

# Coding Example: Find shortest path in a maze (Breadth-First approach)

In this lesson, we will implement the solution of finding shortest path in the maze that we build in the previous lesson. To find the shortest path, we will use the BFS strategy.

```
We'll cover the following

Breadth-First Algorithm

Step 1: Implement a Graph Class

Step 2: Implement Breadth-First Algorithm

Complete Solution
```

### **Breadth-First Algorithm**

The breadth-first (as well as depth-first) search algorithm addresses the problem of finding a path between two nodes by examining all possibilities starting from the root node and stopping as soon as a solution has been found (destination node has been reached). This algorithm runs in linear time with complexity in O(|V| + |E|) (where V is the number of vertices, and E is the number of edges).

Writing such an algorithm is not especially difficult, provided you have the right data structure. In our case, the array representation of the maze is not the most well-suited and we need to transform it into an actual graph as proposed by Valentin Bryukhanov.

#### Step 1: Implement a Graph Class

```
def build_graph(maze):
    height, width = maze.shape
    graph = {(i, j): [] for j in range(width)

for i in range(height) if not maze[i][j]}

for row, col in graph.keys():
    if row < height - 1 and not maze[row + 1][col]:
        graph[(row, col)].append(("S", (row + 1, col)))
        graph[(row + 1, col)].append(("N", (row, col)))

if col < width - 1 and not maze[row][col + 1]:
        graph[(row, col)].append(("E", (row, col + 1)))
        graph[(row, col + 1)].append(("N", (row, col)))

return graph</pre>
```

**Note:** If we had used the depth-first algorithm, there is no guarantee to find the shortest path, only to find a path (if it exists).

#### Step 2: Implement Breadth-First Algorithm

Once this is done, writing the breadth-first algorithm is straightforward. We start from the starting node and we visit nodes at the current depth only (breadth-first, remember?) and we iterate the process until reaching the final node, if possible. The question is then: do we get the shortest path exploring the graph this way? In this specific case, "yes", because we don't have an edge-weighted graph, i.e. all the edges have the same weight (or cost).

```
def breadth_first(maze, start, goal):
    queue = deque([([start], start)])
    visited = set()
    graph = build_graph(maze)

while queue:
    path, current = queue.popleft()
    if current == goal:
        return np.array(path)
    if current in visited:
        continue
    visited.add(current)
    for direction, neighbour in graph[current]:
        p = list(path)
        p.append(neighbour)
        queue.append((p, neighbour))
    return None
```

## **Complete Solution**

Let's merge all this logic into one code and visualize the maze, gradient, and the shortest path! Run the following code and once the output is generated, zoom-in to have a clearer view at the shortest path.

```
6
6 import numpy as np
7 from collections import deque
8 import matplotlib.pyplot as plt
   from scipy.ndimage import generic_filter
12 def build_maze(shape=(65,65), complexity=0.75, density = 0.50):
       Build a maze using given complexity and density
       shape : (rows,cols)
       Size of the maze
       complexity: float
       Mean length of islands (as a ratio of maze size)
       density: float
       Mean numbers of highland (as a ratio of maze surface)
   RUN
                                                                                    SAVE
                                                                                                 RESET
                                                                                                          ×
```

In the next lesson, we will try to solve this same problem using the Bellman-Ford approach!

