

## **Efficient Linesegment Algorithms**

Assume a set of 20 to 100 linesegments, denoted by  $s_i$  defined in Cartesian coordinates via their start and end points as

$$\mathbf{s}_{i} = \begin{pmatrix} x_{s,i} \\ x_{e,i} \\ y_{s,i} \\ y_{e,i} \end{pmatrix} \tag{1}$$

where, e.g.,  $x_{e,i}$  denotes the x coordinate of the end point of the ith line segment. These line segments change with every measurement update, but typically only slightly. However, new line segments might be added, line segments might change in length, or be deleted. We can use this information to make potential pre-processing steps more efficient. In the following we denote as the distance of a point  $x=(x,y)^T$  to a line segment  $s_i$  as the minimum distance in the typical two norm sense, i.e.,

$$d_i^2(\mathbf{x}) = \underset{\mathbf{x}_s \in \mathbf{s}_i}{\operatorname{argmin}} ||\mathbf{x} - \mathbf{x}_s||^2$$
 (2)

Furthermore we define as the distance between two line segments  $s_i$ ,  $s_j$  the distance between one point taken on  $s_i$  and another taken on  $s_j$  such that the distance between these points is minimal, i.e.,

$$d_{i,j}^{2} = \underset{x_{i} \in s_{i}, x_{j} \in s_{j}}{\operatorname{argmin}} ||x_{i} - x_{j}||^{2}$$
(3)

It is worth noting that if the two segments do not intersect, and are not parallel, that the closest distance will always be taken from a start or end point of at least one of the segments.

Given the line segments we are looking for efficient algorithms to calculate the following:

- Given a point  $x=(x,y)^T$  determine the closest line segment from the set of given line segments.
- Given a point x determine the set of all line segments that are in a distance between  $d_{lower}$  and  $d_{upper}$ .
- Determine relative measures between line segments, such as
  - $\circ$  which pairs of line segments  $s_i$ ,  $s_j$  come closer than a distance  $d_{lower}$ .