VECTORS

12^{th} Maths - EXERCISE-10.3

1. Find the angle between two vectors \overrightarrow{a} and \overrightarrow{b} with magnitudes $\sqrt{3}$ and 2 respectively having $\overrightarrow{a} \cdot \overrightarrow{b} = \sqrt{6}$.

Solution: Given points are

$$\|\mathbf{a}^{\top}\mathbf{a}\| = \sqrt{3} \tag{1}$$

$$\|\mathbf{b}^{\mathsf{T}}\mathbf{b}\| = 2\tag{2}$$

$$\mathbf{a}^{\top}\mathbf{b} = \sqrt{6} \tag{3}$$

$$\mathbf{a}^{\top}\mathbf{b} = \sqrt{\mathbf{a}^{\top}\mathbf{a}}\sqrt{\mathbf{b}^{\top}\mathbf{b}}cos\theta \tag{4}$$

$$\sqrt{6} = \sqrt{3} \times 2 \times \cos\theta \tag{5}$$

$$cos\theta = \frac{\sqrt{6}}{\sqrt{3} \times 2}$$

$$= \frac{1}{\sqrt{2}}$$
(6)
$$(7)$$

$$=\frac{1}{\sqrt{2}}\tag{7}$$

$$\theta = 45^{\circ} \tag{8}$$