Equation of Unit Vector

$1 \quad 12^{th} \text{ Maths}$ - Chapter 10

This is Problem-5 from Exercise 5.5

1. Find the value of x for which $x(\hat{i} + \hat{j} + \hat{k})$ is a unit vector

2 Solution

Given points are

$$\mathbf{x} = \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix} \tag{1}$$

unit vector formula is

$$\overrightarrow{x} = \frac{1}{\|\mathbf{x}\|} \mathbf{x} \tag{2}$$

where

$$\|\mathbf{x}\| = \sqrt{\begin{pmatrix} 1 & 1 & 1 \end{pmatrix} \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix}} \tag{3}$$

$$=\sqrt{3}\tag{4}$$

Hence , the unit vector is

$$\overrightarrow{x} = \frac{1}{\sqrt{3}} \begin{pmatrix} 1\\1\\1 \end{pmatrix} \tag{5}$$

$$\overrightarrow{x} = \frac{1}{\sqrt{3}} \begin{pmatrix} 1\\1\\1 \end{pmatrix}$$

$$= \begin{pmatrix} \frac{1}{\sqrt{3}}\\\frac{1}{\sqrt{3}}\\\frac{1}{\sqrt{3}} \end{pmatrix}$$

$$(5)$$