



Regular language

→ Every Regular language is also CFL, but every CFL need not be regular.

• Regular language -

✓ 1. $a^n / n \geq 1$

✓ 2. $a^n b^m / n, m \geq 1$

✓ 3. $a^n b^n / n \leq 10^{10}$

(Language are bounded means - finite)

✓ 4. $ww^R / |w| = 2, \Sigma = \{a, b\}$

✓ 5. $a^n b^m c^k / n, m, k \geq 1$

✓ 6. $a^i b^{2j} / i, j \geq 1$

✓ 7. $a^i b^{4j} / i, j \geq 1$

✓ 8. a^n / n is even.

✓ 9. a^n / n is odd.

✓ 10. $n_a(w) \bmod 3 \leq n_b(w) \bmod 3$

✓ 11. $a^n / n \geq 0$

• Non Regular language

✓ 1. $a^n b^n / n \geq 1$

✓ 2. $ww^R / w \in (a, b)^*$

✓ 3. $ww / w \in (a, b)^*$

✓ 4. a^n / n is prime.

✓ 5. $a^{n^2} / n \geq 1$

✓ 6. $a^{2^n} / n \geq 1$

✓ 7. $a^i b^{j^2} / i, j \geq 1$

✓ 8. $\{w / n_a(w) = n_b(w)\}$

✓ 9. $ww^R / w \in (a, b)^*$

✓ 10. $a^n b^n c^n / n \geq 1$

✓ 11. $a^n b^{m+n} c^m / n, m \geq 1$

RL • $\{w x w^R / w, x \in (0,1)^+\}$ — **RL**

→ $w = 101$

$x = 100$

$w^R = 101$

$$\begin{array}{c} w \quad x \quad w^R \\ \underline{101} \quad \underline{100} \quad \underline{101} \\ w \quad x \quad w^R \end{array}$$

$w = 011$

$x = 1010$

$w^R = 110$

$$\begin{array}{c} w \quad x \quad w^R \\ \underline{011} \quad \underline{1010} \quad \underline{110} \\ w \quad x \quad w^R \end{array}$$

RE of this language = $1(1+0)^*1 + 0(1+0)^*0$

Start and end with same symbol.

N-RL • $\{w x w^R / w \in (0,1)^+, |w| = 5\}$ — Not Regular.

Because x is constant.

RL • $\{x w w^R y / x, y, w \in (0,1)^+\}$ — **RL**

→ $x = 10 \quad w = 100$

$y = 11 \quad w^R = 001$

$$\begin{array}{c} x \quad w \quad w^R \quad y \\ \underline{10} \quad \underline{100} \quad \underline{001} \quad \underline{11} \\ x \quad w \quad w^R \quad y \end{array}$$

RE of this language = $(1+0)^*11(1+0)^* + (0+1)^*00(0+1)^*$

contain 11 or 00 as substring.

N-RL • $\{x w w^R / x, w \in (0,1)^+\}$.

N-RL • $\{x w w^R y / y, w \in (0,1)^+\}$.