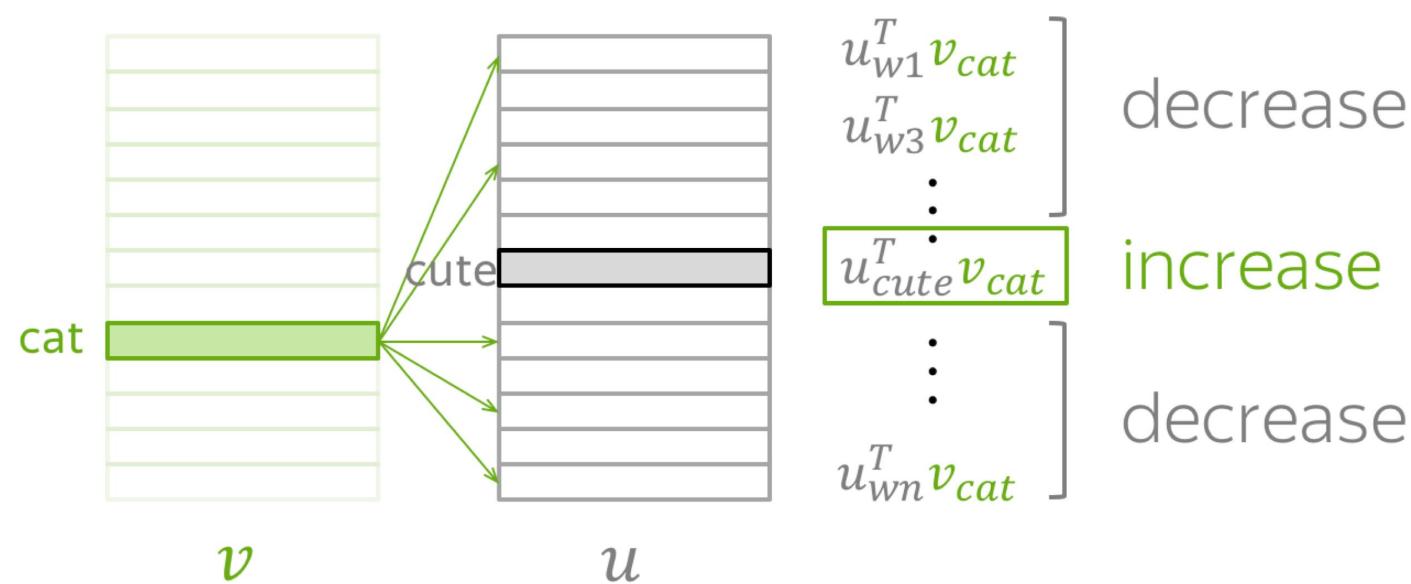
- v_{cat}
- u_{cute} and u_w for w in K negative examples

$K + 2$ vectors

Let's do better: Negative Sampling

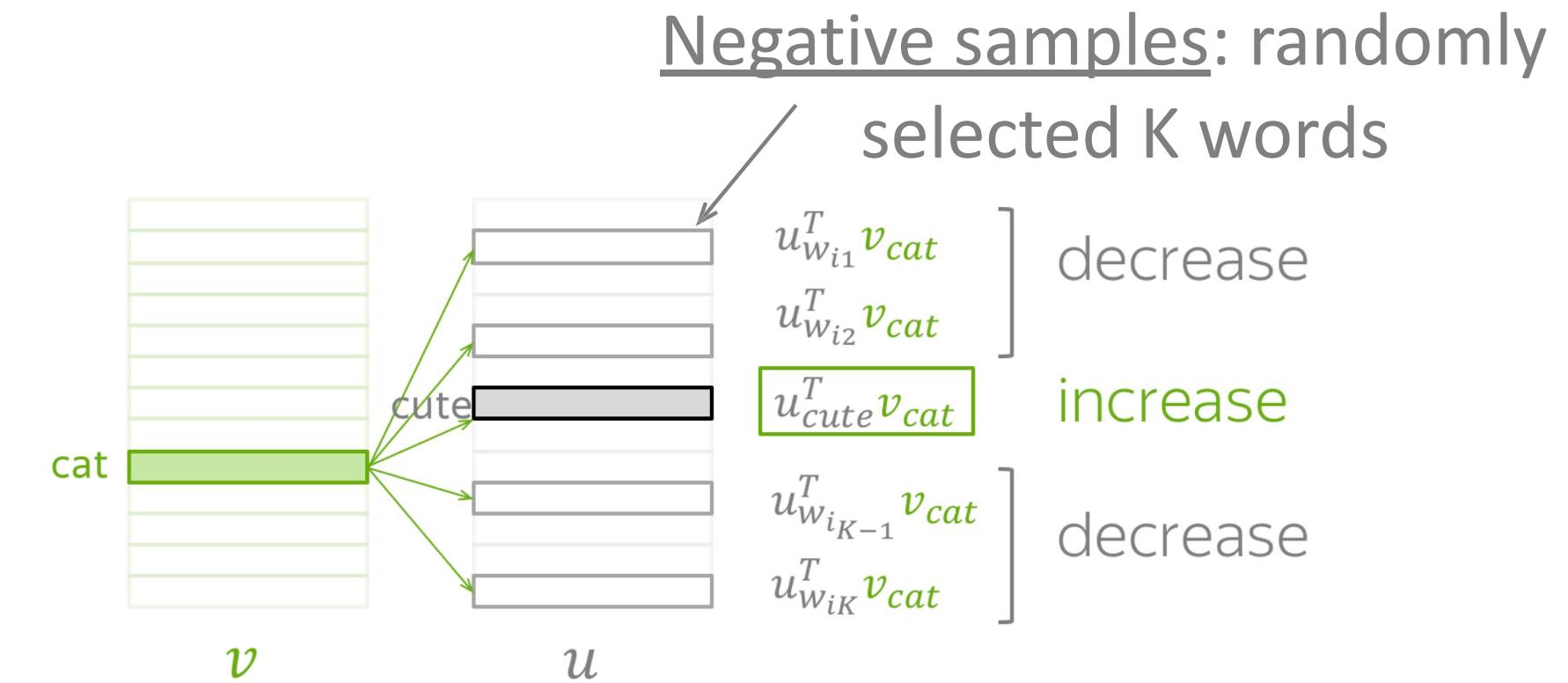
Dot product of v_{cat} :

- with u_{cute} - increase,
- with all other u - decrease



Dot product of v_{cat} :

- with u_{cute} - increase,
- with a subset of other u - decrease



Parameters to be updated:

bad

- v_{cat}
- u_w for all w in the vocabulary

$|V| + 1$ vectors

Parameters to be updated:

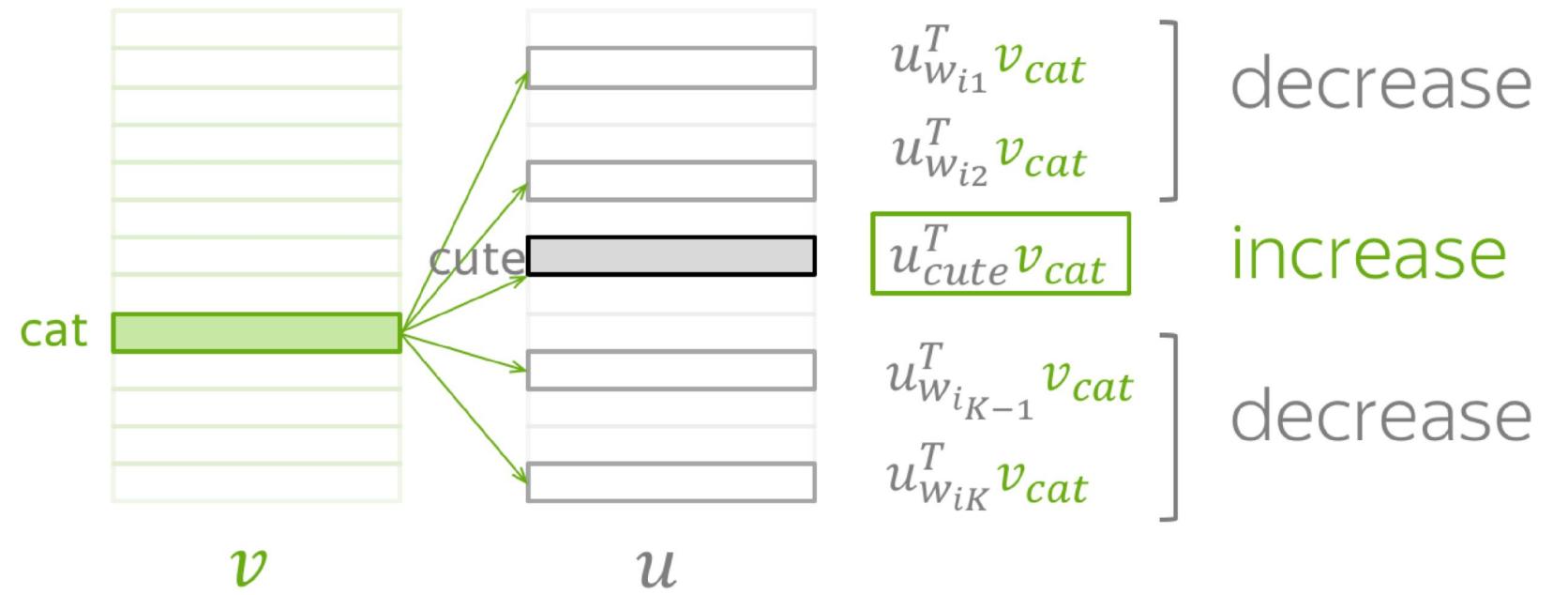
good

- v_{cat}
- u_{cute} and u_w for w in K negative examples

$K + 2$ vectors

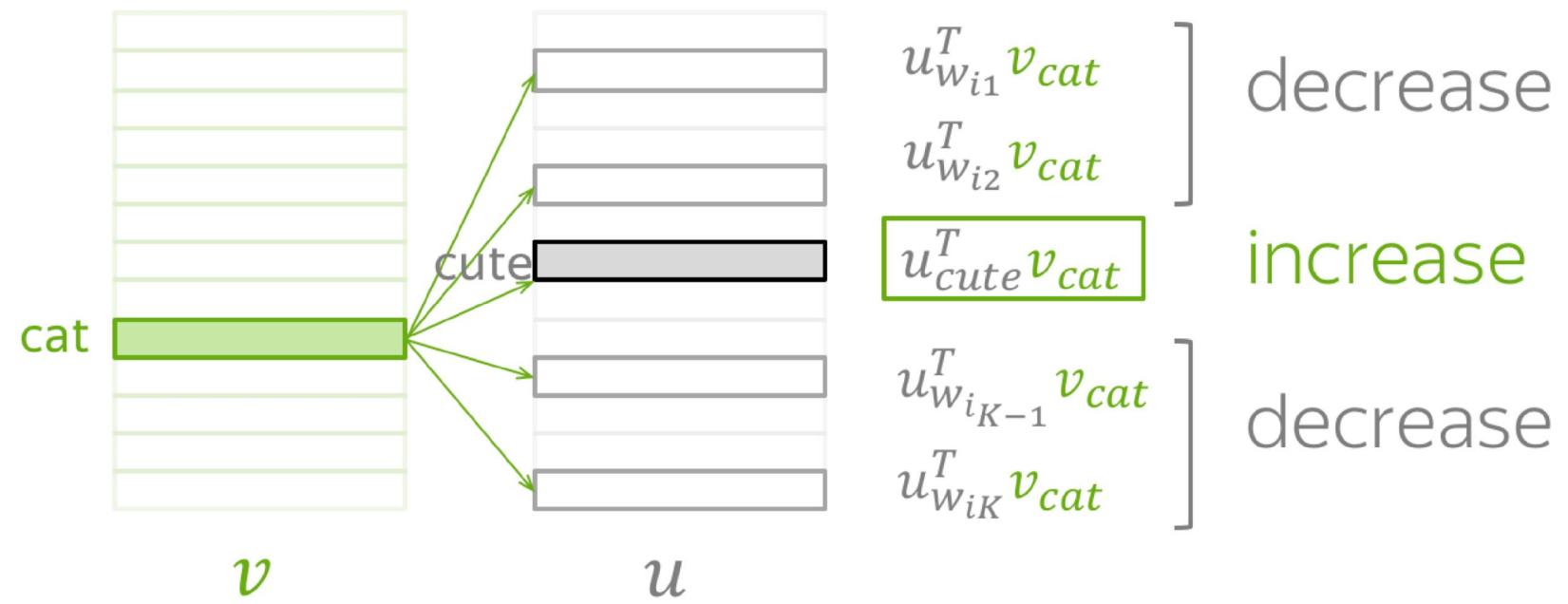
Negative Sampling: Loss Function

We want to do this:



Negative Sampling: Loss Function

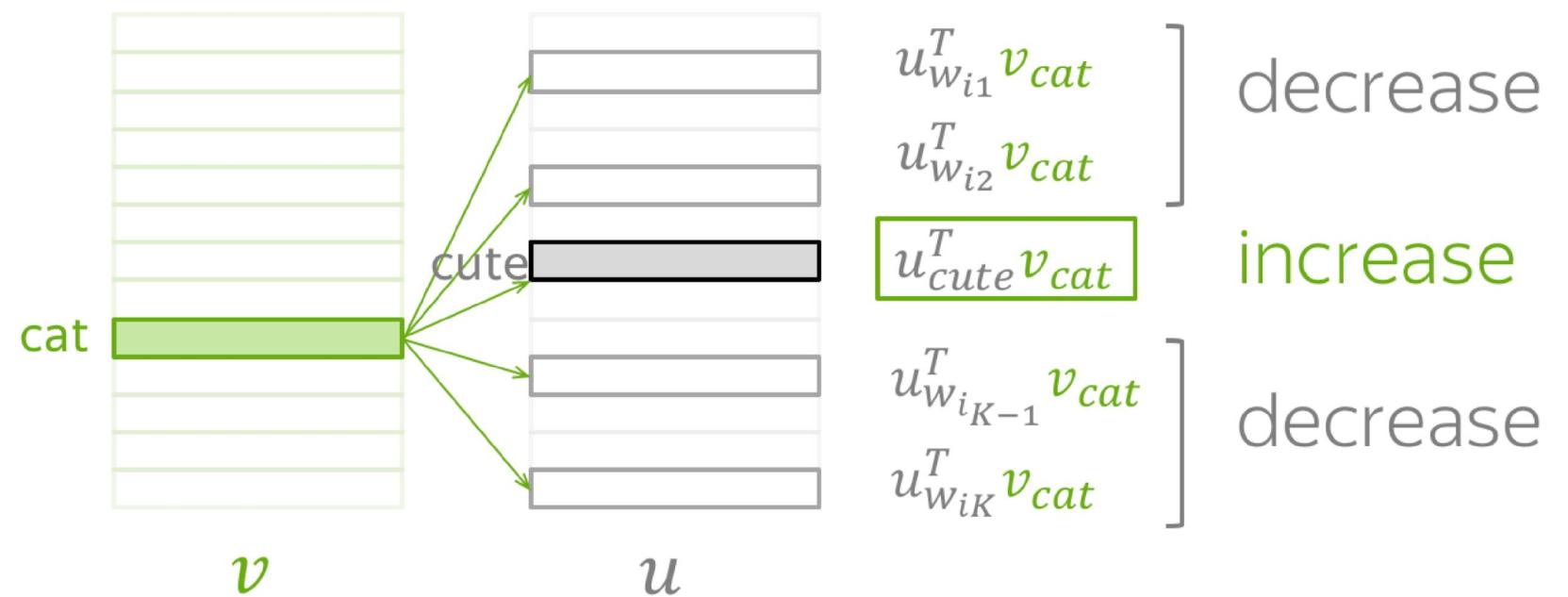
We want to do this: How we do this:



$$J_{t,j}(\theta) = -\log \sigma(u_{cute}^T v_{cat}) - \sum_{w \in \{w_{i_1}, \dots, w_{i_K}\}} \log \sigma(-u_w^T v_{cat})$$

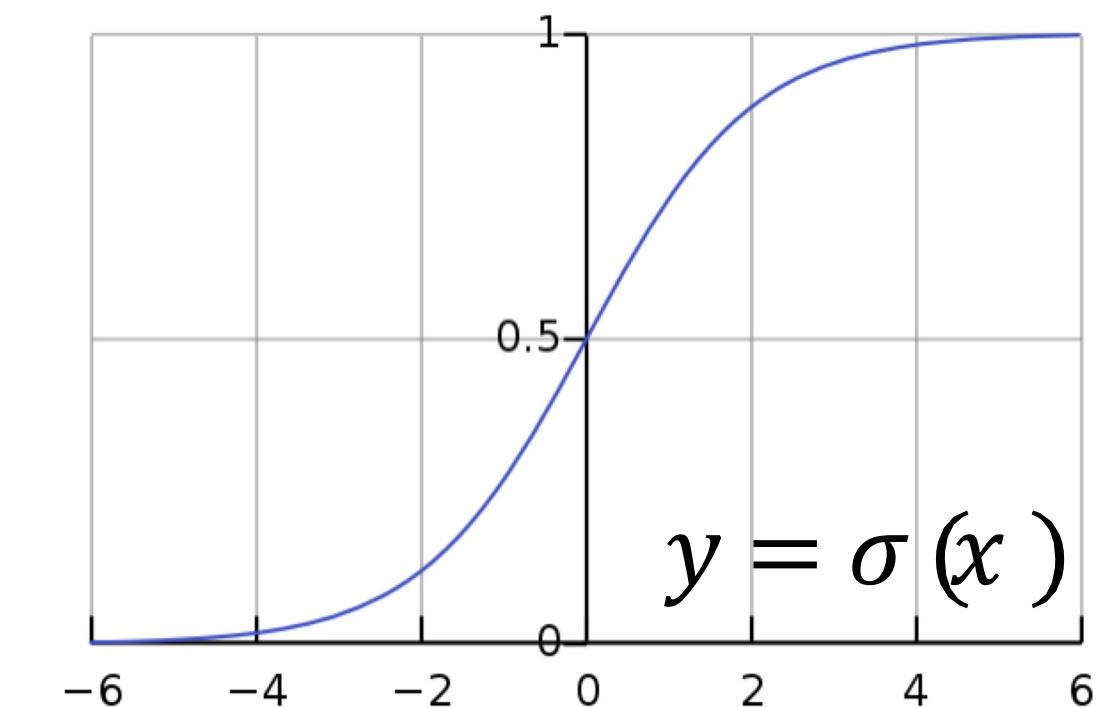
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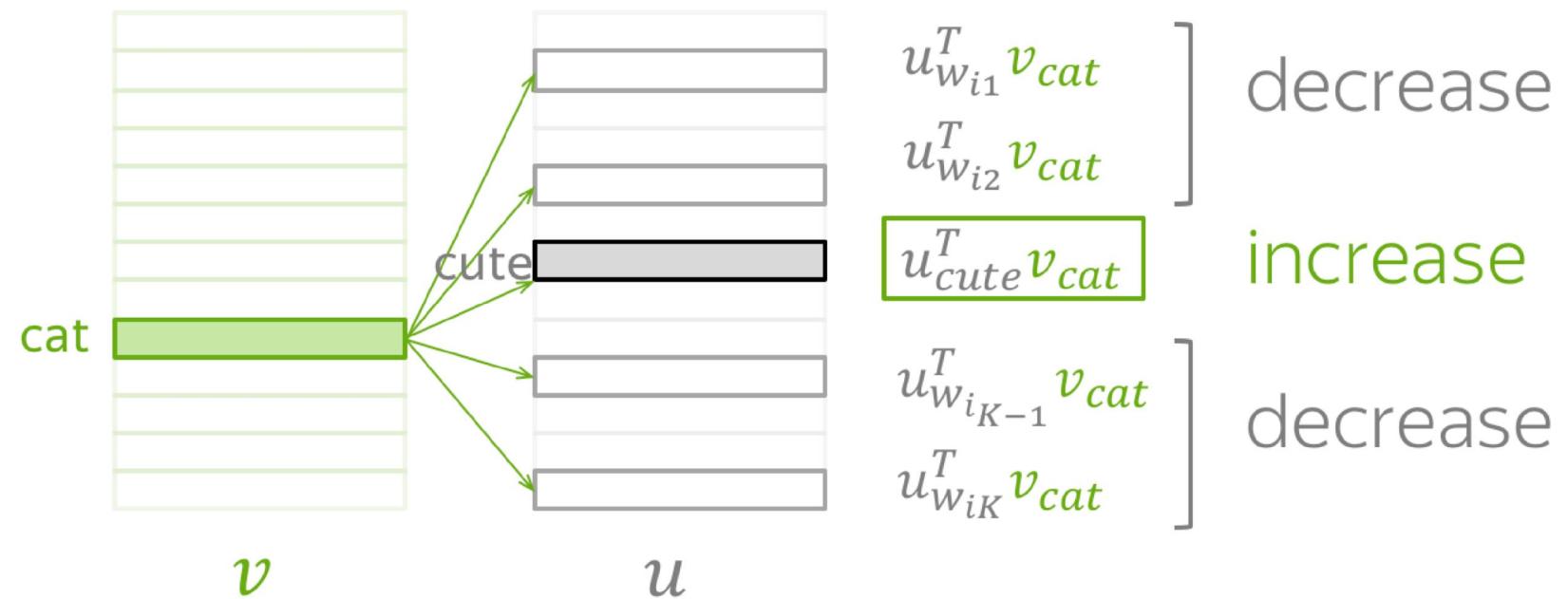
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$$\sigma(x) = \frac{e^x}{1 + e^x} - \text{the sigmoid function}$$



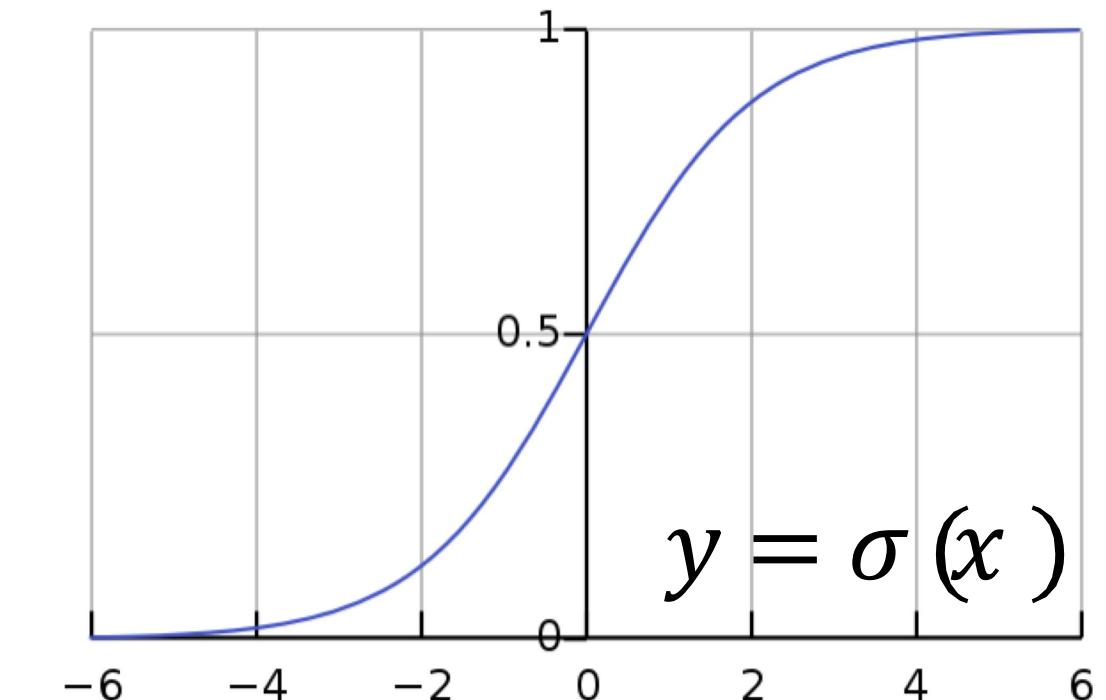
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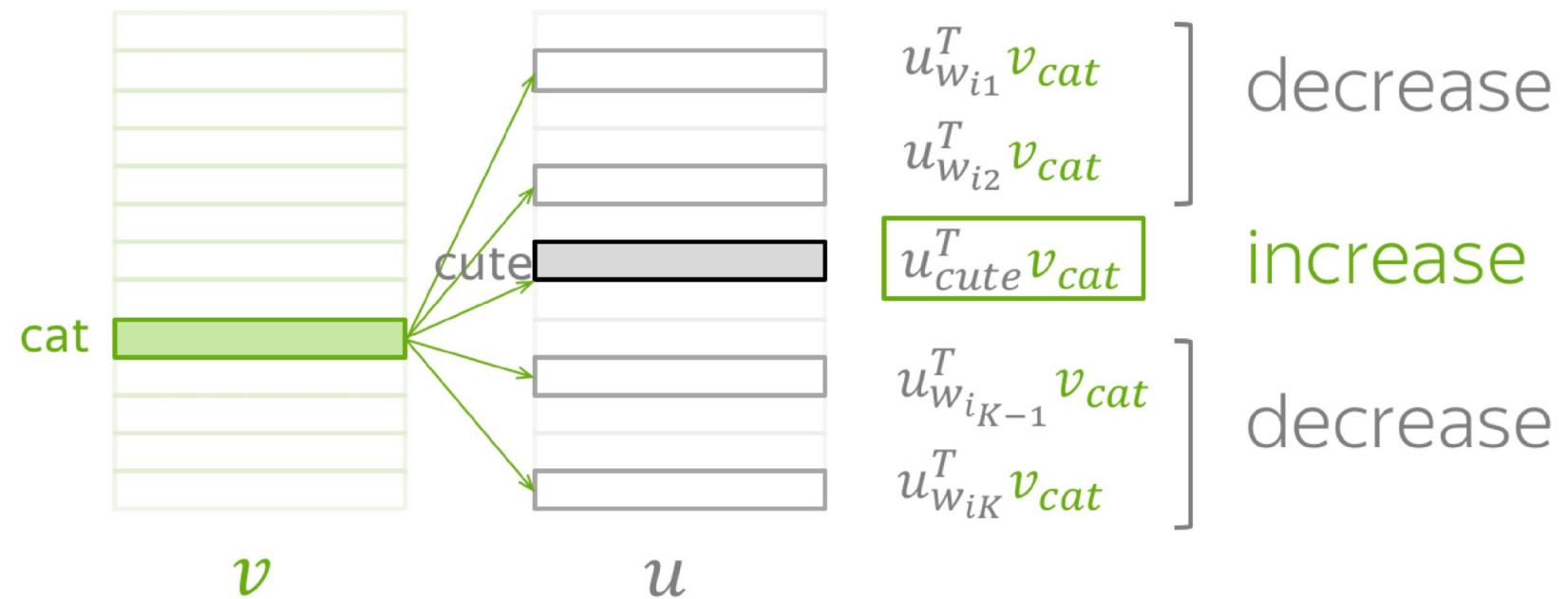
$\sigma(x) = \frac{e^x}{1 + e^x}$ - the sigmoid function



Note: $\sigma(-x) = \frac{1}{1 + e^{-x}} = \frac{e^{-x}}{(1 + e^{-x}) / e^{-x}} = \frac{e^{-x}}{1 + e^{-x}} = 1 - \frac{1}{1 + e^{-x}} = 1 - \sigma(x)$

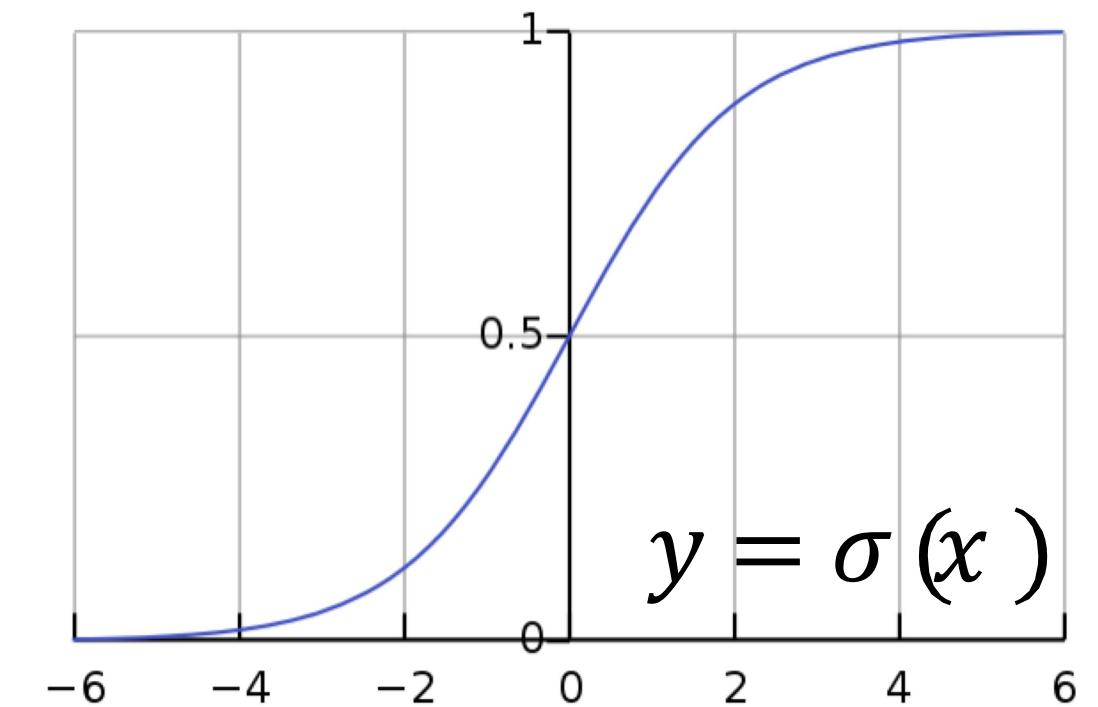
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Then: $J_{t,j}(\theta) = -\log \sigma(u_{cute}^T v_{cat}) - \sum_{w \in \{w_{i_1}, \dots, w_{i_K}\}} \log(1 - \sigma(u_w^T v_{cat}))$

What's inside:

Word2Vec

- Idea
- Objective Function
- Training Procedure
- Faster Training: Negative Sampling
- Word2Vec versions: Skip-Gram vs CBOW
- Final Notes

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Word2Vec

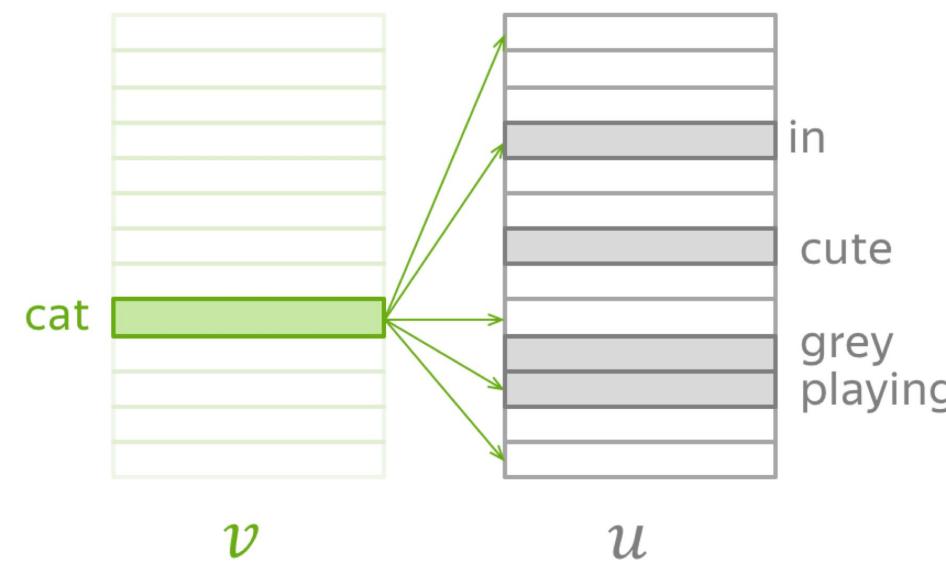
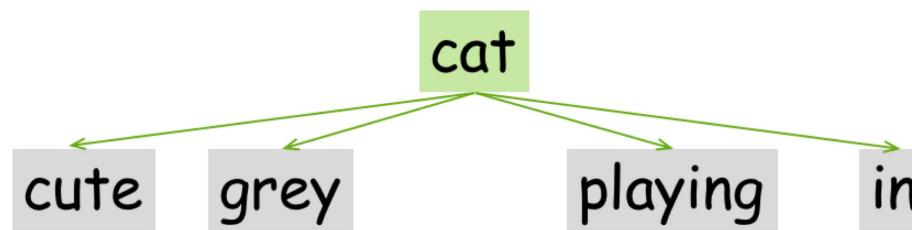
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Word2Vec Variants: Skip-Gram and CBOW

...I saw a

cute grey cat playing in the garden ...

Skip-Gram: from central predict context (one at a time)

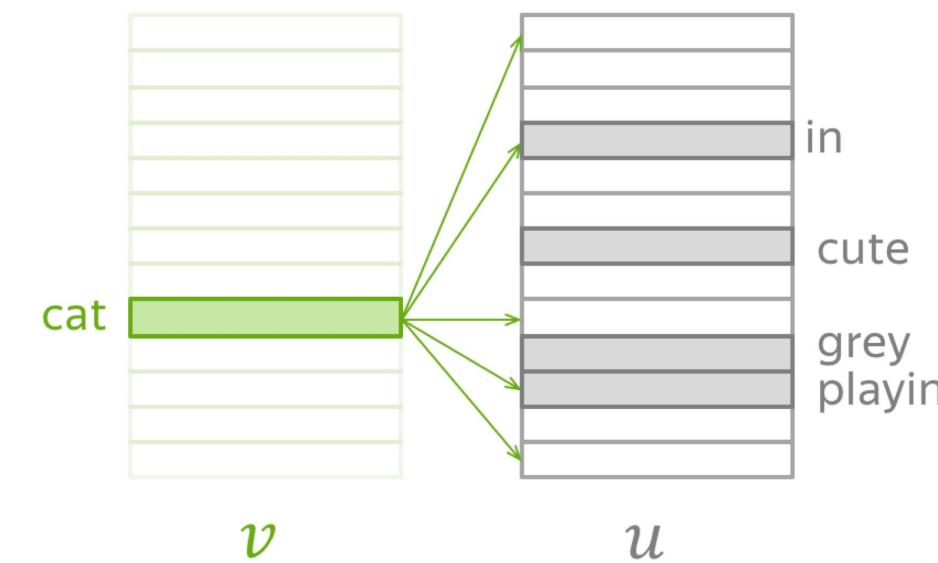
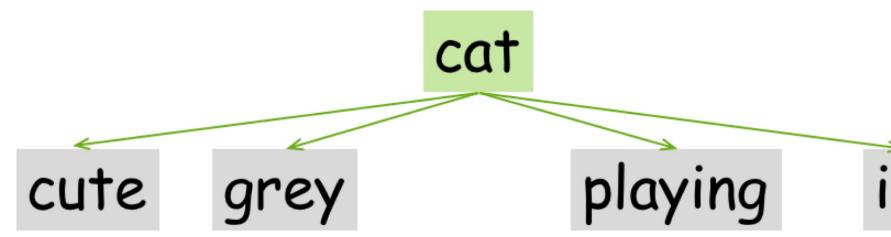


(this is what we did so far)

Word2Vec Variants: Skip-Gram and CBOW

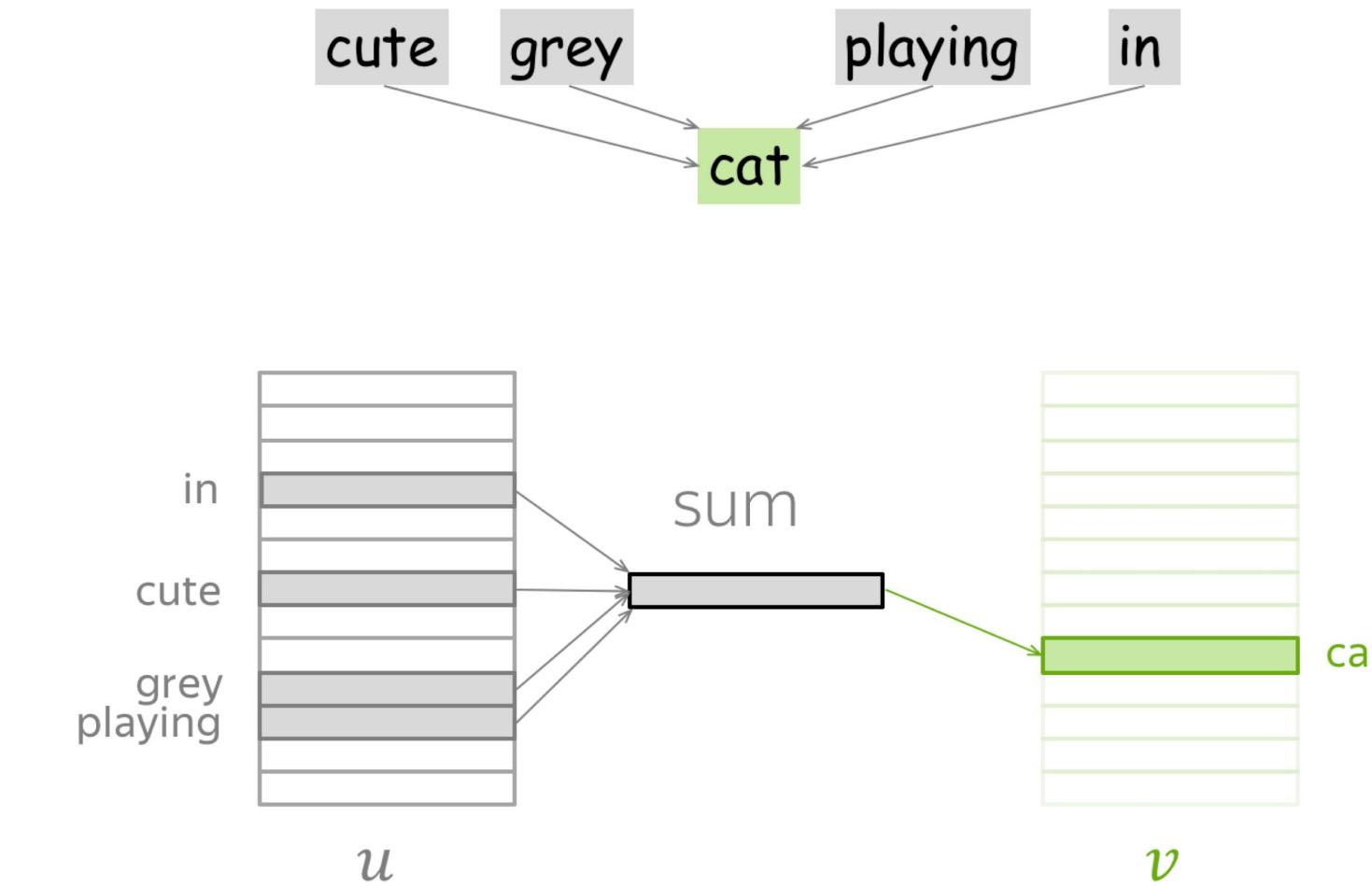
... I saw a cute grey cat playing in the garden ...

Skip-Gram: from **central** predict context
(one at a time)



(this is what we did so far)

CBOW: from sum of context predict **central**



(Continuous Bag of Words)

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(Somewhat) Standard Hyperparameters

- Model: Skip-Gram with negative sampling;
- Number of negative examples: for smaller datasets, 15-20; for huge datasets (which are usually used) it can be 2-5.
- Embedding dimensionality: frequently used value is 300, but other variants (e.g., 100 or 50) are also possible.
- Sliding window (context) size: 5-10.

The Effect of Context Window Size

- Larger windows – more topical similarities
- Smaller windows – more functional and syntactic similarities

dog
bark leash
(grouped together)

walking
run
(grouped together)

Poodle
Rottweiler
Pitbull
(grouped together)

walking
running
approaching
(grouped together)

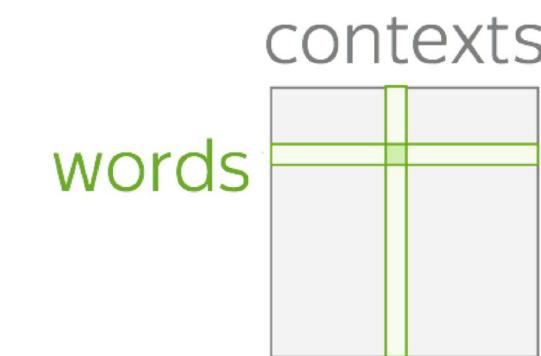
Relation to PMI Matrix Factorization

NLP Course For You



Word2Vec SGNS (Skip-Gram with Negative Sampling) implicitly approximates the factorization of a (shifted) PMI matrix. [Learn more here.](#)

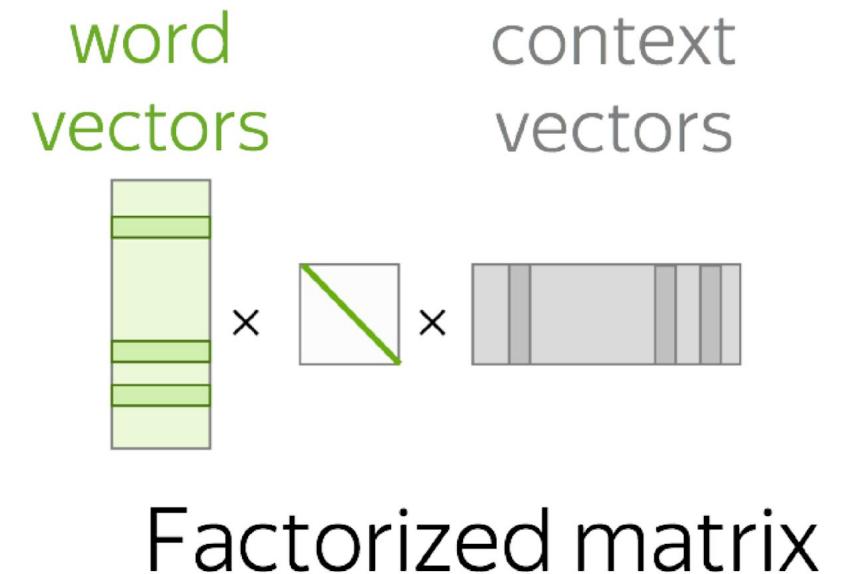
PMI matrix



Explicitly
(SVD)

Implicitly

Word2Vec
(SGNS)



Relation to PMI Matrix Factorization



Related Papers

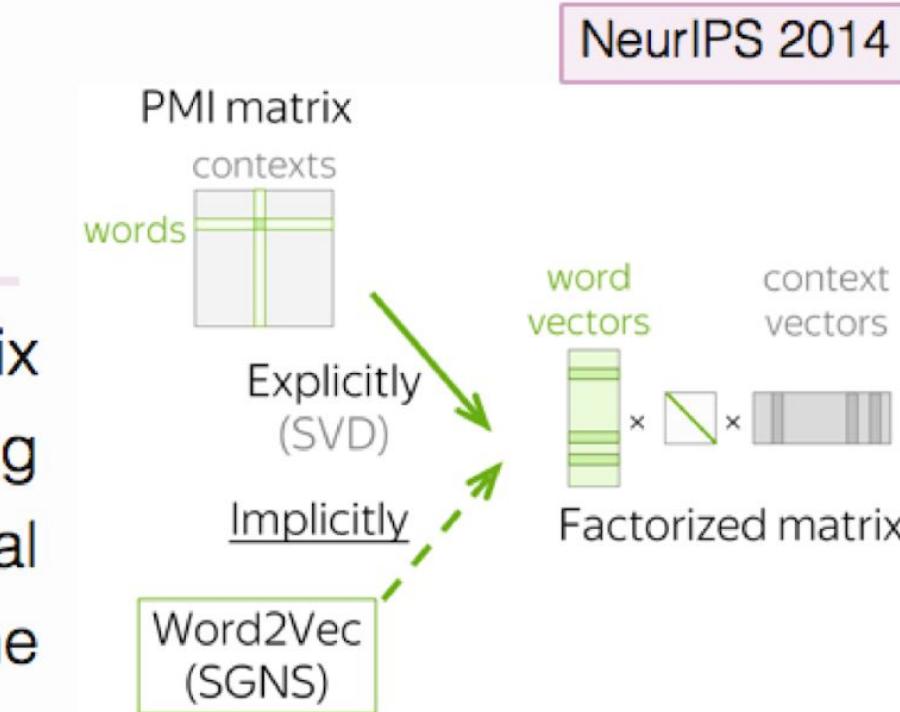
Good Old Classics

Neural Word Embedding as Implicit Matrix Factorization

Omer Levy, Yoav Goldberg

Theoretically, Word2Vec is not so different from matrix factorization approaches! Skip-gram with negative-sampling (SGNS) implicitly factorizes the shifted pointwise mutual information (PMI) matrix: $PMI(w, c) - \log k$, where k is the number of negative examples in negative sampling.

► More details



More Hacks in Training



Research Thinking

Word2Vec

Are all context words equally important for training?

During Word2Vec training, we make an update for each of the context words. For example, for the central word **cat** we make an update for each of the words **cute, grey, playing, in**.

...I saw a **cute** **grey** **cat** playing in the ...
...I saw a **cute** **grey** **cat** playing in the ...
...I saw a **cute** **grey** **cat** playing in the ...
...I saw a **cute** **grey** **cat** **playing** in the ...
...I saw a **cute** **grey** **cat** **playing** in the ...

? Are all context words equally important?

Which word types give more/less information than others? Think about some characteristics of words that can influence their importance. Do not forget the previous exercise!

► Possible answers

? How can we use this to modify training?

► Tricks from the original Word2Vec



What is going to happen:

- Why do we need word representations?
- One-hot Vectors
- Distributional Semantics
- Count-Based Methods
- Word2Vec (Prediction-based Method)
- GloVe
- Evaluation
-  Analysis and Interpretability

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GloVe

(kind of both count-based and prediction-based)



GloVe: Global Vectors for Word Representation

Count-based

Information
comes from:

Vectors are:
obtained via
dimensionality reduction

global corpus
statistics

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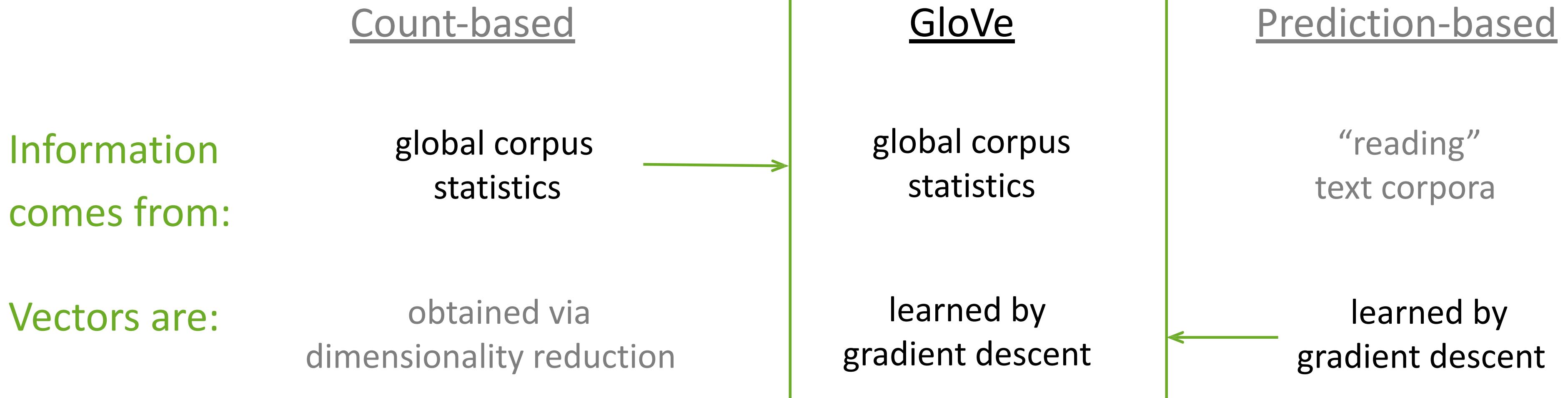
obtained via
dimensionality reduction

Prediction-based

“reading”
text corpora

learned by
gradient descent

GloVe: Global Vectors for Word Representation



GloVe: Global Vectors for Word Representation

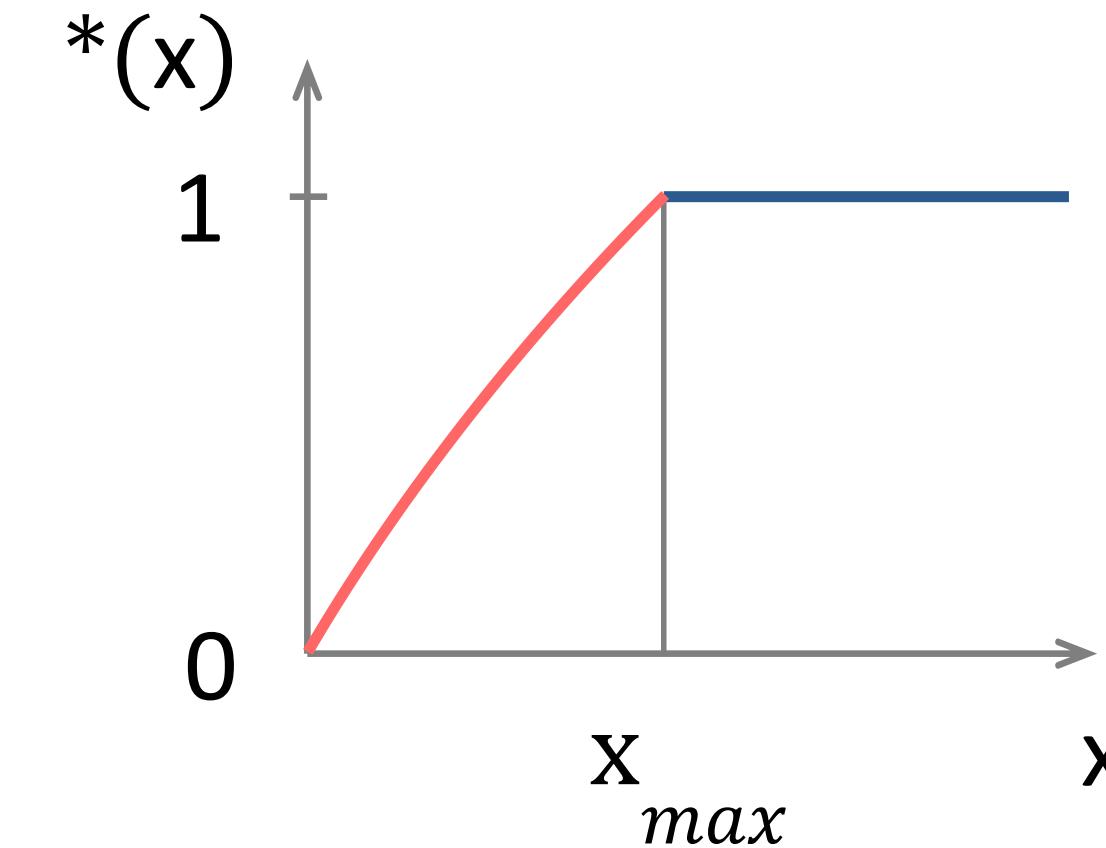
context vector word vector bias terms (also learned)

$$J(") = \$(N(w, c)) - (u^T v_c + b_w + b_{\bar{w}} - \log N(w, c))^2$$

$w, c \in V$

Weighting function to:

- penalize rare events
- not to over-weight frequent events



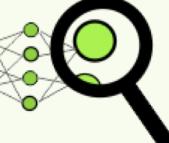
$\begin{cases} (x/x_{max})^\alpha & \text{if } x < x_{max}, \\ 1 & \text{otherwise.} \end{cases}$

$\alpha = 0.75, x_{max} = 100$

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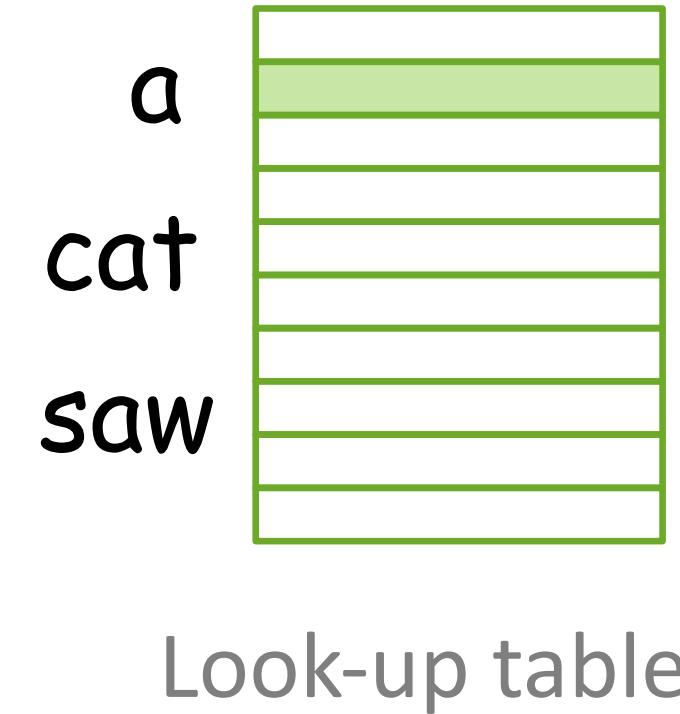
Evaluation: Intrinsic and Extrinsic



Intrinsic Evaluation: Based on Internal Properties

How well do embeddings
capture meaning?

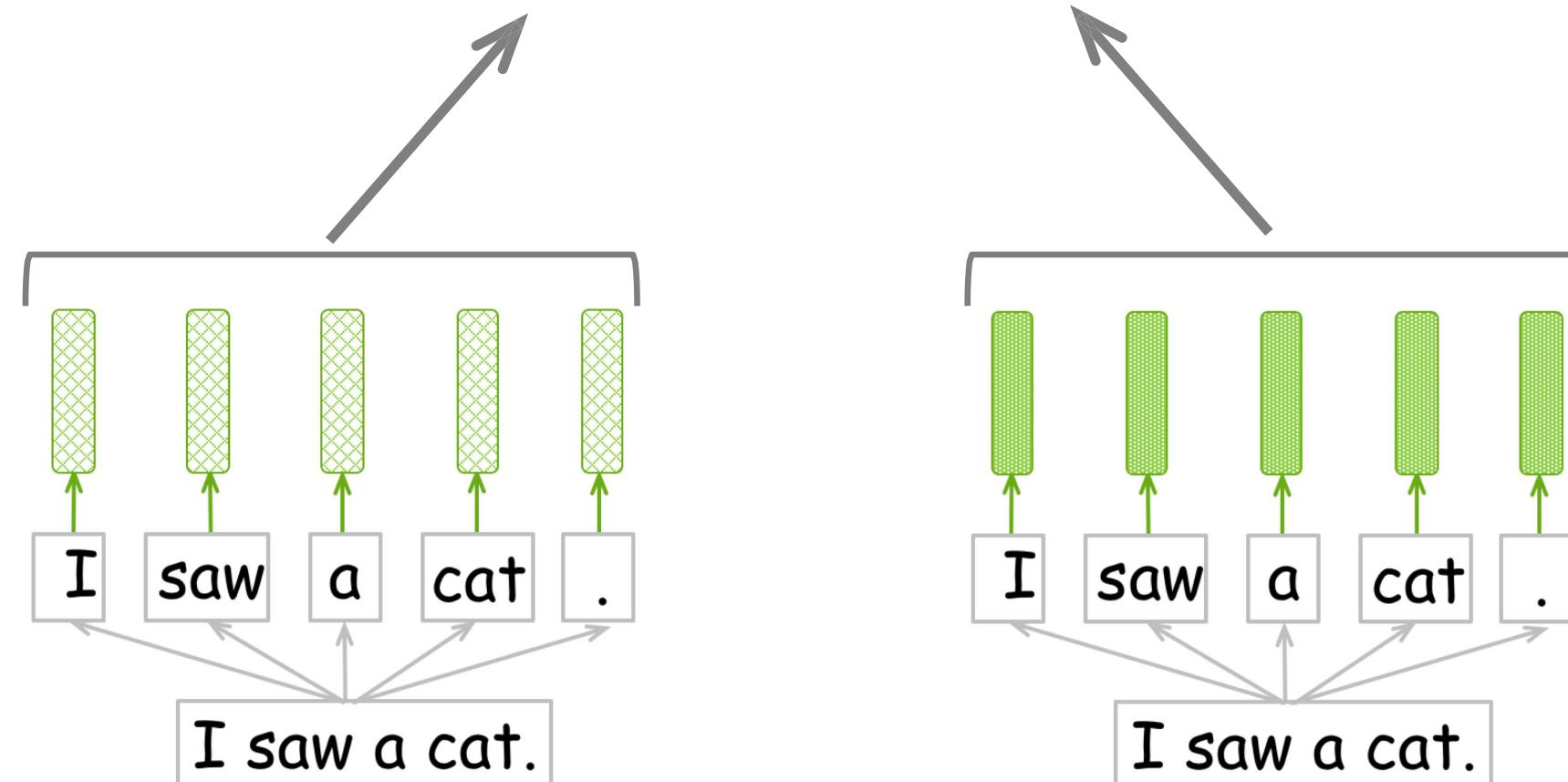
- word similarity
- word analogy
- ...



We'll look at this in detail in the Analysis and Interpretability part!

Extrinsic Evaluation: On a Real Task

Your algorithm for some real task (e.g., classification)



some
embeddings

some other
embeddings

Model with which embeddings performs better?

Train the same model several times: one model for each embedding set

For the same dataset, you can get representations using different word embeddings

Intrinsic vs Extrinsic: How to Choose?

Intrinsic:

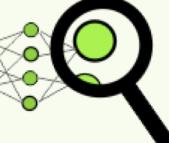
- usually fast
- does not tell what is better in practice

Extrinsic:

- tells directly what is better in practice
- training several real-task models is expensive

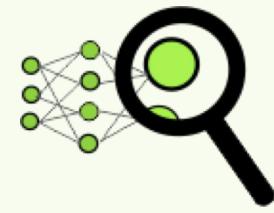
...in the end, this is up to you

What is going to happen:

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Analysis and Interpretability

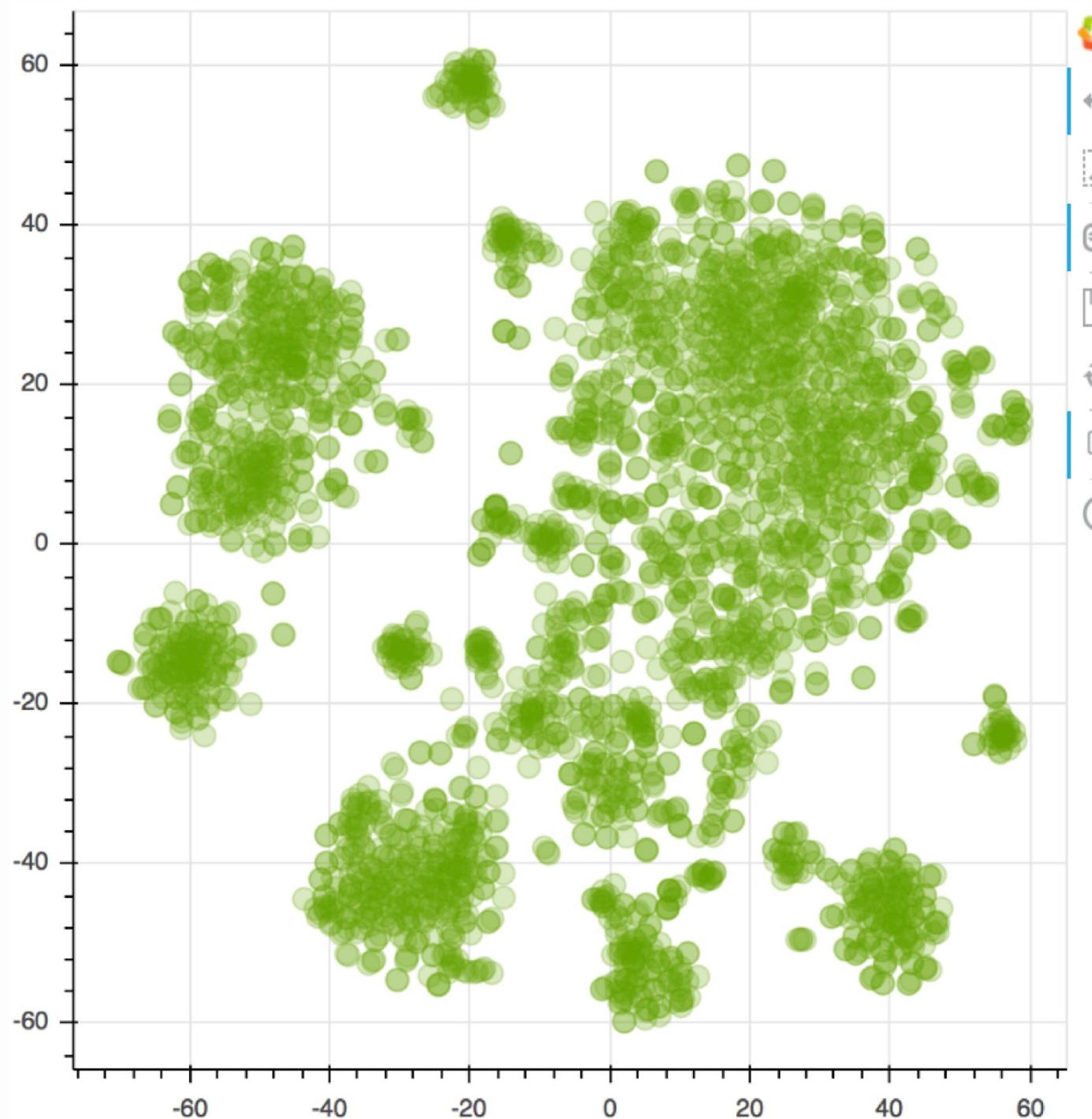


🔍 Take a Walk Through Space... Semantic Space!



How to: Walk through semantic space and try to find:

- language clusters: Spanish, Arabic, Russian, English. Can you find more languages?
- clusters for: food, family, names, geographical locations. What else can you find?



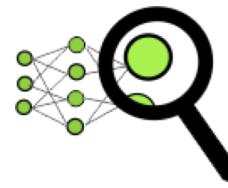
Open right now and
take your time!

(come back in 5-10 minutes)

NLP Course **For You**



[https://lena-voita.github.io/
nlp_course/
word_embeddings.html](https://lena-voita.github.io/nlp_course/word_embeddings.html)



Nearest Neighbors

Closest to frog:

frogs

toad

litoria

leptodactylidae

rana

lizard

eleutherodactylus

litoria



leptodactylidae



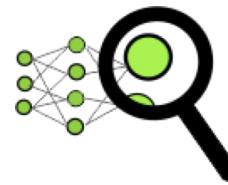
rana



eleutherodactylus



The example is from the [GloVe project page](#).



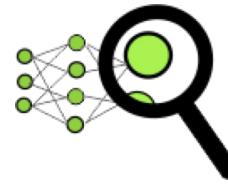
Word Similarity Benchmarks

The benchmarks that estimate the quality of embeddings:

- Contain word pairs with similarity scores from humans
- For evaluation, use correlation between the two similarity scores: from humans and from embeddings

<u>word</u>	<u>pair</u>	<u>score</u>
vulgarism	profanity	9.62
subdividing	separate	8.67
friendships	brotherhood	7.5
exceedance	probability	5.0
assigned	allow	3.5
marginalize	interact	2.5
misleading	beat	1.25
radiators	beginning	0

Several pairs from the Rare Words similarity benchmark.

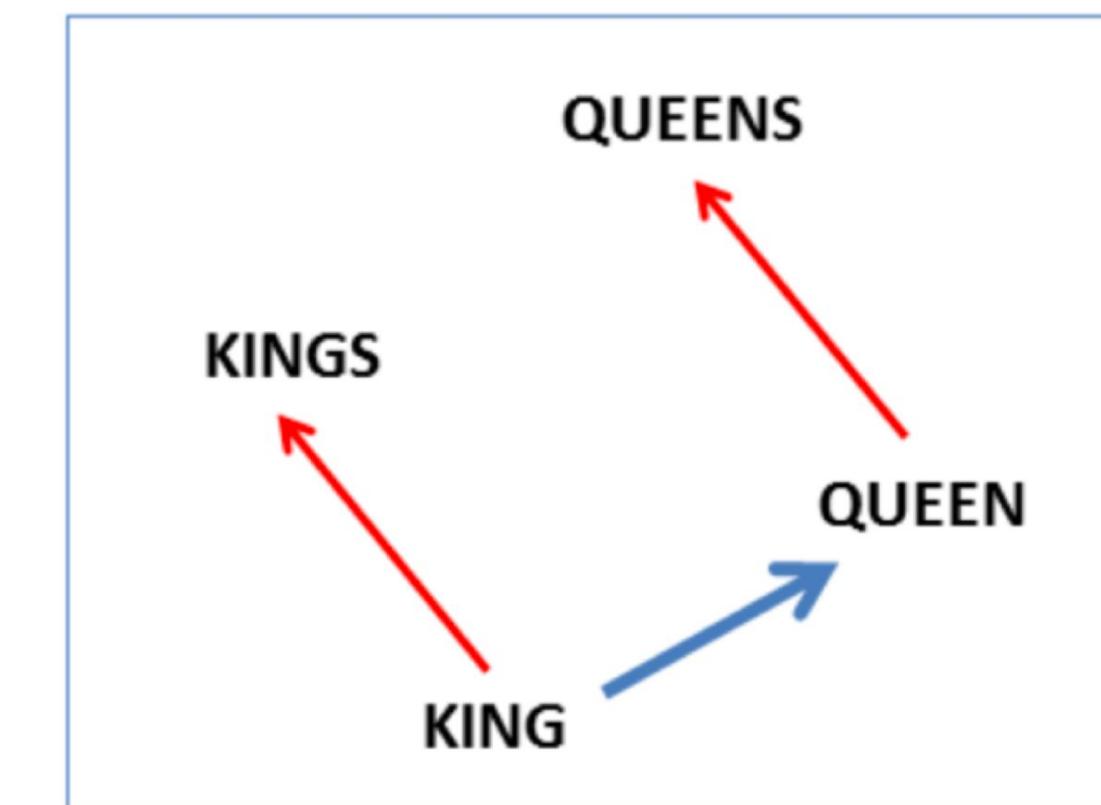
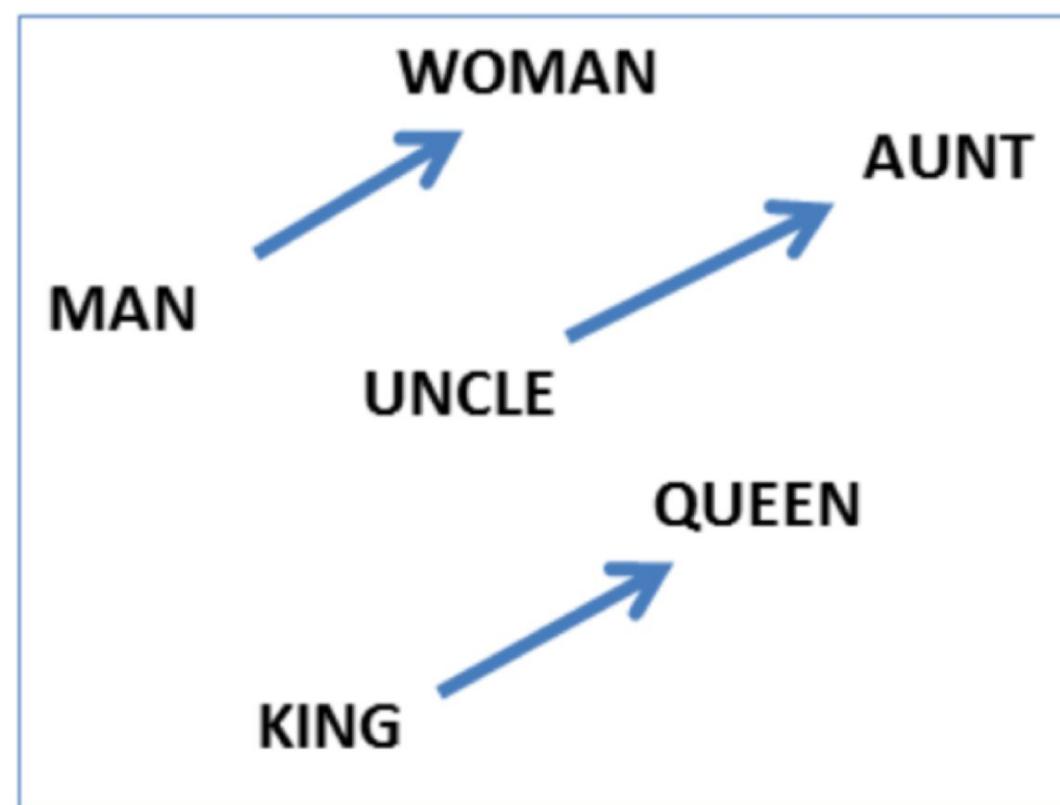


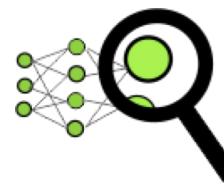
Linear Structure

Many semantic and syntactic relationships between words are (almost) linear in the embedding space!

semantic: $v(\text{king}) - v(\text{man}) + v(\text{woman}) \approx v(\text{queen})$

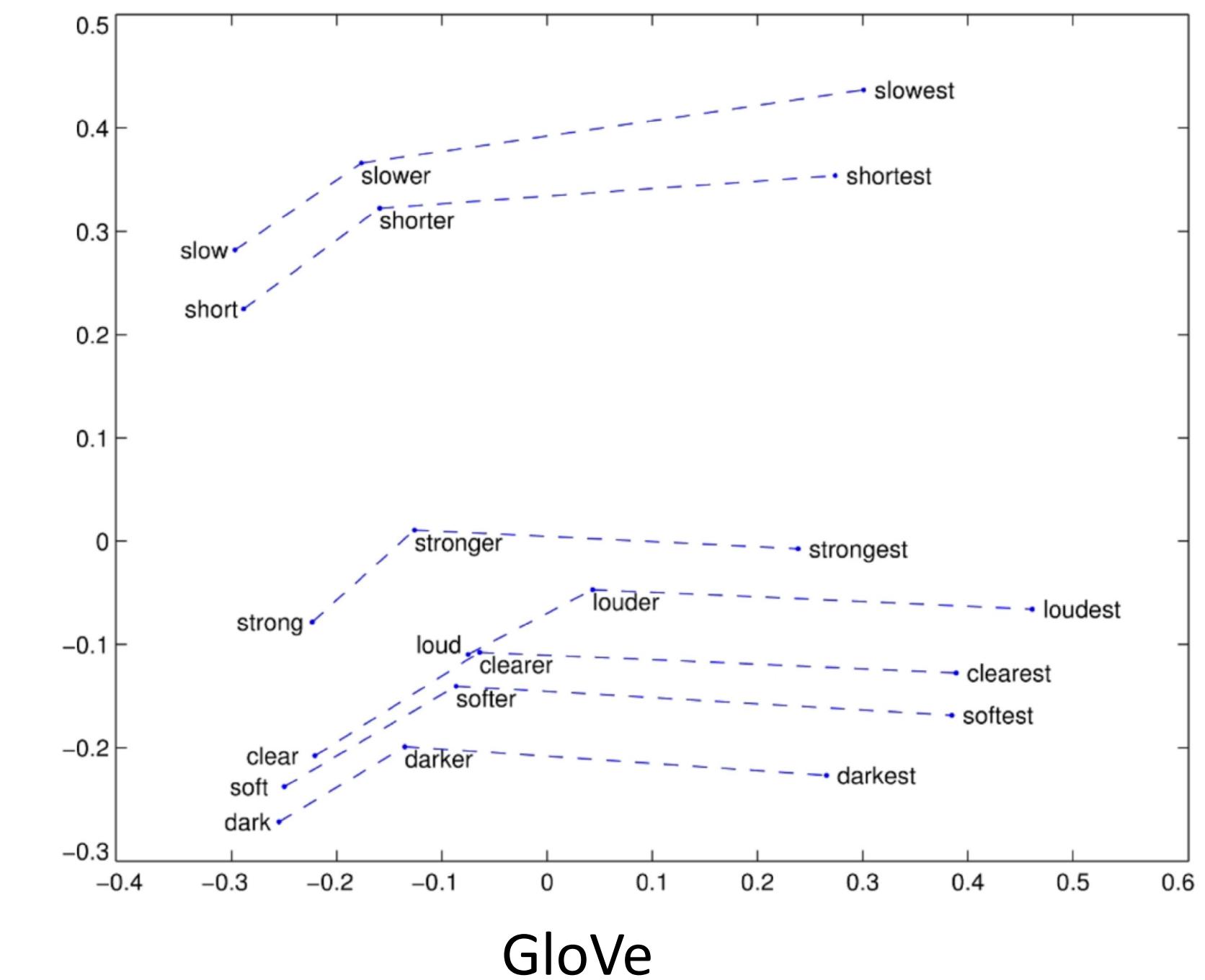
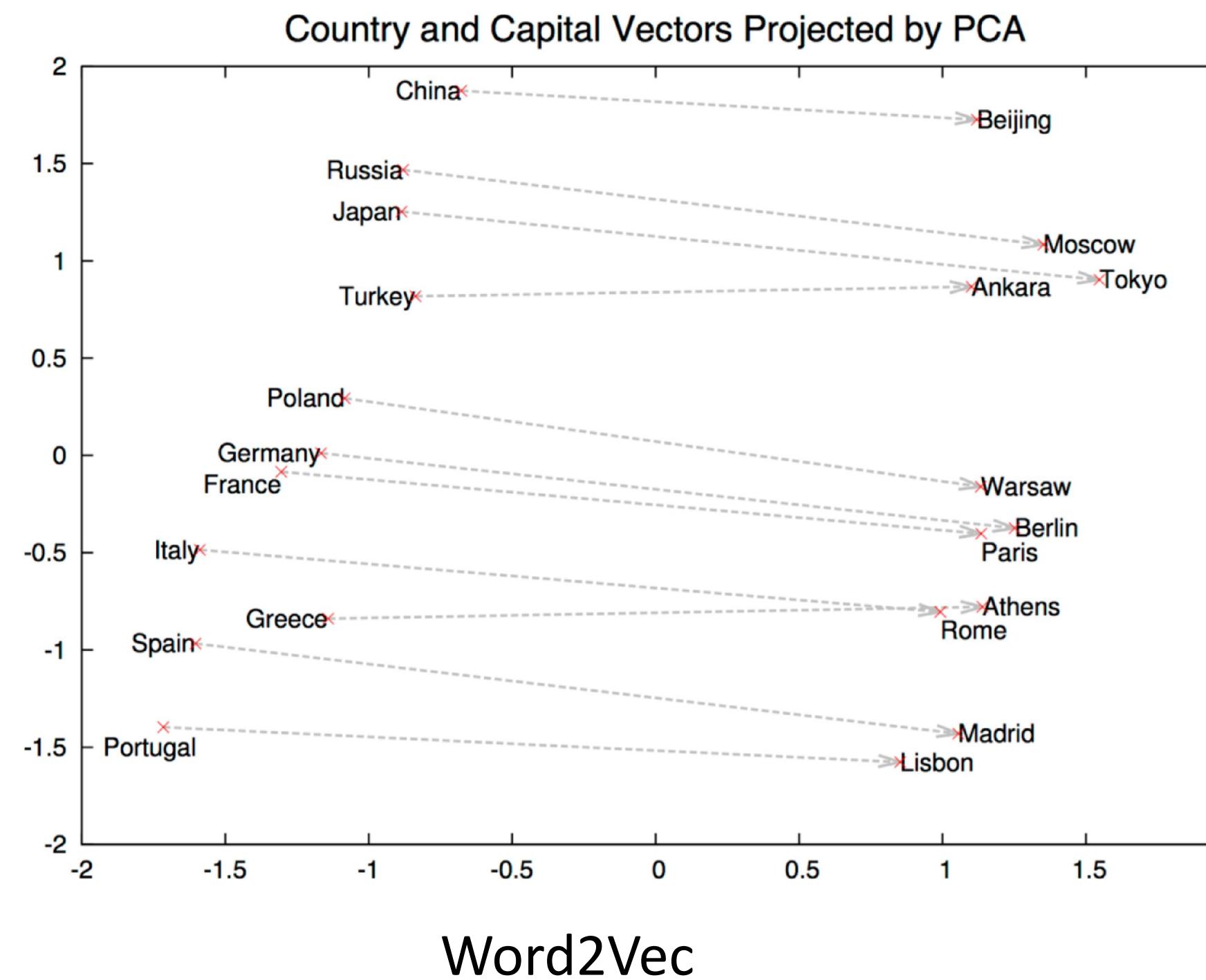
syntactic: $v(\text{kings}) - v(\text{king}) + v(\text{queen}) \approx v(\text{queens})$

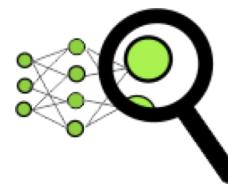




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Word Similarity Benchmarks

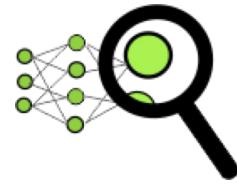
Analogy: a is to a^* as b is to

Task: $v(a^*) - v(a) + v(b) \approx ? \longrightarrow$

- find the closest vector
- check if it corresponds to the correct word

relation	word pair 1		word pair 2	
man-woman	brother	sister	grandson	granddaughter
currency	Angola	kwanza	Iran	rial
opposite	possibly	impossibly	ethical	unethical
past tense	walking	walked	swimming	swam
superlative	easy	easiest	lucky	luckiest

Examples of relations and word pairs from [the Google analogy test set](#).



Similarities Across Languages

The recipe for building large dictionaries from small ones

Ingredients:

- corpus in one language
(e.g., English)
- corpus in another language
(e.g., Spanish)
- very small dictionary

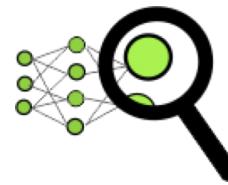
cat \leftrightarrow gato

cow \leftrightarrow vaca

dog \leftrightarrow perro

fox \leftrightarrow zorro

...



Similarities Across Languages

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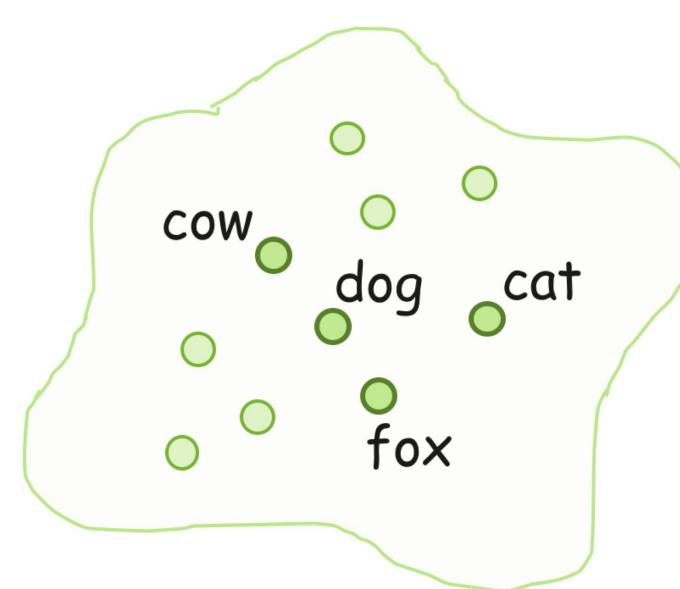
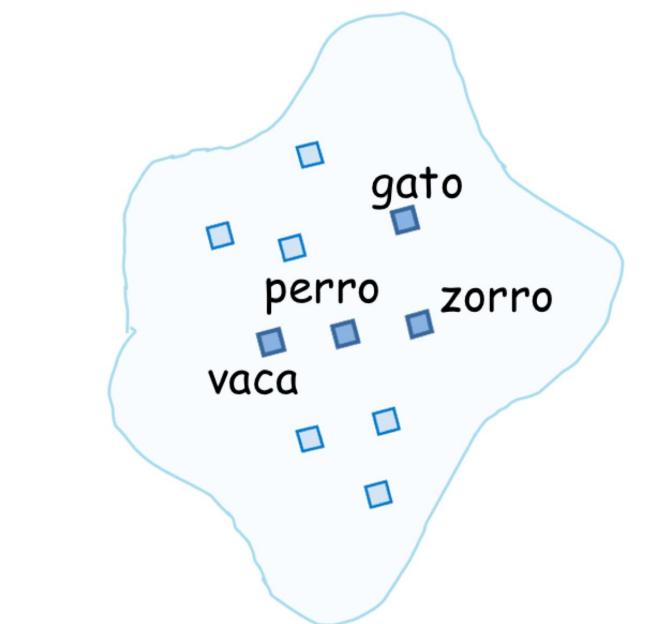
$\text{dog} \leftrightarrow \text{perro}$

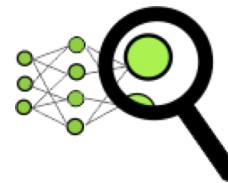
$\text{fox} \leftrightarrow \text{zorro}$

...

Step 1:

- train embeddings for each language





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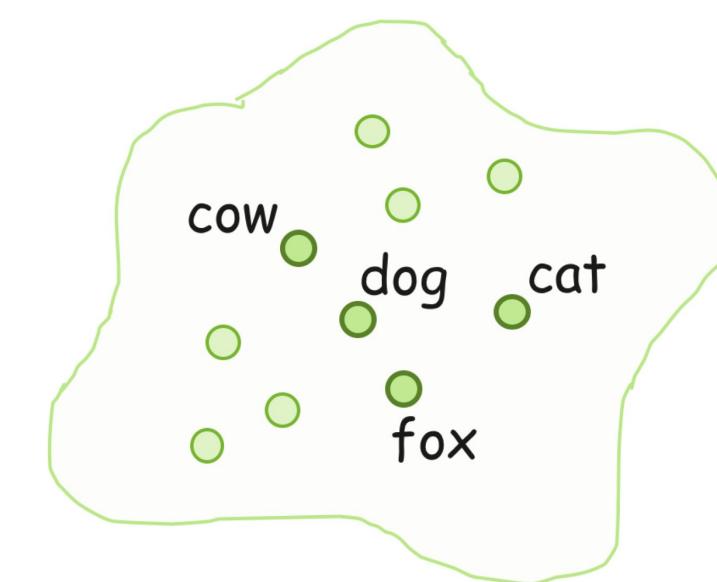
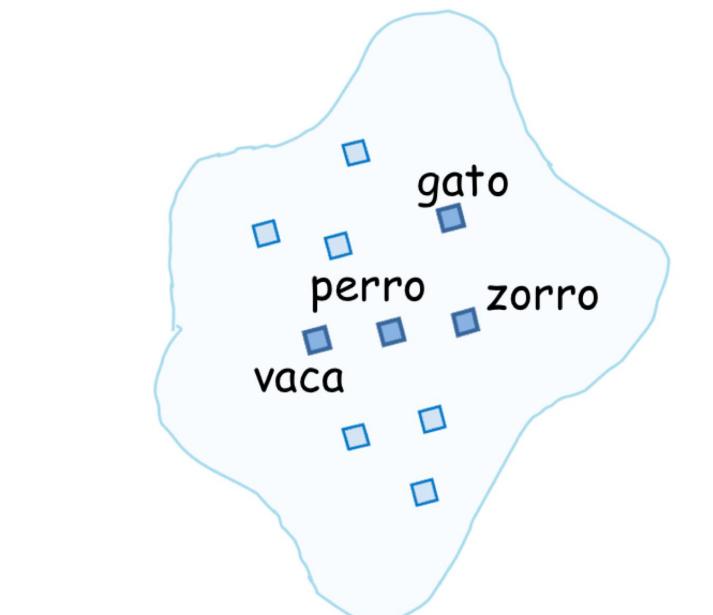
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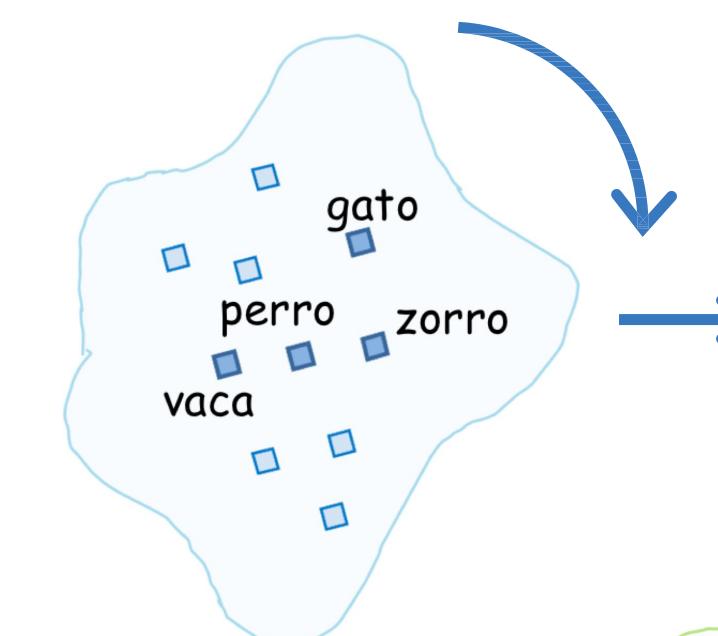
Step 1:

- train embeddings for each language

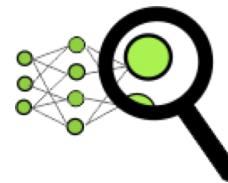


Step 2:

- linearly map one embeddings to the other to match words from the dictionary



match the pairs you know



Similarities Across Languages

The recipe for building large dictionaries from small ones

Ingredients:

- corpus in one language (e.g., English)
- corpus in another language (e.g., Spanish)
- very small dictionary

cat ↔ gato

cow ↔ vaca

dog ↔ perro

fox ↔ zorro

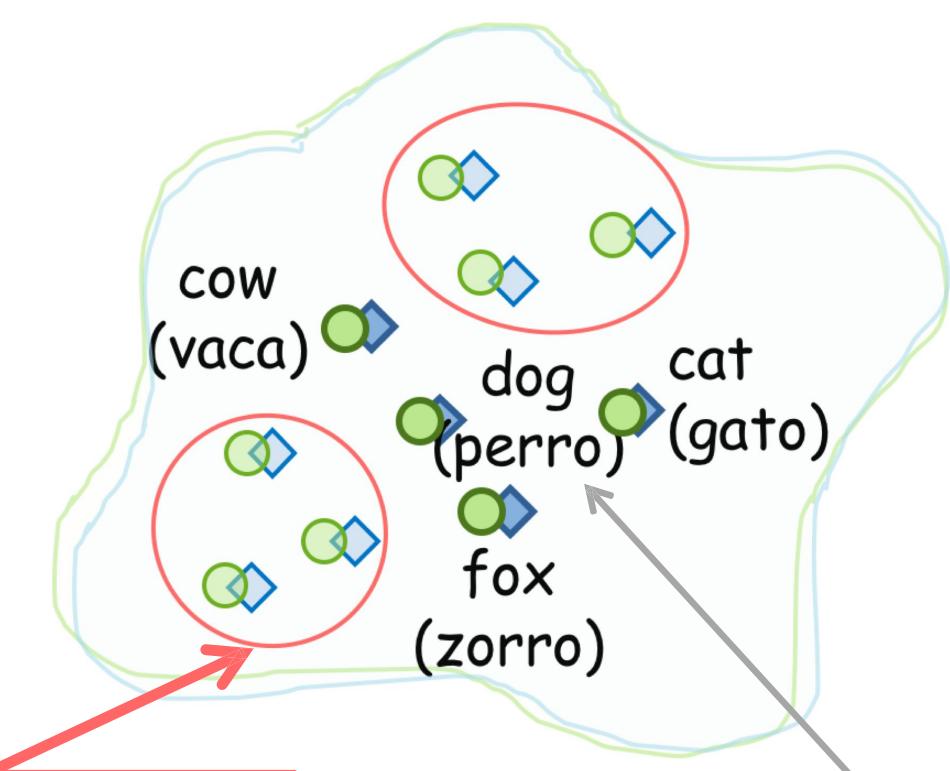
...

Steps 1-2:

- match words from the vocabulary

Step 3:

- after matching the two spaces, get new pairs from the new matches



**new translations –
you learned them!**

old translations –
the ones you knew

More in NLP Course For You





Research Thinking

Count-Based Methods

Improve Simple Co-Occurrence Counts

The simplest co-occurrence counts treat context words equally, although these words are at different relative positions from the central word. For example, from one sentence the central word **cat** will get a co-occurrence count of 1 for each of the words **cute**, **grey**, **playing**, **in** (look at the example to the right).

co-occurrence counts
for one sentence

...I saw a cute grey cat playing in the ...
grey 0 0 1 1 0 1 1 0 0
...I saw a cute grey cat playing in the ...

?

Are context words at different distances equally important? If not, how can we modify co-occurrence counts?

► Possible answers

?

In language, word order is important; specifically, left and right contexts have different meanings. How can we distinguish between the left and right contexts?

► One of the existing approaches



Research Thinking



Related Papers

What's inside:

- Good Old Classics
- Analyzing Geometry
- Biases in Word Embeddings
- Semantic Change
- Theory to the Rescue! - coming soon
- Cross-Lingual Embeddings - coming soon
- ... to be updated

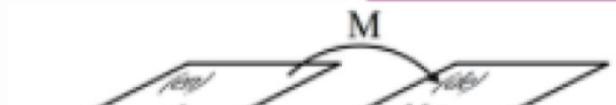
Characterizing Departures from Linearity in Word Translation

Ndapa Nakashole, Raphael Flauger

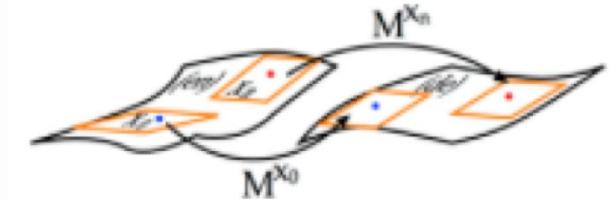
We learned that we can (almost) match semantic spaces for different languages linearly. But is the "true" underlying mapping between languages indeed linear? If it is linear globally, then all local linear mappings have to be similar (to the global linear mapping, and hence to each other). Well, they are not.

► More details

ACL 2018



Global linear mapping



Local linear mappings (for small neighborhoods)



NLP Course For You



Research Thinking
Related Papers



Have Fun!

dream - night + day = ?

world future

everything thing

next

Choose your answer

Thank you!

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