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## Coding Example: Find shortest path in a maze (Bellman-Ford approach)

In this lesson, we will implement the solution of finding the shortest path in the maze using the Bellman-Ford approach.

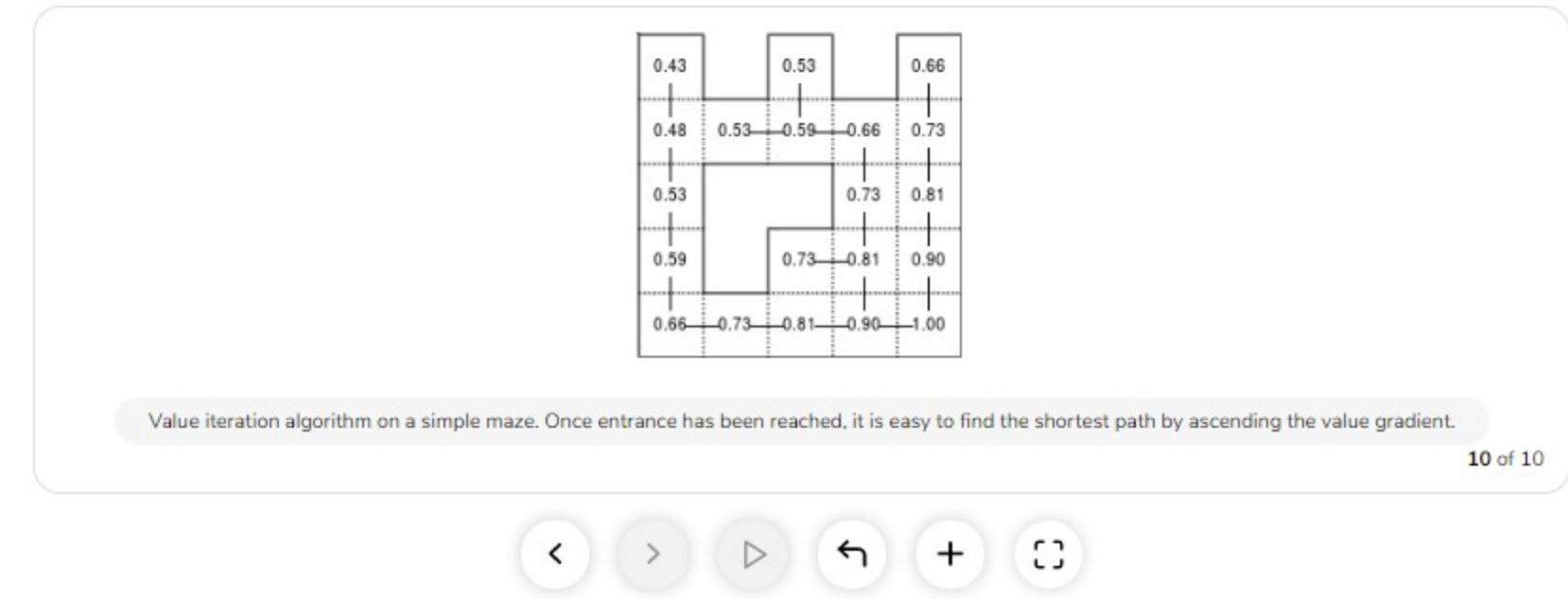
We'll cover the following

- Bellman-Ford Algorithm
- Complete Solution
- Further Readings

### Bellman-Ford Algorithm #

The Bellman-Ford algorithm is an algorithm that is able to find the optimal path in a graph using a diffusion process. The optimal path is found by ascending the resulting gradient. This algorithm runs in quadratic time  $O(|V||E|)$  (where  $V$  is the number of vertices, and  $E$  is the number of edges).

However, in our simple case, we won't hit the worst case scenario. Once this is done, we can ascend the gradient from the starting node. You can check on the figure that this leads to the shortest path.



We start by setting the exit node to the value 1, while every other node is set to 0, except the walls. Then we iterate a process such that each cell's new value is computed as the maximum value between the current cell value and the discounted (`gamma=0.9` in the case below) 4 neighbour values. The process starts as soon as the starting node value becomes strictly positive.

The NumPy implementation is straightforward if we take advantage of the `generic_filter` (from `scipy.ndimage`) for the diffusion process:

```
1 import numpy as np
2 def diffuse(Z):
3     # North, West, Center, East, South
4     return max(gamma*Z[0], gamma*Z[1], Z[2], gamma*Z[3], gamma*Z[4])
5
6 # Build gradient array
7 G = np.zeros(Z.shape)
8
9 # Initialize gradient at the entrance with value 1
10 G[start] = 1
11
12 # Discount factor
13 gamma = 0.99
14
15 # We iterate until value at exit is > 0. This requires the maze
16 # to have a solution or it will be stuck in the loop.
17 while G[goal] == 0.0:
18     G = Z * generic_filter(G, diffuse, footprint=[[0, 1, 0],
19                                                  [1, 1, 1],
20                                                  [0, 1, 0]])
```

But in this specific case, it is rather slow. We'd better cook-up our own solution, reusing part of the game of life code:

```
1 import numpy as np
2
3 # Build gradient array
4 G = np.zeros(Z.shape)
5
6 # Initialize gradient at the entrance with value 1
7 G[start] = 1
8
9 # Discount factor
10 gamma = 0.99
11
12 # We iterate until value at exit is > 0. This requires the maze
13 # to have a solution or it will be stuck in the loop.
14 G_gamma = np.empty_like(G)
15 while G[goal] == 0.0:
16     np.multiply(G, gamma, out=G_gamma)
17     N = G_gamma[0:-2,1:-1]
18     W = G_gamma[1:-1,0:-2]
19     C = G[1:-1,1:-1]
20     E = G_gamma[1:-1,2:]
21     S = G_gamma[2:,1:-1]
22     G[1:-1,1:-1] = Z[1:-1,1:-1]*np.maximum(N,np.maximum(W,
23                                                    np.maximum(C,np.maximum(E,S))))
```

Once this is done, we can ascend the gradient to find the shortest path as illustrated on the figure below:



### Complete Solution #

Let's, once again, visualize the maze by replacing Breadth-First implementation with Bellman-Ford's. Run the following code and once the output is generated, zoom-in to have a clearer view at the shortest path.

1 # -----

2 # From Numpy to Python

3 # Copyright (2017) Nicolas P. Rougier - BSD license

4 # More information at <https://github.com/rougier/numpy-book>

5 # -----

6 import numpy as np

7 from collections import deque

8 import matplotlib.pyplot as plt

9 from scipy.ndimage import generic\_filter

10

11

12 def build\_maze(shape=(65,65), complexity=0.75, density = 0.50):

13 """

14 Build a maze using given complexity and density

15

16 Parameters

17 =====

18

19 shape : (rows,cols)

20 | Size of the maze

21

22 complexity: float

23 | Mean length of islands (as a ratio of maze size)

24

25 density: float

26 | Mean numbers of highland (as a ratio of maze surface)

27

28 """

RUN

SAVE

RESET

X

### Further Readings #

- Labyrinth Algorithms, Valentin Bryukhanov, 2014.

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Coding Example: Fluid Dynamics

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